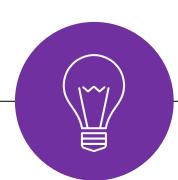
# Word Embeddings

## March 31st, 2020 http://adl.miulab.tw



# Applied Deep Learning









# **Meaning Representations in Computers**

- Knowledge-based representation
- **Corpus-based representation** 
  - Atomic symbol  $\checkmark$
  - Neighbors  $\checkmark$

3

- High-dimensional sparse word vector
- Low-dimensional dense word vector
  - Method 1 dimension reduction Ο
  - Method 2 direct learning Ο

# **Meaning Representations in Computers**

#### Knowledge-based representation

#### **Corpus-based representation**

#### Atomic symbol $\checkmark$

Neighbors

4

- High-dimensional sparse word vector
- Low-dimensional dense word vector
  - Method 1 dimension reduction  $\bigcirc$
  - Method 2 direct learning 0



Atomic symbols: *one-hot* representation 

car [0 0 0 0 0 0

Issues: difficult to compute the similarity (i.e. comparing "car" and "motorcycle")

car

Idea: words with similar meanings often have similar neighbors

## $[0\ 0\ 0\ 0\ 0\ 0\ 1\ 0\ 0\ \dots\ 0] = 0$ motorcycle

# **Meaning Representations in Computers**

- Knowledge-based representation
- **Corpus-based representation** 
  - Atomic symbol
  - Neighbors  $\checkmark$

6

- High-dimensional sparse word vector
- Low-dimensional dense word vector
  - Method 1 dimension reduction  $\bigcirc$
  - Method 2 direct learning Ο

# Window-based Co-occurrence Matrix

## Example

7

- Window length=1
- Left or right context
- Corpus:

love NTU.

I love deep learning.

l enjoy learning.

#### Issues:

- matrix size increases with vocabulary
- high dimensional
- sparsity  $\rightarrow$  poor robustness

#### similarity > 0

Counts		love	enjoy	NTU	deep	learning
	0	2	1	0	0	0
love	2	0	0	1	1	0
enjoy	1	0	0	0	0	1
NTU	0	1	0	0	0	0
deep	0	1	0	0	0	1
learning	0	0	1	0	1	0

Idea: low dimensional word vector



# **Meaning Representations in Computers**

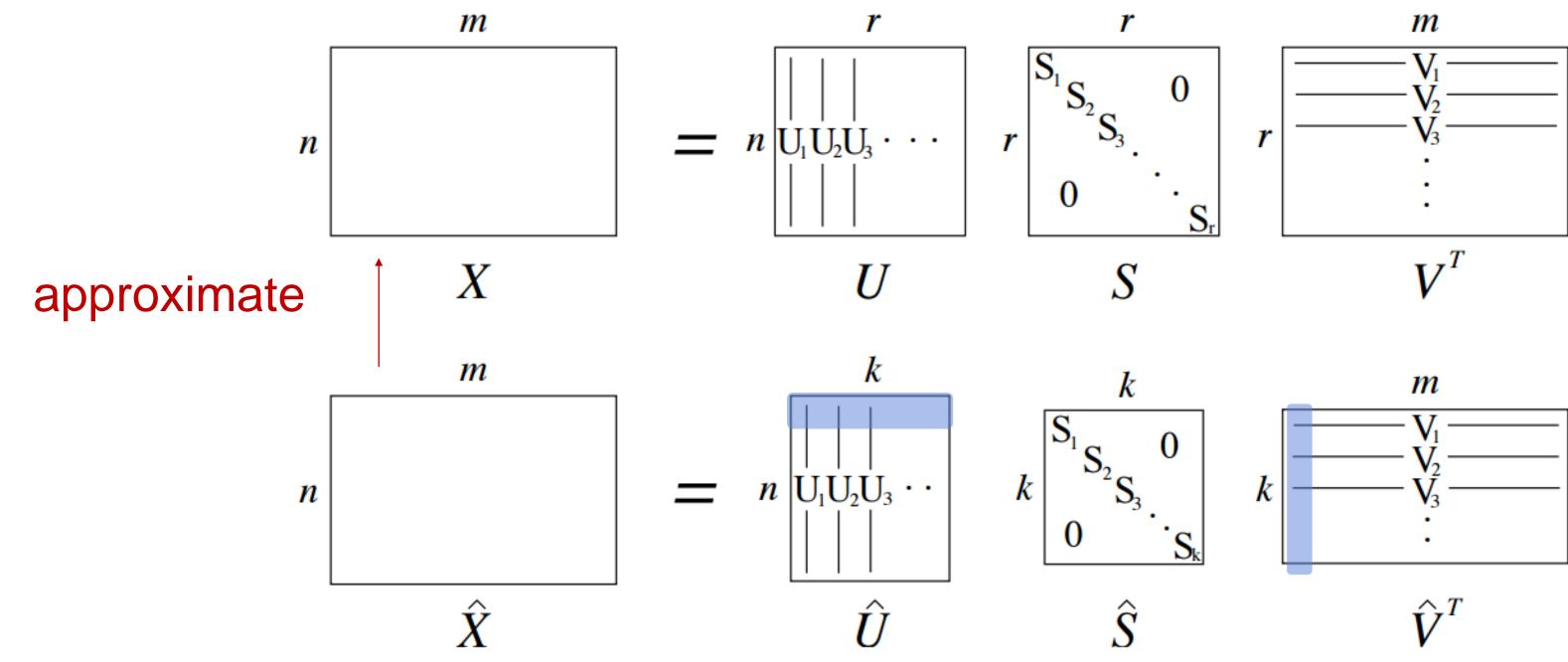
- Knowledge-based representation
- **Corpus-based representation** 
  - Atomic symbol
  - Neighbors  $\checkmark$

8

- High-dimensional sparse word vector
- Low-dimensional dense word vector
  - Method 1 dimension reduction Ο
  - Method 2 direct learning 0

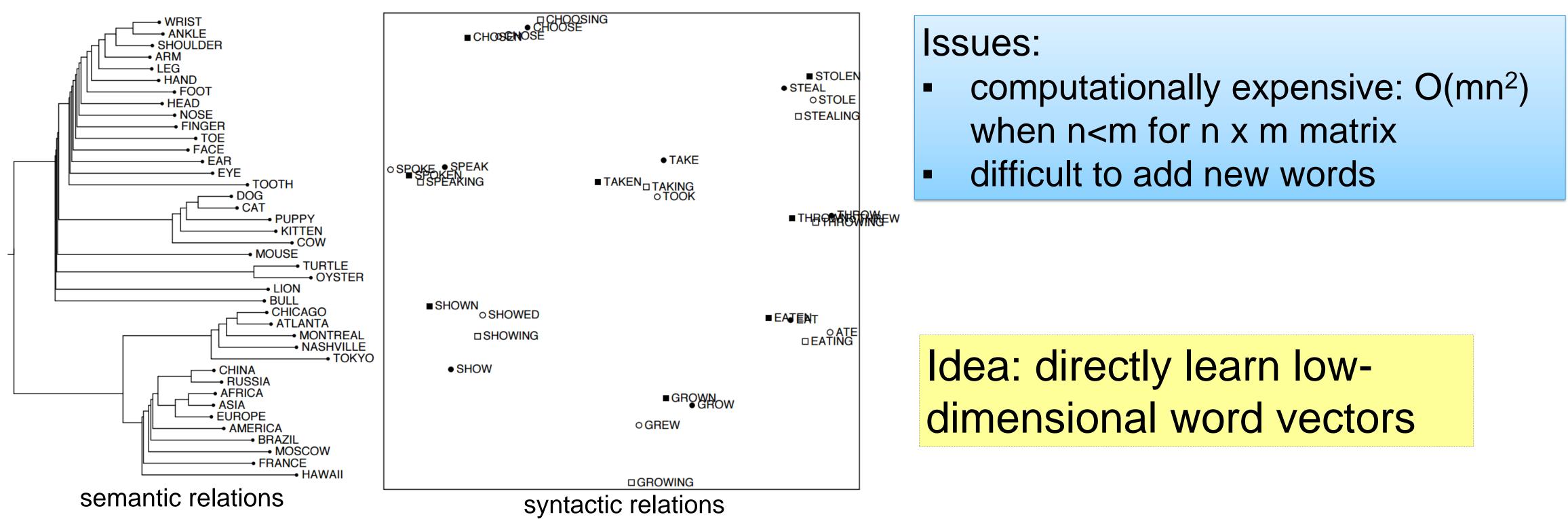
### **Low-Dimensional Dense Word Vector** 9

- Method 1: dimension reduction on the matrix
- Singular Value Decomposition (SVD) of co-occurrence matrix X



#### Low-Dimensional Dense Word Vector 10

Method 1: dimension reduction on the matrix Singular Value Decomposition (SVD) of co-occurrence matrix X



## Word Representation 11

- Knowledge-based representation
- **Corpus-based representation** 
  - Atomic symbol  $\checkmark$
  - Neighbors  $\checkmark$ 
    - High-dimensional sparse word vector
    - Low-dimensional dense word vector
      - Method 1 dimension reduction Ο
      - Method 2 direct learning  $\rightarrow$  word embedding Ο

# Word Embedding

12

Method 2: directly learn low-dimensional word vectors 

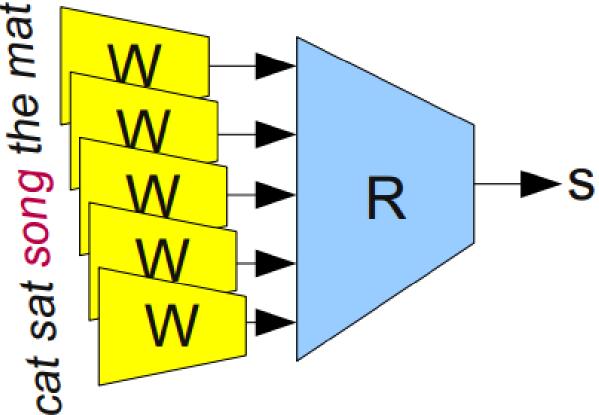
- Ο
- A neural probabilistic language model (Bengio et al., 2003) Ο
- NLP (almost) from Scratch (Collobert & Weston, 2008) Ο
- Recent and most popular models: word2vec (Mikolov et al. 2013) and Glove 0 (Pennington et al., 2014)

