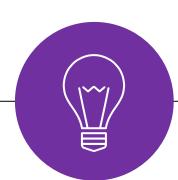
Word Embeddings

March 31st, 2020 http://adl.miulab.tw



Applied Deep Learning









Meaning Representations in Computers

- Knowledge-based representation
- **Corpus-based representation**
 - Atomic symbol \checkmark
 - Neighbors \checkmark

3

- High-dimensional sparse word vector
- Low-dimensional dense word vector
 - Method 1 dimension reduction Ο
 - Method 2 direct learning Ο

Meaning Representations in Computers

Knowledge-based representation

Corpus-based representation

Atomic symbol \checkmark

Neighbors

4

- High-dimensional sparse word vector
- Low-dimensional dense word vector
 - Method 1 dimension reduction \bigcirc
 - Method 2 direct learning 0



Atomic symbols: *one-hot* representation

car [0 0 0 0 0 0

Issues: difficult to compute the similarity (i.e. comparing "car" and "motorcycle")

car

Idea: words with similar meanings often have similar neighbors

$[0\ 0\ 0\ 0\ 0\ 0\ 1\ 0\ 0\ \dots\ 0] = 0$ motorcycle

Meaning Representations in Computers

- Knowledge-based representation
- **Corpus-based representation**
 - Atomic symbol
 - Neighbors \checkmark

6

- High-dimensional sparse word vector
- Low-dimensional dense word vector
 - Method 1 dimension reduction \bigcirc
 - Method 2 direct learning Ο

Window-based Co-occurrence Matrix

Example

7

- Window length=1
- Left or right context
- Corpus:

love NTU.

I love deep learning.

l enjoy learning.

Issues:

- matrix size increases with vocabulary
- high dimensional
- sparsity \rightarrow poor robustness

similarity > 0

Counts		love	enjoy	NTU	deep	learning
	0	2	1	0	0	0
love	2	0	0	1	1	0
enjoy	1	0	0	0	0	1
NTU	0	1	0	0	0	0
deep	0	1	0	0	0	1
learning	0	0	1	0	1	0

Idea: low dimensional word vector



Meaning Representations in Computers

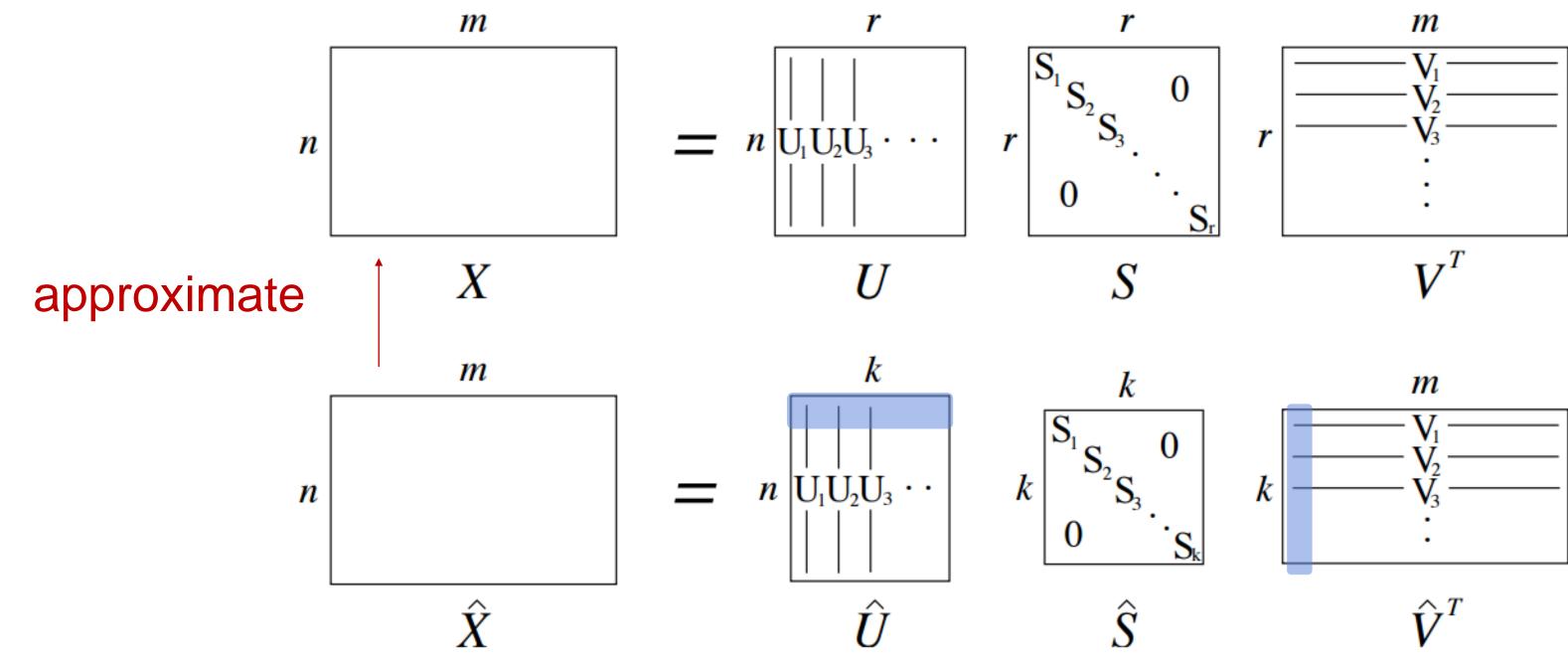
- Knowledge-based representation
- **Corpus-based representation**
 - Atomic symbol
 - Neighbors \checkmark

