

```
def countdown(x):
```

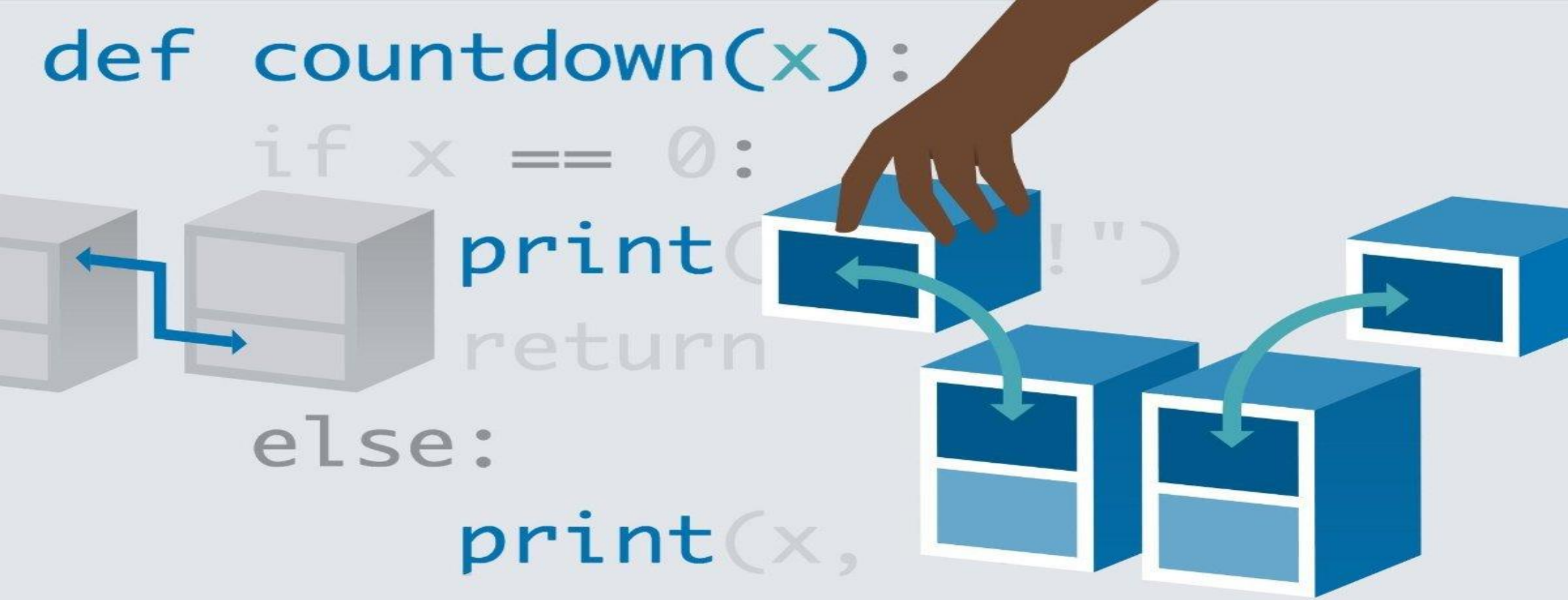
```
    if x == 0:
```

```
        print("Bang!")
```

```
    return
```

```
    else:
```

```
        print(x,
```



Algorithm Design and Analysis Introduction

<http://ada.miulab.tw>

Yun-Nung (Vivian) Chen



國立臺灣大學
National Taiwan University



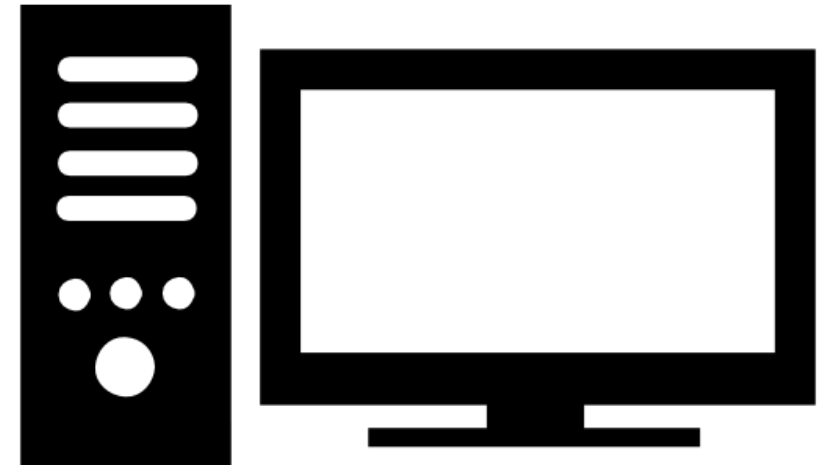
Outline

- Terminology
 - Problem (問題)
 - Problem instance (個例)
 - Computation model (計算模型)
 - Algorithm (演算法)
 - The hardness of a problem (難度)
- Algorithm Design & Analysis Process
- Review: Asymptotic Analysis
- Algorithm Complexity
- Problem Complexity



Efficiency Measurement = Speed

- Why we care?
 - Computers may be fast, but they are not infinitely fast
 - Memory may be inexpensive, but it is not free





Terminology

Textbook Ch. 1 – The Role of Algorithms in Computing

Problem (問題)



The champion problem

- Input: n distinct integers $A[1], A[2], \dots, A[n]$.
- Output: the index i with $1 \leq i \leq n$ such that

$$A[i] = \max_{1 \leq j \leq n} A[j].$$

Problem Instance (個例)

- An **instance** of the champion problem

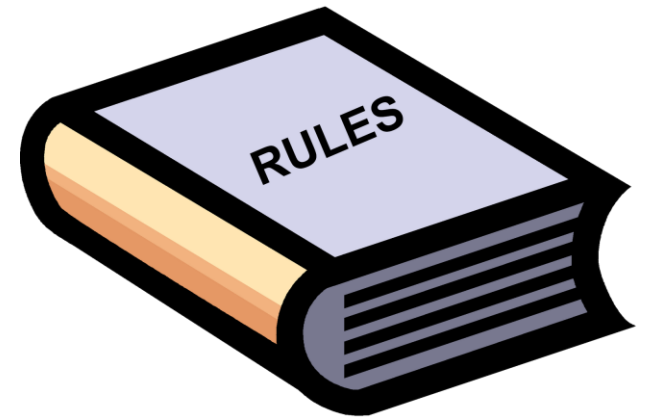
5 distinct integers 7, 4, 2, 9, 8.