# Learning representations by back-propagation. (Rumelhart et al., 1986)

# Word Embedding Benefit

13

Given an <u>unlabeled</u> training corpus, produce a vector for each word that encodes its semantic information. These vectors are useful because: 1) semantic similarity between two words can be calculated as the cosine similarity between their corresponding word vectors 2) word vectors as powerful features for various supervised NLP tasks since the vectors contain semantic information 3) propagate any information into them via neural networks and update during training





# Word Embeddings Word2Vec

### Word2Vec – Skip-Gram Model 15

- Goal: predict surrounding words within a window of each word Objective function: maximize the probability of any context word given the
- current center word

$$w_{1}, w_{2}, \cdots, w_{t-m}, \cdots, w_{t-1}, w_{t}, w_{t+1}, \cdots, w_{t+m}, \cdots, w_{T-1}, w_{T}$$

$$w_{I} \qquad w_{O}$$

$$w_{O} \qquad w_{O} \qquad w_{O}$$

$$w_{1}, w_{2}, \cdots, w_{t-m}, \cdots, w_{t-1}, w_{t} w_{t+1}, \cdots, w_{t+m}, \cdots, w_{T-1}, w_{T}$$

$$w_{I} c w_{O}$$

$$p(w_{O,1}, w_{O,2}, \cdots, w_{O,C} \mid w_{I}) = \prod_{c=1}^{C} p(w_{O,c} \mid w_{I})$$

$$target word vector$$

$$p(w_{O} \mid w_{I}) = \frac{\exp(v_{w_{O}}^{\prime T} v_{w_{I}})}{\sum_{j} \exp(v_{w_{j}}^{\prime T} v_{w_{I}})}$$

$$target word vector$$

$$w_{I} c w_{I} v_{I} v$$

$$w_{1}, w_{2}, \cdots, \underbrace{w_{t-m}, \cdots, w_{t-1}, (w_{t})}_{w_{I}} \underbrace{w_{t+1}, \cdots, w_{t+m}}_{context window}, \cdots, w_{T-1}, w_{T}$$

$$p(w_{O,1}, w_{O,2}, \cdots, w_{O,C} \mid w_{I}) = \prod_{c=1}^{C} p(w_{O,c} \mid w_{I})$$

$$target word vector$$

$$C(\theta) = -\sum_{w_{I}} \sum_{c=1}^{C} \log p(w_{O,c} \mid w_{I})$$

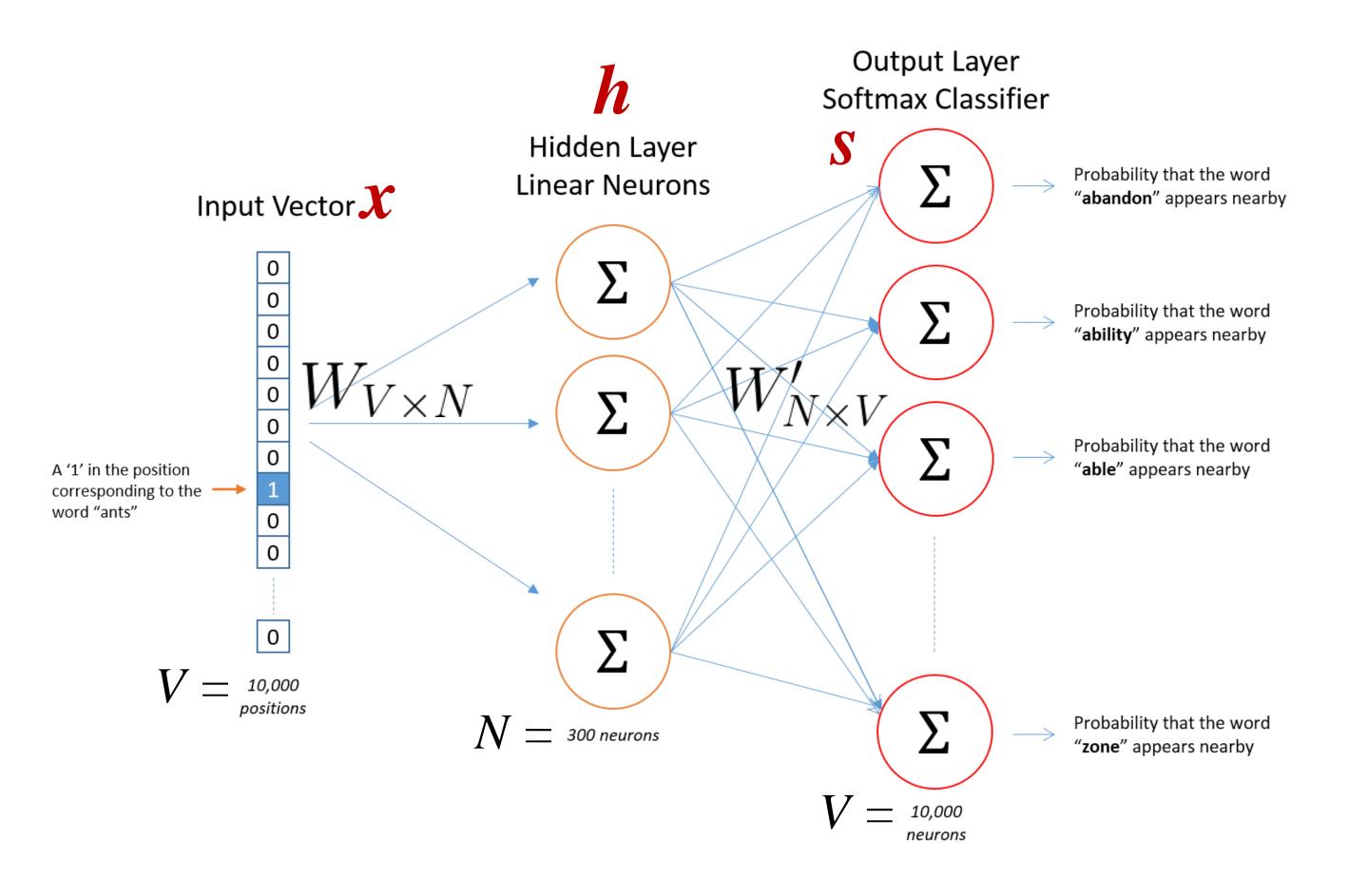
$$p(w_{O} \mid w_{I}) = \frac{\exp(v_{w_{O}}^{\prime T} (w_{w_{I}}))}{\sum_{j} \exp(v_{w_{j}}^{\prime T} v_{w_{I}})}$$
outside target word

Benefit: faster, easily incorporate a new sentence/document or add a word to vocab