8

- High-dimensional sparse word vector
- Low-dimensional dense word vector
 - Method 1 dimension reduction Ο
 - Method 2 direct learning 0

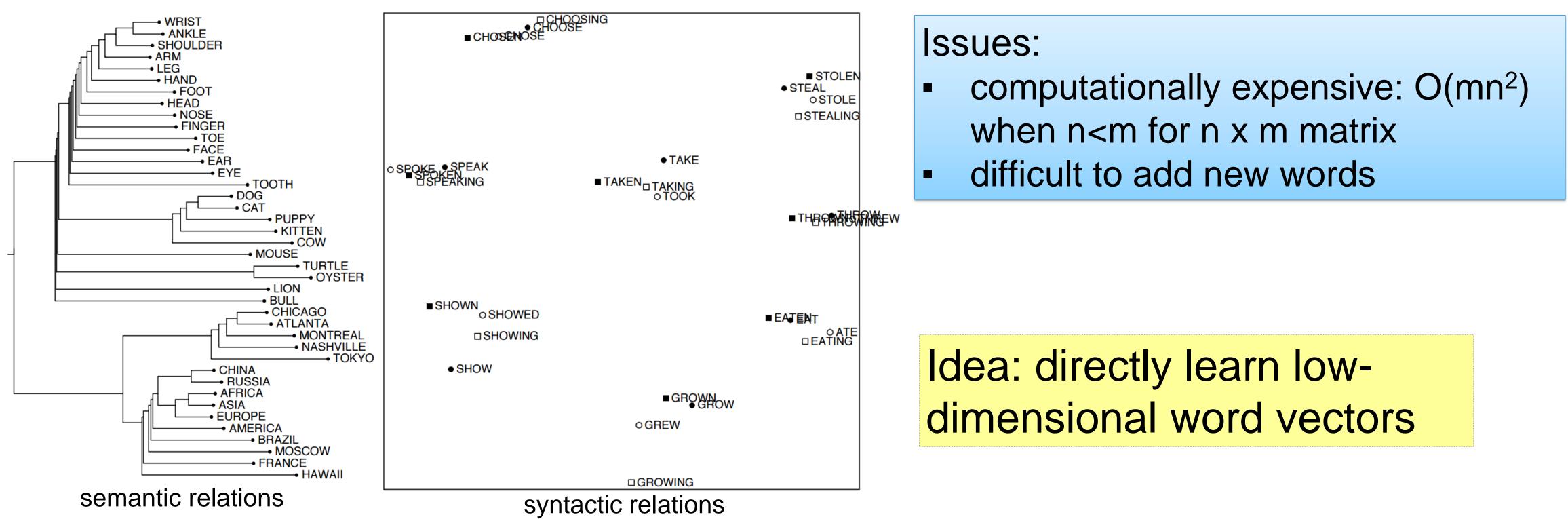
Low-Dimensional Dense Word Vector 9

- Method 1: dimension reduction on the matrix
- Singular Value Decomposition (SVD) of co-occurrence matrix X



Low-Dimensional Dense Word Vector 10

Method 1: dimension reduction on the matrix Singular Value Decomposition (SVD) of co-occurrence matrix X



Word Representation 11

- Knowledge-based representation
- **Corpus-based representation**
 - Atomic symbol \checkmark
 - Neighbors \checkmark
 - High-dimensional sparse word vector
 - Low-dimensional dense word vector
 - Method 1 dimension reduction Ο
 - Method 2 direct learning \rightarrow word embedding Ο

Word Embedding

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Method 2: directly learn low-dimensional word vectors

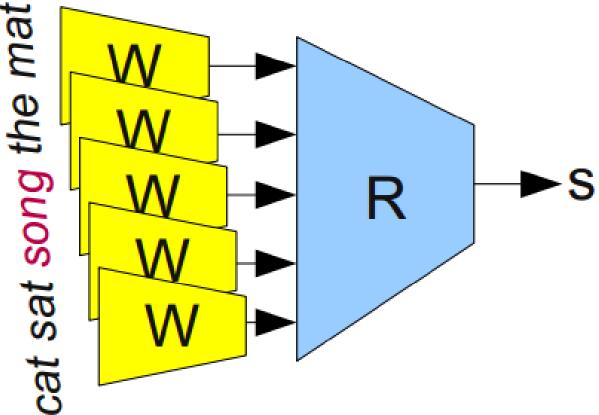
- Ο
- A neural probabilistic language model (Bengio et al., 2003) Ο
- NLP (almost) from Scratch (Collobert & Weston, 2008) Ο
- Recent and most popular models: word2vec (Mikolov et al. 2013) and Glove 0 (Pennington et al., 2014)

Learning representations by back-propagation. (Rumelhart et al., 1986)

Word Embedding Benefit