7	4	2	9	8
A[1]	A[2]	A[3]	A[4]	A[5]



Computation Model (計算模型)

- Each problem must have its rule (遊戲規則)
- Computation model (計算模型) = rule (遊戲規則)
- The problems with different rules have different hardness levels



Hardness (難易程度)

- How difficult to solve a problem
 - Example: how hard is the champion problem?
 - Following the comparison-based rule

What does “solve (解)” mean?

What does “difficult (難)” mean?

Problem Solving (解題)

- Definition of “solving” a problem
 - Giving an **algorithm** (演算法) that produces a correct output for **any instance** of the problem.

Algorithm (演算法)



- Algorithm: a detailed step-by-step instruction
 - Must follow the game rules
 - Like a step-by-step recipe
 - Programming language doesn't matter→ problem-solving recipe (technology)
- If an algorithm produces a correct output for any instance of the problem
→ this algorithm “**solves**” the problem

Hardness (難度)

- Hardness of the problem
 - How much **effort** the best algorithm needs to solve any problem instance
- 防禦力
 - 看看最厲害的賽亞人要花多少**攻擊力**才能打贏對手



攻擊力 50000



防禦力 100000



Algorithm Design & Analysis Process



Algorithm Design & Analysis Process

- 1 Formulate a **problem**
- 2 Develop an **algorithm**
- 3 Prove the **correctness**
- 4 Analyze **running time/space** requirement

Design
Step

Analysis
Step

1. Problem Formulation



The champion problem

- Input: n distinct integers $A[1], A[2], \dots, A[n]$.
- Output: the index i with $1 \leq i \leq n$ such that

$$A[i] = \max_{1 \leq j \leq n} A[j].$$

2. Algorithm Design



- Create a detailed recipe for solving the problem
 - Follow the **comparison-based** rule
 - 不准偷看信封的內容
 - 請別人幫忙「比大小」

- Algorithm: 擂台法

```
1.  int  $i, j$ ;  
2.   $j = 1$ ;  
3.  for ( $i = 2$ ;  $i \leq n$ ;  $i++$ )  
4.      if ( $A[i] > A[j]$ )  
5.           $j = i$ ;  
6.  return  $j$ ;
```

Q1: Is this a comparison-based algorithm?

Q2: Does it solve the champion



3. Correctness of the Algorithm

- Prove by contradiction (反證法)

The algorithm solves the champion problem.

Proof Let j^* be the correct answer. That is, $A[j^*] = \max\{A[1], \dots, A[n]\}$.

- If $j^* = 1$, then Step 5 is never reached. Therefore, 1 is correctly returned.
- If $j^* > 1$, then in the iteration of the for-loop with $i = j^*$, j becomes j^* . By definition of j^* , $A[j^*] > A[i]$ holds for each $i = j^* + 1, \dots, n$. Therefore, in the remaining iterations of the for-loop, the value of j does not change. Hence, at the end of the algorithm, j^* is correctly returned.

```
1.  int i, j;  
2.  j = 1;  
3.  for (i = 2; i <= n; i++)  
4.      if (A[i] > A[j])  
5.          j = i;  
6.  return j;
```


Hardness of The Champion Problem

- How much **effort** the best algorithm needs to solve any problem instance
 - Follow the **comparison-based** rule
 - 不准偷看信封的內容
 - 請別人幫忙「比大小」
- **Effort**: we first use the times of comparison for measurement

```
1.  int  $i, j$ ;  
2.   $j = 1$ ;  
3.  for ( $i = 2$ ;  $i \leq n$ ;  
         $i++$ )  
4.      if ( $A[i] > A[j]$ )  
5.           $j = i$ ;  
6.  return  $j$ ;
```

$(n - 1)$ comparisons



Hardness of The Champion Problem

- The hardness of the champion problem is $(n - 1)$ comparisons
 - a) There is an algorithm that can solve the problem using at most $(n - 1)$ comparisons
 - This can be proved by 擂臺法, which uses $(n - 1)$ comparisons for any problem instance
 - b) For any algorithm, there exists a problem instance that requires $(n - 1)$ comparisons
 - Why?

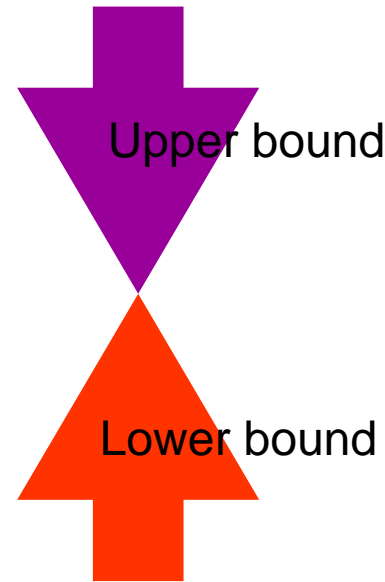
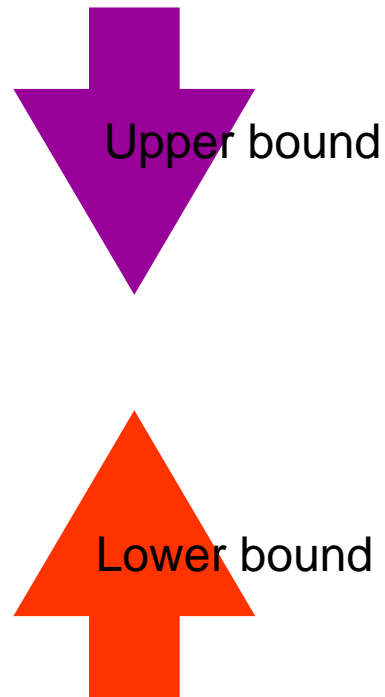


