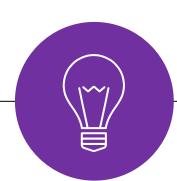
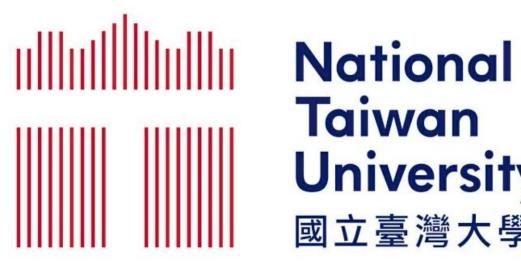
Word Embeddings

March 22nd, 2021 http://adl.miulab.tw















Meaning Representations in Computers

- Knowledge-based representation
- **Corpus-based representation**
 - Atomic symbol \checkmark
 - Neighbors \checkmark

3

- High-dimensional sparse word vector
- Low-dimensional dense word vector
 - Method 1 dimension reduction Ο
 - Method 2 direct learning Ο



Meaning Representations in Computers

Knowledge-based representation

Corpus-based representation

Atomic symbol \checkmark

Neighbors

4

- High-dimensional sparse word vector
- Low-dimensional dense word vector
 - Method 1 dimension reduction \bigcirc
 - Method 2 direct learning Ο





Atomic symbols: *one-hot* representation

car [0 0 0 0 0 0

Issues: difficult to compute the similarity (i.e. comparing "car" and "motorcycle")

car

Idea: words with similar meanings often have similar neighbors

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motorcycle



Meaning Representations in Computers

- Knowledge-based representation
- **Corpus-based representation**
 - Atomic symbol
 - Neighbors \checkmark

6

- High-dimensional sparse word vector
- Low-dimensional dense word vector
 - Method 1 dimension reduction \bigcirc
 - Method 2 direct learning Ο



Window-based Co-occurrence Matrix

Example

7

- Window length=1
- Left or right context
- Corpus:

love NTU.

I love deep learning.

enjoy learning.

Issues:

- matrix size increases with vocabulary
- high dimensional
- sparsity \rightarrow poor robustness

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similarity > 0

Counts		love	enjoy	NTU	deep	learning
	0	2	1	0	0	0
love	2	0	0	1	1	0
enjoy	1	0	0	0	0	1
NTU	0	1	0	0	0	0
deep	0	1	0	0	0	1
learning	0	0	1	0	1	0

Idea: low dimensional word vector





Meaning Representations in Computers

- Knowledge-based representation
- **Corpus-based representation**
 - Atomic symbol
 - Neighbors \checkmark

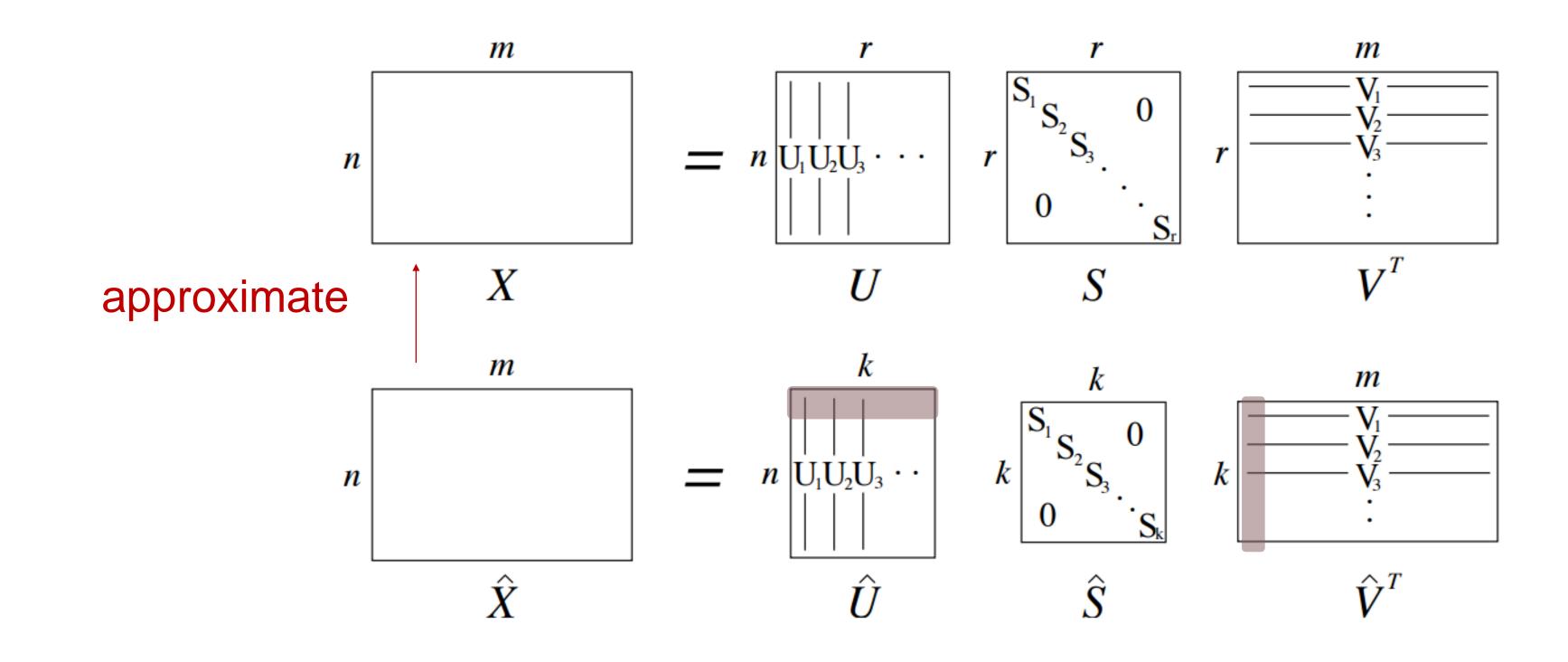
8

- High-dimensional sparse word vector
- Low-dimensional dense word vector
 - Method 1 dimension reduction 0
 - Method 2 direct learning Ο



Low-Dimensional Dense Word Vector 9

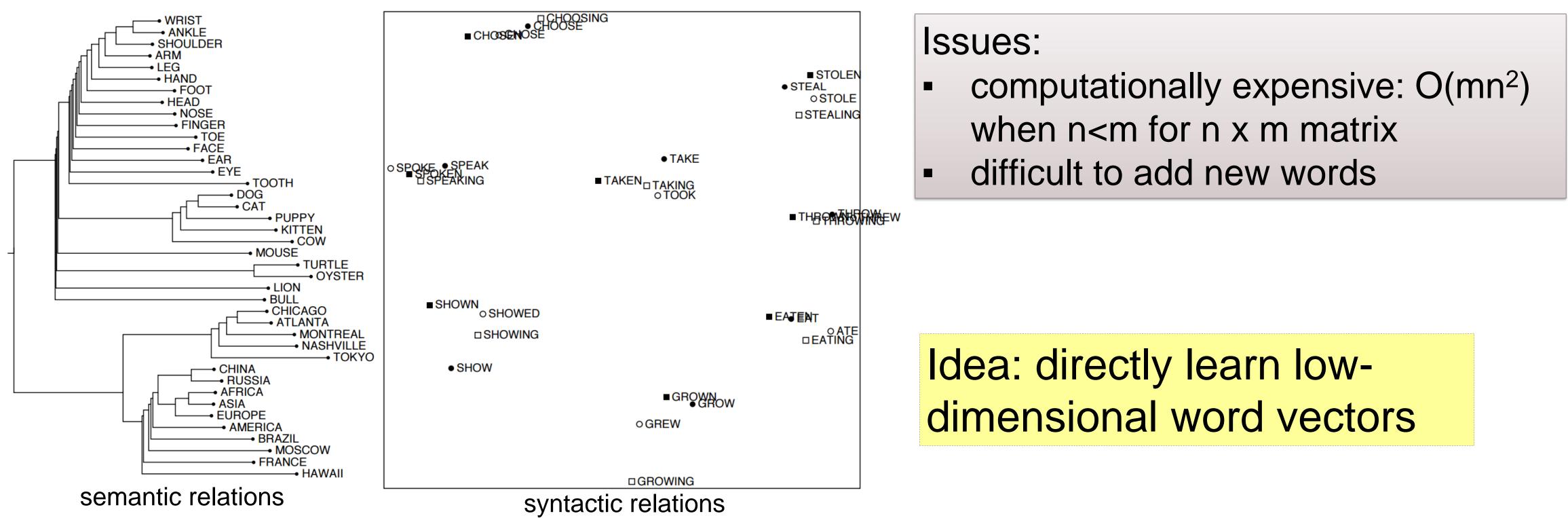
- Method 1: dimension reduction on the matrix
- Singular Value Decomposition (SVD) of co-occurrence matrix X





Low-Dimensional Dense Word Vector 10

Method 1: dimension reduction on the matrix Singular Value Decomposition (SVD) of co-occurrence matrix X





Word Representation 11

- Knowledge-based representation
- **Corpus-based representation**
 - Atomic symbol \checkmark
 - Neighbors \checkmark
 - High-dimensional sparse word vector
 - Low-dimensional dense word vector
 - Method 1 dimension reduction Ο
 - Method 2 direct learning \rightarrow word embedding Ο



Word Embedding

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Method 2: directly learn low-dimensional word vectors Learning representations by back-propagation. (Rumelhart et al., 1986) 0 A neural probabilistic language model (Bengio et al., 2003) 0 NLP (almost) from Scratch (Collobert & Weston, 2008) Ο

- 0 (Pennington et al., 2014)