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Given an <u>unlabeled</u> training corpus, produce a vector for each word that encodes its semantic information. These vectors are useful because: 1) semantic similarity between two words can be calculated as the cosine similarity between their corresponding word vectors 2) word vectors as powerful features for various supervised NLP tasks since the vectors contain semantic information 3) propagate any information into them via neural networks and update during training





Word Embeddings Word2Vec

Word2Vec – Skip-Gram Model 15

- Goal: predict surrounding words within a window of each word Objective function: maximize the probability of any context word given the
- current center word

$$w_{1}, w_{2}, \cdots, w_{t-m}, \cdots, w_{t-1}, w_{t}, w_{t+1}, \cdots, w_{t+m}, \cdots, w_{T-1}, w_{T}$$

$$w_{I} \qquad w_{O}$$

$$w_{O} \qquad w_{O} \qquad w_{O}$$

$$w_{1}, w_{2}, \cdots, w_{t-m}, \cdots, w_{t-1}, w_{t} w_{t+1}, \cdots, w_{t+m}, \cdots, w_{T-1}, w_{T}$$

$$w_{I} c w_{O}$$

$$p(w_{O,1}, w_{O,2}, \cdots, w_{O,C} \mid w_{I}) = \prod_{c=1}^{C} p(w_{O,c} \mid w_{I})$$

$$target word vector$$

$$p(w_{O} \mid w_{I}) = \frac{\exp(v_{w_{O}}^{\prime T} v_{w_{I}})}{\sum_{j} \exp(v_{w_{j}}^{\prime T} v_{w_{I}})}$$