Hardness of The Champion Problem

- Q: Is there an algorithm that only needs $n - 2$ comparisons?
 - A: Impossible!
 - Reason
 - A single comparison only decides a loser
 - If there are only $n - 2$ comparisons, the most number of losers is $n - 2$
 - There exists a least 2 integers that did not lose
- any algorithm cannot tell who the champion is

Finding Hardness

- Use the **upper bound** and the **lower bound**
- When they meet each other, we know the hardness of the problem



Hardness of The Champion Problem

- Upper bound

- how many comparisons are sufficient to solve the champion problem
- Each algorithm provides an upper bound
- The smarter algorithm provides tighter, lower, and better upper bound

- Lower bound

- how many comparisons in the worst case are necessary to solve the champion problem
- Some arguments provide different lower bounds
- Higher lower bound is better

多此一舉擂台法

```
1.  int i, j;  
2.  j = 1;  
3.  for (i = 2; i <= n; i++)  
4.      if ((A[i] > A[j]) && (A[j] < A[i]))  
5.          j = i;  
6.  return j;
```

→ $(2n - 2)$ comparisons

Every integer needs to be in the comparison once
→ $(n/2)$ comparisons

When upper bound = lower bound, the problem is solved.
→ We figure out the hardness of the problem

4. Algorithm Analysis

- The majority of researchers in algorithms studies the time and space required for solving problems in two directions
 - Upper bounds: designing and analyzing algorithms
 - Lower bounds: providing arguments
- When the upper and lower bounds match, we have an **optimal algorithm** and the problem is completely **resolved**



$O \quad \Omega \quad \Theta \quad o \quad \omega$



教過

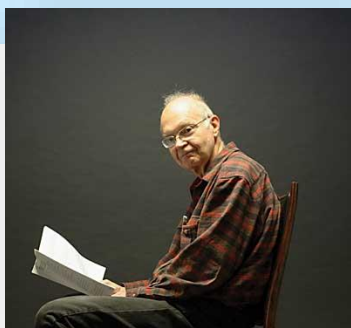
我早就會了!



Asymptotic Analysis



Edmund Landau
(1877-1938)



Donald E. Knuth
(1938-)

Motivation

- The hardness of the champion problem is exactly $n - 1$ comparisons
- Different problems may have different 「難度量尺」
 - cannot be interchangeable
- Focus on the standard **growth of the function** to ignore the unit and coefficient effects

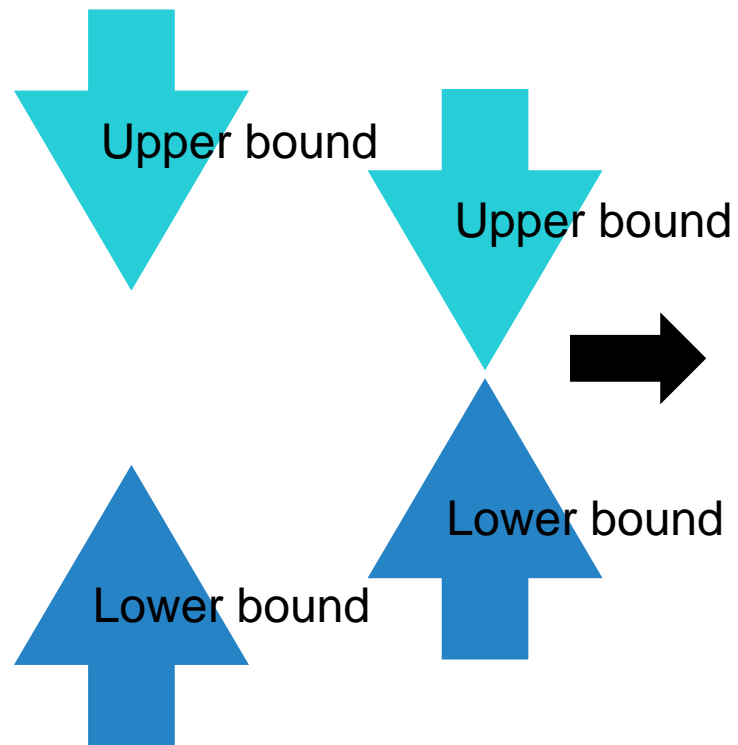


Goal: Finding Hardness

- For a problem P , we want to figure out
 - The hardness (complexity) of this problem P is $\Theta(f(n))$
 - n is the instance size of this problem P
 - $f(n)$ is a function
 - $\Theta(f(n))$ means that “it **exactly equals to** the growth of the function”
- Then we can argue that under the comparison-based computation model
 - The hardness of the champion problem is $\Theta(n)$
 - The hardness of the sorting problem is $\Theta(n \log n)$

Goal: Finding Hardness

- Use the upper bound and the lower bound
- When they match, we know the hardness of the problem



use $O(f(n))$ and $o(f(n))$

upper bound is $O(h(n))$ & lower bound is $\Omega(h(n))$
→ the problem complexity is exactly $\Theta(h(n))$

use $\Omega(g(n))$ and $\omega(g(n))$

Goal: Finding Hardness

- First learn how to analyze / measure the effort an algorithm needs
 - Time complexity
 - Space complexity
- Focus on **worst-case** complexity
 - “average-case” analysis requires the assumption about the probability distribution of problem instances