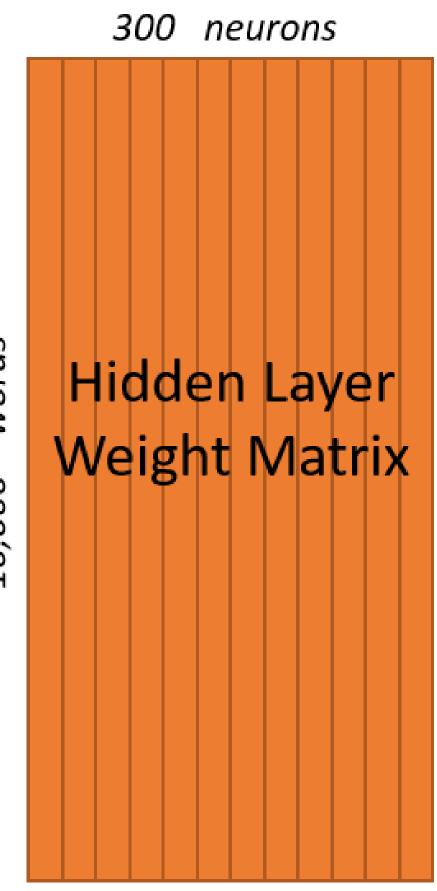


#### Goal: predict surrounding words within a window of each word





## Hidden Layer Matrix $\rightarrow$ Word Embedding Matrix



words 10,000

 $W_{V \times N}$ 

300 features words Word Vector Lookup Table! 10,000

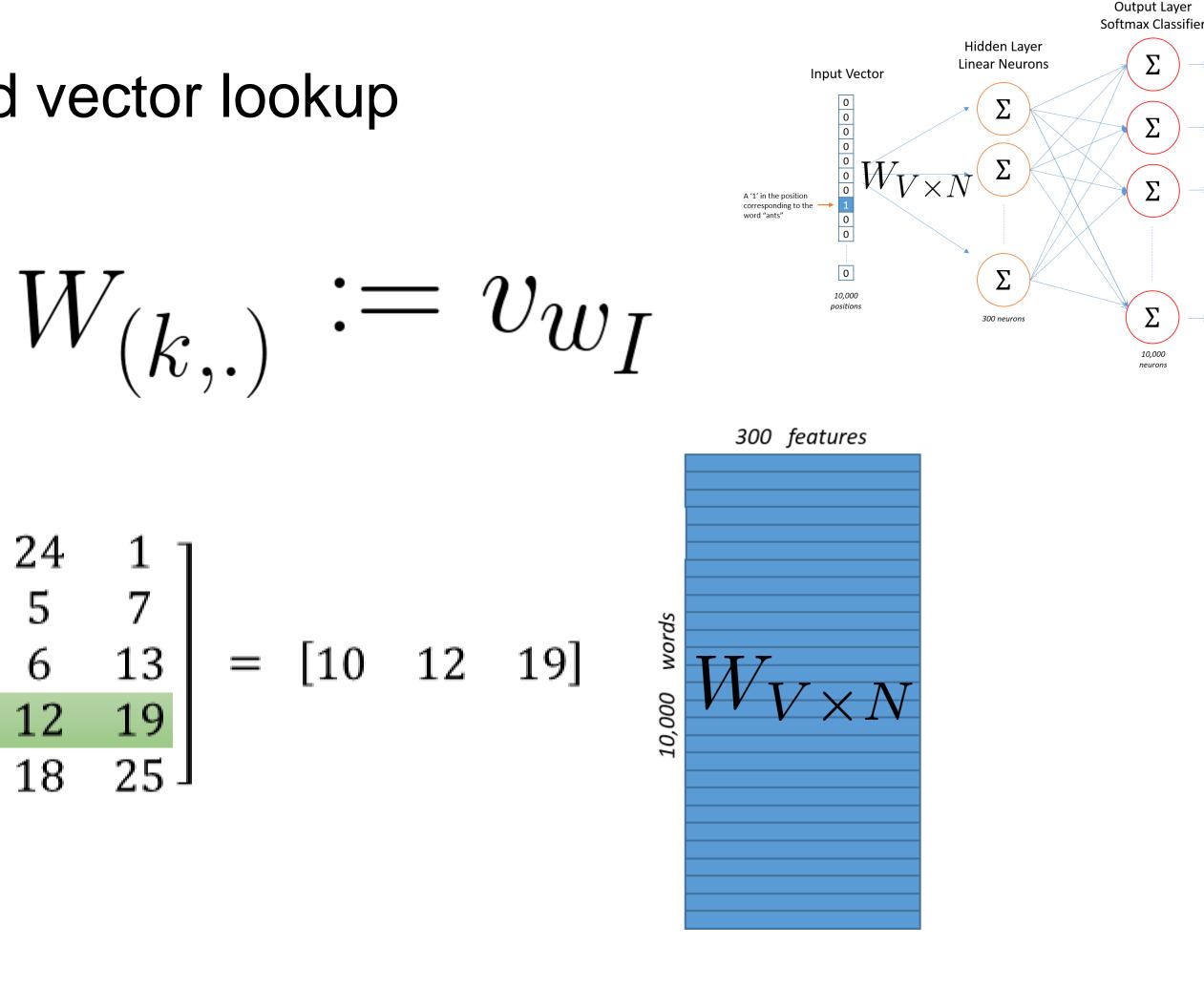
## Weight Matrix Relation 18

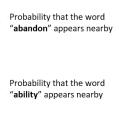
Hidden layer weight matrix = word vector lookup 

$$h = x^T W = \mathbf{I}$$

 $\begin{bmatrix} 0 & 0 & 0 & 1 & 0 \end{bmatrix} \times \begin{bmatrix} 17 & 24 & 1 \\ 23 & 5 & 7 \\ 4 & 6 & 13 \\ 10 & 12 & 19 \end{bmatrix} = \begin{bmatrix} 10 & 12 & 19 \end{bmatrix}$ 18

Each vocabulary entry has two vectors: as a target word and as a context word





Probability that the word "able" appears nearby

Probability that the word "zone" appears nearby

## Weight Matrix Relation 19

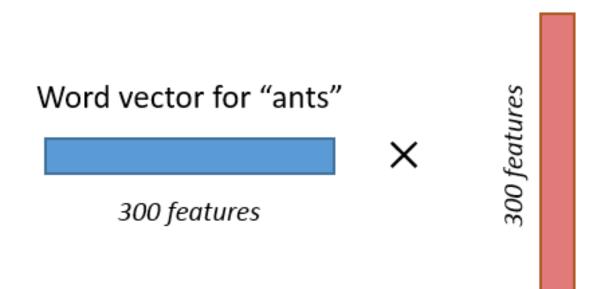
Output layer weight matrix = weighted sum as final score 

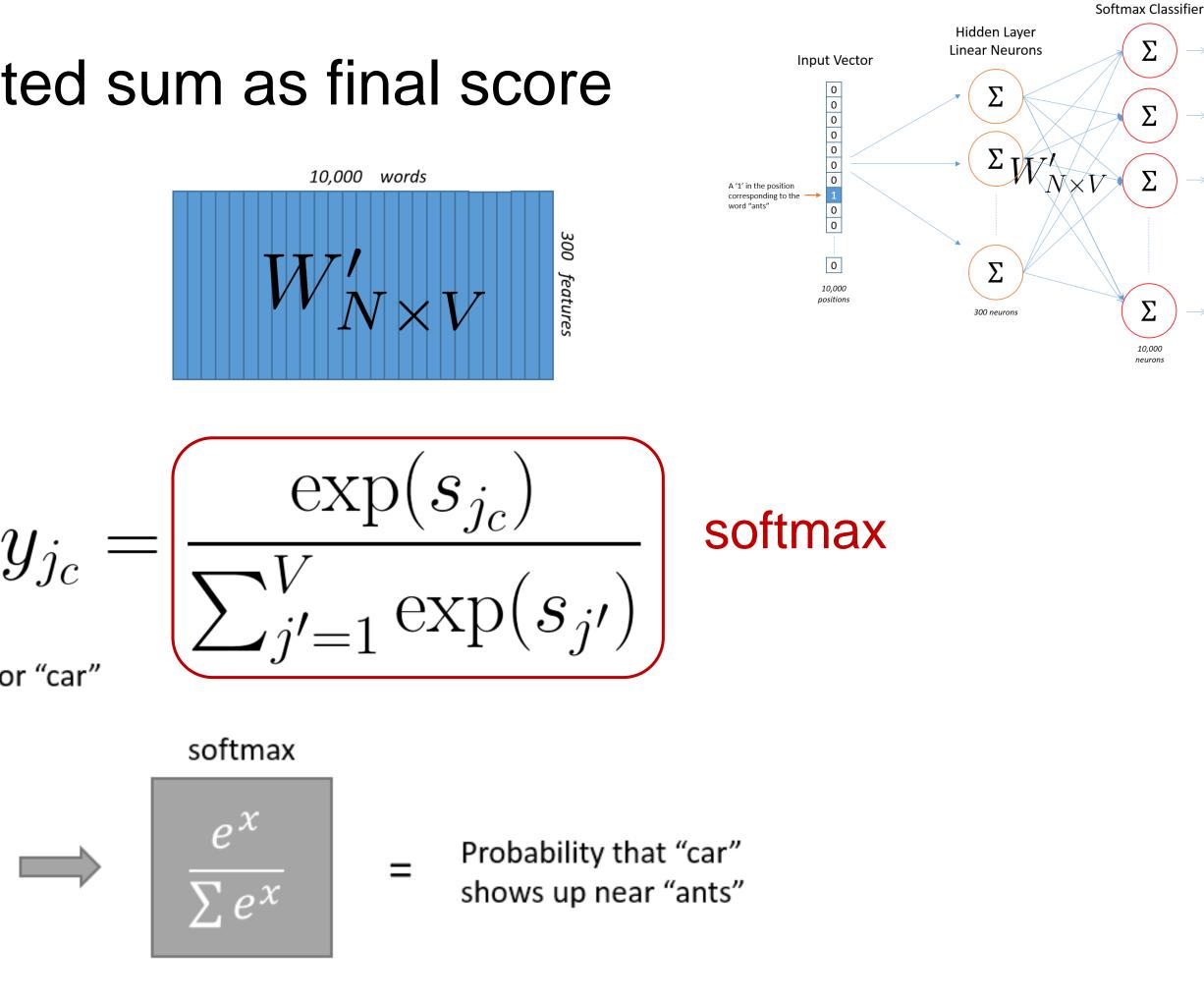
$$s_j = h v'_{w_j}$$

$$p(w_j = w_{O,c} \mid w_I) = q$$

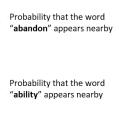
within the context window

Output weights for "car"