$$target word vector$$

$$w_{I} c w_{I} v_{I} v$$

$$w_{1}, w_{2}, \cdots, \underbrace{w_{t-m}, \cdots, w_{t-1}, (w_{t})}_{w_{I}} \underbrace{w_{t+1}, \cdots, w_{t+m}}_{context window}, \cdots, w_{T-1}, w_{T}$$

$$p(w_{O,1}, w_{O,2}, \cdots, w_{O,C} \mid w_{I}) = \prod_{c=1}^{C} p(w_{O,c} \mid w_{I})$$

$$target word vector$$

$$C(\theta) = -\sum_{w_{I}} \sum_{c=1}^{C} \log p(w_{O,c} \mid w_{I})$$

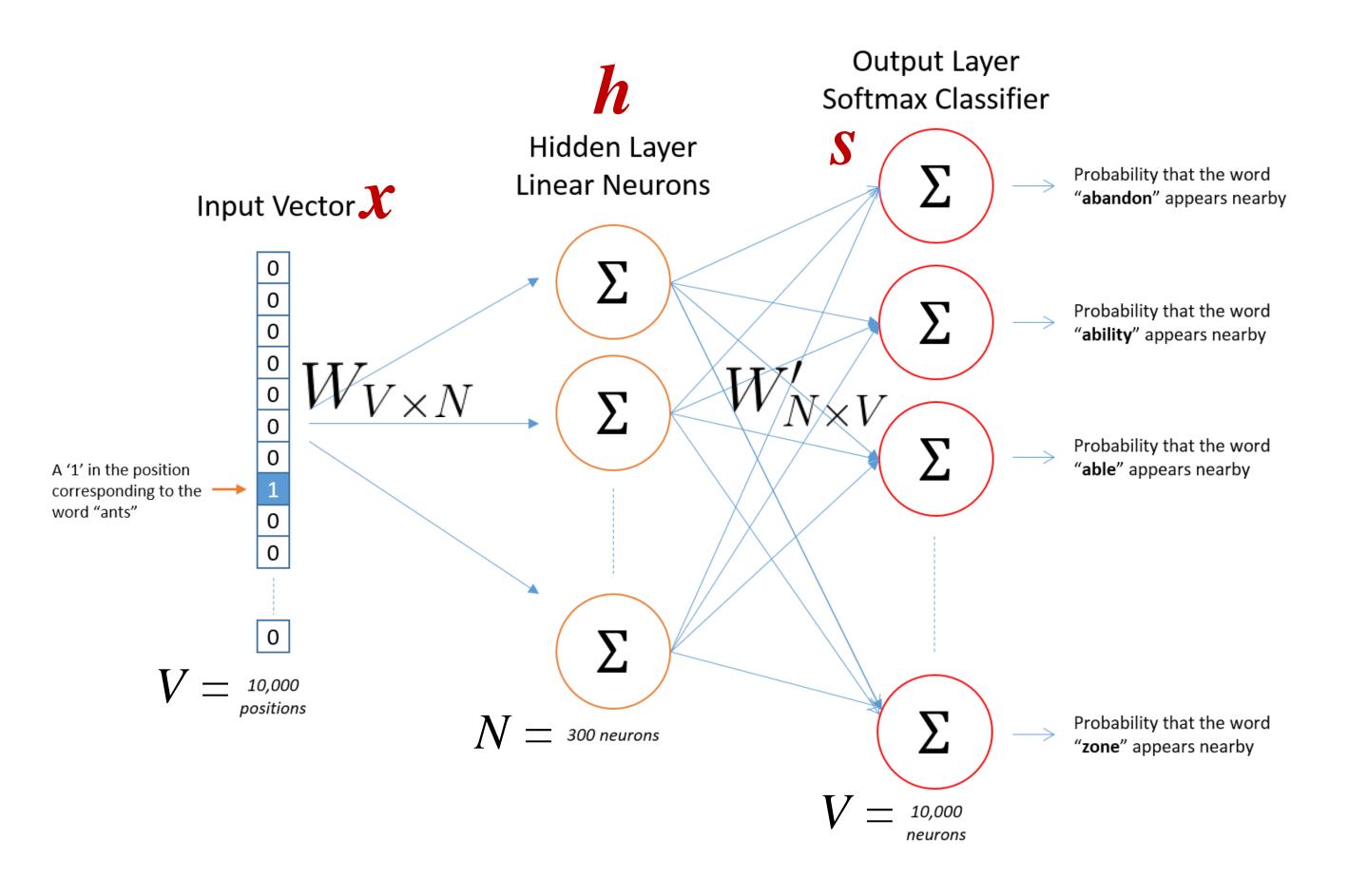
$$p(w_{O} \mid w_{I}) = \frac{\exp(v_{w_{O}}^{\prime T} (w_{w_{I}}))}{\sum_{j} \exp(v_{w_{j}}^{\prime T} v_{w_{I}})}$$
outside target word