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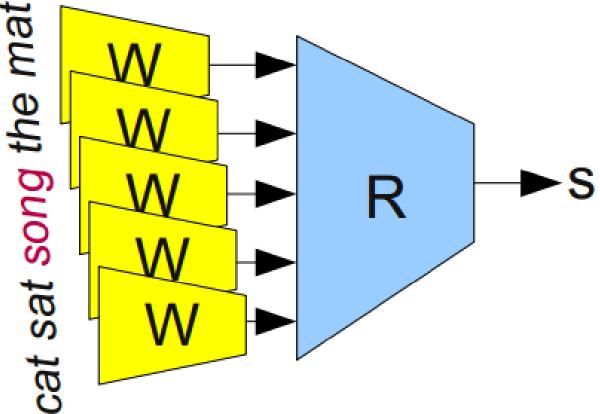
Recent and most popular models: word2vec (Mikolov et al. 2013) and Glove



Word Embedding Benefit

13

Given an <u>unlabeled</u> training corpus, produce a vector for each word that encodes its semantic information. These vectors are useful because: 1) semantic similarity between two words can be calculated as the cosine similarity between their corresponding word vectors 2) word vectors as powerful features for various supervised NLP tasks since the vectors contain semantic information 3) propagate any information into them via neural networks and update during training







Word Embeddings Word2Vec





Word2Vec – Skip-Gram Model 15

- Goal: predict surrounding words within a window of each word
- current center word

$$w_{1}, w_{2}, \cdots, w_{t-m}, \cdots, w_{t-1}, w_{t} w_{t+1}, \cdots, w_{t+m}, \cdots, w_{T-1}, w_{T}$$

$$w_{I} c w_{O}$$

$$w_{O}$$

$$w_{1}, w_{2}, \cdots, w_{t-m}, \cdots, w_{t-1}, w_{t} w_{t+1}, \cdots, w_{t+m}, \cdots, w_{T-1}, w_{T}$$

$$w_{I} C w_{O}$$

$$p(w_{O,1}, w_{O,2}, \cdots, w_{O,C} \mid w_{I}) = \prod_{c=1}^{C} p(w_{O,c} \mid w_{I})$$

$$target word vector$$

$$C(\theta) = -\sum_{w_{I}} \sum_{c=1}^{C} \log p(w_{O,c} \mid w_{I})$$

$$p(w_{O} \mid w_{I}) = \frac{\exp(v_{w_{O}}^{'T} v_{w_{I}})}{\sum_{j} \exp(v_{w_{j}}^{'T} v_{w_{I}})}$$
outside target word

$$w_{1}, w_{2}, \cdots, \underbrace{w_{t-m}, \cdots, w_{t-1}, w_{t}}_{W_{I}} \underbrace{w_{t+1}, \cdots, w_{t+m}}_{context window}, \cdots, w_{T-1}, w_{T}$$

$$p(w_{O,1}, w_{O,2}, \cdots, w_{O,C} \mid w_{I}) = \prod_{c=1}^{C} p(w_{O,c} \mid w_{I})$$

$$target word vector$$

$$C(\theta) = -\sum_{w_{I}} \sum_{c=1}^{C} \log p(w_{O,c} \mid w_{I})$$

$$p(w_{O} \mid w_{I}) = \frac{\exp(v_{w_{O}}^{\prime T} \underbrace{v_{w_{I}}}_{\sum_{j} \exp(v_{w_{j}}^{\prime T} v_{w_{I}})})$$

$$outside target word$$

Benefit: faster, easily incorporate a new sentence/document or add a word to vocab

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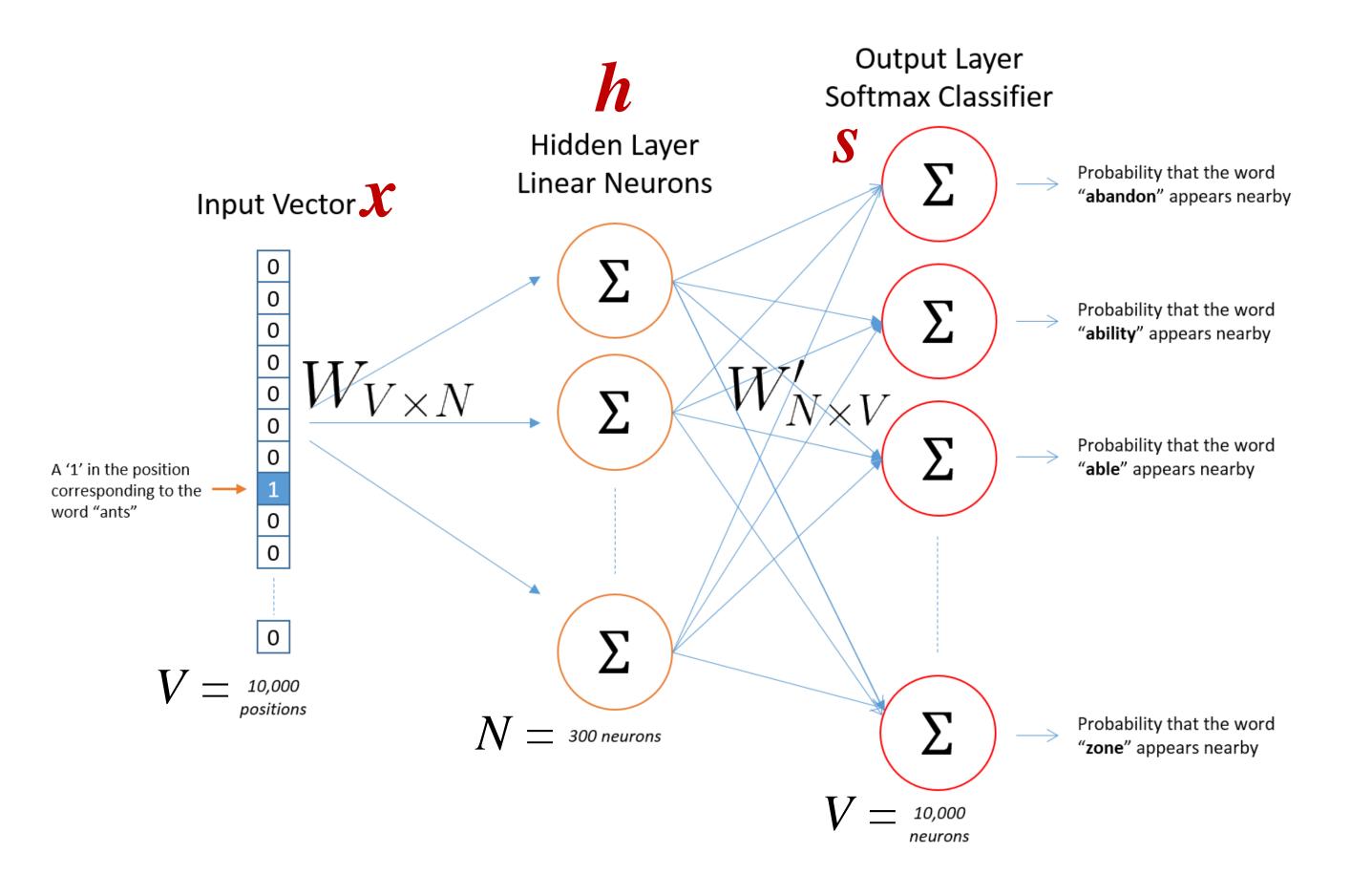
Objective function: maximize the probability of any context word given the







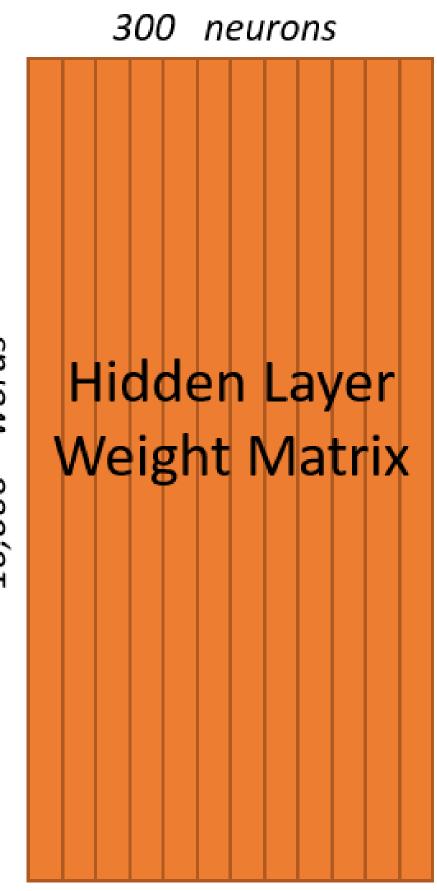
Goal: predict surrounding words within a window of each word