#### Each vocabulary entry has two vectors: as a target word and as a context word

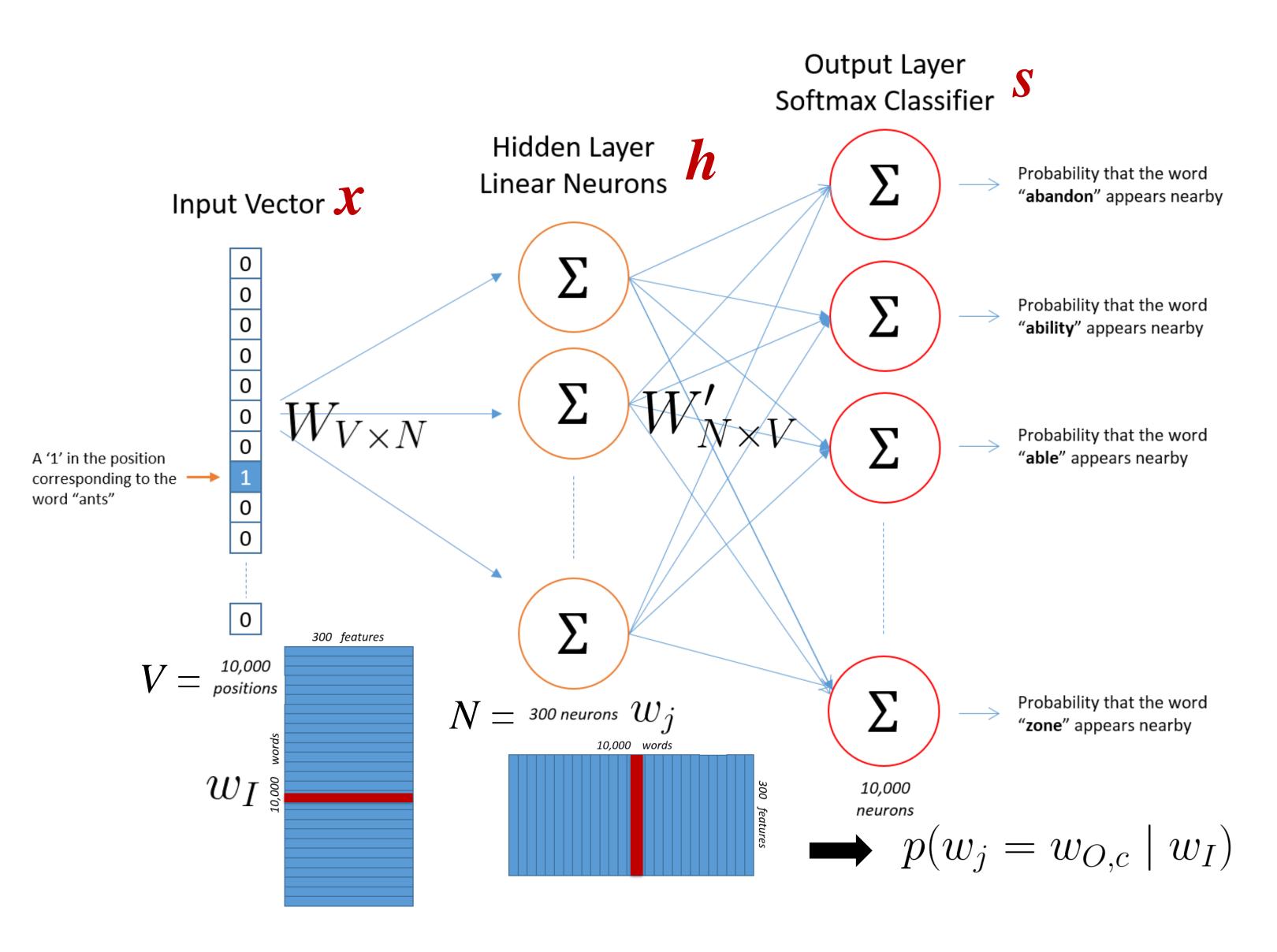


Output Layer

Probability that the word "able" appears nearby

Probability that the word "zone" appears nearby

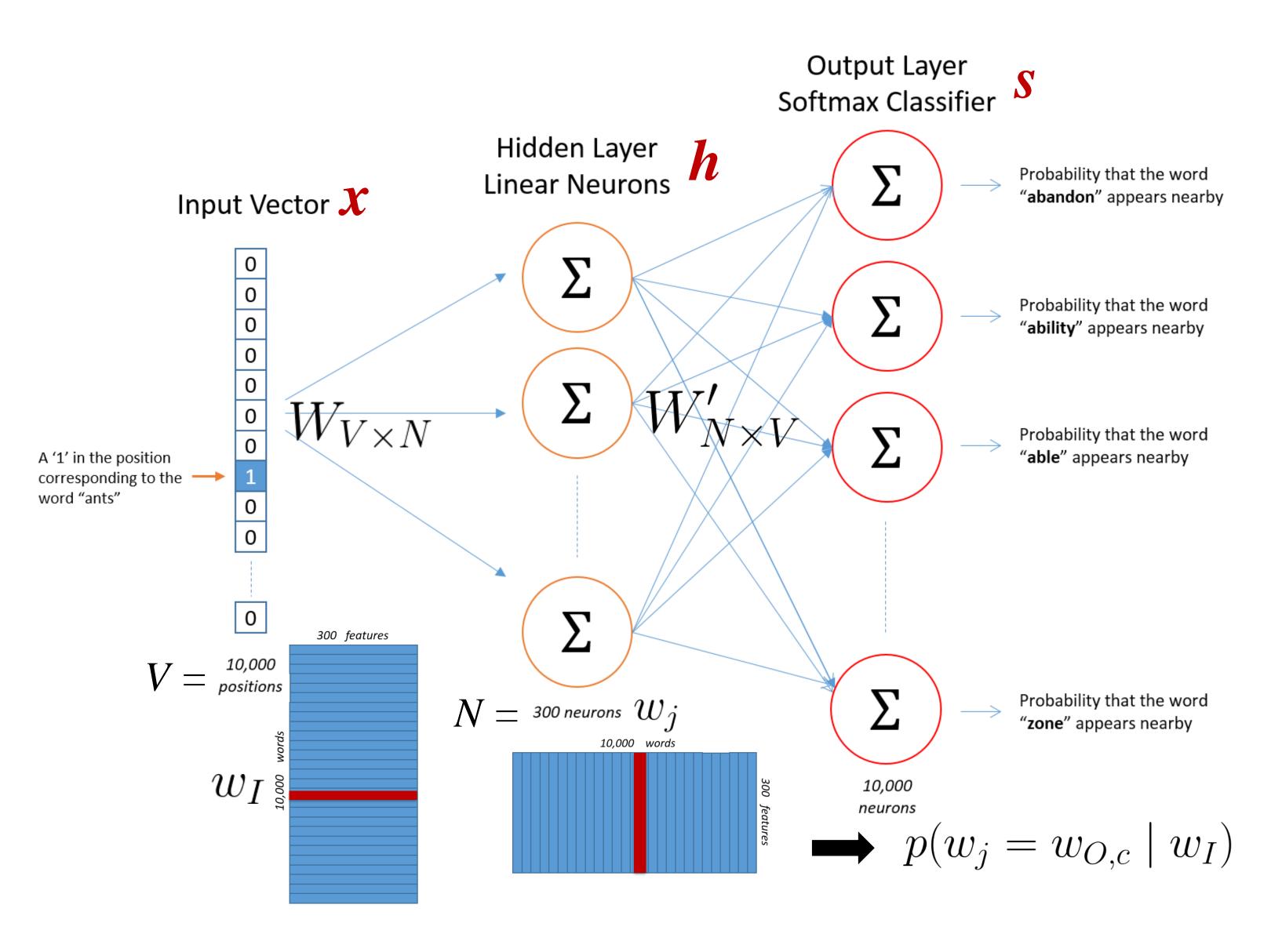
### Word2Vec Skip-Gram Illustration 20



# Word Embeddings Word2Vec Training



## Word2Vec Skip-Gram Illustration



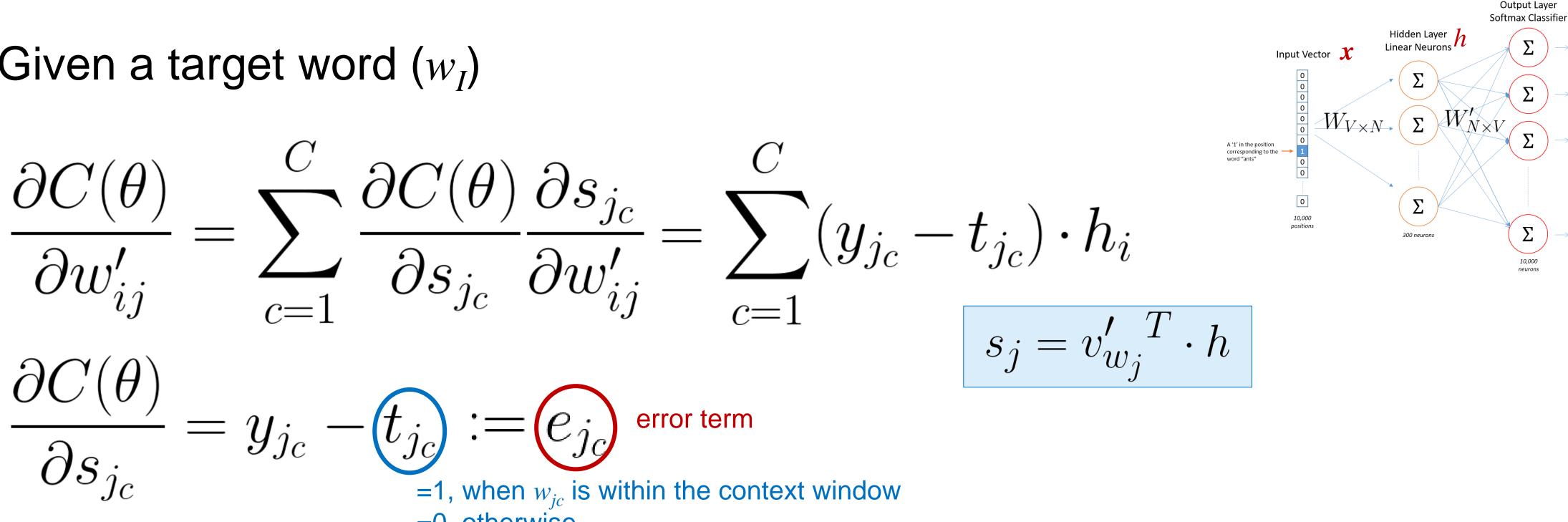


Given a target word  $(w_I)$ 

 $C(\theta) = -\log p(w_{O,1}, w_{O,2}, \cdots, w_{O,C} \mid w_I)$  $= -\log \prod_{c=1}^{C} \frac{\exp(s_{j_c})}{\sum_{j'=1}^{V} \exp(s_{j'})}$ C $= -\sum s_{j_c} + C \log \sum \exp(s_{j'})$ c=1i'=1

### SGD Update for W' 24

Given a target word  $(w_I)$ 



=0, otherwise

$$w_{ij}^{\prime (t+1)} = w_{ij}^{\prime (t)} - \eta \cdot \sum_{c=1}^{C} (y_{j_c} - t_{j_c}) \cdot h_i$$



