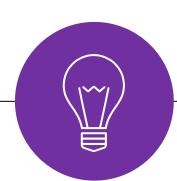
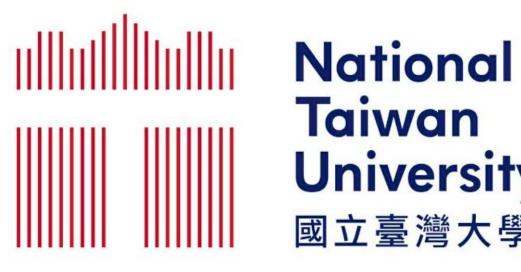
# Word Embeddings

### March 22nd, 2021 http://adl.miulab.tw















# **Meaning Representations in Computers**

- Knowledge-based representation
- **Corpus-based representation** 
  - Atomic symbol  $\checkmark$
  - Neighbors  $\checkmark$

3

- High-dimensional sparse word vector
- Low-dimensional dense word vector
  - Method 1 dimension reduction Ο
  - Method 2 direct learning Ο



# **Meaning Representations in Computers**

#### Knowledge-based representation

#### **Corpus-based representation**

#### Atomic symbol $\checkmark$

Neighbors

4

- High-dimensional sparse word vector
- Low-dimensional dense word vector
  - Method 1 dimension reduction  $\bigcirc$
  - Method 2 direct learning Ο





Atomic symbols: *one-hot* representation 

car [0 0 0 0 0 0

Issues: difficult to compute the similarity (i.e. comparing "car" and "motorcycle")

car

Idea: words with similar meanings often have similar neighbors

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### motorcycle



# **Meaning Representations in Computers**

- Knowledge-based representation
- **Corpus-based representation** 
  - Atomic symbol
  - Neighbors  $\checkmark$

6

- High-dimensional sparse word vector
- Low-dimensional dense word vector
  - Method 1 dimension reduction  $\bigcirc$
  - Method 2 direct learning Ο



# Window-based Co-occurrence Matrix

#### Example

7

- Window length=1
- Left or right context
- Corpus:

love NTU.

I love deep learning.

enjoy learning.

#### Issues:

- matrix size increases with vocabulary
- high dimensional
- sparsity  $\rightarrow$  poor robustness

#### Slido: #ADL2021

#### similarity > 0

| Counts   |   | love | enjoy | NTU | deep | learning |
|----------|---|------|-------|-----|------|----------|
|          | 0 | 2    | 1     | 0   | 0    | 0        |
| love     | 2 | 0    | 0     | 1   | 1    | 0        |
| enjoy    | 1 | 0    | 0     | 0   | 0    | 1        |
| NTU      | 0 | 1    | 0     | 0   | 0    | 0        |
| deep     | 0 | 1    | 0     | 0   | 0    | 1        |
| learning | 0 | 0    | 1     | 0   | 1    | 0        |

Idea: low dimensional word vector





# **Meaning Representations in Computers**

- Knowledge-based representation
- **Corpus-based representation** 
  - Atomic symbol
  - Neighbors  $\checkmark$

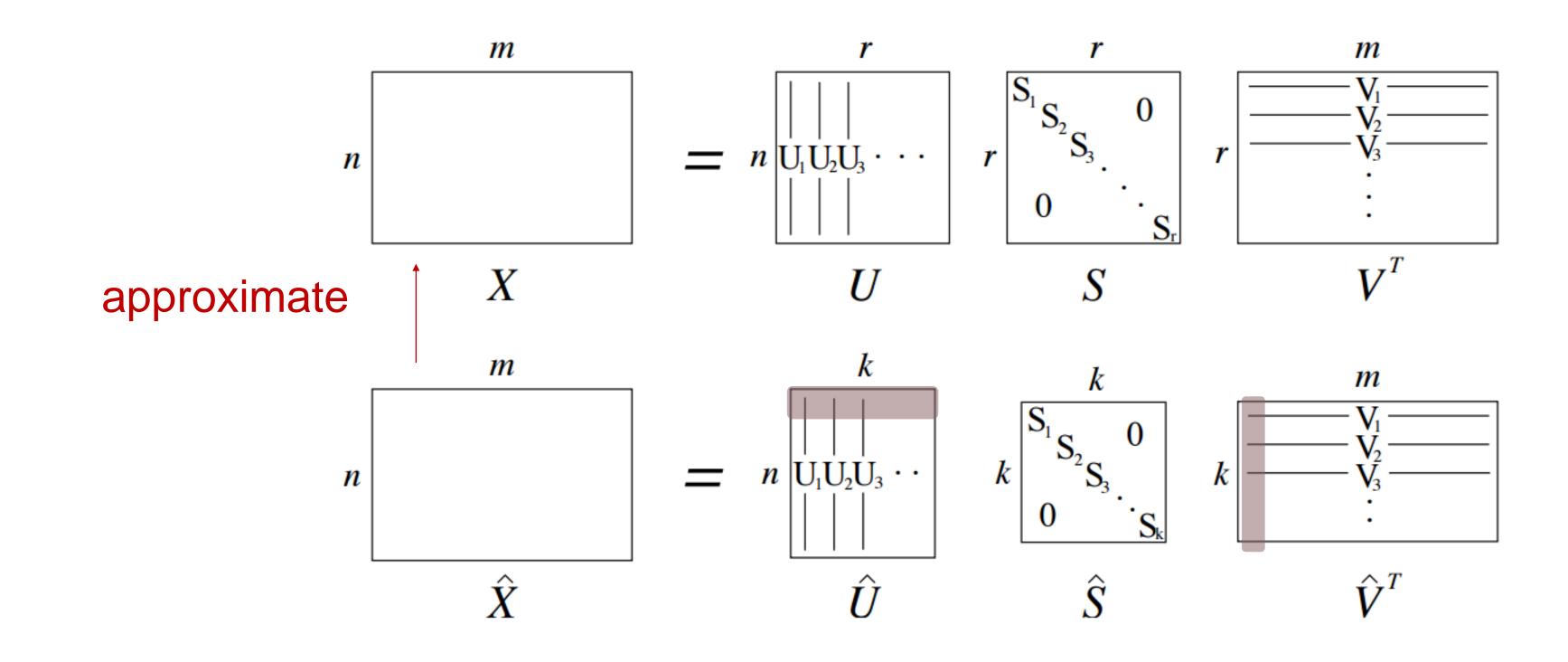
8

- High-dimensional sparse word vector
- Low-dimensional dense word vector
  - Method 1 dimension reduction 0
  - Method 2 direct learning Ο



### **Low-Dimensional Dense Word Vector** 9

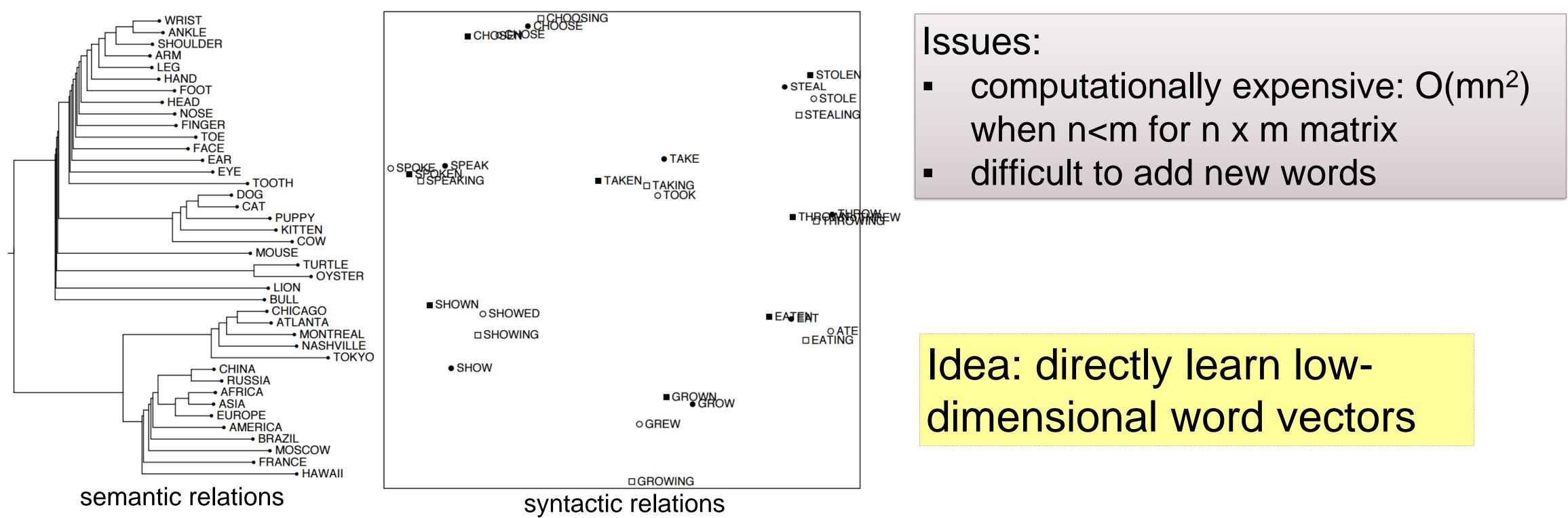
- Method 1: dimension reduction on the matrix
- Singular Value Decomposition (SVD) of co-occurrence matrix X





#### Low-Dimensional Dense Word Vector 10

Method 1: dimension reduction on the matrix Singular Value Decomposition (SVD) of co-occurrence matrix X





### Word Representation 11

- Knowledge-based representation
- **Corpus-based representation** 
  - Atomic symbol  $\checkmark$
  - Neighbors  $\checkmark$ 
    - High-dimensional sparse word vector
    - Low-dimensional dense word vector
      - Method 1 dimension reduction Ο
      - Method 2 direct learning  $\rightarrow$  word embedding Ο