Types	Description
Worst Case	Maximum running time for any instance of size n
Average Case	Expected running time for a random instance of size n
Amortized	Worse-case running time for a series of operations

Review of Asymptotic Notation

(Textbook Ch. 3.1)

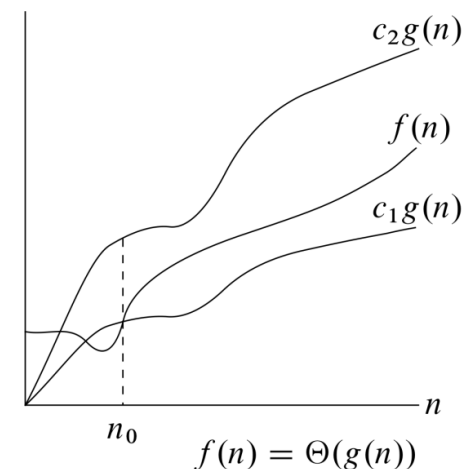
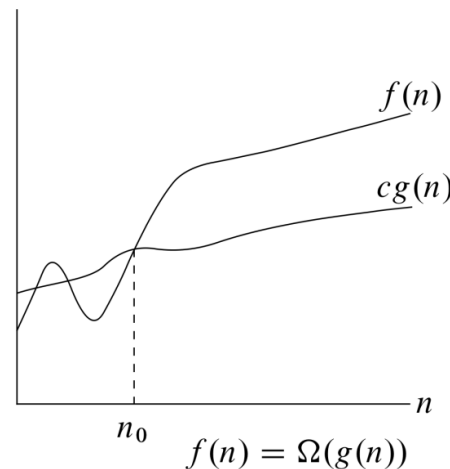
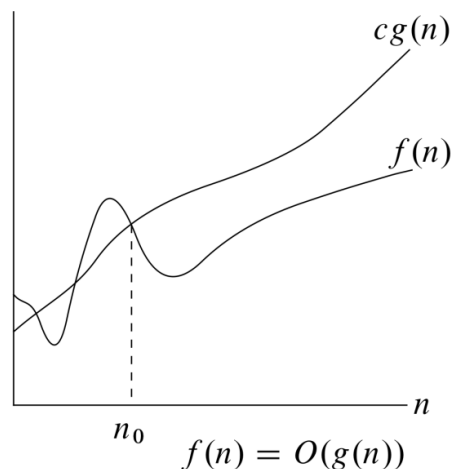
- $f(n)$ = time or space of an algorithm for an input of size n
- Asymptotic analysis: focus on the **growth** of $f(n)$ as $n \rightarrow \infty$



Review of Asymptotic Notation

(Textbook Ch. 3.1)

- $f(n)$ = time or space of an algorithm for an input of size n
- Asymptotic analysis: focus on the **growth** of $f(n)$ as $n \rightarrow \infty$
- O , or Big-Oh: **upper** bounding function
- Ω , or Big-Omega: **lower** bounding function
- Θ , or Big-Theta: **tightly** bounding function



Formal Definition of Big-Oh

(Textbook Ch. 3.1)

- For any two functions $f(n)$ and $g(n)$,

$$f(n) = O(g(n))$$

if there exist positive constants n_0 and c s.t.

$$0 \leq f(n) \leq c \cdot g(n)$$

for all $n \geq n_0$.

$g(n)$ 的某個常數倍 $c \cdot g(n)$ 可以在 n 夠大時壓得住 $f(n)$

$$f(n) = O(g(n))$$

- Intuitive interpretation
 - $f(n)$ does not grow faster than $g(n)$
- Comments
 - 1) $f(n) = O(g(n))$ roughly means $f(n) \leq g(n)$ in terms of rate of growth
 - 2) “=” is not “equality”, it is like “**∈ (belong to)**”

The equality is $\{f(n)\} \subseteq O(g(n))$
 - 3) We do not write $O(g(n)) = f(n)$
- Note
 - $f(n)$ and $g(n)$ can be negative for some integers n
 - In order to compare using asymptotic notation O , both have to be non-negative for sufficiently large n
 - This requirement holds for other notations, i.e. Ω , Θ , o , ω

Review of Asymptotic Notation

(Textbook Ch. 3.1)

- Benefit
 - Ignore the low-order terms, units, and coefficients
 - Simplify the analysis
 - Example: $f(n) = 5n^3 + 7n^2 - 8$
 - Upper bound: $f(n) = O(n^3)$, $f(n) = O(n^4)$, $f(n) = O(n^3 \log_2 n)$
 - Lower bound: $f(n) = \Omega(n^3)$, $f(n) = \Omega(n^2)$, $f(n) = \Omega(n \log_2 n)$
 - Tight bound: $f(n) = \Theta(n^3)$
 - Q: $f(n) = O(n^3)$ and $f(n) = O(n^4)$, so $O(n^3) = O(n^4)$?
 - $O(n^3)$ represents **a set of functions** that are upper bounded by cn^3 for some constant c when n is large enough
 - In asymptotic analysis, “=” means “**∈ (belong to)**”
- “=” doesn’t mean “equal to”

Exercise: $100n^2 = O(n^3 - n^2)$?

- Draft.

$$100n^2 \leq 100(n^3 - n^2)$$

$$\leftarrow 200n^2 \leq 100n^3$$

$$\leftarrow 2 \leq n$$

- Let $n_0 = 2$ and $c = 100$

$$100n^2 \leq 100(n^3 - n^2)$$

holds for $n \geq 2$

$$100n^2 = O(n^3 - n^2)$$

Exercise: $n^2 = O(n)$?

- Disproof.

- Assume for a contradiction that there exist positive constants c and n_0 s.t.

$$n^2 \leq cn$$

holds for any integer n with $n \geq n_0$.