Benefit: faster, easily incorporate a new sentence/document or add a word to vocab



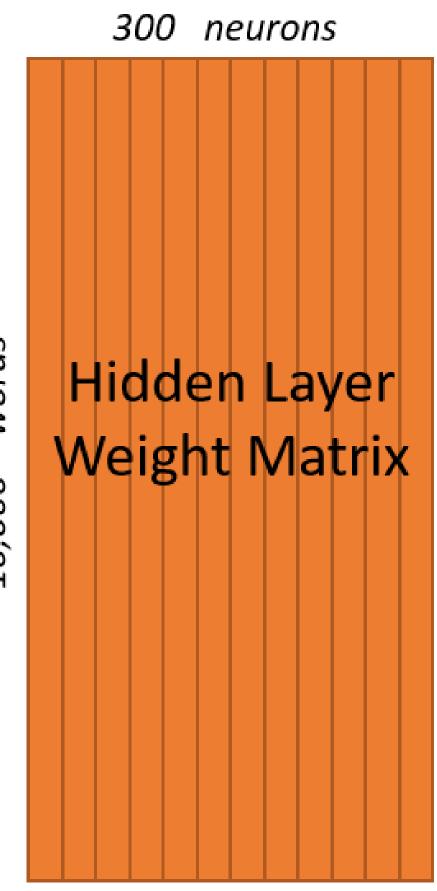


Goal: predict surrounding words within a window of each word





Hidden Layer Matrix \rightarrow Word Embedding Matrix



words 10,000

 $W_{V \times N}$

300 features words Word Vector Lookup Table! 10,000

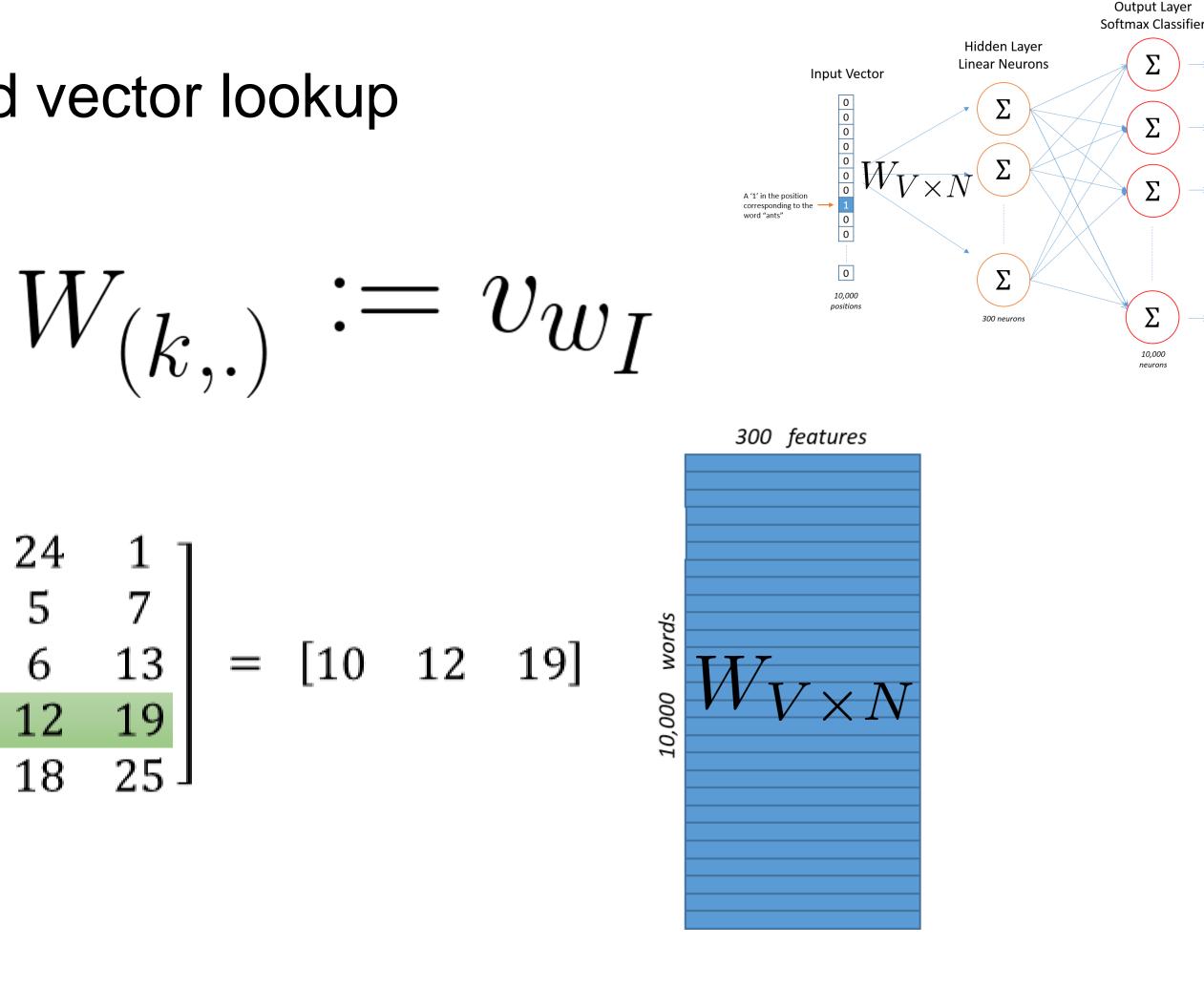
Weight Matrix Relation 18

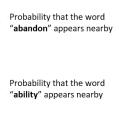
Hidden layer weight matrix = word vector lookup

$$h = x^T W = \mathbf{I}$$

 $\begin{bmatrix} 0 & 0 & 0 & 1 & 0 \end{bmatrix} \times \begin{bmatrix} 17 & 24 & 1 \\ 23 & 5 & 7 \\ 4 & 6 & 13 \\ 10 & 12 & 19 \end{bmatrix} = \begin{bmatrix} 10 & 12 & 19 \end{bmatrix}$ 18

Each vocabulary entry has two vectors: as a target word and as a context word





Probability that the word "able" appears nearby

Probability that the word "zone" appears nearby

Weight Matrix Relation 19

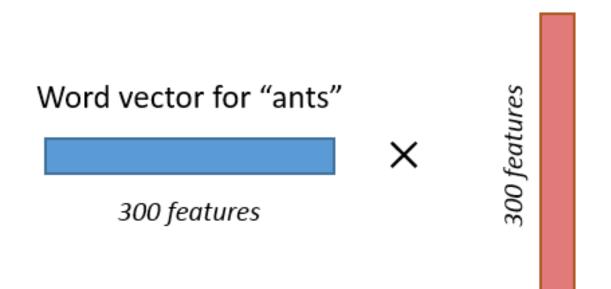
Output layer weight matrix = weighted sum as final score