# Word Embedding

12

Method 2: directly learn low-dimensional word vectors Learning representations by back-propagation. (Rumelhart et al., 1986) 0 A neural probabilistic language model (Bengio et al., 2003) 0 NLP (almost) from Scratch (Collobert & Weston, 2008) Ο

- 0 (Pennington et al., 2014)

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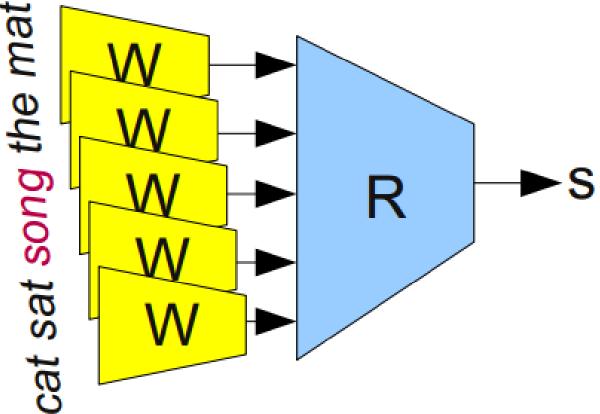
Recent and most popular models: word2vec (Mikolov et al. 2013) and Glove



# Word Embedding Benefit

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Given an <u>unlabeled</u> training corpus, produce a vector for each word that encodes its semantic information. These vectors are useful because: 1) semantic similarity between two words can be calculated as the cosine similarity between their corresponding word vectors 2) word vectors as powerful features for various supervised NLP tasks since the vectors contain semantic information 3) propagate any information into them via neural networks and update during training







# Word Embeddings Word2Vec





### Word2Vec – Skip-Gram Model 15

- Goal: predict surrounding words within a window of each word
- current center word

$$w_{1}, w_{2}, \cdots, w_{t-m}, \cdots, w_{t-1}, w_{t} w_{t+1}, \cdots, w_{t+m}, \cdots, w_{T-1}, w_{T}$$

$$w_{I} c w_{O}$$

$$w_{O}$$

$$w_{1}, w_{2}, \cdots, w_{t-m}, \cdots, w_{t-1}, w_{t} w_{t+1}, \cdots, w_{t+m}, \cdots, w_{T-1}, w_{T}$$

$$w_{I} C w_{O}$$

$$p(w_{O,1}, w_{O,2}, \cdots, w_{O,C} \mid w_{I}) = \prod_{c=1}^{C} p(w_{O,c} \mid w_{I})$$

$$target word vector$$

$$C(\theta) = -\sum_{w_{I}} \sum_{c=1}^{C} \log p(w_{O,c} \mid w_{I})$$

$$p(w_{O} \mid w_{I}) = \frac{\exp(v_{w_{O}}^{'T} v_{w_{I}})}{\sum_{j} \exp(v_{w_{j}}^{'T} v_{w_{I}})}$$
outside target word

$$w_{1}, w_{2}, \cdots, \underbrace{w_{t-m}, \cdots, w_{t-1}, w_{t}}_{W_{I}} \underbrace{w_{t+1}, \cdots, w_{t+m}}_{context window}, \cdots, w_{T-1}, w_{T}$$

$$p(w_{O,1}, w_{O,2}, \cdots, w_{O,C} \mid w_{I}) = \prod_{c=1}^{C} p(w_{O,c} \mid w_{I})$$

$$target word vector$$

$$C(\theta) = -\sum_{w_{I}} \sum_{c=1}^{C} \log p(w_{O,c} \mid w_{I})$$

$$p(w_{O} \mid w_{I}) = \frac{\exp(v_{w_{O}}^{\prime T} \underbrace{v_{w_{I}}}_{\sum_{j} \exp(v_{w_{j}}^{\prime T} v_{w_{I}})})$$

$$outside target word$$

Benefit: faster, easily incorporate a new sentence/document or add a word to vocab

#### Slido: #ADL2021

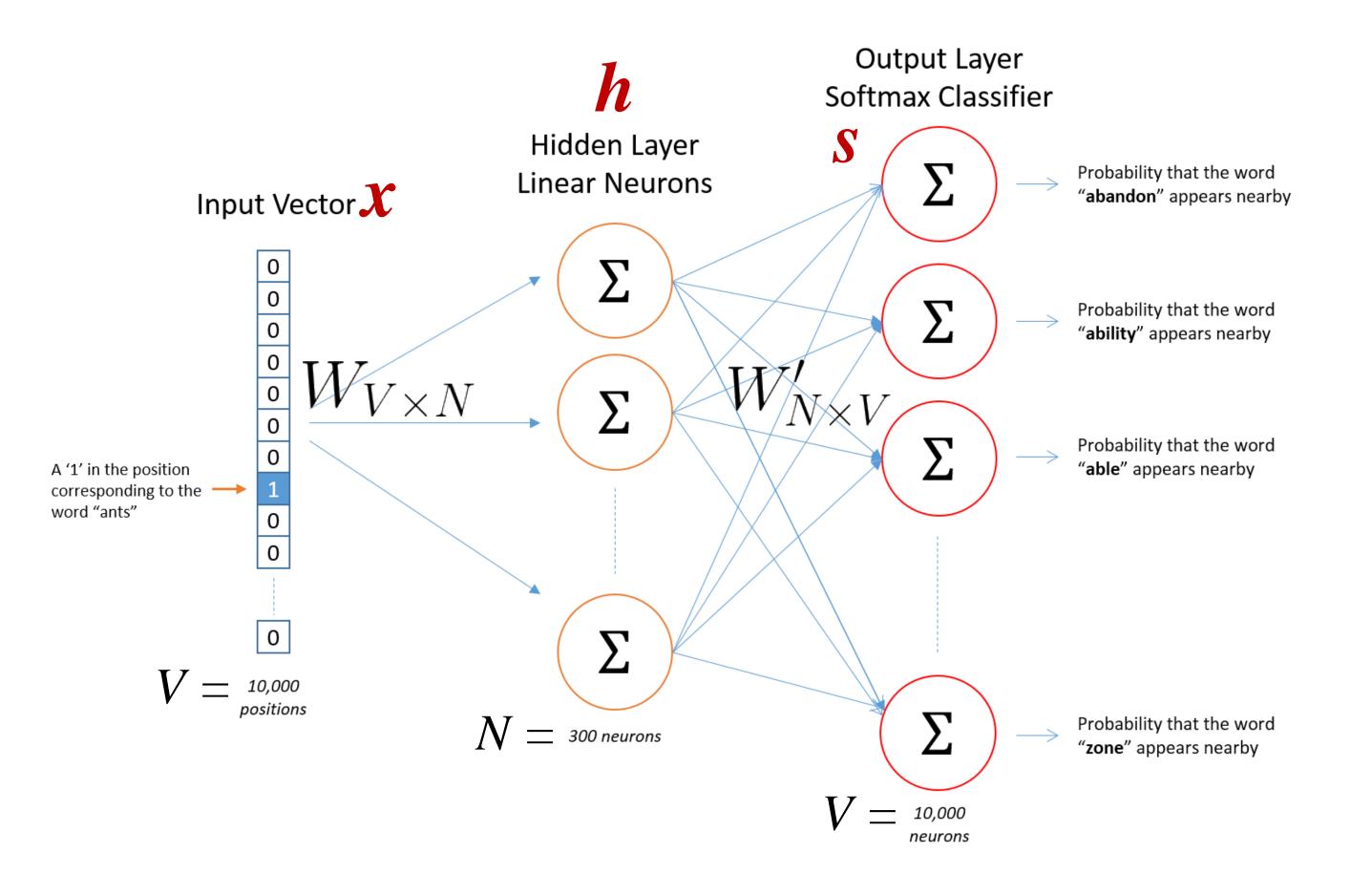
# Objective function: maximize the probability of any context word given the







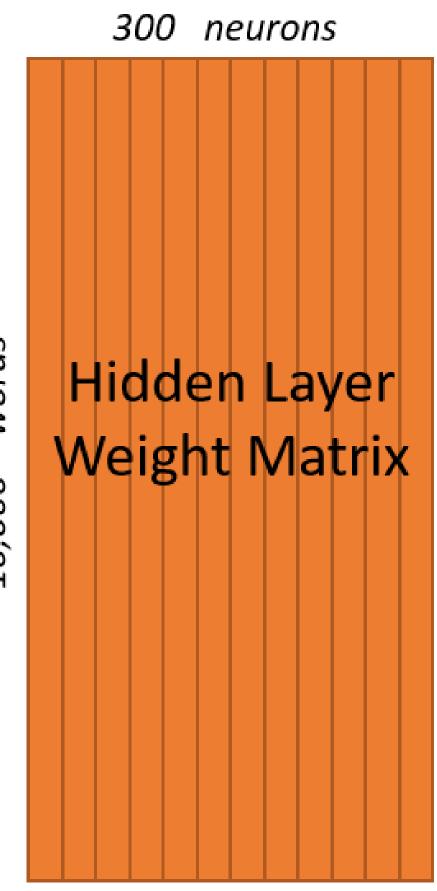
#### Goal: predict surrounding words within a window of each word