Probability that the word bandon" appears near

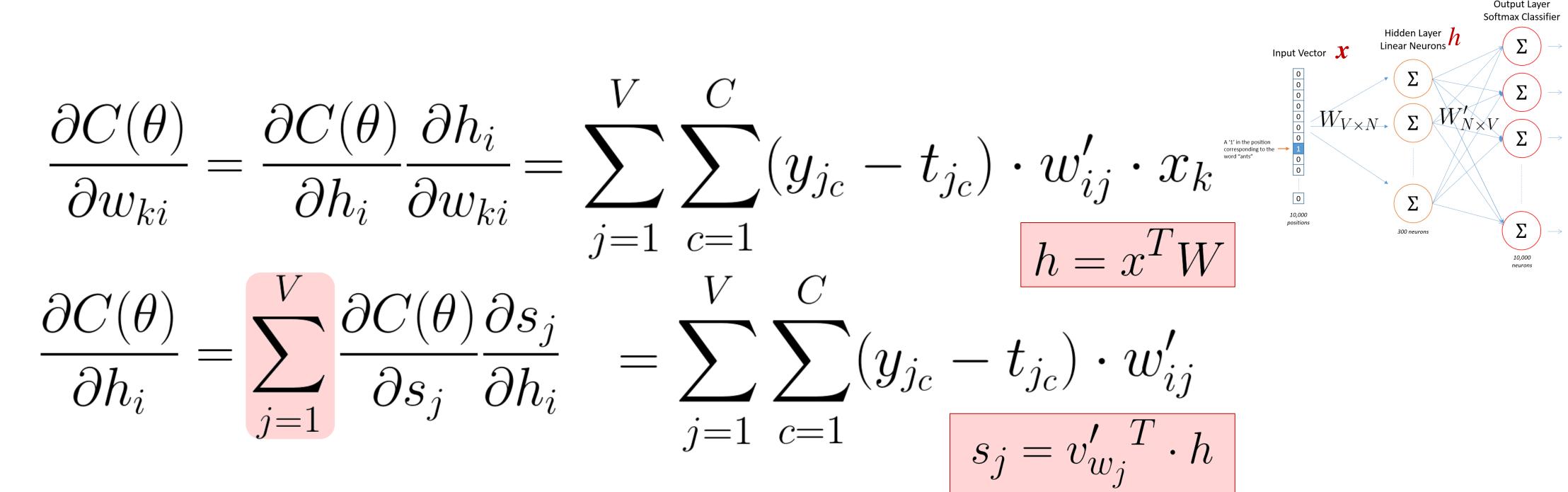
Probability that the word ability" appears near

Probability that the word "able" appears nearby

Probability that the word "zone" appears nearby



# SGD Update for W



 $w_{ij}^{(t+1)} = w_{ij}^{(t)} - \eta \cdot \sum_{i=1}^{t} \sum_{j=1}^{t} w_{ij}^{(t)} - \eta \cdot \sum_{j=1}^{t} w_{ij}^{(t)} + \psi_{ij}^{(t)} + \psi$ *j*=

$$\sum_{i=1}^{C} \sum_{c=1}^{C} (y_{j_c} - t_{j_c}) \cdot w'_{ij} \cdot x_j$$



Probability that the word "**abandon"** appears nearby

Probability that the word "**ability**" appears nearby

Probability that the word "**able**" appears nearby

Probability that the word "zone" appears nearby

$$\begin{array}{l} \mathbf{5} \quad \mathbf{SGD Update} \\ w_{ij}^{\prime (t+1)} &= w_{ij}^{\prime (t)} - \eta \cdot \sum_{c=1}^{C} (y_{j_c} - t_{j_c}) \cdot h_i \\ w_{ij}^{\prime (t+1)} &= v_{w_j}^{\prime (t)} - \eta \cdot EI_j \cdot h \\ w_{ij}^{(t+1)} &= w_{ij}^{(t)} - \eta \cdot \sum_{j=1}^{V} \sum_{c=1}^{C} (y_{j_c} - t_{j_c}) \cdot w_{ij}^{\prime} \cdot x_j \\ w_{ij}^{(t+1)} &= w_{w_I}^{(t)} - \eta \cdot EH^T \\ v_{w_I}^{(t+1)} &= v_{w_I}^{(t)} - \eta \cdot EH^T \\ \end{array}$$

large vocabularies or large training corpora  $\rightarrow$  expensive computations

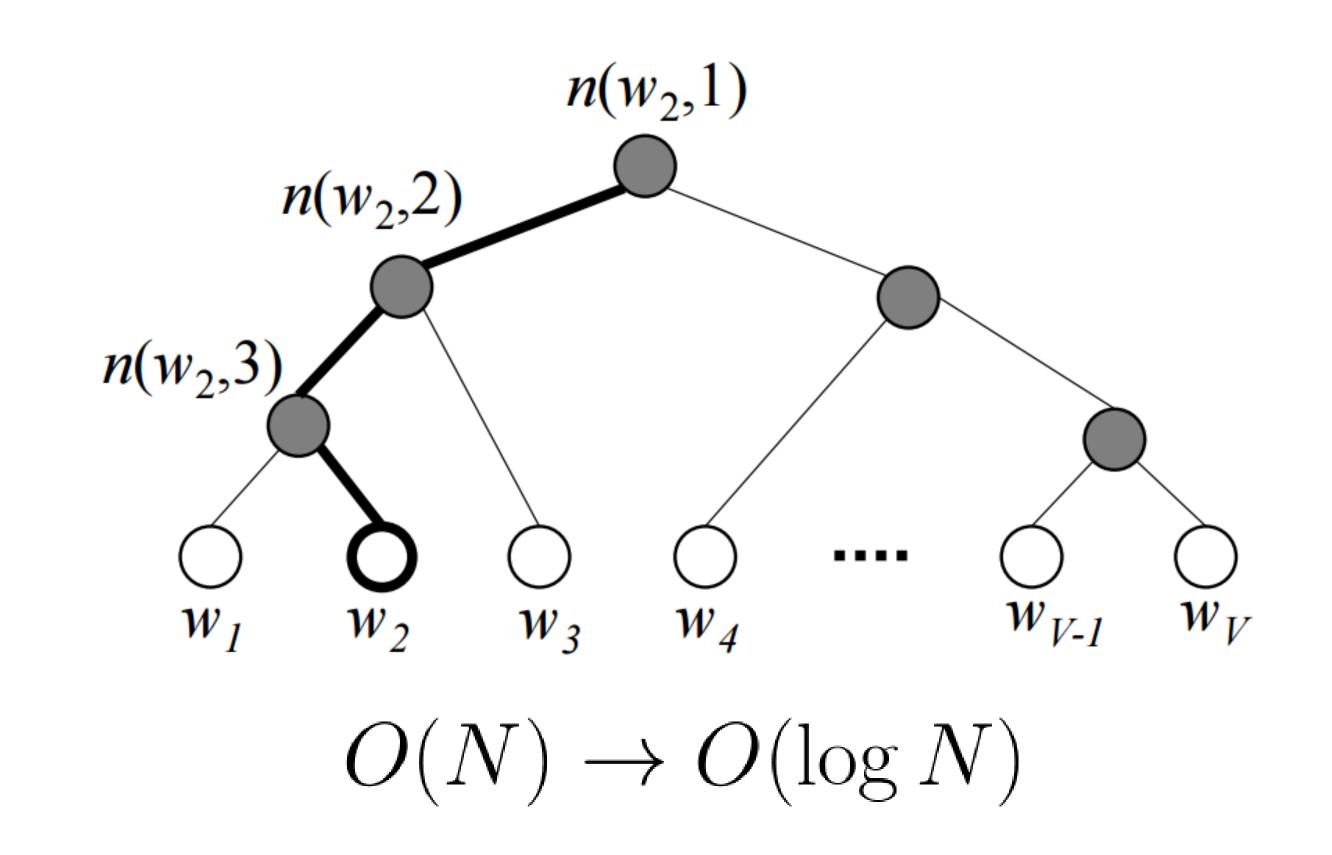
limit the number of output vectors that must be updated per training instance  $\rightarrow$  hierarchical softmax, sampling

# Word Embeddings Negative Sampling





Idea: compute the probability of leaf nodes using the paths 



Mikolov et al., "Distributed representations of words and phrases and their compositionality," in NIPS, 2013.

## **Negative Sampling** 29

Idea: only update a sample of output vectors 

$$C(\theta) = -\log \sigma(v'_{w_O}{}^T v_{w_I}) + \sum_{w_j \in \mathcal{W}_{neg}} \log \sigma(v'_{w_j}{}^T v_{w_I})$$
$$v'_{w_j}{}^{(t+1)} = v'_{w_j}{}^{(t)} - \eta \cdot EI_j \cdot h$$
$$EI_j = \sigma(v'_{w_j}{}^T v_{w_I}) - t_j$$
$$V_{w_I}{}^{(t+1)} = v^{(t)}_{w_I} - \eta \cdot EH^T$$
$$EH = \sum_{w_j \in \{w_O\} \cup \mathcal{W}_{neg}} EI_j \cdot v'_{w_j}$$
$$w_j \in \{w_O\} \cup \mathcal{W}_{neg}$$

Mikolov et al., "Distributed representations of words and phrases and their compositionality," in NIPS, 2013.

## **Negative Sampling** 30

- Sampling methods
  - Random sampling  $w_i \in \{w_O\} \cup \mathcal{W}_{neg}$ 0
  - Ο

Idea: less frequent words sampled more often

Empirical setting: unigram model raised to the power of 3/4

Word	Probabi
is	
constitution	
bombastic	

Mikolov et al., "Distributed representations of words and phrases and their compositionality," in NIPS, 2013.