Slido: #ADL2021 Hidden Layer Matrix \rightarrow Word Embedding Matrix



words 10,000 $W_{V \times N}$

300 features words Word Vector Lookup Table! 10,000



Weight Matrix Relation 18

Hidden layer weight matrix = word vector lookup

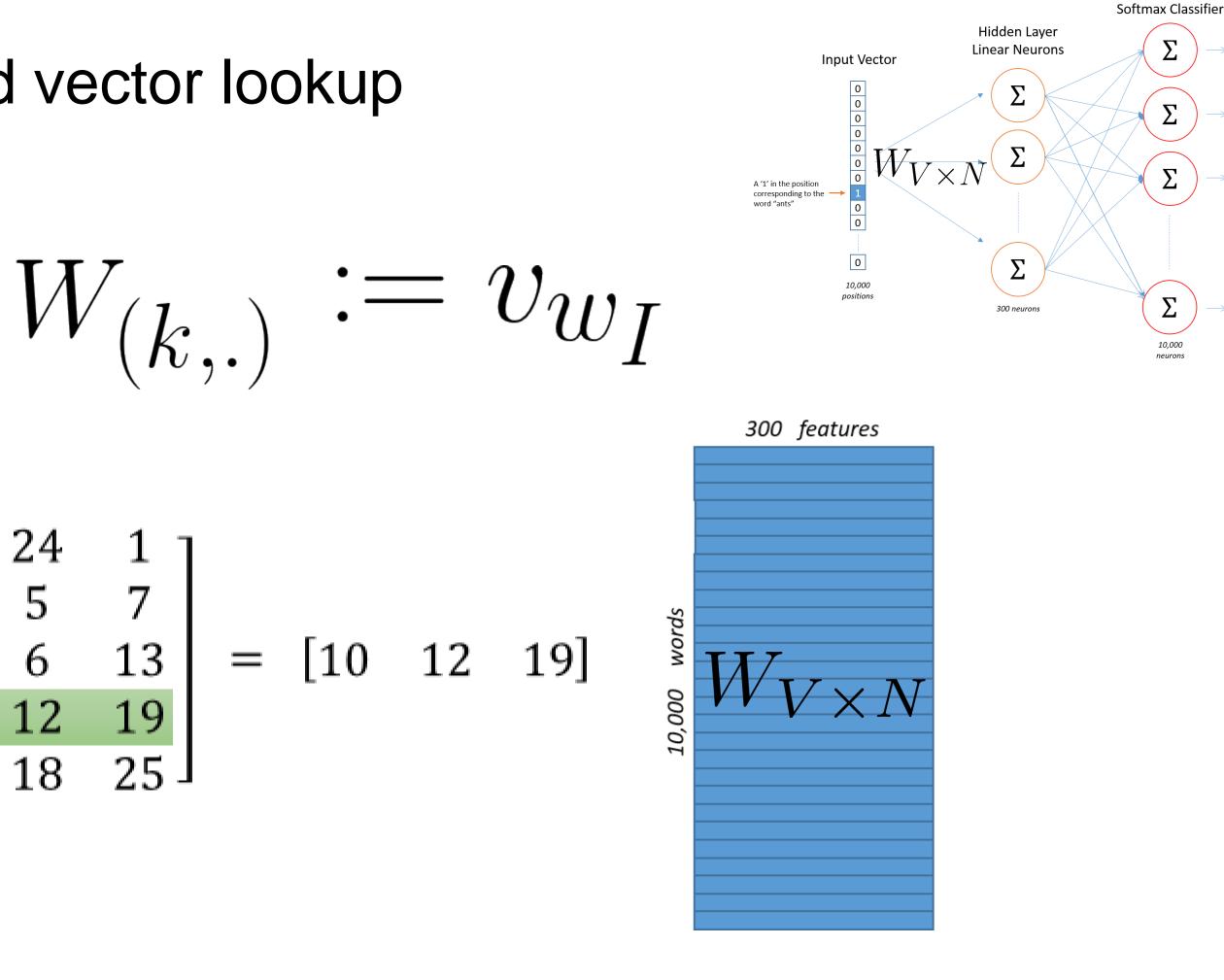
$$h = x^T W = \mathbf{I}$$

 $\begin{bmatrix} 0 & 0 & 0 & 1 & 0 \end{bmatrix} \times \begin{bmatrix} 17 & 24 & 1 \\ 23 & 5 & 7 \\ 4 & 6 & 13 \\ 10 & 12 & 19 \end{bmatrix} = \begin{bmatrix} 10 & 12 & 19 \end{bmatrix}$ 18

Each vocabulary entry has two vectors: as a target word and as a context word

Slido: #ADL2021

Output Layer





Probability that the word "abandon" appears nearby

Probability that the word "ability" appears nearby

Probability that the word "able" appears nearby

Probability that the word "zone" appears nearby

Weight Matrix Relation 19

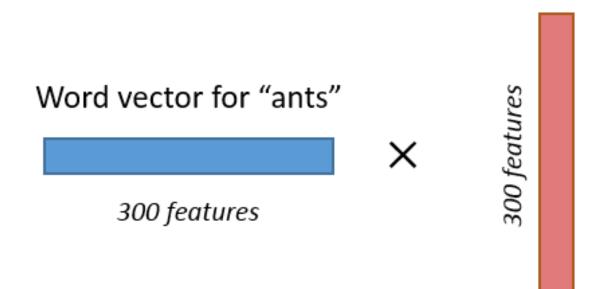
Output layer weight matrix = weighted sum as final score

$$s_j = h v'_{w_j}$$

$$p(w_j = w_{O,c} \mid w_I) = q$$

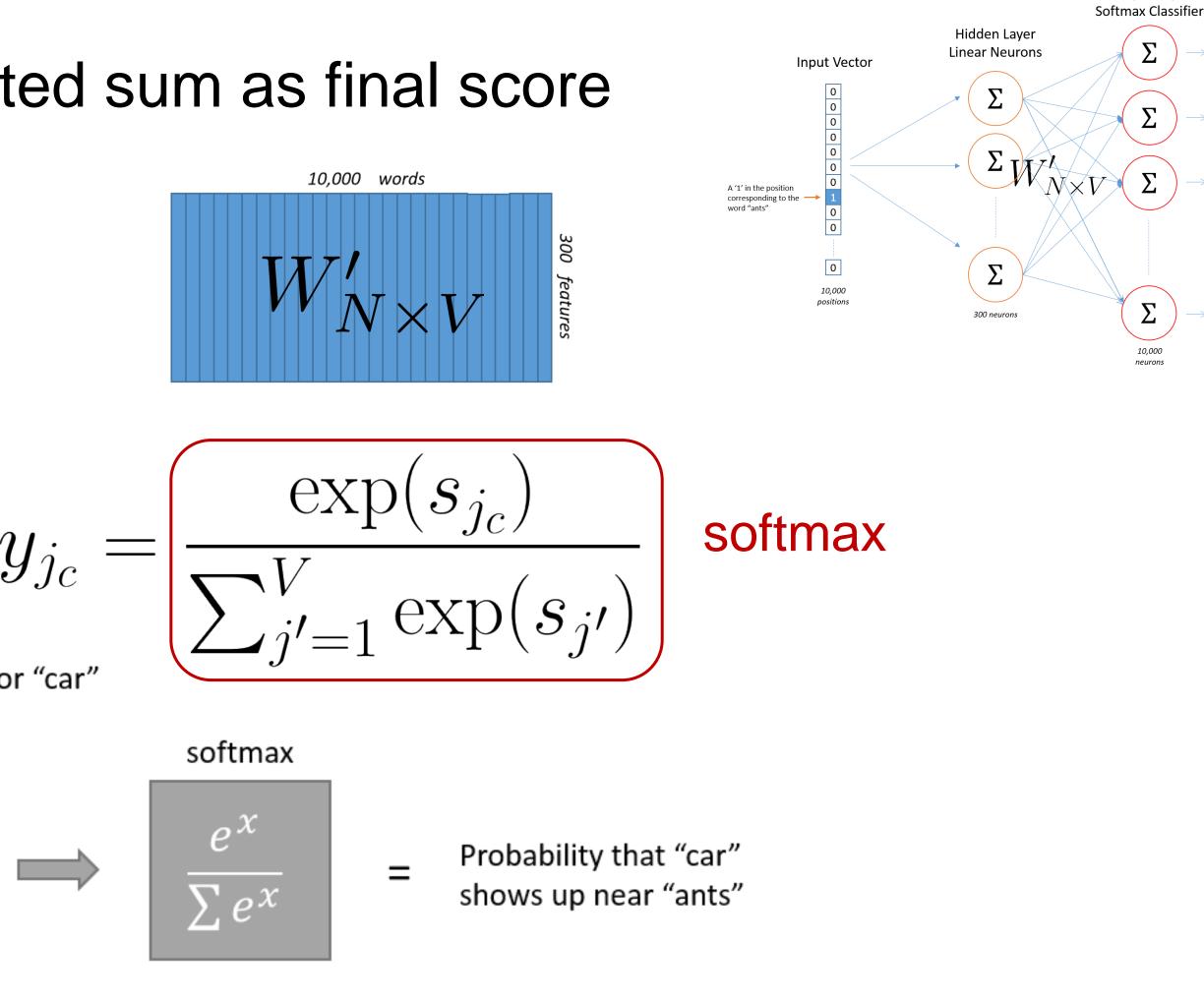
within the context window

Output weights for "car"