### Slido: #ADL2021 Hidden Layer Matrix $\rightarrow$ Word Embedding Matrix



words 10,000  $W_{V \times N}$ 

300 features words Word Vector Lookup Table! 10,000



### Weight Matrix Relation 18

Hidden layer weight matrix = word vector lookup 

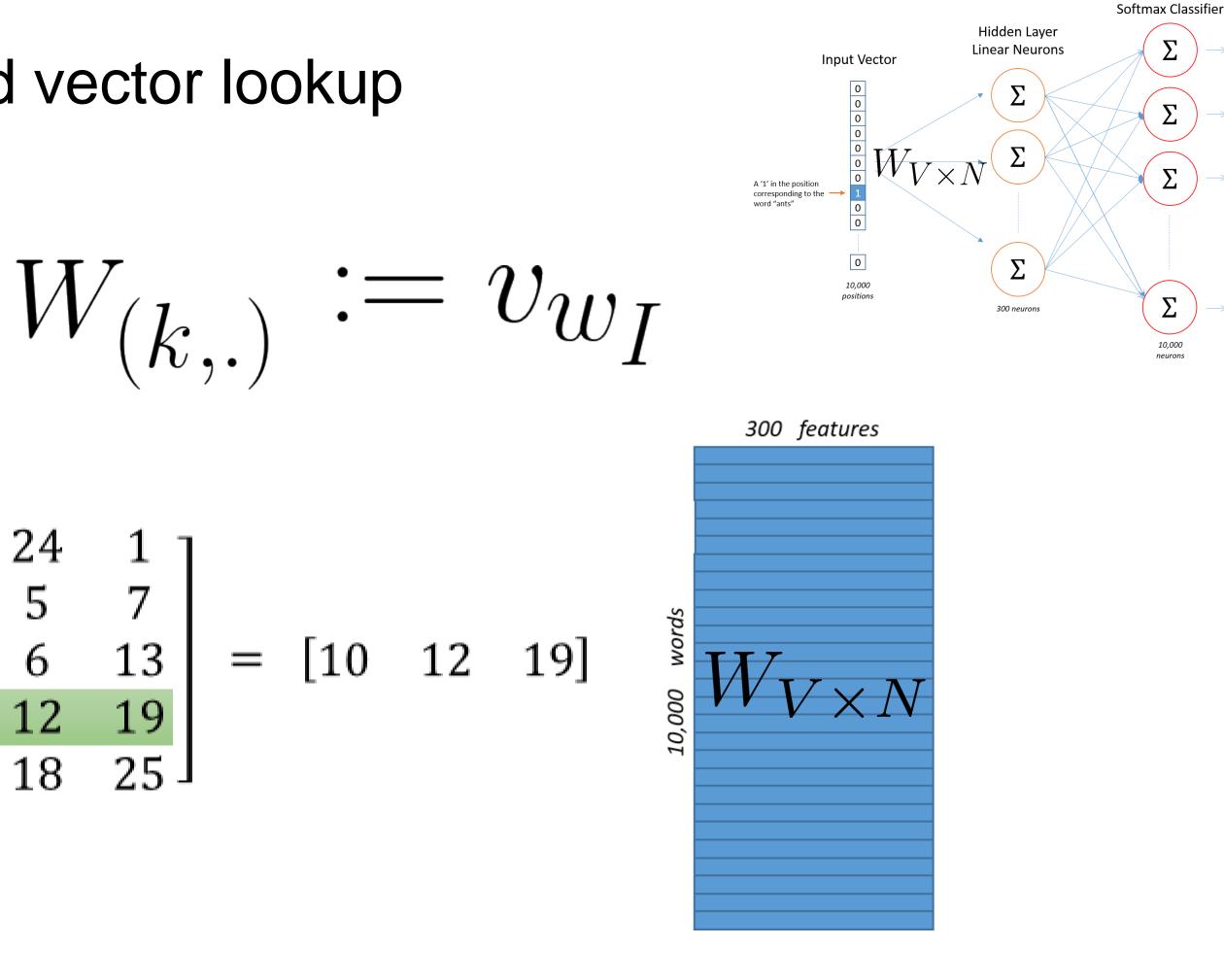
$$h = x^T W = \mathbf{I}$$

 $\begin{bmatrix} 0 & 0 & 0 & 1 & 0 \end{bmatrix} \times \begin{bmatrix} 17 & 24 & 1 \\ 23 & 5 & 7 \\ 4 & 6 & 13 \\ 10 & 12 & 19 \end{bmatrix} = \begin{bmatrix} 10 & 12 & 19 \end{bmatrix}$ 18

Each vocabulary entry has two vectors: as a target word and as a context word

#### Slido: #ADL2021

Output Layer





Probability that the word "abandon" appears nearby

Probability that the word "ability" appears nearby

Probability that the word "able" appears nearby

Probability that the word "zone" appears nearby

### Weight Matrix Relation 19

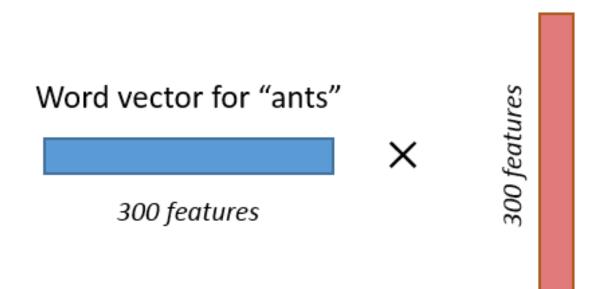
Output layer weight matrix = weighted sum as final score 

$$s_j = h v'_{w_j}$$

$$p(w_j = w_{O,c} \mid w_I) = q$$

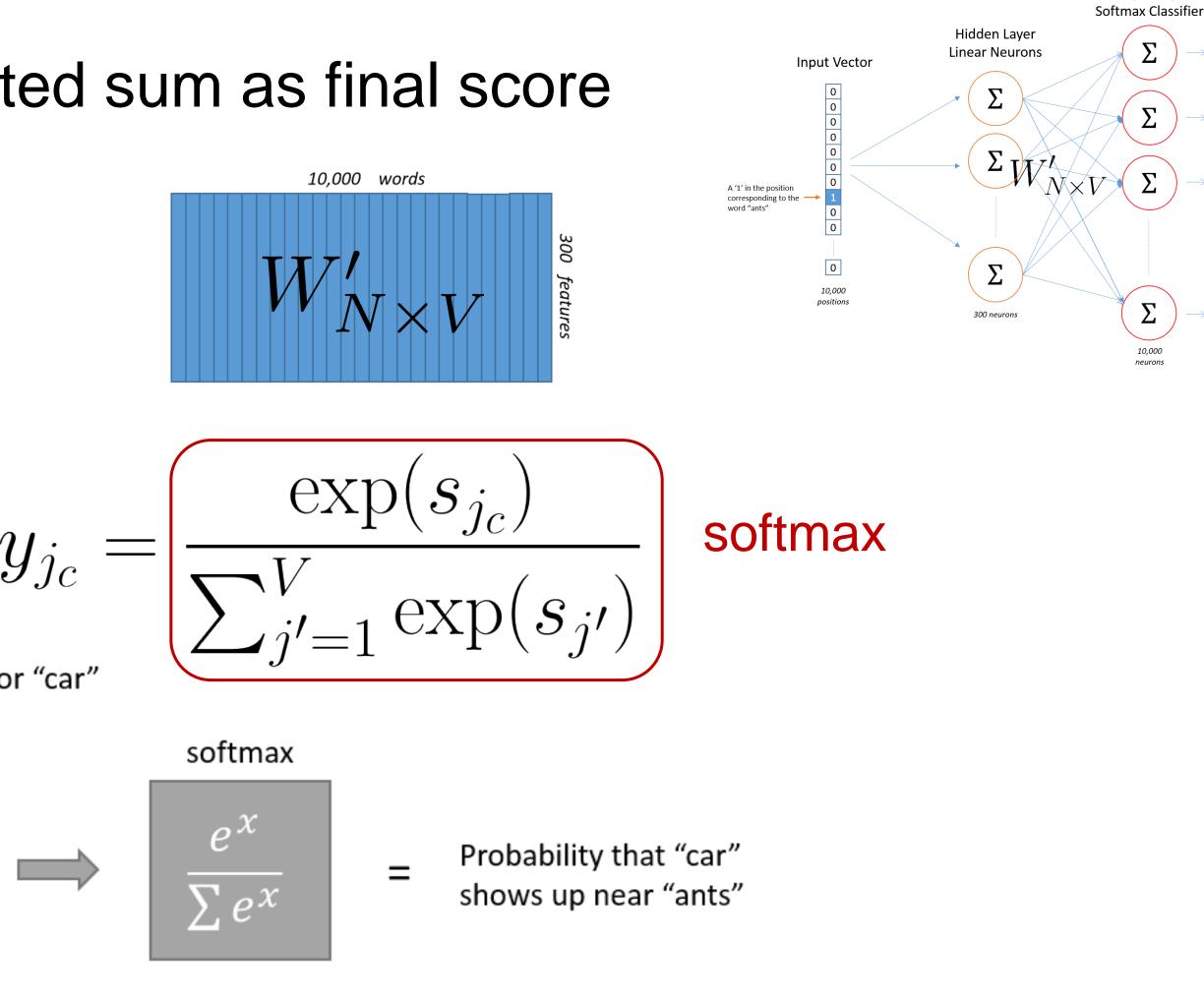
within the context window

Output weights for "car"