Distribution sampling:  $w_i$  is sampled from P(w) What is a good P(w)?

lity to be sampled for "neg"

 $0.9^{3/4} = 0.92$ 

 $0.09^{3/4} = 0.16$ 

 $0.01^{3/4} = 0.032$ 

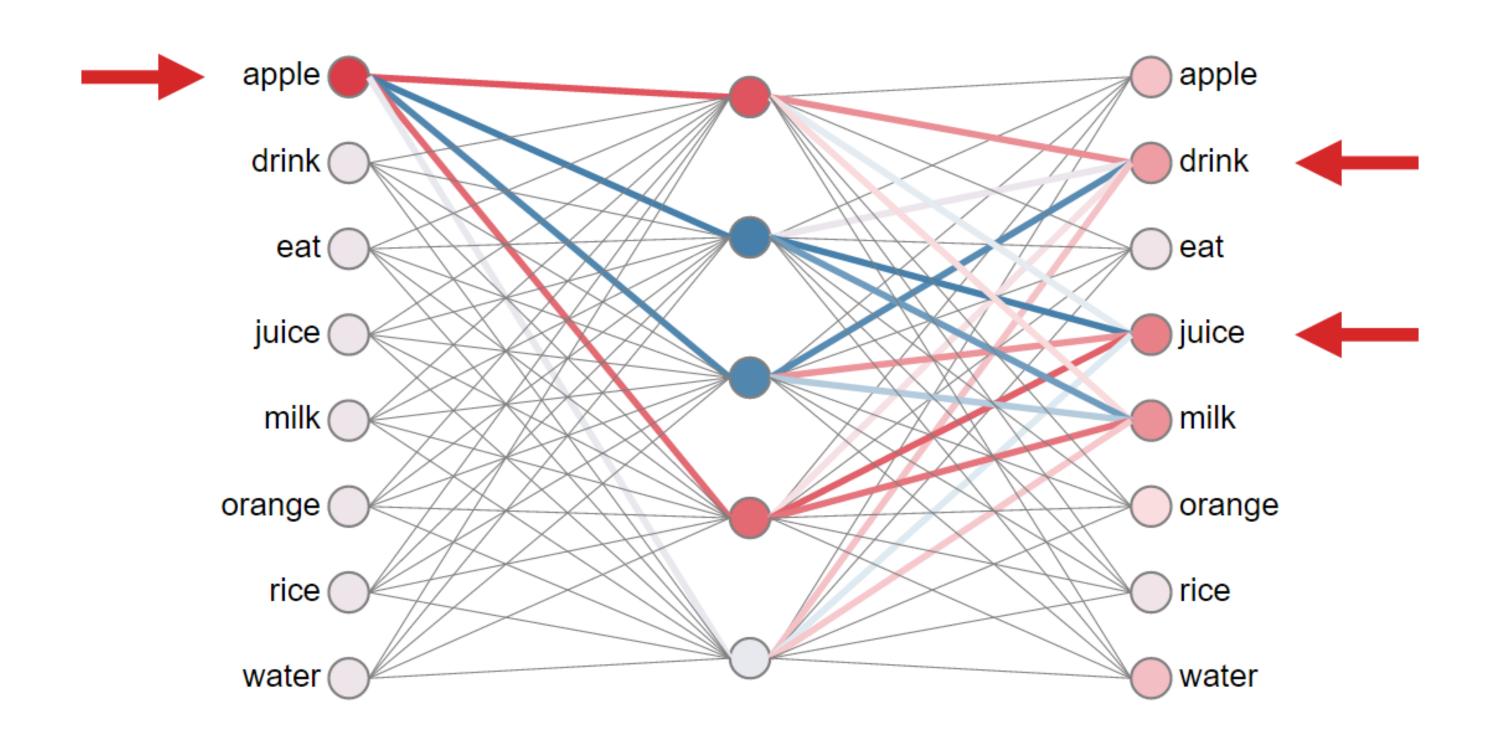


# <sup>31</sup> Word Embeddings Word2Vec Variants



## Word2Vec Skip-Gram Visualization <a href="https://ronxin.github.io/wevi/">https://ronxin.github.io/wevi/</a>

Skip-gram training data: e^water



apple|drink^juice,orange|eat^apple,rice|drink^juice,juice|drink^milk,milk|drink^rice,water|drink^mil k,juice|orange^apple,juice|apple^drink,milk|rice^drink,drink|milk^water,drink|water^juice,drink|juic



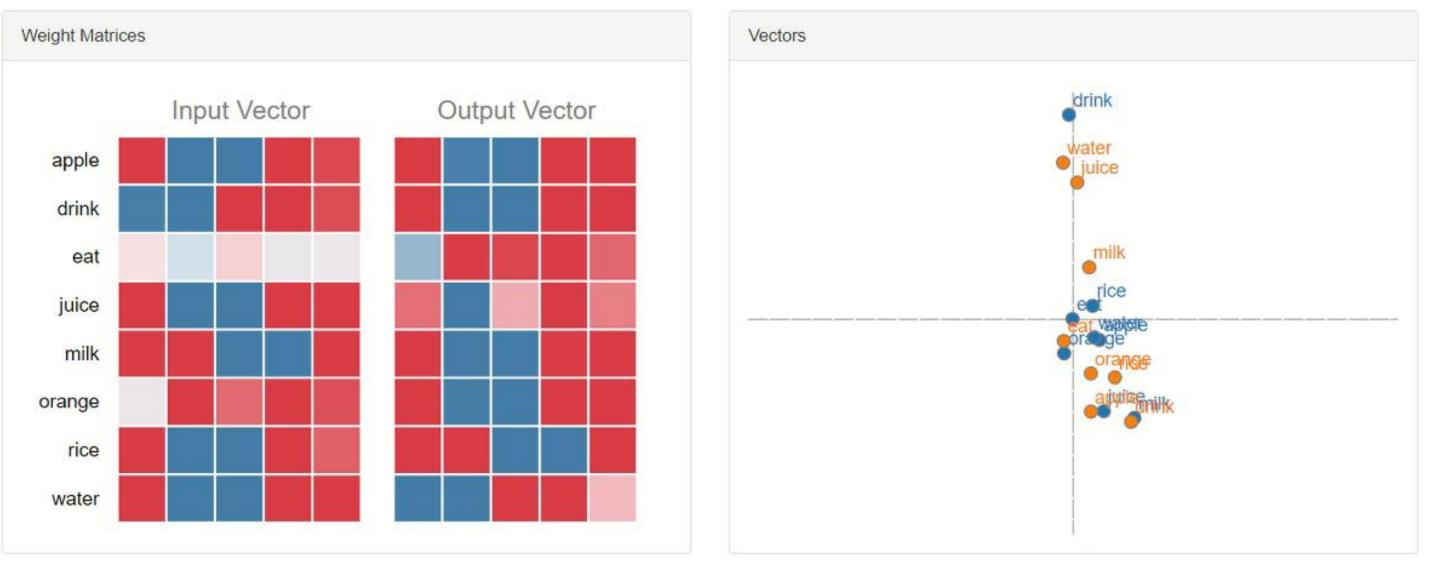


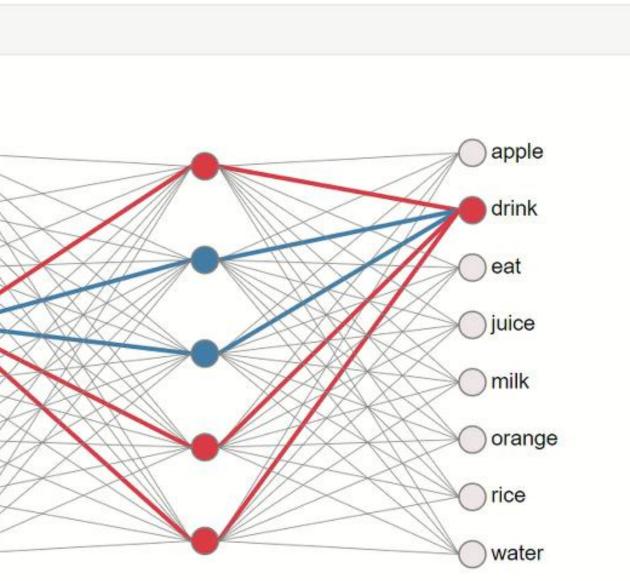


#### wevi: word embedding visual inspector

Everything you need to know about this tool - Source code

Control Panel	Neurons
Config:	
{"hidden_size":5,"random_state":1,"learning_rate":0 .2}	apple
Training data (context target):	drink
apple/drink^juice,orange/eat^apple,rice/drink^juice,j	eat
uice drink^milk,milk drink^rice,water drink^milk,juice  orange^apple,juice apple^drink,milk rice^drink,drink  milk^water,drink water^juice,drink juice^water	juice
Presets: Fruit and juice (Skip-gram) ▼	milk
Update and Restart Update Learning Rate	orange
Next 20 100 500 PCA	rice
	water





# Word2Vec Variants

34

2013)

 $p(w_{t-m}, \cdots w_{t-1}, w_t)$ 

- surrounding words (Mikolov+, 2013)
- $p(w_t \mid w_{t-m}, \cdots, w_{t-1}, w_{t+1}, \cdots, w_{t+m})$ contexts (Mikolov+, 2013)

$$p(w_{t+1} \mid w_t)$$

## Practice the derivation by yourself!!

Mikolov et al., "Efficient estimation of word representations in vector space," in ICLR Workshop, 2013. Mikolov et al., "Linguistic regularities in continuous space word representations," in NAACL HLT, 2013.