Slido: #ADL2021

Output Layer



Each vocabulary entry has two vectors: as a target word and as a context word



Probability that the word "abandon" appears nearby

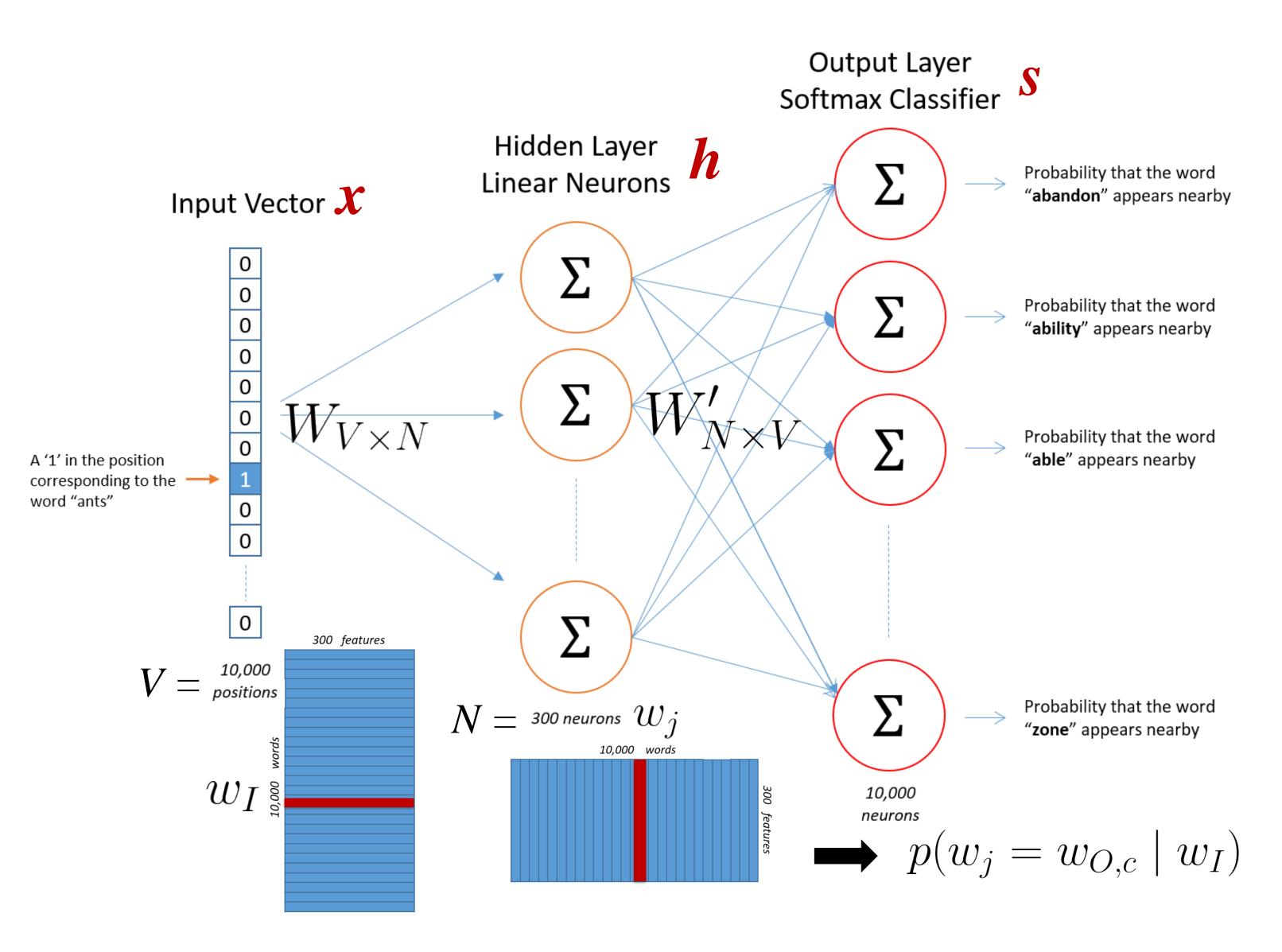
Probability that the word "ability" appears nearby

Probability that the word "able" appears nearby

Probability that the word "zone" appears nearby

Word2Vec Skip-Gram Illustration

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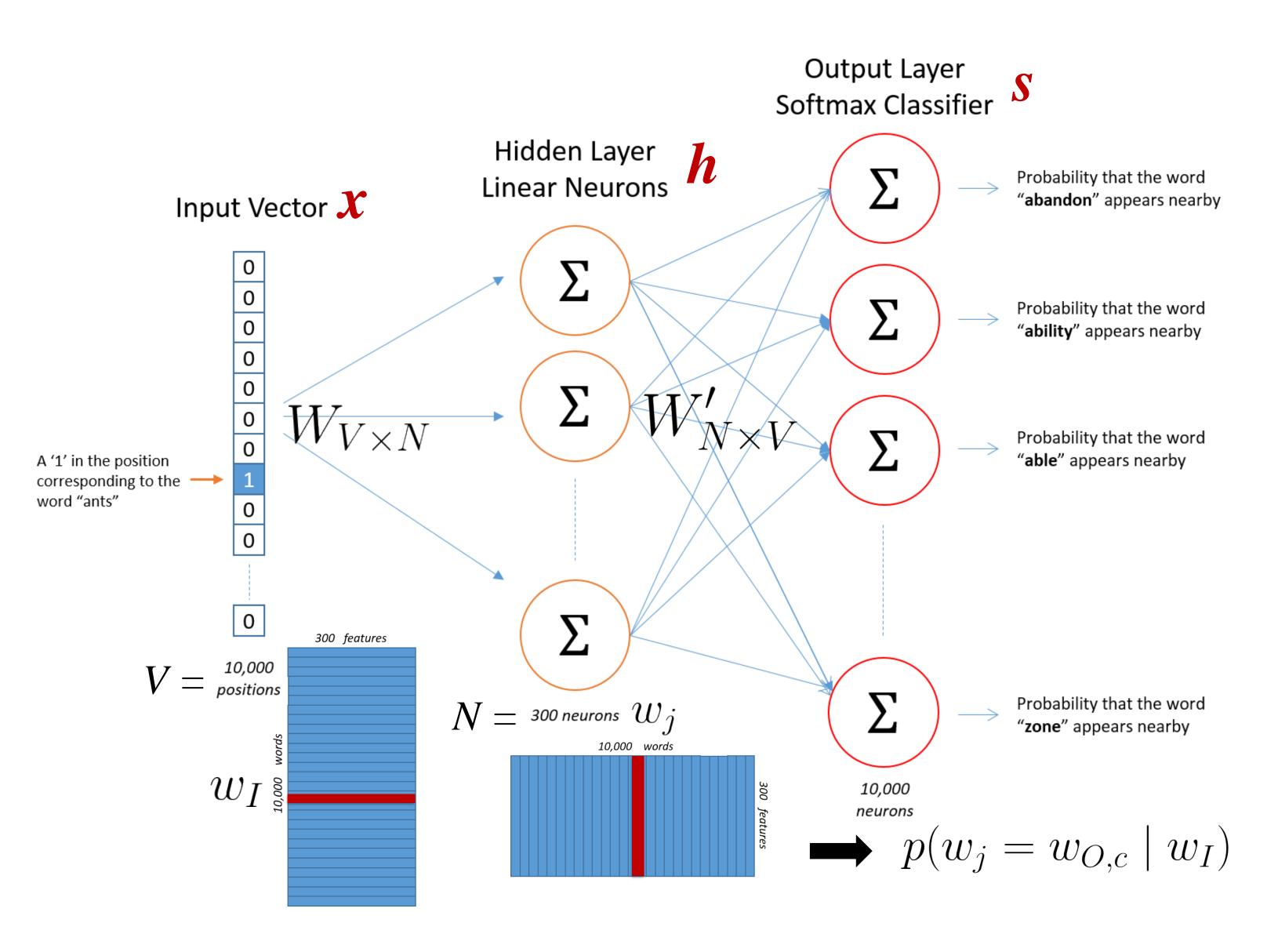


Word Embeddings 21 Word2Vec Training





Word2Vec Skip-Gram Illustration







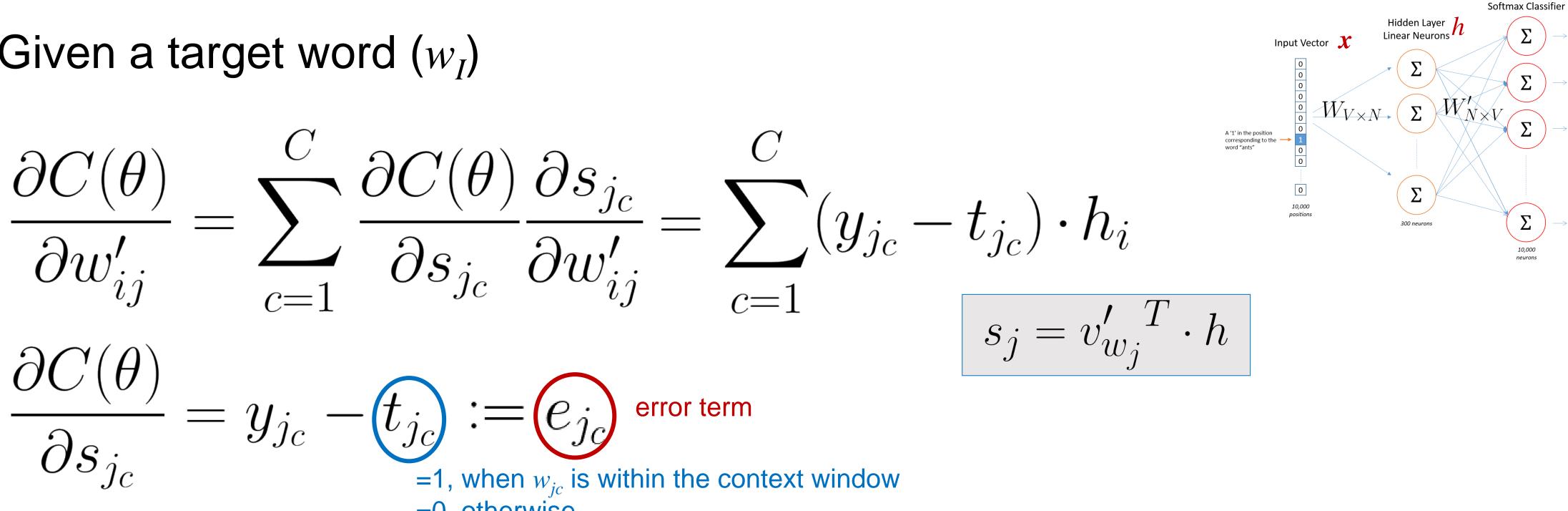
Given a target word (w_I)

 $C(\theta) = -\log p(w_{O,1}, w_{O,2}, \cdots, w_{O,C} \mid w_I)$ $= -\log \prod_{c=1}^{C} \frac{\exp(s_{j_c})}{\sum_{j'=1}^{V} \exp(s_{j'})}$ C $= -\sum s_{j_c} + C \log \sum \exp(s_{j'})$ c=1i'=1