#### Slido: #ADL2021

Output Layer



#### Each vocabulary entry has two vectors: as a target word and as a context word



Probability that the word "abandon" appears nearby

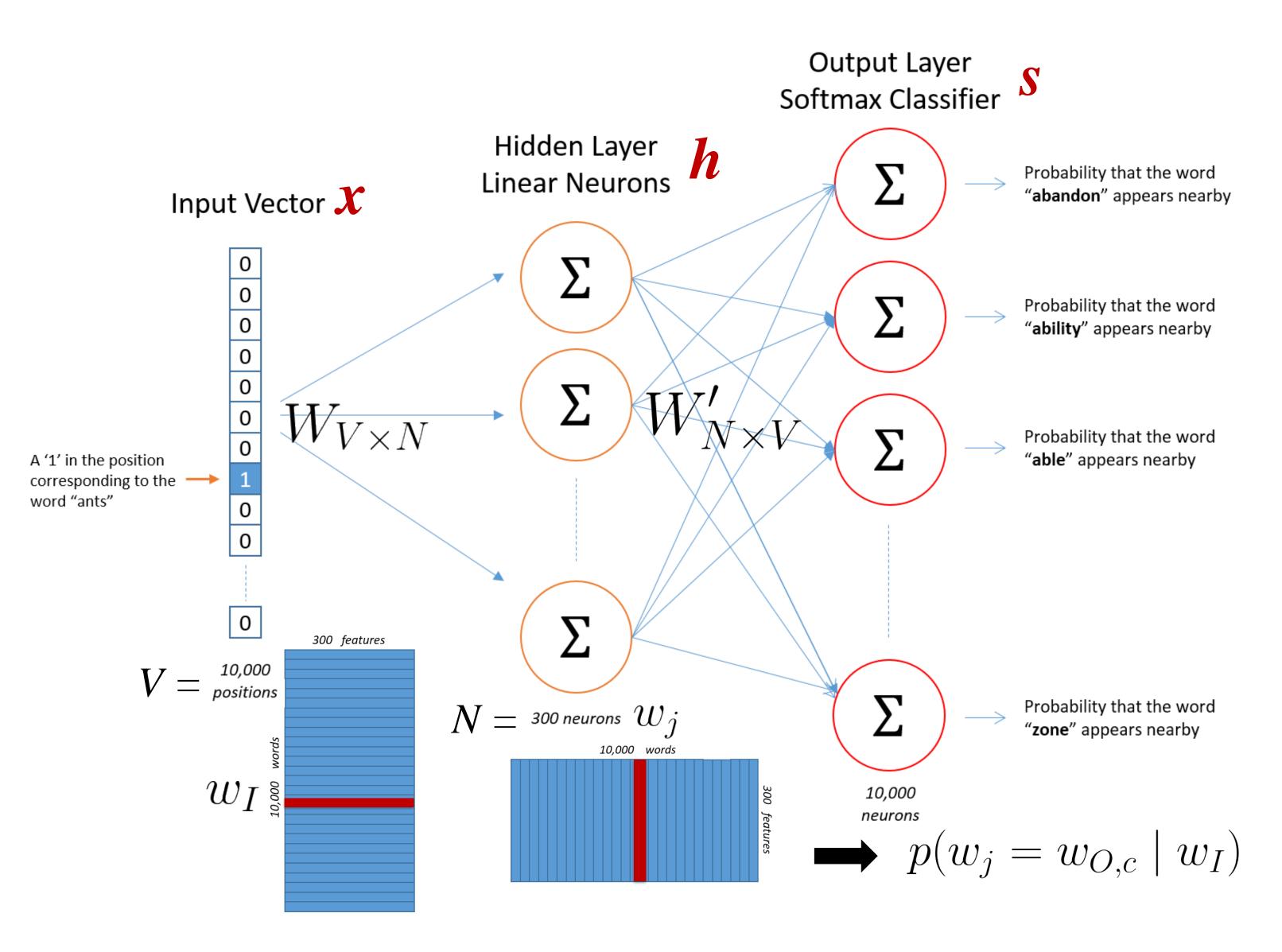
Probability that the word "ability" appears nearby

Probability that the word "able" appears nearby

Probability that the word "zone" appears nearby

# Word2Vec Skip-Gram Illustration

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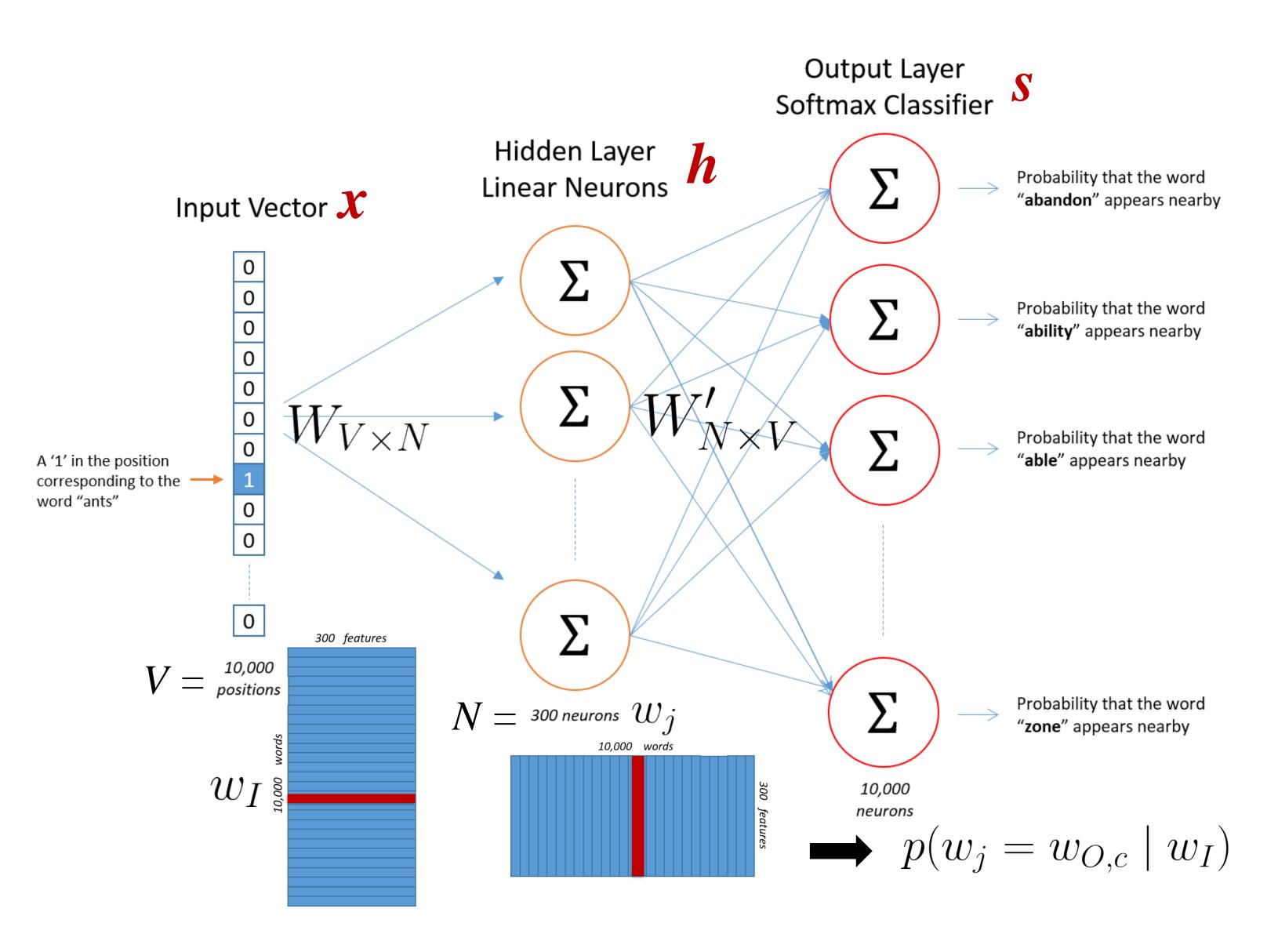


### Word Embeddings 21 Word2Vec Training





### Word2Vec Skip-Gram Illustration







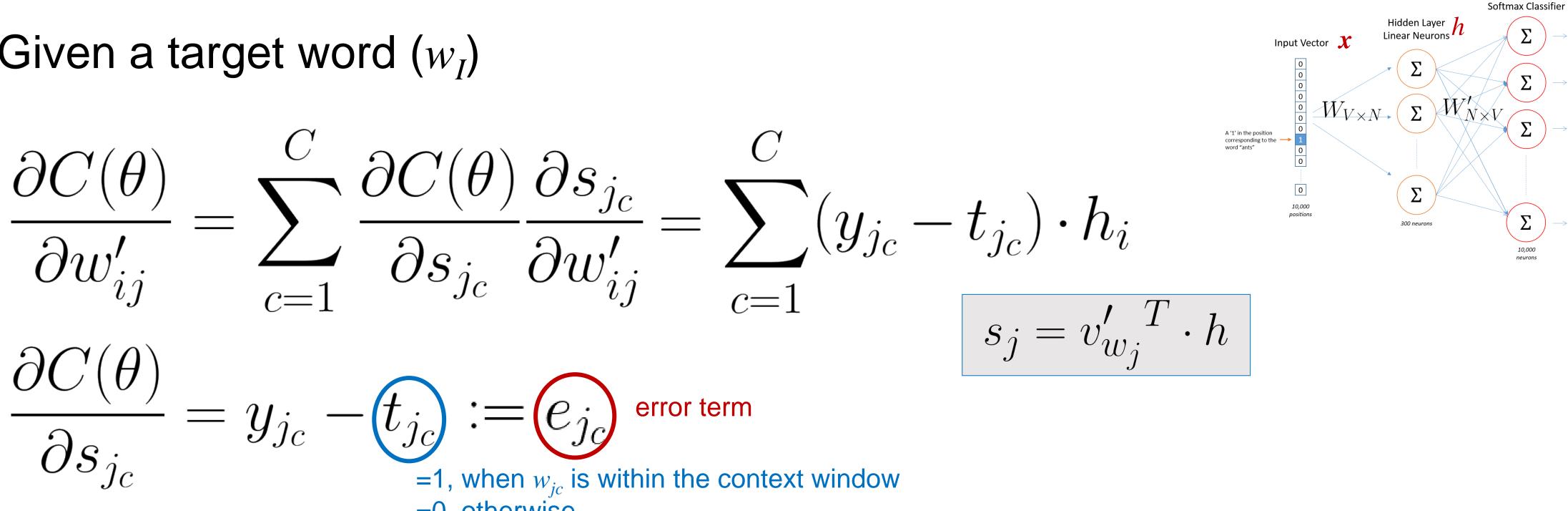
Given a target word  $(w_I)$ 

 $C(\theta) = -\log p(w_{O,1}, w_{O,2}, \cdots, w_{O,C} \mid w_I)$  $= -\log \prod_{c=1}^{C} \frac{\exp(s_{j_c})}{\sum_{j'=1}^{V} \exp(s_{j'})}$ C $= -\sum s_{j_c} + C \log \sum \exp(s_{j'})$ c=1i'=1