**Skip-gram**: predicting surrounding words given the target word (Mikolov+,

$$w_{t+1}, \cdots, w_{t+m} \mid w_t)$$

**CBOW (continuous bag-of-words)**: predicting the target word given the

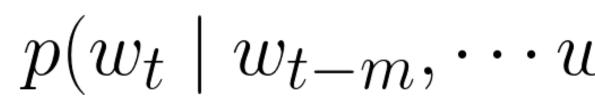
# LM (Language modeling): predicting the next words given the proceeding

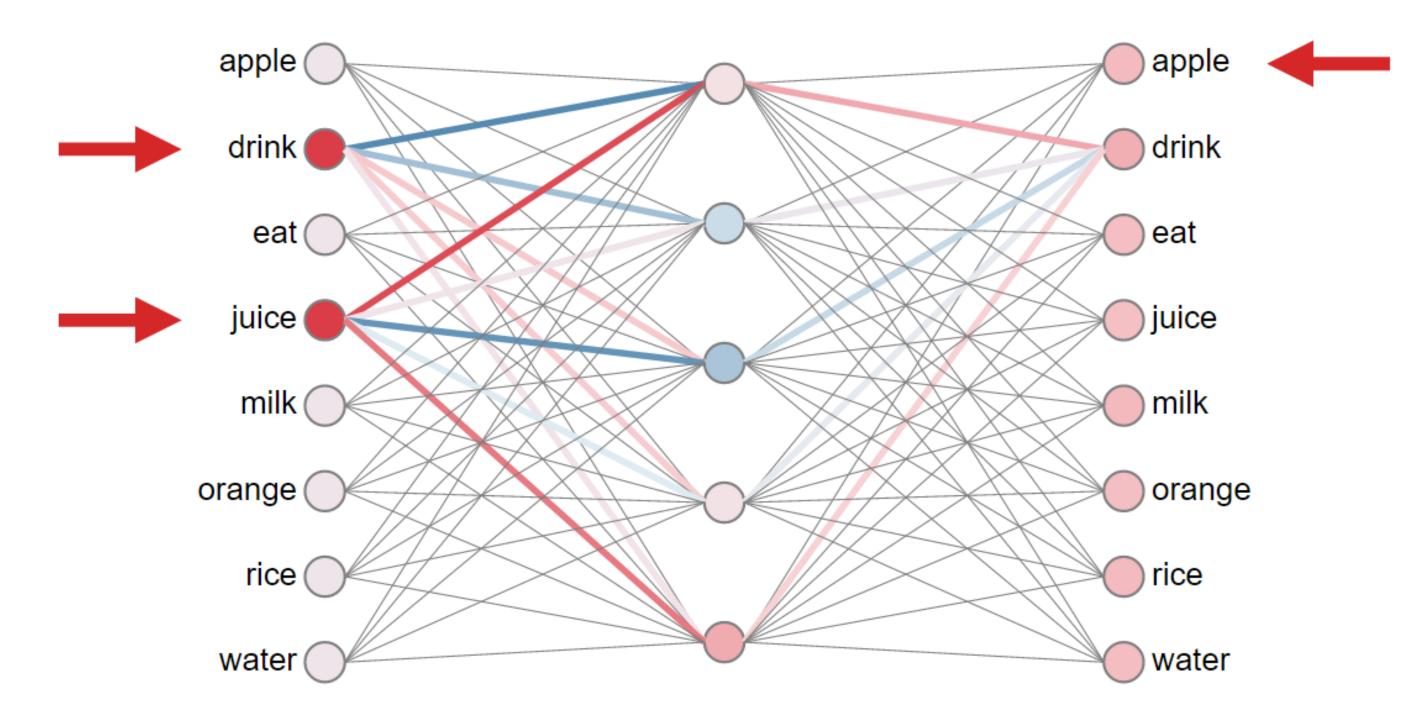






Goal: predicting the target word given the surrounding words 

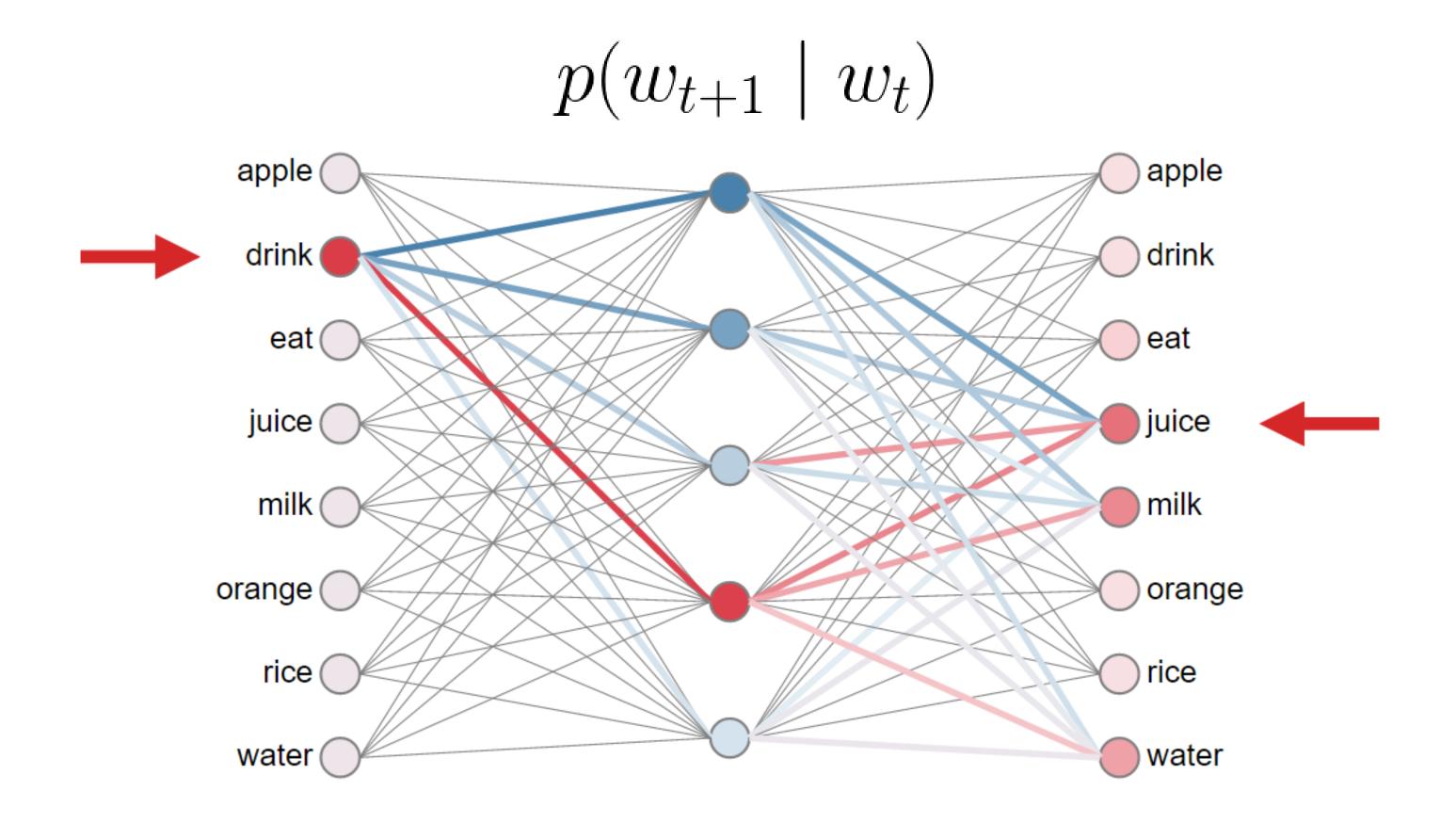




$$v_{t-1}, w_{t+1}, \cdots, w_{t+m}$$



## • Goal: predicting the next words given the proceeding contexts







#### Count-based

- LSA, HAL (Lund & Burgess), COALS (Rohde et al), Hellinger-PCA (Lebret & Collobert)
- Pros  $\bigcirc$ 
  - Fast training
  - Efficient usage of statistics
- Cons  $\bigcirc$ 
  - Primarily used to capture word similarity
  - Disproportionate importance given to large counts

# Combining the benefits from both worlds $\rightarrow$ GloVe

#### **Direct prediction**

#### NNLM, HLBL, RNN, Skipgram/CBOW 0 (Bengio et al; Collobert & Weston; Huang et al; Mnih & Hinton; Mikolov et al; Mnih & Kavukcuoglu)

#### Pros $\bigcirc$

- Generate improved performance on other tasks
- Capture complex patterns beyond word similarity

#### Cons $\bigcirc$

- Benefits mainly from large corpus
- Inefficient usage of statistics





- Idea: ratio of co-occurrence probability can encode meaning
- $P_{ij}$  is the probability that word  $w_i$  appears in the context of word  $w_i$

$$P_{ij} = P(w_j$$

Relationship between the words  $w_i$  and  $w_j$ 

	x = solid	x = gas	x = water	x = random
$P(x \mid ice)$	large	small	large	small
$P(x \mid \text{stream})$	small	large	large	small
$\frac{P(x \mid \text{ice})}{P(x \mid \text{stream})}$	large	small	~ 1	~ 1

Pennington et al., "GloVe: Global Vectors for Word Representation," in EMNLP, 2014.

$$w_i) = X_{ij}/X_i$$



The relationship of  $w_i$  and  $w_j$  approximates the ratio of their co-occurrence probabilities with various  $w_k$ 

$$F(w_i, w_j, \tilde{w}_k) = \frac{P_{ik}}{P_{jk}}$$

$$F(w_i - w_j, \tilde{w}_k) = \frac{P_{ik}}{P_{jk}}$$

$$F((v_{w_i} - v_{w_j})^T v'_{\tilde{w}_k}) = \frac{P_{ik}}{P_{jk}} \quad F(\cdot) = \exp(\cdot)$$

$$v_{w_i} \cdot v'_{\tilde{w}_k} = v_{w_i}^T v'_{\tilde{w}_k} = \log P(w_k \mid w_i)$$