- Assume $n = 1 + \lceil \max(n_0, c) \rceil$

and because $n > n_0, n > c$, it follows that

$$n^2 > cn$$

- Due to contradiction, we know that

$$n^2 \neq O(n)$$

Rules

(Textbook Ch. 3.1)

The following statements hold for any real-valued functions $f(n)$ and $g(n)$, where there is a constant n_0 such that $f(n)$ and $g(n)$ are nonnegative for any integer $n \geq n_0$.

- Rule 1: $f(n) = O(f(n))$.
- Rule 2: If c is a positive constant, then $c \cdot O(f(n)) = O(f(n))$.
- Rule 3: If $f(n) = O(g(n))$, then $O(f(n)) = O(g(n))$.
- Rule 4: $O(f(n)) \cdot O(g(n)) = O(f(n) \cdot g(n))$.
- Rule 5: $O(f(n) \cdot g(n)) = f(n) \cdot O(g(n))$.

Other Notations

(Textbook Ch. 3.1)

$f(n) = O(g(n)) \rightarrow f(n) \leq g(n)$ in rate of growth

$f(n) = \Omega(g(n)) \rightarrow f(n) \geq g(n)$ in rate of growth

$f(n) = \Theta(g(n)) \rightarrow f(n) = g(n)$ in rate of growth

$f(n) = o(g(n)) \rightarrow f(n) < g(n)$ in rate of growth

$f(n) = \omega(g(n)) \rightarrow f(n) > g(n)$ in rate of growth

Goal: Finding Hardness

- First learn how to analyze / measure the effort an algorithm needs
 - Time complexity
 - Space complexity
- Focus on **worst-case** complexity
 - “average-case” analysis requires the assumption about the probability distribution of problem instances

Using O to give upper bounds on the worst-case time complexity of algorithms

Algorithm Analysis



- 擂台法

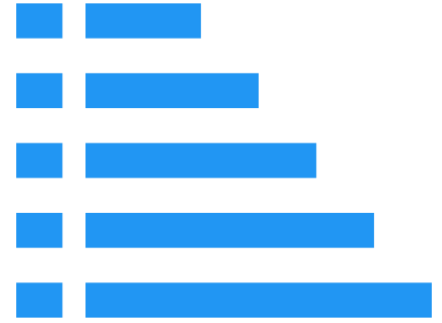
1.	int i, j ;	$O(1)$ time
2.	$j = 1$;	$O(1)$ time
3.	for ($i = 2$; $i \leq n$; $i++$)	$O(n)$ iterations
4.	if ($A[i] > A[j]$)	$O(1)$ time
5.	$j = i$;	$O(1)$ time
6.	return j ;	$O(1)$ time

Adding everything together
→ an upper bound on the
worst-case time complexity

- The worst-case time complexity is
 $O(1) + O(1) + O(n) \cdot (O(1) + O(1)) + O(1)$

$$\begin{aligned} & 3 \cdot O(1) + O(n) \cdot (2O(1)) \\ &= O(1) + O(n) \cdot O(1) && \text{Rule 2} \\ &= O(1) + O(n) && \text{Rule 4} \\ &= O(n) + O(n) && 1 = O(n) \text{ \& Rule 3} \\ &= 2 \cdot O(n) && \text{Rule 2} \\ &= O(n) \end{aligned}$$

Sorting Problem



- Input:

An array A of n distinct integers.

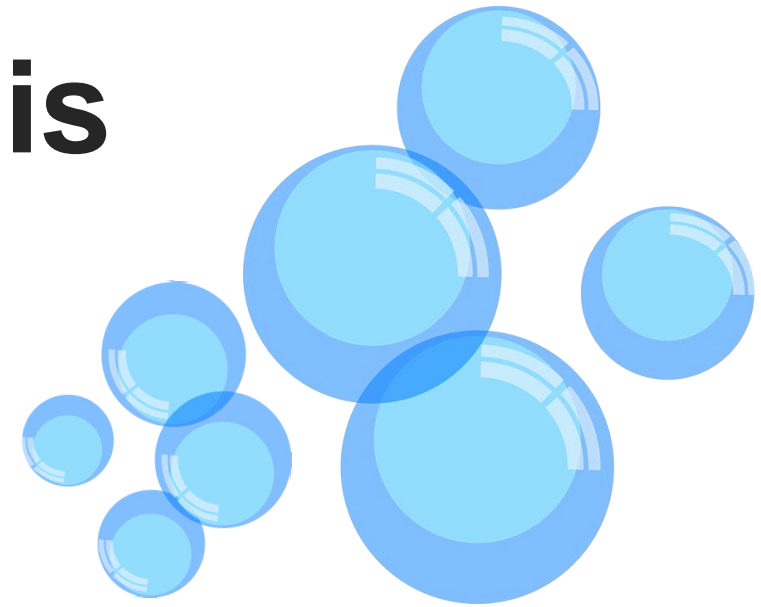
- Output:

Reorder A such that $A[1] < A[2] < \dots < A[n]$.

Algorithm Analysis

- Bubble-Sort Algorithm

1.	int <i>i</i> , <i>done</i> ;	$O(1)$ time
2.	do {	$f(n)$ iterations
3.	<i>done</i> = 1;	$O(1)$ time
4.	for (<i>i</i> = 1; <i>i</i> < <i>n</i> ; <i>i</i> ++) {	$O(n)$ iterations
5.	if (<i>A</i> [<i>i</i>] > <i>A</i> [<i>i</i> + 1]) {	$O(1)$ time
6.	exchange <i>A</i> [<i>i</i>] and <i>A</i> [<i>i</i> + 1];	$O(1)$ time
7.	<i>done</i> = 0;	$O(1)$ time
8.	}	
9.	}	
10.	} while (<i>done</i> == 0)	



$$\begin{aligned} &O(1) + f(n) \cdot (O(1) + O(n) \cdot O(1)) \\ &= O(1) + f(n) \cdot O(n) \\ &= f(n) \cdot O(n) \\ &= O(n^2) \end{aligned}$$