### SGD Update for W' 24

Given a target word  $(w_I)$ 



=0, otherwise

$$w'_{ij}{}^{(t+1)} = w'_{ij}{}^{(t)} - \eta$$

#### Slido: #ADL2021

$$\sum_{c=1}^{C} (y_{j_c} - t_{j_c}) \cdot h_i$$



**Output Layer** 

Probability that the word andon" appears near

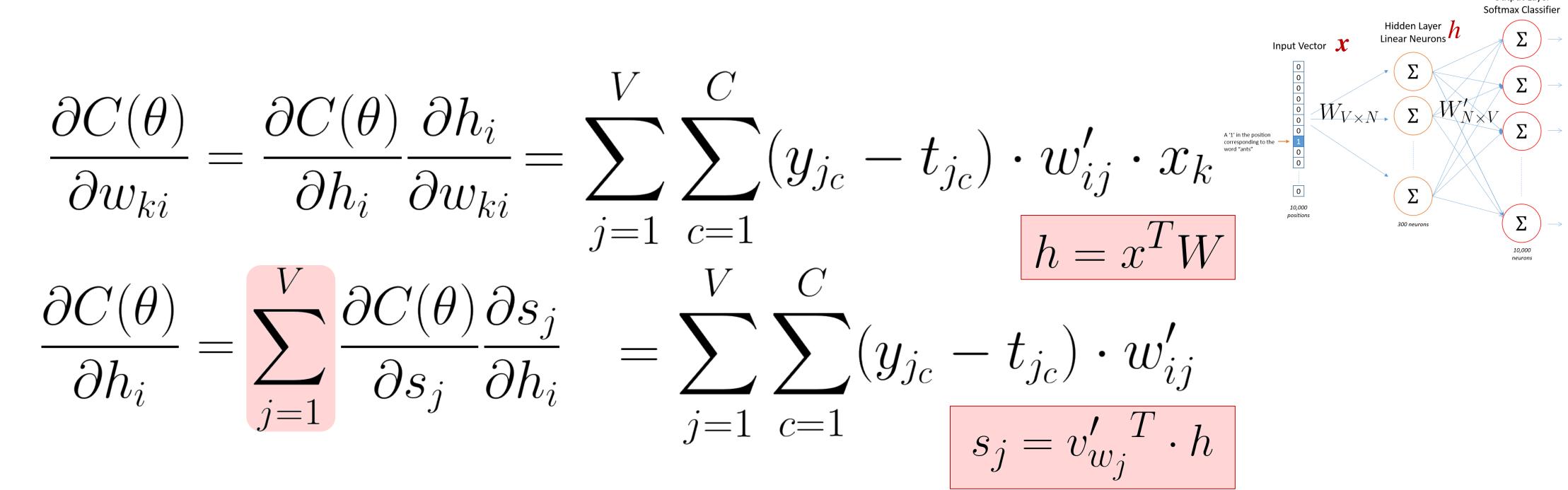
Probability that the word ability" appears near

Probability that the word "able" appears nearby

Probability that the word "zone" appears nearby



### SGD Update for W



 $w_{ij}^{(t+1)} = w_{ij}^{(t)} - \eta \cdot \mathbf{y}$ j=

#### Slido: #ADL2021

$$\sum_{i=1}^{C} \sum_{c=1}^{C} (y_{j_c} - t_{j_c}) \cdot w'_{ij} \cdot x_j$$



Probability that the word "**abandon**" appears nearby

Probability that the word "**ability**" appears nearby

Probability that the word "**able**" appears nearby

Probability that the word "zone" appears nearby

$$6 - SGD Update$$

$$w_{ij}^{\prime(t+1)} = w_{ij}^{\prime(t)} - \eta \cdot \sum_{c=1}^{C} (y_{jc} - t_{jc}) \cdot h_i \left[ EI_j = \sum_{c=1}^{C} (y_{jc} - t_{jc}) \right]$$

$$v_{wj}^{\prime(t+1)} = v_{wj}^{\prime(t)} - \eta \cdot EI_j \cdot h$$

$$w_{ij}^{(t+1)} = w_{ij}^{(t)} - \eta \cdot \sum_{j=1}^{V} \sum_{c=1}^{C} (y_{jc} - t_{jc}) \cdot w_{ij}^{\prime} \cdot x_j$$

$$v_{wI}^{(t+1)} = v_{wI}^{(t)} - \eta \cdot EH^T$$

$$EH_i = \sum_{j=1}^{V} EI_j \cdot w_{ij}^{\prime} \cdot x_j$$

large vocabularies or large training corpora  $\rightarrow$  expensive computations

limit the number of output vectors that must be updated per training instance  $\rightarrow$  hierarchical softmax, sampling

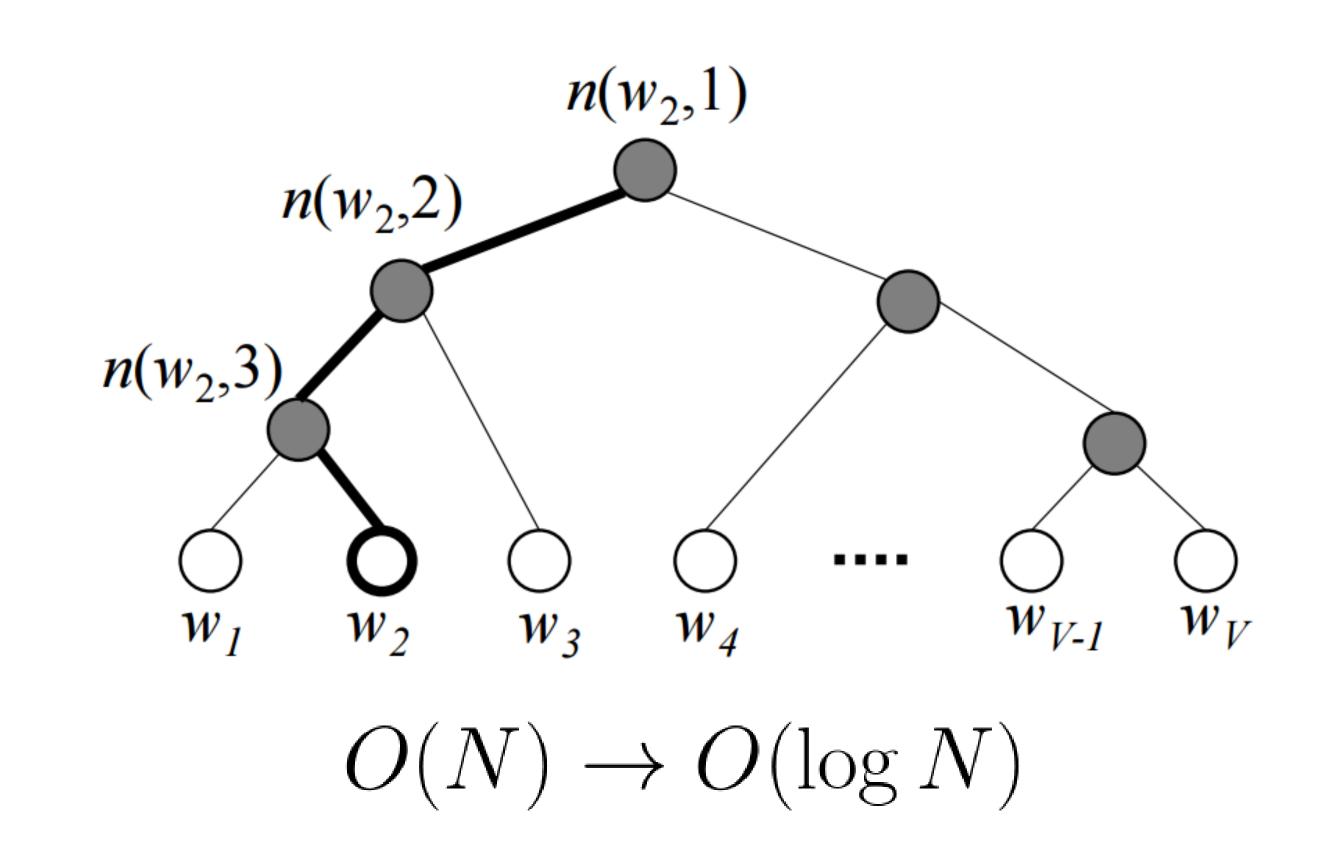


### Word Embeddings 27 **Negative Sampling**





Idea: compute the probability of leaf nodes using the paths 



Mikolov et al., "Distributed representations of words and phrases and their compositionality," in NIPS, 2013.





### 29 **Negative Sampling**

Idea: only update a sample of output vectors 

$$C(\theta) = -\log \sigma(v'_{w_O}{}^T v_{w_I}) + \sum_{w_j \in \mathcal{W}_{neg}} \log \sigma(v'_{w_j}{}^T v_{w_I})$$
$$\frac{v'_{w_j}{}^{(t+1)} = v'_{w_j}{}^{(t)} - \eta \cdot EI_j \cdot h}{v_{w_I}{}^{(t+1)} = v_{w_I}{}^{(t)} - \eta \cdot EH^T}$$
$$EI_j = \sigma(v'_{w_j}{}^T v_{w_I}) - t_j$$
$$EH = \sum_{w_j \in \{w_O\} \cup \mathcal{W}_{neg}} EI_j \cdot v'_{w_j}$$
$$w_j \in \{w_O\} \cup \mathcal{W}_{neg}$$

Mikolov et al., "Distributed representations of words and phrases and their compositionality," in NIPS, 2013.



### **Negative Sampling** 30

- Sampling methods
  - Random sampling  $w_i \in \{w_O\} \cup \mathcal{W}_{neg}$ 0
  - Ο

Idea: less frequent words sampled more often

Empirical setting: unigram model raised to the power of 3/4

| Word         | Probabi |
|--------------|---------|
| is           |         |
| constitution |         |
| bombastic    |         |

Mikolov et al., "Distributed representations of words and phrases and their compositionality," in NIPS, 2013.