Pennington et al., "GloVe: Global Vectors for Word Representation," in EMNLP, 2014.



$$v_{w_{i}} \cdot v_{\tilde{w}_{j}}' = v_{w_{i}}^{T} v_{\tilde{w}_{j}}' = \log P(w_{j} \mid w_{i}) \qquad P_{ij} = X_{ij}/X_{i}$$
  
$$= \log P_{ij} = \log(X_{ij}) - \log(X_{i})$$
  
$$v_{w_{i}}^{T} v_{\tilde{w}_{j}}' + b_{i} + \tilde{b}_{j} = \log(X_{ij})$$
  
$$C(\theta) = \sum_{i,j=1}^{V} f(P_{ij})(v_{w_{i}} \cdot v_{\tilde{w}_{j}}' - \log P_{ij})^{2}$$
  
$$C(\theta) = \sum_{i,j=1}^{V} f(X_{ij})(v_{w_{i}}^{T} v_{\tilde{w}_{j}}' + b_{i} + \tilde{b}_{j} - \log X_{ij})^{2}$$

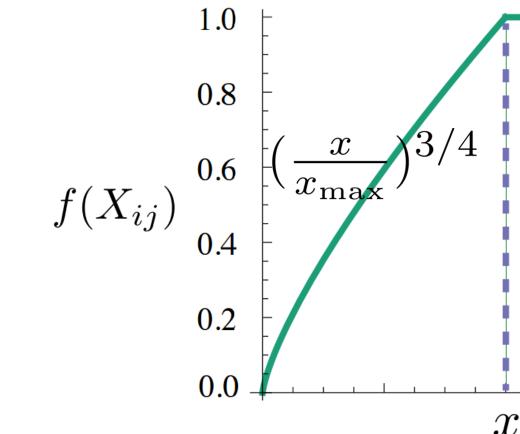
Pennington et al., "GloVe: Global Vectors for Word Representation," in EMNLP, 2014.

## **GIOVe – Weighted Least Squares Regression Model** 42

 $C(\theta) = \sum f(X_{ij})(v_{w_i}^T v_{\tilde{w}_j}' + b_i + \tilde{b}_j - \log X_{ij})^2$ i, j=1

Weighting function should obey f(0) = 0

f(x) should be non-decreasing so that rare co-occurrences are not overweighted



### fast training, scalable, good performance even with small corpus, and small vectors

Pennington et al., "GloVe: Global Vectors for Word Representation," in EMNLP, 2014.

o f(x) should be relatively small for large values of x, so that frequent co-occurrences are not overweighted

0.0 / 1

 $x_{\max}$ 





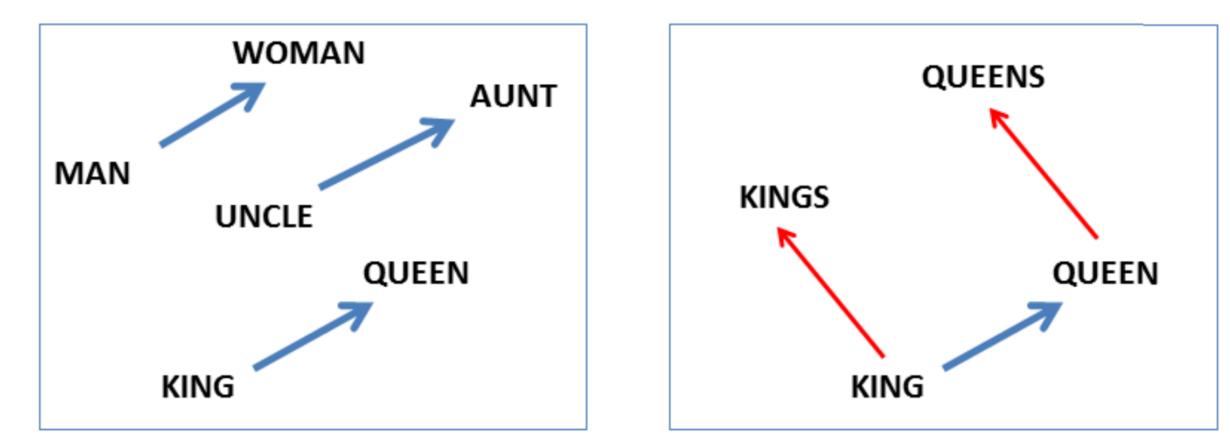
**43** Word Vector Evaluation

## Intrinsic Evaluation – Word Analogies 44

Word linear relationship  $w_A$  :  $w_B$ 

$$x = \arg \max_{x} \frac{(v_{w_B} - v_{w_A} + v_{w_C})^T v_{w_x}}{\|v_{w_B} - v_{w_A} + v_{w_C}\|}$$

Syntactic and Semantic example questions [link] 



Issue: what if the information is there but not linear

$$= w_C : w_x$$

# Intrinsic Evaluation – Word Analogies

- Word linear relationship  $w_A : w_B = w_C : w_x$
- Syntactic and Semantic example questions [link]

### city---in---state

45

Chicago : Illinois = Houston : Texas Chicago : Illinois = Philadelphia : Pennsylvania Chicago : Illinois = Phoenix : Arizona Chicago : Illinois = Dallas : Texas Chicago : Illinois = Jacksonville : Florida Chicago : Illinois = Indianapolis : Indiana Chicago : Illinois = Aus8n : Texas Chicago : Illinois = Detroit : Michigan Chicago : Illinois = Memphis : Tennessee Chicago : Illinois = Boston : Massachusetts

# Issue: different cities may have same name

 $= w_C : w_x$ uestions [link]

capital---country
Abuja : Nigeria = Accra : Ghana
Abuja : Nigeria = Algiers : Algeria
Abuja : Nigeria = Amman : Jordan
Abuja : Nigeria = Ankara : Turkey
Abuja : Nigeria = Antananarivo : Madagascar
Abuja : Nigeria = Apia : Samoa
Abuja : Nigeria = Ashgabat : Turkmenistan
Abuja : Nigeria = Asmara : Eritrea
Abuja : Nigeria = Astana : Kazakhstan

## Issue: can change with time

ar

# 46 Intrinsic Evaluation – Word Analogies

- Word linear relationship  $w_A : w_B = w_C : w_x$
- Syntactic and Semantic example questions [link]

### superlative

- bad : worst = big : biggest
- bad : worst = bright : brightest
- bad : worst = cold : coldest
- bad : worst = cool : coolest
- bad : worst = dark : darkest
- bad : worst = easy : easiest
- bad : worst = fast : fastest
- bad : worst = good : best
- bad : worst = great : greatest

 $= w_C : w_x$ uestions [link]

### past tense

dancing : danced = decreasing : decreased

- dancing : danced = describing : described
- dancing : danced = enhancing : enhanced
- dancing : danced = falling : fell
- dancing : danced = feeding : fed
- dancing : danced = flying : flew
- dancing : danced = generating : generated
- dancing : danced = going : went
- dancing : danced = hiding : hid
- dancing : danced = hiding : hit

# Intrinsic Evaluation – Word Correlation

Comparing word correlation with human-judged scores 

Human-judged word correlation [link] 

47

Word 1	Word 2	Human-Judged Score
tiger	cat	7.35
tiger	tiger	10.00
book	paper	7.46
computer	internet	7.58
plane	car	5.77
professor	doctor	6.62
stock	phone	1.62

## Ambiguity: synonym or same word with different POSs

## **Extrinsic Evaluation – Subsequent Task** 48

Goal: use word vectors in neural net models built for subsequent tasks 

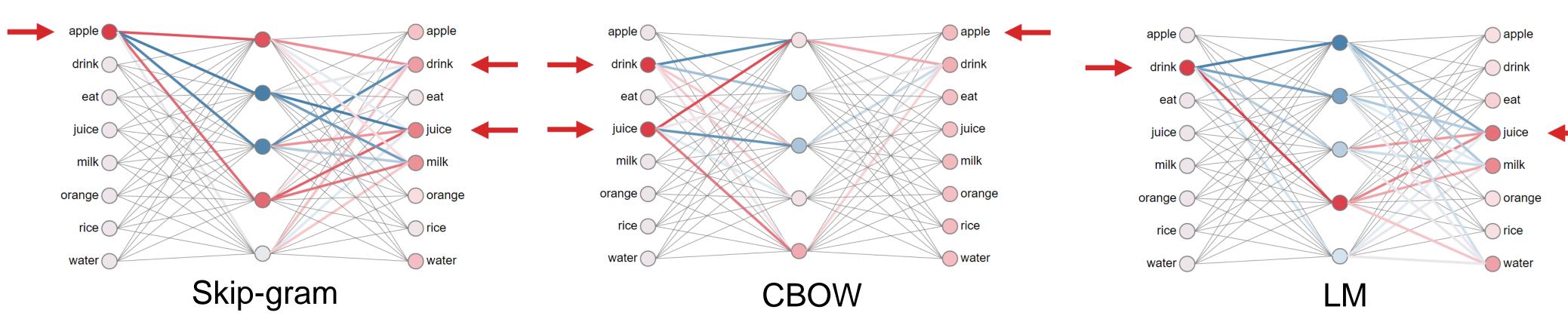
# Benefit

- Ability to also classify words accurately Ex. countries cluster together a classifying location words should be possible with word vectors
- Incorporate any information into them other tasks Ο
  - Ex. project sentiment into words to find most positive/negative words in corpus



## **Concluding Remarks** 49

#### Low dimensional word vector word2vec $\bigcirc$



- GloVe: combining count-based and direct learning 0
- Word vector evaluation
  - Intrinsic: word analogy, word correlation 0
  - Extrinsic: subsequent task 0