$f(n) = O(n)$
prove by induction

Example Illustration

7	3	1	4	6	2	5
3	1	4	6	2	5	7
1	3	4	2	5	6	7
1	3	2	4	5	6	7
1	2	3	4	5	6	7



Goal: Finding Hardness

- First learn how to analyze / measure the effort an algorithm needs
 - Time complexity
 - Space complexity
- Focus on **worst-case** complexity
 - “average-case” analysis requires the assumption about the probability distribution of problem instances

Using O to give **upper bounds** on the worst-case time complexity of algorithms

Using Ω to give **lower bounds** on the worst-case time complexity of algorithms

Algorithm Analysis



- 擂台法

1.	int i ;	$\Omega(1)$ time
2.	int $m = A[1]$;	$\Omega(1)$ time
3.	for ($i = 2$; $i \leq n$; $i++$) {	$\Omega(n)$ iterations
4.	if ($A[i] > m$)	$\Omega(1)$ time
5.	$m = A[i]$;	$\Omega(1)$ time
6.	}	
7.	return m ;	$\Omega(1)$ time

$$\begin{aligned} & 3 \cdot \Omega(1) + \Omega(n) \cdot (2 \cdot \Omega(1)) \\ &= \Omega(1) + \Omega(n) \cdot \Omega(1) \\ &= \Omega(1) + \Omega(n) \\ &= \Omega(n) \end{aligned}$$

Adding everything together
→ a lower bound on the worst-case time complexity?

Algorithm Analysis



- 百般無聊擂台法

1. int i ;	$\Omega(1)$ time
2. int $m = A[1]$;	$\Omega(1)$ time
3. for ($i = 2$; $i \leq n$; $i++$) {	$\Omega(n)$ iterations
4. if ($A[i] > m$)	$\Omega(1)$ time
5. $m = A[i]$;	$\Omega(1)$ time
6. if ($i == n$)	$\Omega(1)$ time
7. do $i++$ n times	$\Omega(n)$ time
8. }	
9. return m ;	$\Omega(1)$ time

$$\begin{aligned} & 3 \cdot \Omega(1) + \Omega(n) \cdot (3 \cdot \Omega(1) + \Omega(n)) \\ &= \Omega(1) + \Omega(n) \cdot \Omega(n) \\ &= \Omega(1) + \Omega(n^2) \\ &= \Omega(n^2) \end{aligned}$$

Adding together may result in errors.
The safe way is to analyze using **problem instances**.

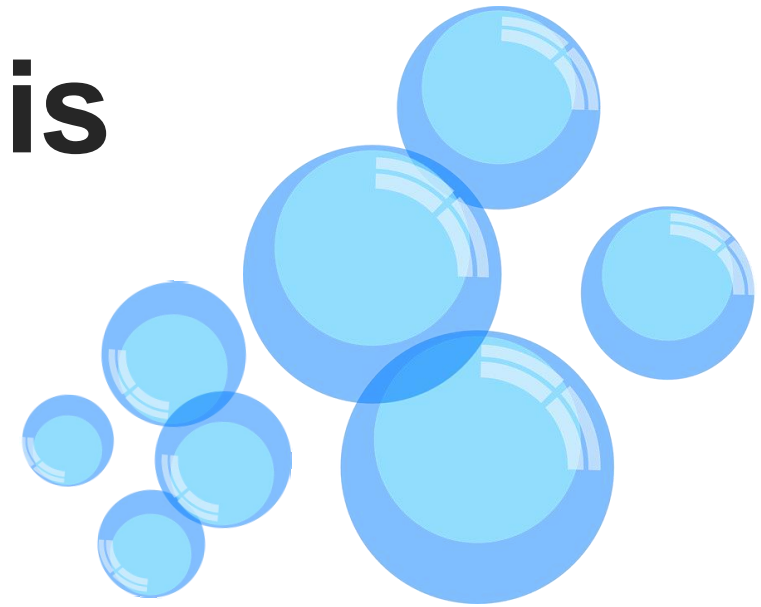
e.g. try $A[i] = i$ or $A[i] = 2(n - i)$ to check the time complexity $\rightarrow \Omega(1)$