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# Distribution sampling: $w_i$ is sampled from P(w) What is a good P(w)?

#### ility to be sampled for "neg"

 $0.9^{3/4} = 0.92$  $0.09^{3/4} = 0.16$ 

 $0.01^{3/4} = 0.032$ 





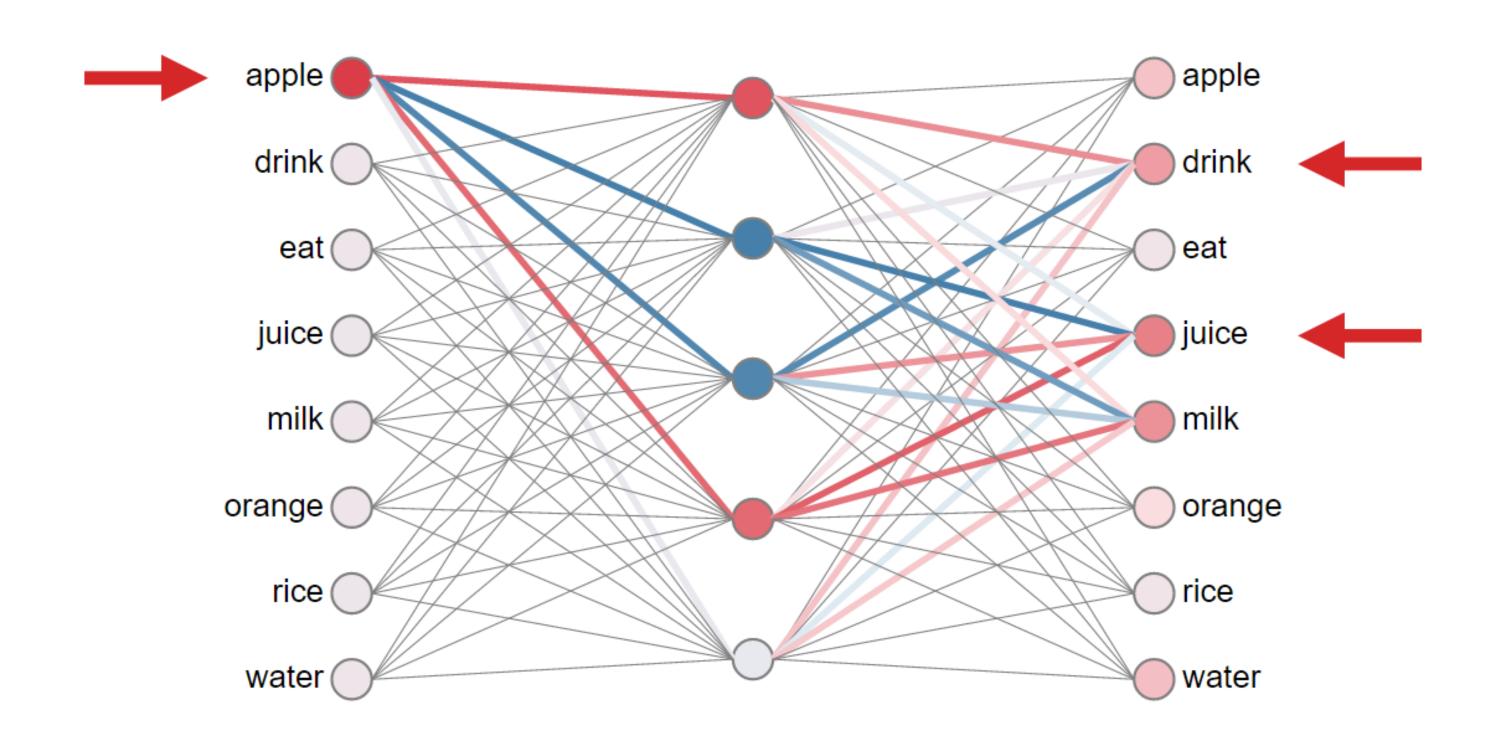
### Word Embeddings 31 Word2Vec Variants





### Word2Vec Skip-Gram Visualization <a href="https://ronxin.github.io/wevi/">https://ronxin.github.io/wevi/</a>

Skip-gram training data: e^water



#### Slido: #ADL2021

apple|drink^juice,orange|eat^apple,rice|drink^juice,juice|drink^milk,milk|drink^rice,water|drink^mil k,juice|orange^apple,juice|apple^drink,milk|rice^drink,drink|milk^water,drink|water^juice,drink|juic

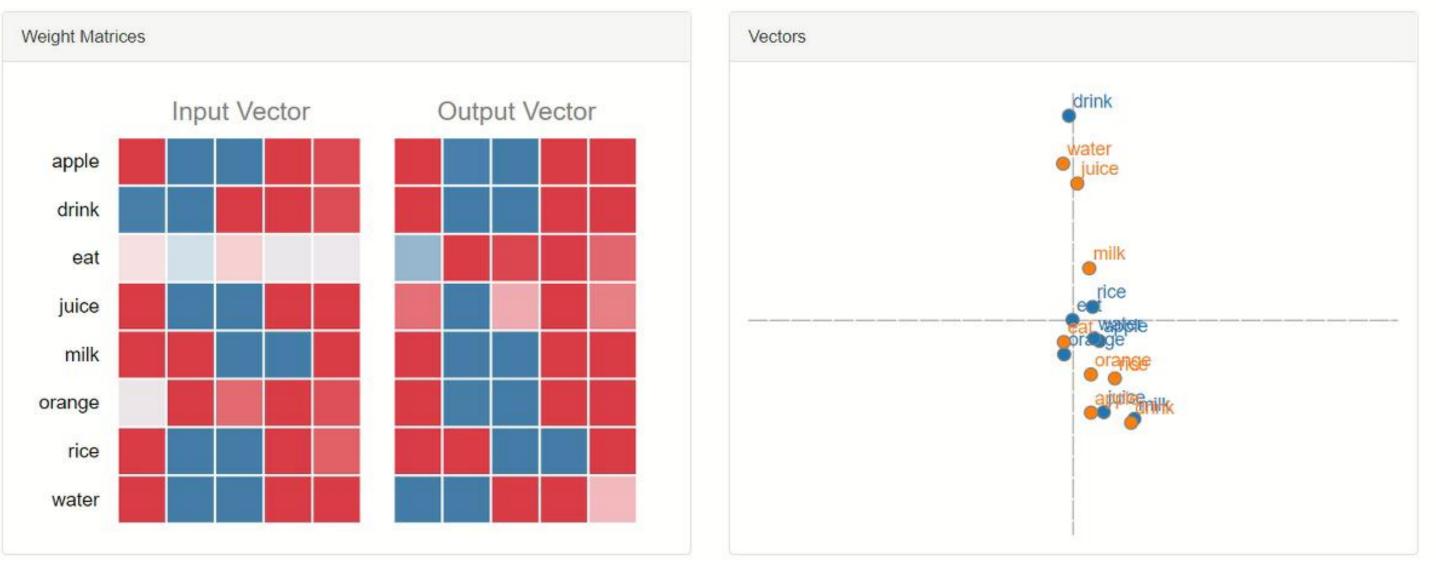


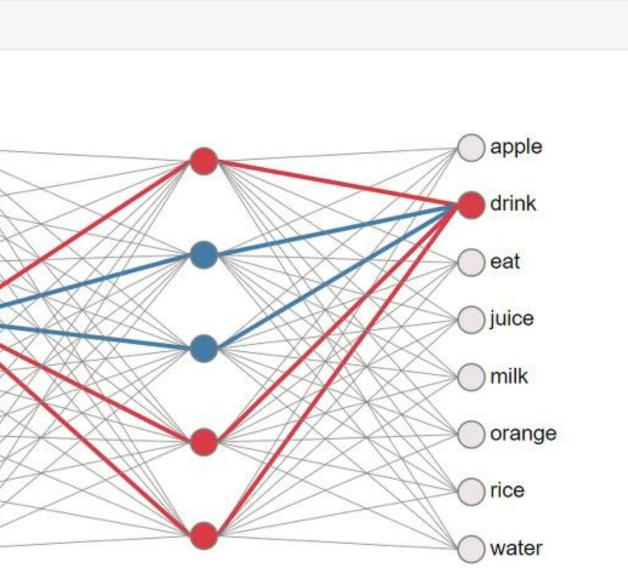


#### wevi: word embedding visual inspector

Everything you need to know about this tool - Source code

| Control Panel  | Neurons |
|--|---------|
| Config:  |         |
| {"hidden_size":5,"random_state":1,"learning_rate":0<br>.2}   | apple   |
| Training data (context target):  | drink   |
| apple/drink^juice,orange/eat^apple,rice/drink^juice,j  | eat     |
| uice drink^milk,milk drink^rice,water drink^milk,juice<br> orange^apple,juice apple^drink,milk rice^drink,drink<br> milk^water,drink water^juice,drink juice^water | juice   |
| Presets: Fruit and juice (Skip-gram) <b>v</b>  | milk    |
| Update and Restart Update Learning Rate  | orange  |
| Next 20 100 500 PCA  | rice    |
|  | water   |
|  |         |







## Word2Vec Variants

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2013)

 $p(w_{t-m}, \cdots w_{t-1}, w_t)$ 

- surrounding words (Mikolov+, 2013)
- contexts (Mikolov+, 2013)

$$p(w_{t+1} \mid w_t)$$

### Practice the derivation by yourself!!

Mikolov et al., "Efficient estimation of word representations in vector space," in ICLR Workshop, 2013. Mikolov et al., "Linguistic regularities in continuous space word representations," in NAACL HLT, 2013.