SGD Update for W' 24

Given a target word (w_I)



=0, otherwise

$$w'_{ij}{}^{(t+1)} = w'_{ij}{}^{(t)} - \eta$$

Slido: #ADL2021

$$\sum_{c=1}^{C} (y_{j_c} - t_{j_c}) \cdot h_i$$



Output Layer

Probability that the word andon" appears near

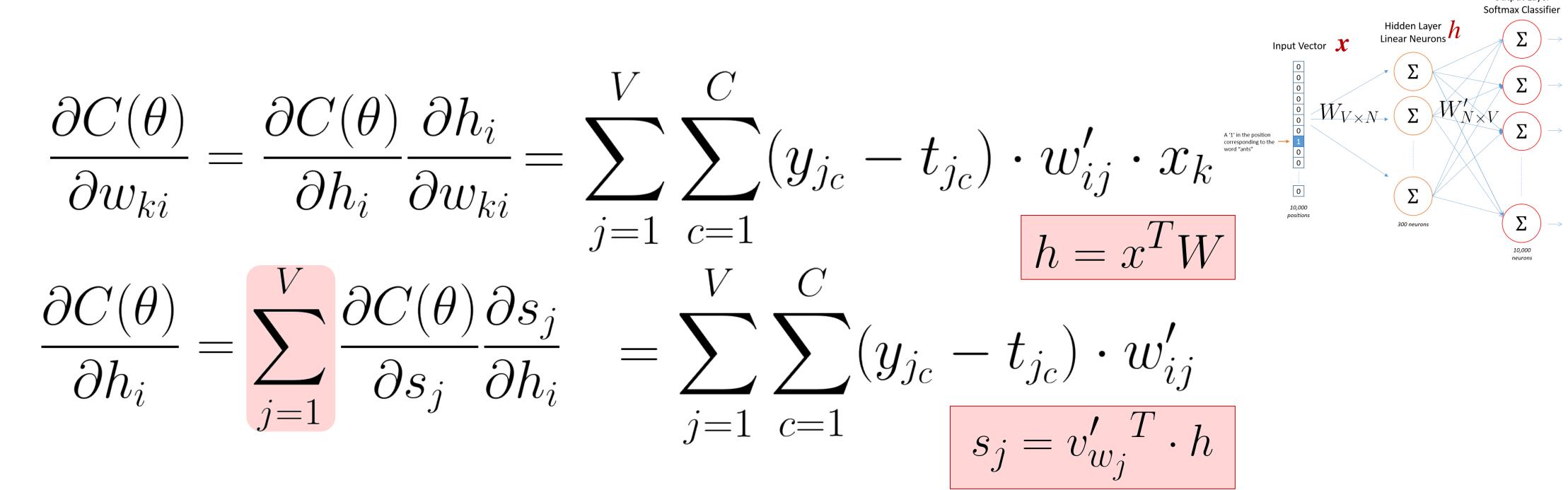
Probability that the word ability" appears near

Probability that the word "able" appears nearby

Probability that the word "zone" appears nearby



SGD Update for W



 $w_{ij}^{(t+1)} = w_{ij}^{(t)} - \eta \cdot \mathbf{y}$ j=

Slido: #ADL2021

$$\sum_{i=1}^{C} \sum_{c=1}^{C} (y_{j_c} - t_{j_c}) \cdot w'_{ij} \cdot x_j$$



Probability that the word "**abandon**" appears nearby

Probability that the word "**ability**" appears nearby

Probability that the word "**able**" appears nearby

Probability that the word "zone" appears nearby

$$6 - SGD Update$$

$$w_{ij}^{\prime(t+1)} = w_{ij}^{\prime(t)} - \eta \cdot \sum_{c=1}^{C} (y_{jc} - t_{jc}) \cdot h_i \left[EI_j = \sum_{c=1}^{C} (y_{jc} - t_{jc}) \right]$$

$$v_{wj}^{\prime(t+1)} = v_{wj}^{\prime(t)} - \eta \cdot EI_j \cdot h$$

$$w_{ij}^{(t+1)} = w_{ij}^{(t)} - \eta \cdot \sum_{j=1}^{V} \sum_{c=1}^{C} (y_{jc} - t_{jc}) \cdot w_{ij}^{\prime} \cdot x_j$$

$$v_{wI}^{(t+1)} = v_{wI}^{(t)} - \eta \cdot EH^T$$

$$EH_i = \sum_{j=1}^{V} EI_j \cdot w_{ij}^{\prime} \cdot x_j$$

large vocabularies or large training corpora \rightarrow expensive computations

limit the number of output vectors that must be updated per training instance \rightarrow hierarchical softmax, sampling

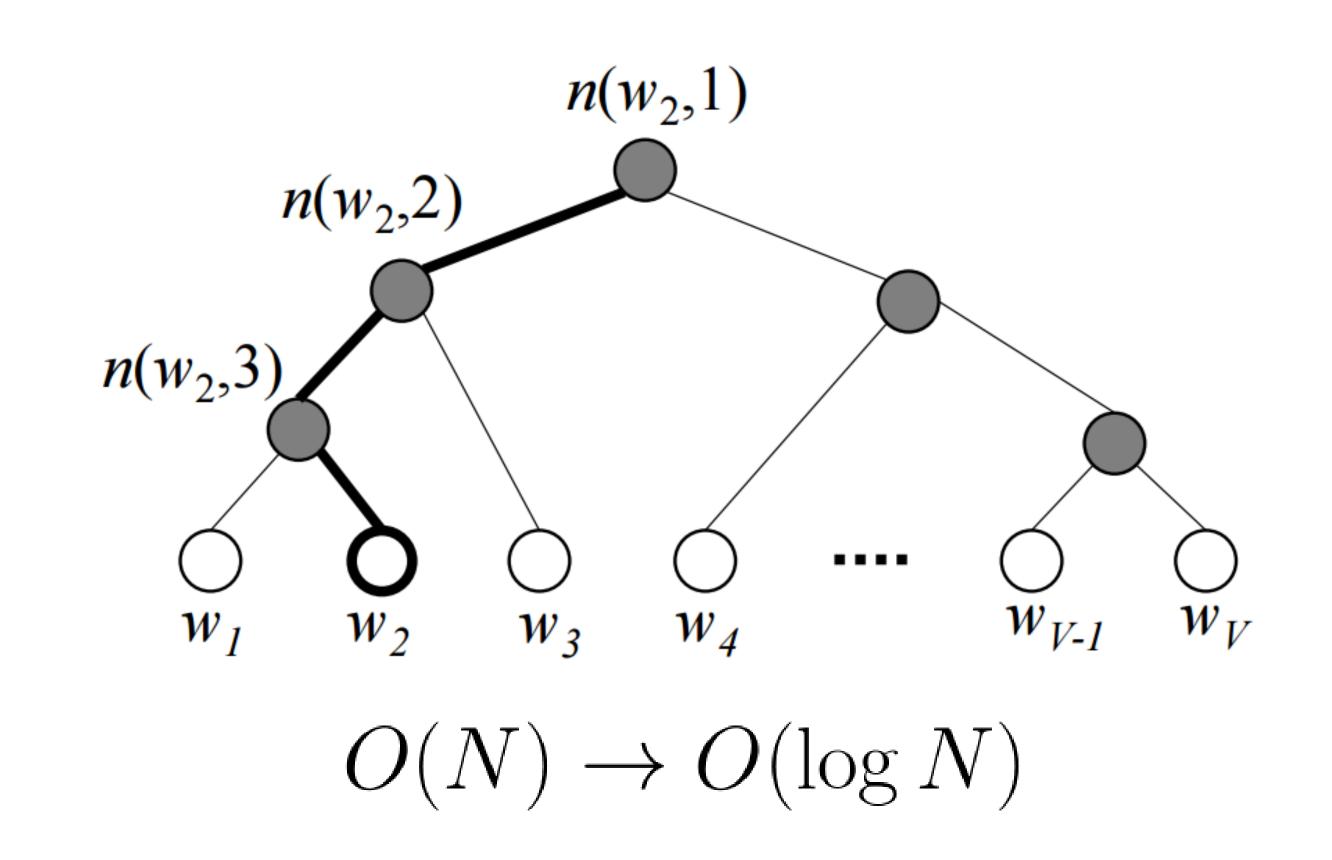


Word Embeddings 27 **Negative Sampling**





Idea: compute the probability of leaf nodes using the paths



Mikolov et al., "Distributed representations of words and phrases and their compositionality," in NIPS, 2013.





29 **Negative Sampling**

Idea: only update a sample of output vectors

$$C(\theta) = -\log \sigma(v'_{w_O}{}^T v_{w_I}) + \sum_{w_j \in \mathcal{W}_{neg}} \log \sigma(v'_{w_j}{}^T v_{w_I})$$
$$\frac{v'_{w_j}{}^{(t+1)} = v'_{w_j}{}^{(t)} - \eta \cdot EI_j \cdot h}{v_{w_I}{}^{(t+1)} = v_{w_I}{}^{(t)} - \eta \cdot EH^T}$$
$$EI_j = \sigma(v'_{w_j}{}^T v_{w_I}) - t_j$$
$$EH = \sum_{w_j \in \{w_O\} \cup \mathcal{W}_{neg}} EI_j \cdot v'_{w_j}$$
$$w_j \in \{w_O\} \cup \mathcal{W}_{neg}$$

Mikolov et al., "Distributed representations of words and phrases and their compositionality," in NIPS, 2013.