Algorithm Analysis

- Bubble-Sort Algorithm

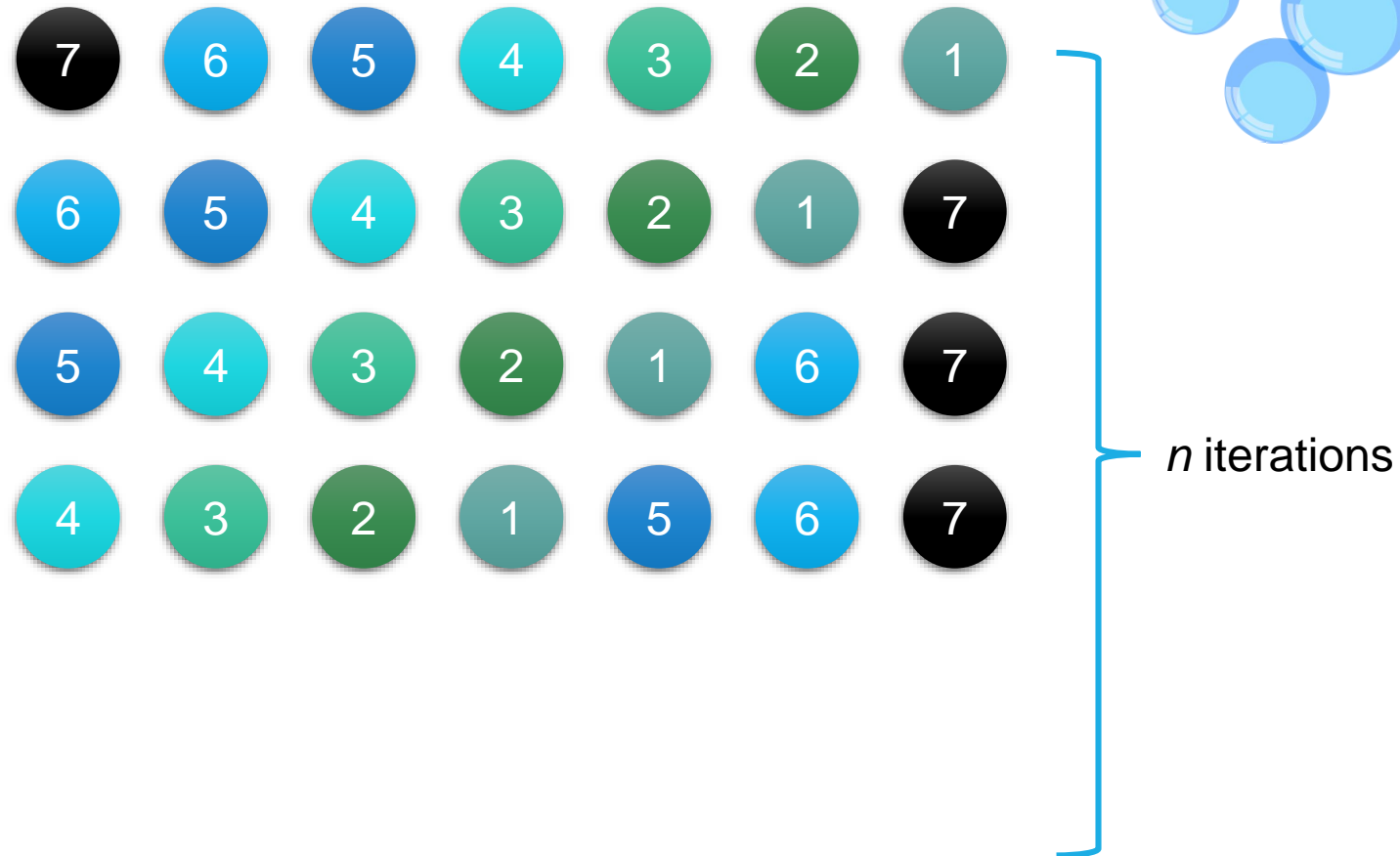
```
1.  int i, done;
2.  do { f(n) iterations
3.      done = 1;
4.      for (i = 1; i < n; i++) { Ω(n) time
5.          if (A[i] > A[i + 1]) {
6.              exchange A[i] and A[i + 1];
7.              done = 0;
8.          }
9.      }
10. } while (done == 0)
```



When A is decreasing, $f(n) = \Omega(n)$.
Therefore, the worst-case time complexity
of Bubble-Sort is

$$f(n) \cdot \Omega(n) = \Omega(n^2)$$

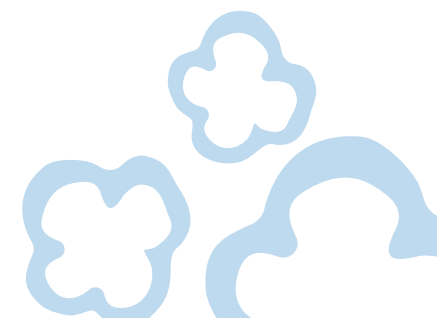
Example Illustration





Algorithm Complexity

In the worst case, what is the growth of function an algorithm takes



Time Complexity of an **Algorithm**

- We say that the (worst-case) time complexity of Algorithm A is $\Theta(f(n))$ if
 1. Algorithm A runs in time $O(f(n))$ &
 2. Algorithm A runs in time $\Omega(f(n))$ (in the worst case)
 - An input instance $I(n)$ s.t. Algorithm A runs in $\Omega(f(n))$ for each n

Tightness of the Complexity

- If we say that the time complexity analysis about $O(f(n))$ is **tight**
- = the algorithm runs in time $\Omega(f(n))$ in the worst case
- = (worst-case) time complexity of the algorithm is $\Theta(f(n))$
 - Not over-estimate the worst-case time complexity of the algorithm
- If we say that the time complexity analysis of Bubble-Sort algorithm about $O(n^2)$ is **tight**
- = Time complexity of Bubble-Sort algorithm is $\Omega(n^2)$
- = Time complexity of Bubble-Sort algorithm is $\Theta(n^2)$

Algorithm Analysis

- 百般無聊擂台法

1.	int i ;	$O(1)$ time
2.	int $m = A[1]$;	$O(1)$ time
3.	for ($i = 2$; $i \leq n$; $i++$) {	$O(n)$ iterations
4.	if ($A[i] > m$)	$O(1)$ time
5.	$m = A[i]$;	$O(1)$ time
6.	if ($i == n$)	$O(1)$ time
7.	do $i++$ n times	$O(n)$ time
8.	}	
9.	return m ;	$O(1)$ time

The worst-case time complexity of
「百般無聊擂台法」 is $\Theta(n)$.

non-tight analysis

$$\begin{aligned} & 3 \cdot O(1) + O(n) \cdot (3 \cdot O(1) + O(n)) \\ &= O(1) + O(n) \cdot O(n) \\ &= O(1) + O(n^2) \\ &= O(n^2) \end{aligned}$$

tight analysis

Step 3 takes $O(n)$ iterations for the for-loop, where only last iteration takes $O(n)$ time and the rest take $O(1)$ time.

The steps 3-8 take time

$$O(n) \cdot O(1) + 1 \cdot O(n) = O(n)$$

The same analysis holds for $\Omega(n)$

Algorithm Comparison

- Q: can we say that Algorithm 1 is a better algorithm than Algorithm 2 if
 - Algorithm 1 runs in $O(n)$ time
 - Algorithm 2 runs in $O(n^2)$ time
- A: No! The algorithm with a lower upper bound on its worst-case time does not necessarily have a lower time complexity.