#### Slido: #ADL2021

**Skip-gram**: predicting surrounding words given the target word (Mikolov+,

$$w_{t+1}, \cdots, w_{t+m} \mid w_t)$$

**CBOW (continuous bag-of-words)**: predicting the target word given the

 $p(w_t \mid w_{t-m}, \cdots, w_{t-1}, w_{t+1}, \cdots, w_{t+m})$ LM (Language modeling): predicting the next words given the proceeding

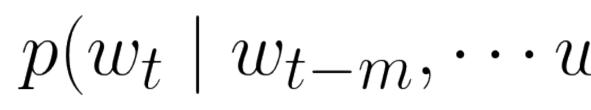


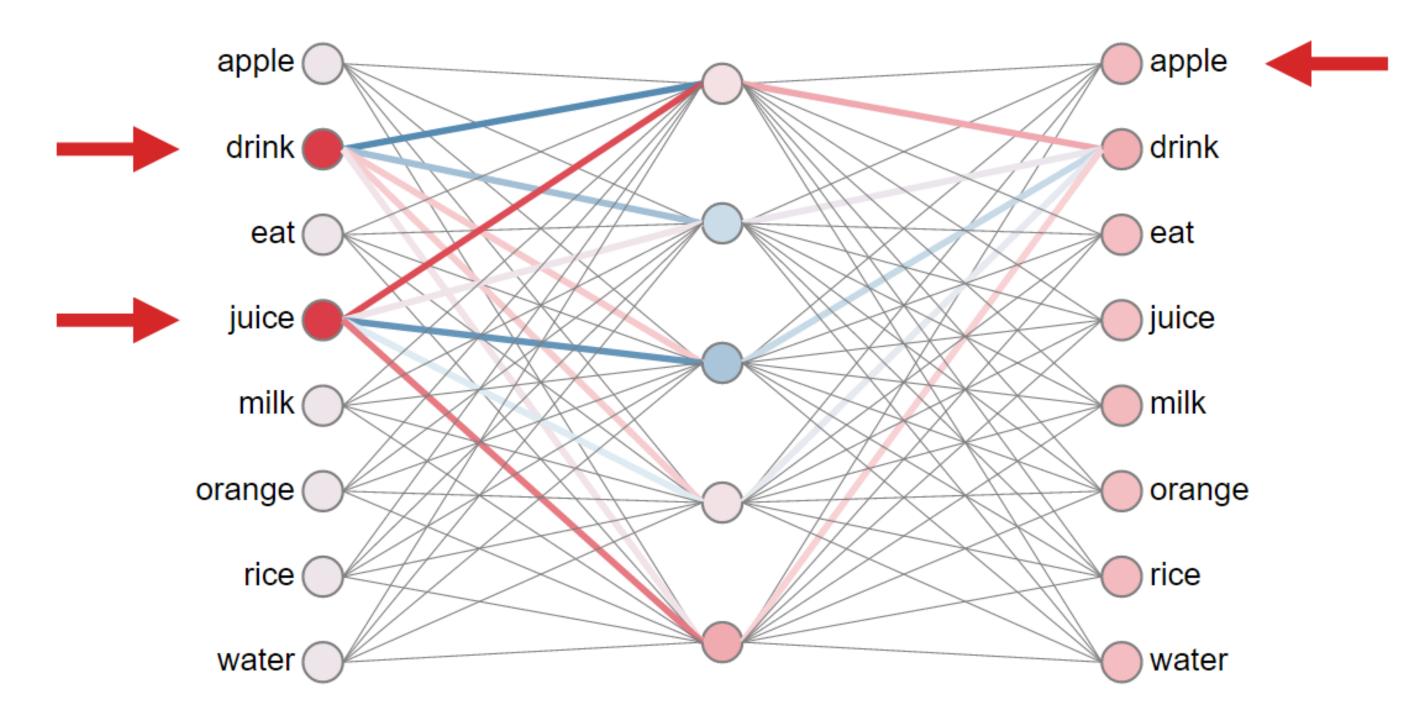






Goal: predicting the target word given the surrounding words 



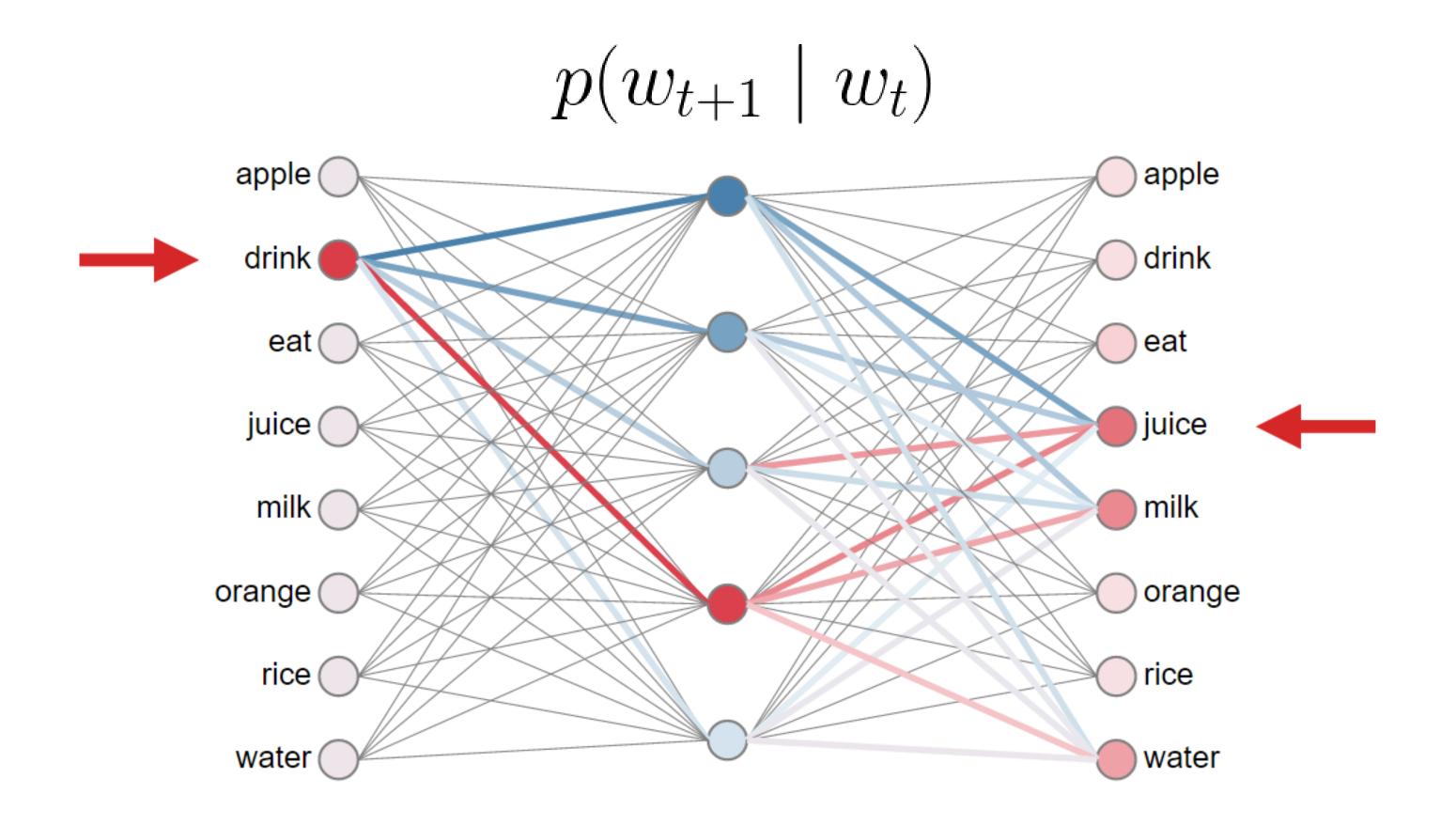


$$v_{t-1}, w_{t+1}, \cdots, w_{t+m}$$





#### Goal: predicting the next words given the proceeding contexts











### Count-based

- LSA, HAL (Lund & Burgess), COALS (Rohde et al), Hellinger-PCA (Lebret & Collobert)
- Pros  $\bigcirc$ 
  - Fast training
  - Efficient usage of statistics
- Cons  $\bigcirc$ 
  - Primarily used to capture word similarity
  - Disproportionate importance given to large counts

# Combining the benefits from both worlds $\rightarrow$ GloVe

### Slido: #ADL2021

### **Direct prediction**

### NNLM, HLBL, RNN, Skipgram/CBOW 0 (Bengio et al; Collobert & Weston; Huang et al; Mnih & Hinton; Mikolov et al; Mnih & Kavukcuoglu)

### Pros $\bigcirc$

- Generate improved performance on other tasks
- Capture complex patterns beyond word similarity

### Cons $\bigcirc$

- Benefits mainly from large corpus
- Inefficient usage of statistics







- Idea: ratio of co-occurrence probability can encode meaning
- $P_{ii}$  is the probability that word  $w_i$  appears in the context of word  $w_i$

$$P_{ij} = P(w_j$$

Relationship between the words  $w_i$  and  $w_j$ 

|  | x = solid | x = gas | x = water | x = random |
|--|-----------|---------|-----------|------------|
| $P(x \mid ice)$  | large     | small   | large     | small      |
| $P(x \mid \text{stream})$                              | small     | large   | large     | small      |
| $\frac{P(x \mid \text{ice})}{P(x \mid \text{stream})}$ | large     | small   | ~ 1       | ~ 1        |

Pennington et al., "GloVe: Global Vectors for Word Representation," in EMNLP, 2014.

$$w_i) = X_{ij}/X_i$$





The relationship of  $w_i$  and  $w_j$  approximates the ratio of their co-occurrence probabilities with various  $w_k$ 

$$F(w_i, w_j, \tilde{w}_k) = \frac{P_{ik}}{P_{jk}}$$

$$F(w_i - w_j, \tilde{w}_k) = \frac{P_{ik}}{P_{jk}}$$

$$F((v_{w_i} - v_{w_j})^T v'_{\tilde{w}_k}) = \frac{P_{ik}}{P_{jk}} \quad F(\cdot) = \exp(\cdot)$$

$$v_{w_i} \cdot v'_{\tilde{w}_k} = v_{w_i}^T v'_{\tilde{w}_k} = \log P(w_k \mid w_i)$$

Pennington et al., "GloVe: Global Vectors for Word Representation," in EMNLP, 2014.







$$v_{w_{i}} \cdot v_{\tilde{w}_{j}}' = v_{w_{i}}^{T} v_{\tilde{w}_{j}}' = \log P(w_{j} \mid w_{i}) \qquad P_{ij} = X_{ij}/X_{i}$$
$$= \log P_{ij} = \log(X_{ij}) - \log(X_{i})$$
$$v_{w_{i}}^{T} v_{\tilde{w}_{j}}' + b_{i} + \tilde{b}_{j} = \log(X_{ij})$$
$$C(\theta) = \sum_{i,j=1}^{V} f(P_{ij})(v_{w_{i}} \cdot v_{\tilde{w}_{j}}' - \log P_{ij})^{2}$$
$$C(\theta) = \sum_{i,j=1}^{V} f(X_{ij})(v_{w_{i}}^{T} v_{\tilde{w}_{j}}' + b_{i} + \tilde{b}_{j} - \log X_{ij})^{2}$$

Pennington et al., "GloVe: Global Vectors for Word Representation," in EMNLP, 2014.