Negative Sampling 30

- Sampling methods
 - Random sampling $w_i \in \{w_O\} \cup \mathcal{W}_{neg}$ 0
 - Ο

Idea: less frequent words sampled more often

Empirical setting: unigram model raised to the power of 3/4

Word	Probabi
is	
constitution	
bombastic	

Mikolov et al., "Distributed representations of words and phrases and their compositionality," in NIPS, 2013.

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Distribution sampling: w_i is sampled from P(w) What is a good P(w)?

ility to be sampled for "neg"

 $0.9^{3/4} = 0.92$ $0.09^{3/4} = 0.16$

 $0.01^{3/4} = 0.032$





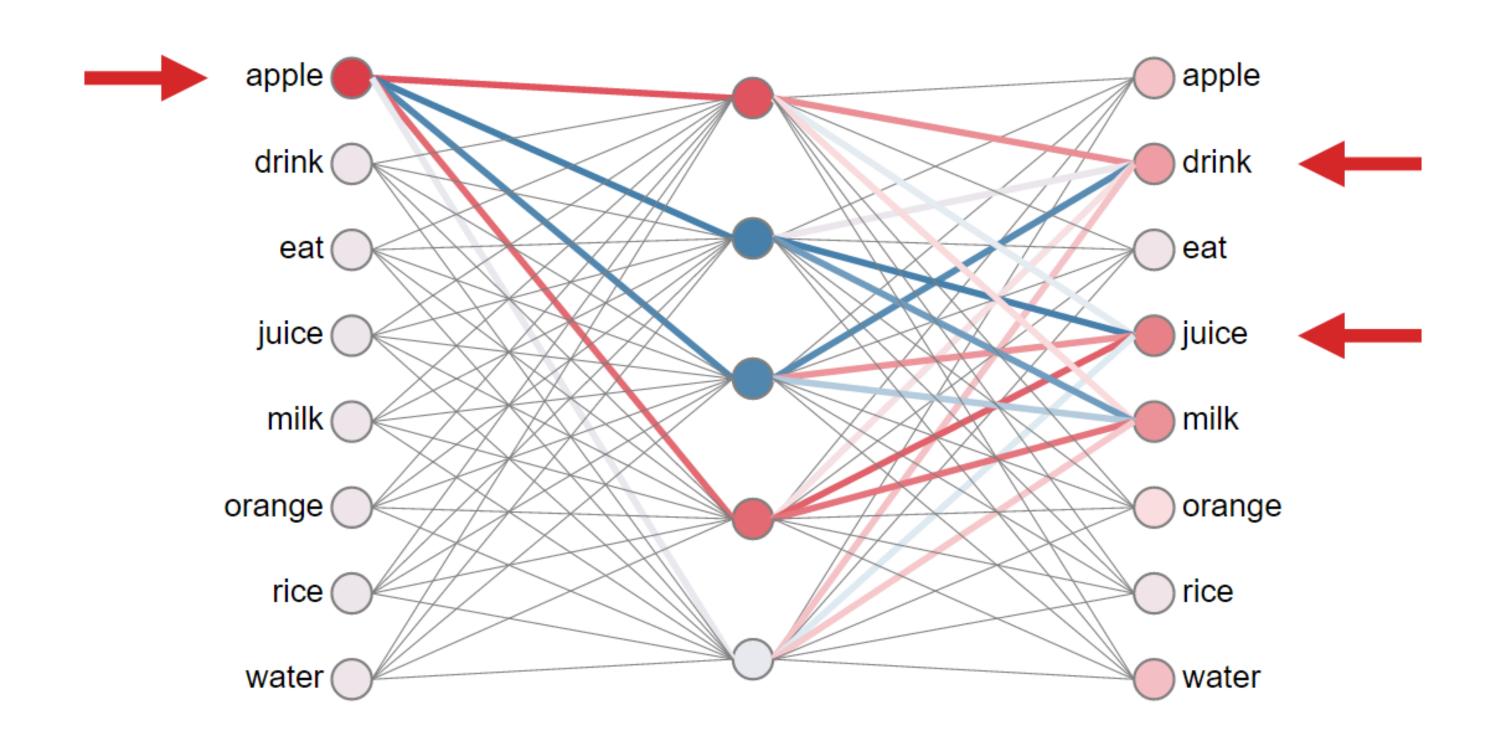
Word Embeddings 31 Word2Vec Variants





Word2Vec Skip-Gram Visualization https://ronxin.github.io/wevi/

Skip-gram training data: e^water



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apple|drink^juice,orange|eat^apple,rice|drink^juice,juice|drink^milk,milk|drink^rice,water|drink^mil k,juice|orange^apple,juice|apple^drink,milk|rice^drink,drink|milk^water,drink|water^juice,drink|juic

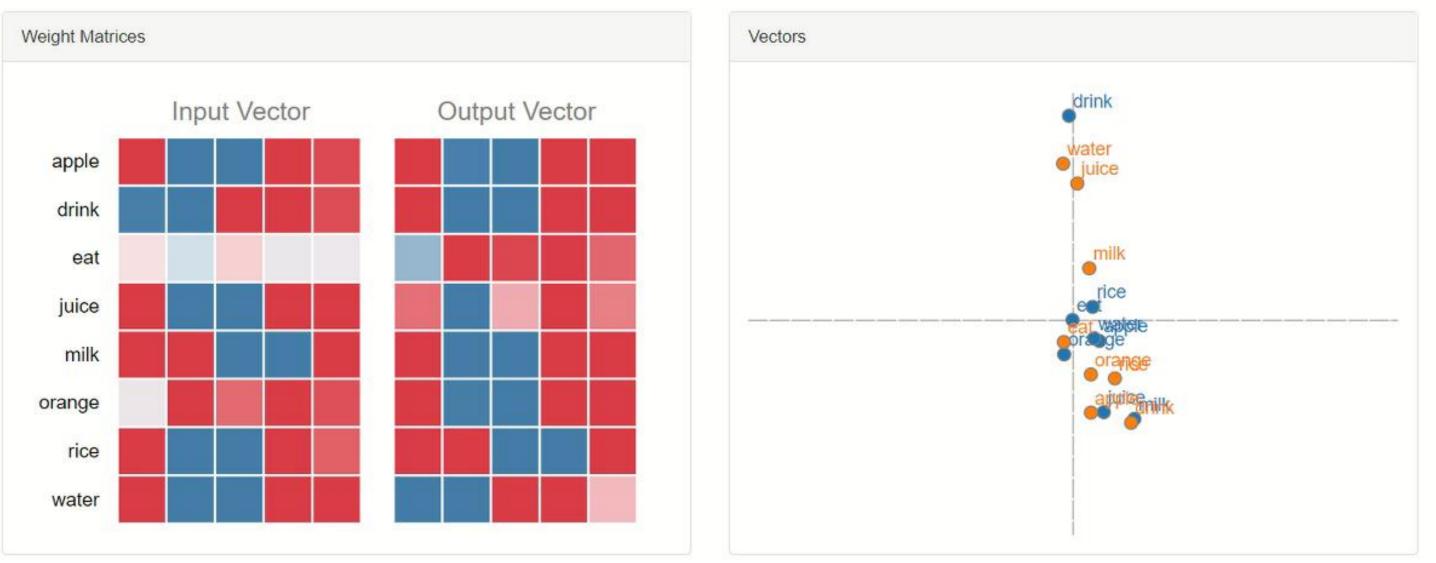


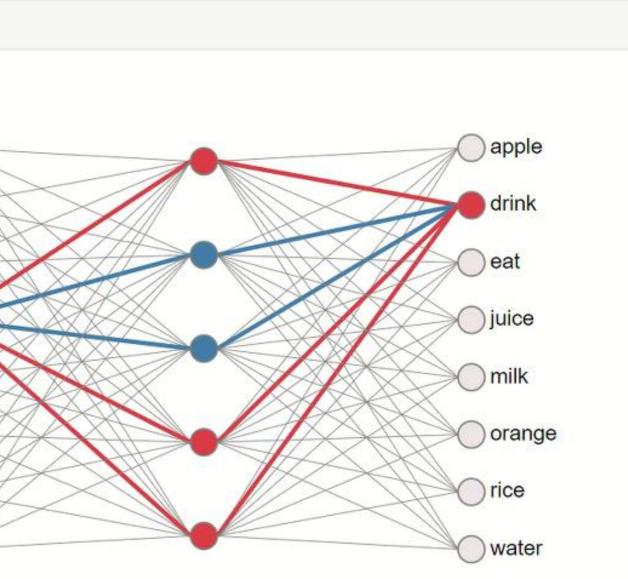


wevi: word embedding visual inspector

Everything you need to know about this tool - Source code

Control Panel	Neurons
Config:	
{"hidden_size":5,"random_state":1,"learning_rate":0 .2}	apple
Training data (context target):	drink
apple/drink^juice,orange/eat^apple,rice/drink^juice,j	eat
uice drink^milk,milk drink^rice,water drink^milk,juice orange^apple,juice apple^drink,milk rice^drink,drink milk^water,drink water^juice,drink juice^water	juice
Presets: Fruit and juice (Skip-gram) v	milk
Update and Restart Update Learning Rate	orange
Next 20 100 500 PCA	rice
	water







Word2Vec Variants

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2013)

 $p(w_{t-m}, \cdots w_{t-1}, w_t)$

- surrounding words (Mikolov+, 2013)
- contexts (Mikolov+, 2013)

$$p(w_{t+1} \mid w_t)$$

Practice the derivation by yourself!!

Mikolov et al., "Efficient estimation of word representations in vector space," in ICLR Workshop, 2013. Mikolov et al., "Linguistic regularities in continuous space word representations," in NAACL HLT, 2013.