Comparing A and B

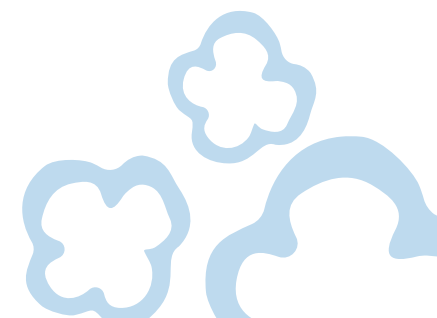
- Algorithm A is **no worse than** Algorithm B in terms of worst-case time complexity if there exists a positive function $f(n)$ s.t.
 - Algorithm A runs in time $O(f(n))$ &
 - Algorithm B runs in time $\Omega(f(n))$ in the worst case
 - Algorithm A is **(strictly) better than** Algorithm B in terms of worst-case time complexity if there exists a positive function $f(n)$ s.t.
 - Algorithm A runs in time $O(f(n))$ &
 - Algorithm B runs in time $\omega(f(n))$ in the worst case
- or
- Algorithm A runs in time $o(f(n))$ &
 - Algorithm B runs in time $\Omega(f(n))$ in the worst case





Problem Complexity

In the worst case, what is the growth of the function the optimal algorithm of the problem takes



Time Complexity of a Problem

- We say that the (worst-case) time complexity of Problem P is $\Theta(f(n))$ if
 1. The time complexity of Problem P is $O(f(n))$ &
 - There exists an $O(f(n))$ -time algorithm that solves Problem P
 2. The time complexity of Problem P is $\Omega(f(n))$
 - Any algorithm that solves Problem P requires $\Omega(f(n))$ time
- The time complexity of the champion problem is $\Theta(n)$ because
 1. The time complexity of the champion problem is $O(n)$ &
 - 「擂臺法」 is the $O(n)$ -time algorithm
 2. The time complexity of the champion problem is $\Omega(n)$
 - Any algorithm requires $\Omega(n)$ time to make each integer in comparison at least once

Optimal Algorithm

- If Algorithm A is an **optimal algorithm** for Problem P in terms of worst-case time complexity
 - Algorithm A runs in time $O(f(n))$ &
 - The time complexity of Problem P is $\Omega(f(n))$ in the worst case
- Examples (the champion problem)
 - 擂台法 → **optimal algorithm**
 - It runs in $O(n)$ time &
 - Any algorithm solving the problem requires time $\Omega(n)$ in the worst case
 - 百般無聊擂台法 → **optimal algorithm**
 - It runs in $O(n)$ time &
 - Any algorithm solving the problem requires time $\Omega(n)$ in the worst case

Comparing P and Q

- Problem P is **no harder than** Problem Q in terms of (worst-case) time complexity if there exists a function $f(n)$ s.t.
 - The (worst-case) time complexity of Problem P is $O(f(n))$ &
 - The (worst-case) time complexity of Problem Q is $\Omega(f(n))$
 - Problem P is **(strictly) easier than** Problem Q in terms of (worst-case) time complexity if there exists a function $f(n)$ s.t.
 - The (worst-case) time complexity of Problem P is $O(f(n))$ &
 - The (worst-case) time complexity of Problem Q is $\omega(f(n))$
- or
- The (worst-case) time complexity of Problem P is $o(f(n))$ &
 - The (worst-case) time complexity of Problem Q is $\Omega(f(n))$



Concluding Remarks

- Algorithm Design and Analysis Process

- 1) Formulate a **problem**
- 2) Develop an **algorithm**
- 3) Prove the **correctness**
- 4) Analyze **running time/space** requirement

Design Step

Analysis Step

- Usually brute force (暴力法) is not very efficient

- Analysis Skills

- Prove by contradiction
- Induction
- Asymptotic analysis
- Problem instance

- Algorithm Complexity

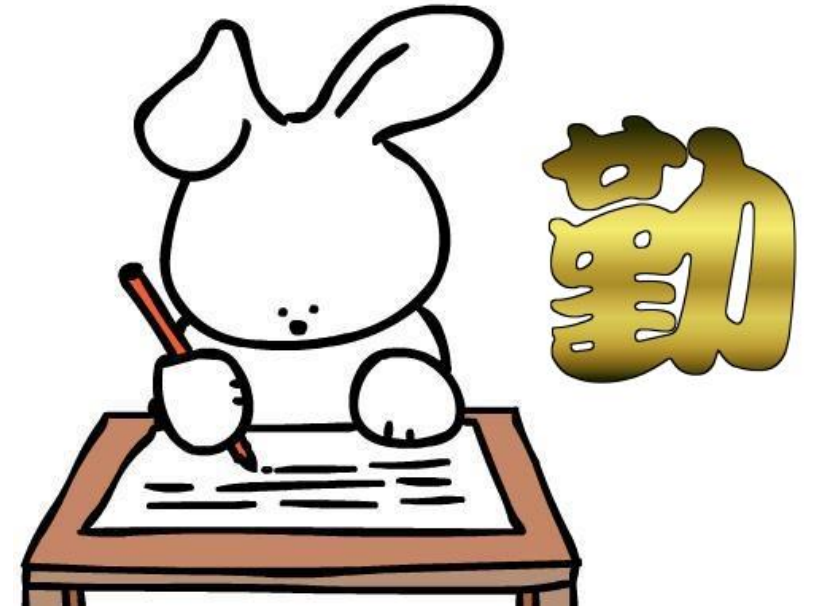
- In the worst case, what is the growth of function an algorithm takes

- Problem Complexity

- In the worst case, what is the growth of the function the optimal algorithm of the problem takes

Reading Assignment

- Textbook Ch. 3 – Growth of Function





Question?

Important announcement will be sent to
@ntu.edu.tw mailbox & post to the course website

Course Website: <http://ada.miulab.tw>
Email: ada-ta@csie.ntu.edu.tw