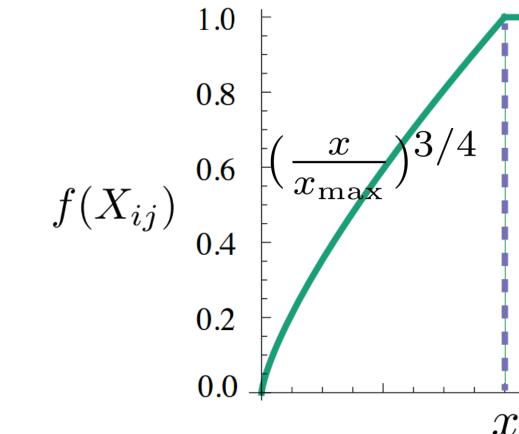


### Slido: #ADL2021 42 **GIOVe – Weighted Least Squares Regression Model**

 $C(\theta) = \sum f(X_{ij})(v_{w_i}^T v_{\tilde{w}_j}' + b_i + \tilde{b}_j - \log X_{ij})^2$ i.i=1

Weighting function should obey f(0) = 0

f(x) should be non-decreasing so that rare co-occurrences are not overweighted



### fast training, scalable, good performance even with small corpus, and small vectors

Pennington et al., "GloVe: Global Vectors for Word Representation," in EMNLP, 2014.

o f(x) should be relatively small for large values of x, so that frequent co-occurrences are not overweighted

0.0

 $x_{\max}$ 





Slido: #ADL2021

# 43 Word Vector Evaluation

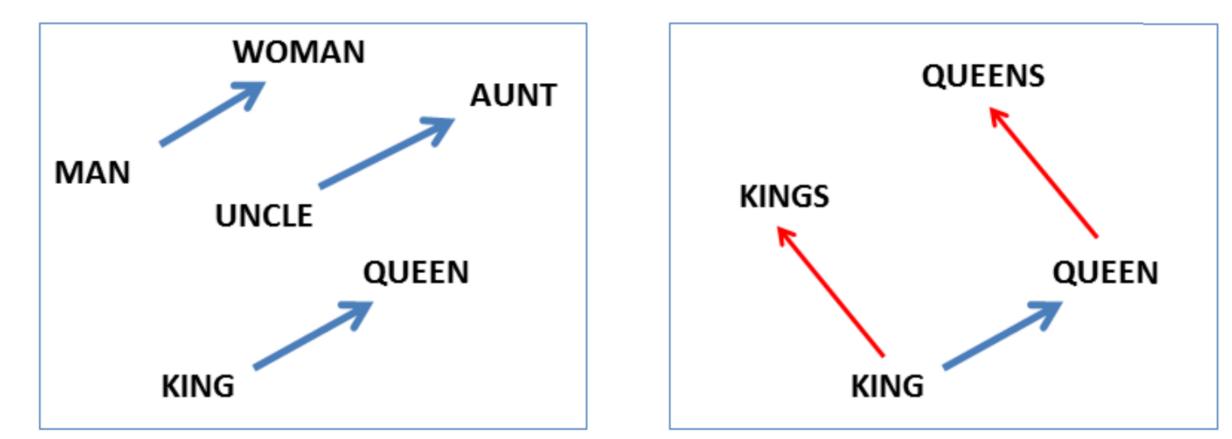


## Intrinsic Evaluation – Word Analogies 44

Word linear relationship  $w_A$  :  $w_B$ 

$$x = \arg \max_{x} \frac{(v_{w_B} - v_{w_A} + v_{w_C})^T v_{w_x}}{\|v_{w_B} - v_{w_A} + v_{w_C}\|}$$

Syntactic and Semantic example questions [link] 



Issue: what if the information is there but not linear

$$= w_C : w_x$$



# Slido: #ADL2021 Intrinsic Evaluation – Word Analogies

- Word linear relationship  $w_A: w_B = w_C: w_x$
- Syntactic and **Semantic** example questions [link]

### city---in---state

45

capital---country Chicago : Illinois = Houston : Texas Abuja : Nigeria = Accra : Ghana Chicago : Illinois = Philadelphia : Pennsylvania Abuja : Nigeria = Algiers : Algeria Chicago : Illinois = Phoenix : Arizona Abuja : Nigeria = Amman : Jordan Chicago : Illinois = Dallas : Texas Abuja : Nigeria = Ankara : Turkey Chicago : Illinois = Jacksonville : Florida Abuja : Nigeria = Antananarivo : Madagascar Chicago : Illinois = Indianapolis : Indiana Abuja : Nigeria = Apia : Samoa Chicago : Illinois = Aus8n : Texas Abuja : Nigeria = Ashgabat : Turkmenistan Chicago : Illinois = Detroit : Michigan Abuja : Nigeria = Asmara : Eritrea Chicago : Illinois = Memphis : Tennessee Abuja : Nigeria = Astana : Kazakhstan Chicago : Illinois = Boston : Massachusetts

## Issue: different cities may have same name

### Issue: can change with time



### Slido: #ADL2021 Intrinsic Evaluation – Word Analogies 46

- Word linear relationship  $w_A : w_B = w_C : w_x$
- **Syntactic** and Semantic example questions [link]

### superlative

- bad : worst = big : biggest
- bad : worst = bright : brightest
- bad : worst = cold : coldest
- bad : worst = cool : coolest
- bad : worst = dark : darkest
- bad : worst = easy : easiest
- bad : worst = fast : fastest
- bad : worst = good : best
- bad : worst = great : greatest

### past tense

dancing : danced = decreasing : decreased

- dancing : danced = describing : described
- dancing : danced = enhancing : enhanced
- dancing : danced = falling : fell
- dancing : danced = feeding : fed
- dancing : danced = flying : flew
- dancing : danced = generating : generated
- dancing : danced = going : went
- dancing : danced = hiding : hid
- dancing : danced = hiding : hit



# Intrinsic Evaluation – Word Correlation

Comparing word correlation with human-judged scores 

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Human-judged word correlation [link] 

| Word 1    | Word 2   | Human-Judged Score |
|-----------|----------|--------------------|
| tiger     | cat      | 7.35               |
| tiger     | tiger    | 10.00              |
| book      | paper    | 7.46               |
| computer  | internet | 7.58               |
| plane     | car      | 5.77               |
| professor | doctor   | 6.62               |
| stock     | phone    | 1.62               |

# Ambiguity: synonym or same word with different POSs



### Slido: #ADL2021 **Extrinsic Evaluation – Subsequent Task** 48

Goal: use word vectors in neural net models built for subsequent tasks 

# Benefit

- Ability to also classify words accurately Ex. countries cluster together a classifying location words should be possible with word vectors
- Incorporate any information into them other tasks  $\bigcirc$ 
  - Ex. project sentiment into words to find most positive/negative words in corpus

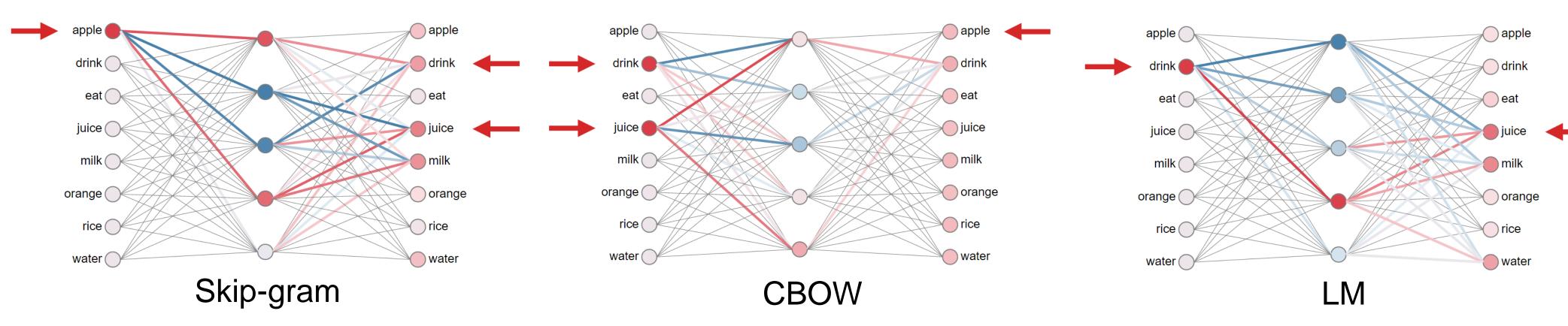




# **Concluding Remarks**

### Low dimensional word vector word2vec $\bigcirc$

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- GloVe: combining count-based and direct learning 0
- Word vector evaluation
  - Intrinsic: word analogy, word correlation 0
  - Extrinsic: subsequent task 0