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Skip-gram: predicting surrounding words given the target word (Mikolov+,

$$w_{t+1}, \cdots, w_{t+m} \mid w_t)$$

CBOW (continuous bag-of-words): predicting the target word given the

 $p(w_t \mid w_{t-m}, \cdots, w_{t-1}, w_{t+1}, \cdots, w_{t+m})$ LM (Language modeling): predicting the next words given the proceeding

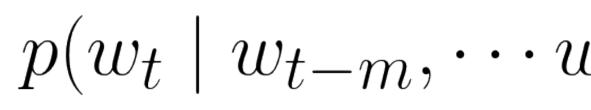


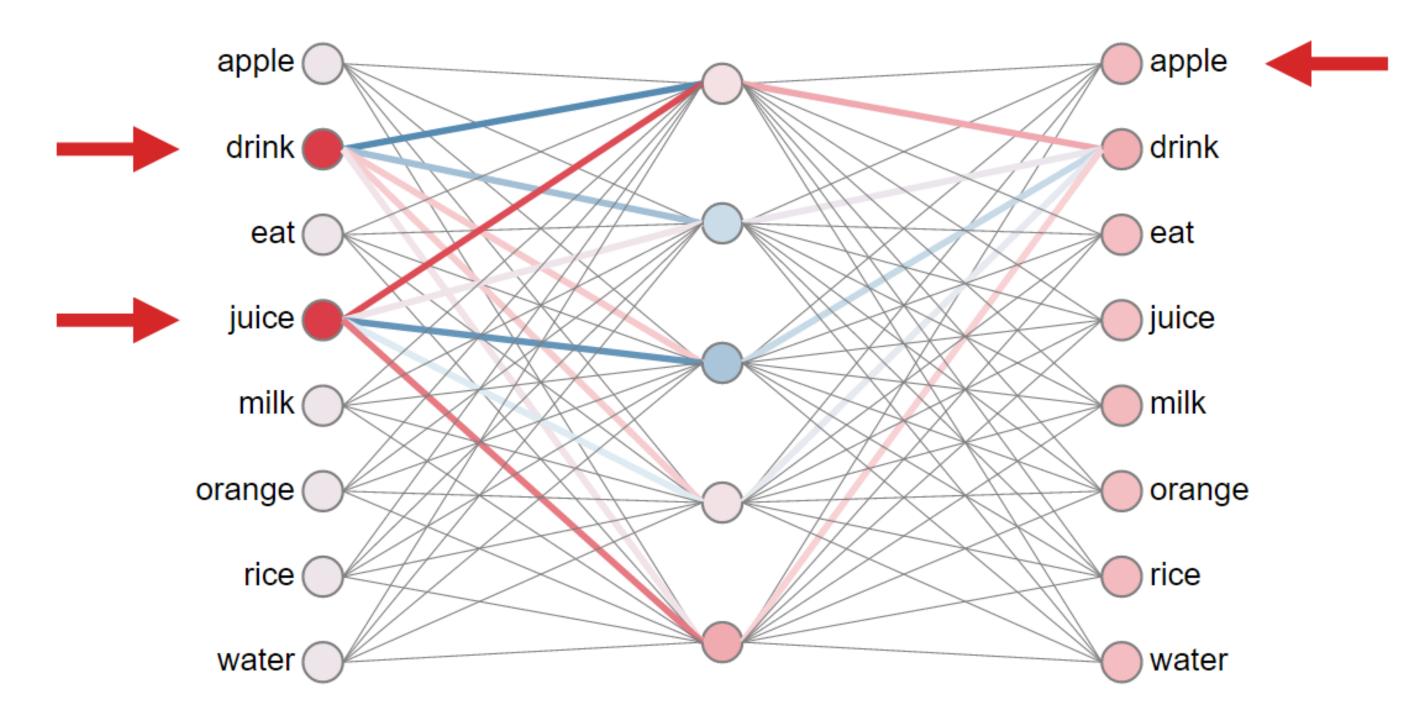






Goal: predicting the target word given the surrounding words



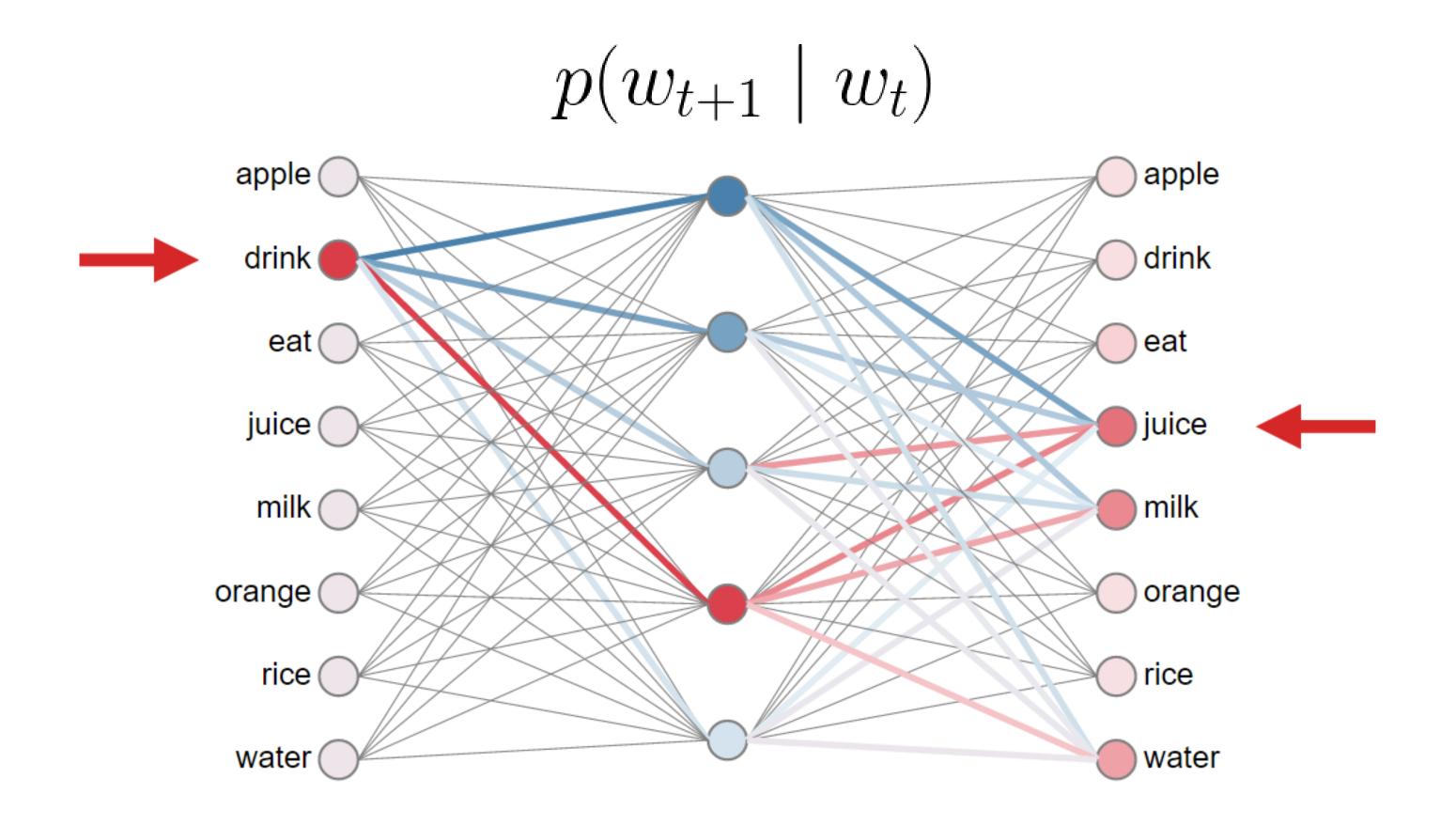


$$v_{t-1}, w_{t+1}, \cdots, w_{t+m}$$





Goal: predicting the next words given the proceeding contexts











Count-based

- LSA, HAL (Lund & Burgess), COALS (Rohde et al), Hellinger-PCA (Lebret & Collobert)
- Pros \bigcirc
 - Fast training
 - Efficient usage of statistics
- Cons \bigcirc
 - Primarily used to capture word similarity
 - Disproportionate importance given to large counts

Combining the benefits from both worlds \rightarrow GloVe

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Direct prediction

NNLM, HLBL, RNN, Skipgram/CBOW 0 (Bengio et al; Collobert & Weston; Huang et al; Mnih & Hinton; Mikolov et al; Mnih & Kavukcuoglu)

Pros \bigcirc

- Generate improved performance on other tasks
- Capture complex patterns beyond word similarity

Cons \bigcirc

- Benefits mainly from large corpus
- Inefficient usage of statistics







- Idea: ratio of co-occurrence probability can encode meaning
- P_{ii} is the probability that word w_i appears in the context of word w_i

$$P_{ij} = P(w_j$$

Relationship between the words w_i and w_j

	x = solid	x = gas	x = water	x = random
$P(x \mid ice)$	large	small	large	small
$P(x \mid \text{stream})$	small	large	large	small
$\frac{P(x \mid \text{ice})}{P(x \mid \text{stream})}$	large	small	~ 1	~ 1

Pennington et al., "GloVe: Global Vectors for Word Representation," in EMNLP, 2014.

$$w_i) = X_{ij}/X_i$$





The relationship of w_i and w_j approximates the ratio of their co-occurrence probabilities with various w_k

$$F(w_i, w_j, \tilde{w}_k) = \frac{P_{ik}}{P_{jk}}$$

$$F(w_i - w_j, \tilde{w}_k) = \frac{P_{ik}}{P_{jk}}$$

$$F((v_{w_i} - v_{w_j})^T v'_{\tilde{w}_k}) = \frac{P_{ik}}{P_{jk}} \quad F(\cdot) = \exp(\cdot)$$

$$v_{w_i} \cdot v'_{\tilde{w}_k} = v_{w_i}^T v'_{\tilde{w}_k} = \log P(w_k \mid w_i)$$

Pennington et al., "GloVe: Global Vectors for Word Representation," in EMNLP, 2014.







$$v_{w_{i}} \cdot v_{\tilde{w}_{j}}' = v_{w_{i}}^{T} v_{\tilde{w}_{j}}' = \log P(w_{j} \mid w_{i}) \qquad P_{ij} = X_{ij}/X_{i}$$
$$= \log P_{ij} = \log(X_{ij}) - \log(X_{i})$$
$$v_{w_{i}}^{T} v_{\tilde{w}_{j}}' + b_{i} + \tilde{b}_{j} = \log(X_{ij})$$
$$C(\theta) = \sum_{i,j=1}^{V} f(P_{ij})(v_{w_{i}} \cdot v_{\tilde{w}_{j}}' - \log P_{ij})^{2}$$
$$C(\theta) = \sum_{i,j=1}^{V} f(X_{ij})(v_{w_{i}}^{T} v_{\tilde{w}_{j}}' + b_{i} + \tilde{b}_{j} - \log X_{ij})^{2}$$

Pennington et al., "GloVe: Global Vectors for Word Representation," in EMNLP, 2014.

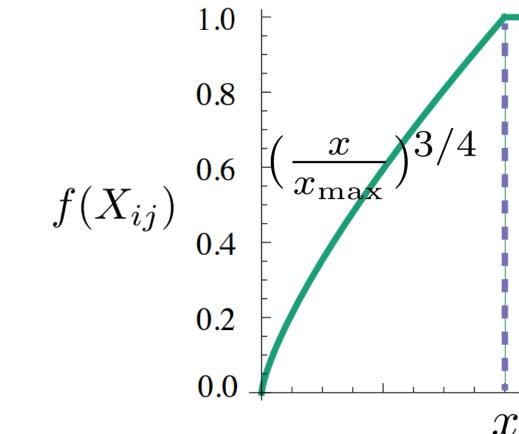


Slido: #ADL2021 42 **GIOVe – Weighted Least Squares Regression Model**

 $C(\theta) = \sum f(X_{ij})(v_{w_i}^T v_{\tilde{w}_j}' + b_i + \tilde{b}_j - \log X_{ij})^2$ i.i=1

Weighting function should obey f(0) = 0

f(x) should be non-decreasing so that rare co-occurrences are not overweighted



fast training, scalable, good performance even with small corpus, and small vectors

Pennington et al., "GloVe: Global Vectors for Word Representation," in EMNLP, 2014.

o f(x) should be relatively small for large values of x, so that frequent co-occurrences are not overweighted

0.0

 x_{\max}





Slido: #ADL2021

43 Word Vector Evaluation

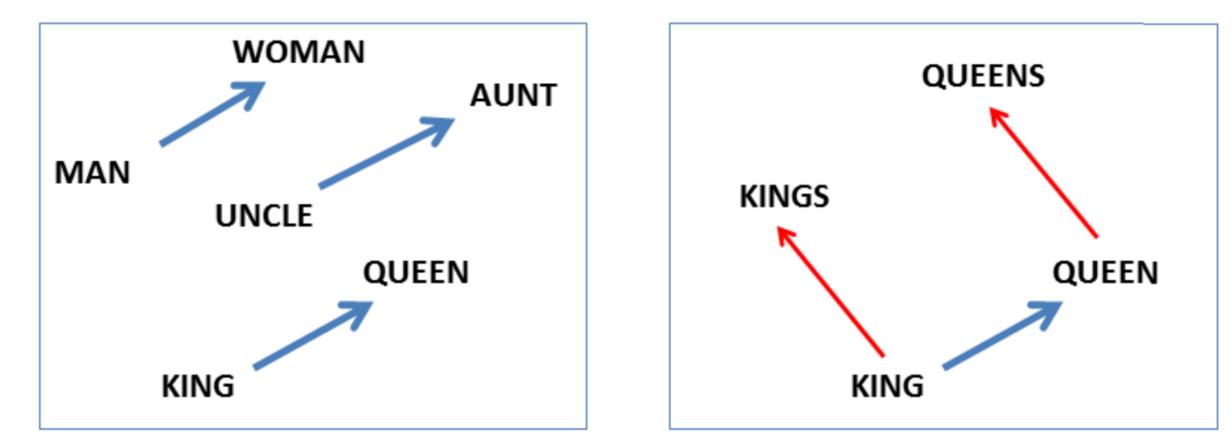


Intrinsic Evaluation – Word Analogies 44

Word linear relationship w_A : w_B

$$x = \arg \max_{x} \frac{(v_{w_B} - v_{w_A} + v_{w_C})^T v_{w_x}}{\|v_{w_B} - v_{w_A} + v_{w_C}\|}$$

Syntactic and Semantic example questions [link]



Issue: what if the information is there but not linear

$$= w_C : w_x$$



Slido: #ADL2021 Intrinsic Evaluation – Word Analogies

- Word linear relationship $w_A: w_B = w_C: w_x$
- Syntactic and **Semantic** example questions [link]

city---in---state

45

capital---country Chicago : Illinois = Houston : Texas Abuja : Nigeria = Accra : Ghana Chicago : Illinois = Philadelphia : Pennsylvania Abuja : Nigeria = Algiers : Algeria Chicago : Illinois = Phoenix : Arizona Abuja : Nigeria = Amman : Jordan Chicago : Illinois = Dallas : Texas Abuja : Nigeria = Ankara : Turkey Chicago : Illinois = Jacksonville : Florida Abuja : Nigeria = Antananarivo : Madagascar Chicago : Illinois = Indianapolis : Indiana Abuja : Nigeria = Apia : Samoa Chicago : Illinois = Aus8n : Texas Abuja : Nigeria = Ashgabat : Turkmenistan Chicago : Illinois = Detroit : Michigan Abuja : Nigeria = Asmara : Eritrea Chicago : Illinois = Memphis : Tennessee Abuja : Nigeria = Astana : Kazakhstan Chicago : Illinois = Boston : Massachusetts

Issue: different cities may have same name

Issue: can change with time



Slido: #ADL2021 Intrinsic Evaluation – Word Analogies 46

- Word linear relationship $w_A : w_B = w_C : w_x$
- **Syntactic** and Semantic example questions [link]

superlative

- bad : worst = big : biggest
- bad : worst = bright : brightest
- bad : worst = cold : coldest
- bad : worst = cool : coolest
- bad : worst = dark : darkest
- bad : worst = easy : easiest
- bad : worst = fast : fastest
- bad : worst = good : best
- bad : worst = great : greatest

past tense

dancing : danced = decreasing : decreased

- dancing : danced = describing : described
- dancing : danced = enhancing : enhanced
- dancing : danced = falling : fell
- dancing : danced = feeding : fed
- dancing : danced = flying : flew
- dancing : danced = generating : generated
- dancing : danced = going : went
- dancing : danced = hiding : hid
- dancing : danced = hiding : hit



Intrinsic Evaluation – Word Correlation

Comparing word correlation with human-judged scores

47

Human-judged word correlation [link]

Word 1	Word 2	Human-Judged Score
tiger	cat	7.35
tiger	tiger	10.00
book	paper	7.46
computer	internet	7.58
plane	car	5.77
professor	doctor	6.62
stock	phone	1.62

Ambiguity: synonym or same word with different POSs



Slido: #ADL2021 **Extrinsic Evaluation – Subsequent Task** 48

Goal: use word vectors in neural net models built for subsequent tasks

Benefit

- Ability to also classify words accurately Ex. countries cluster together a classifying location words should be possible with word vectors
- Incorporate any information into them other tasks \bigcirc
 - Ex. project sentiment into words to find most positive/negative words in corpus

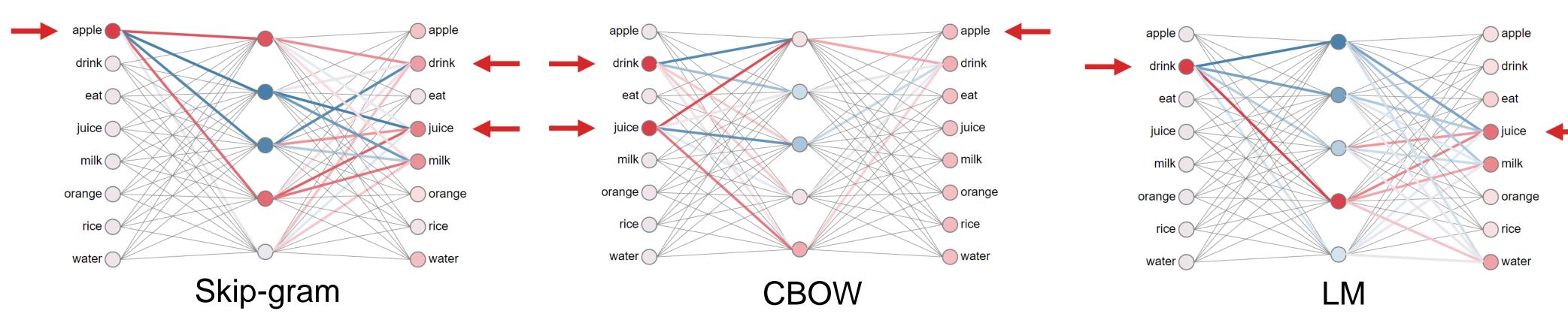




Concluding Remarks

Low dimensional word vector word2vec \bigcirc

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- GloVe: combining count-based and direct learning 0
- Word vector evaluation
 - Intrinsic: word analogy, word correlation 0
 - Extrinsic: subsequent task 0