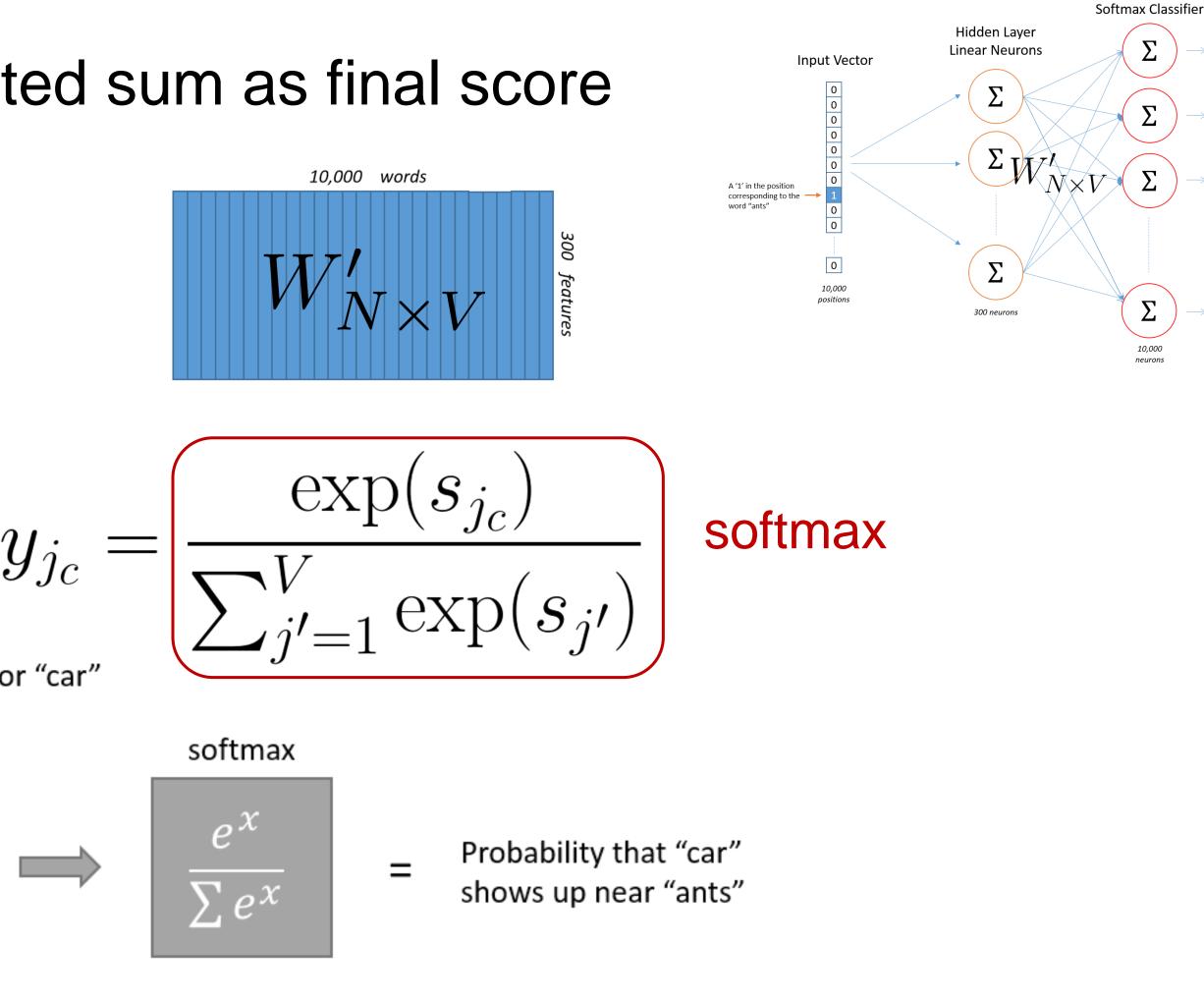
$$s_j = h v'_{w_j}$$

$$p(w_j = w_{O,c} \mid w_I) = q$$

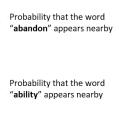
within the context window

Output weights for "car"





Each vocabulary entry has two vectors: as a target word and as a context word

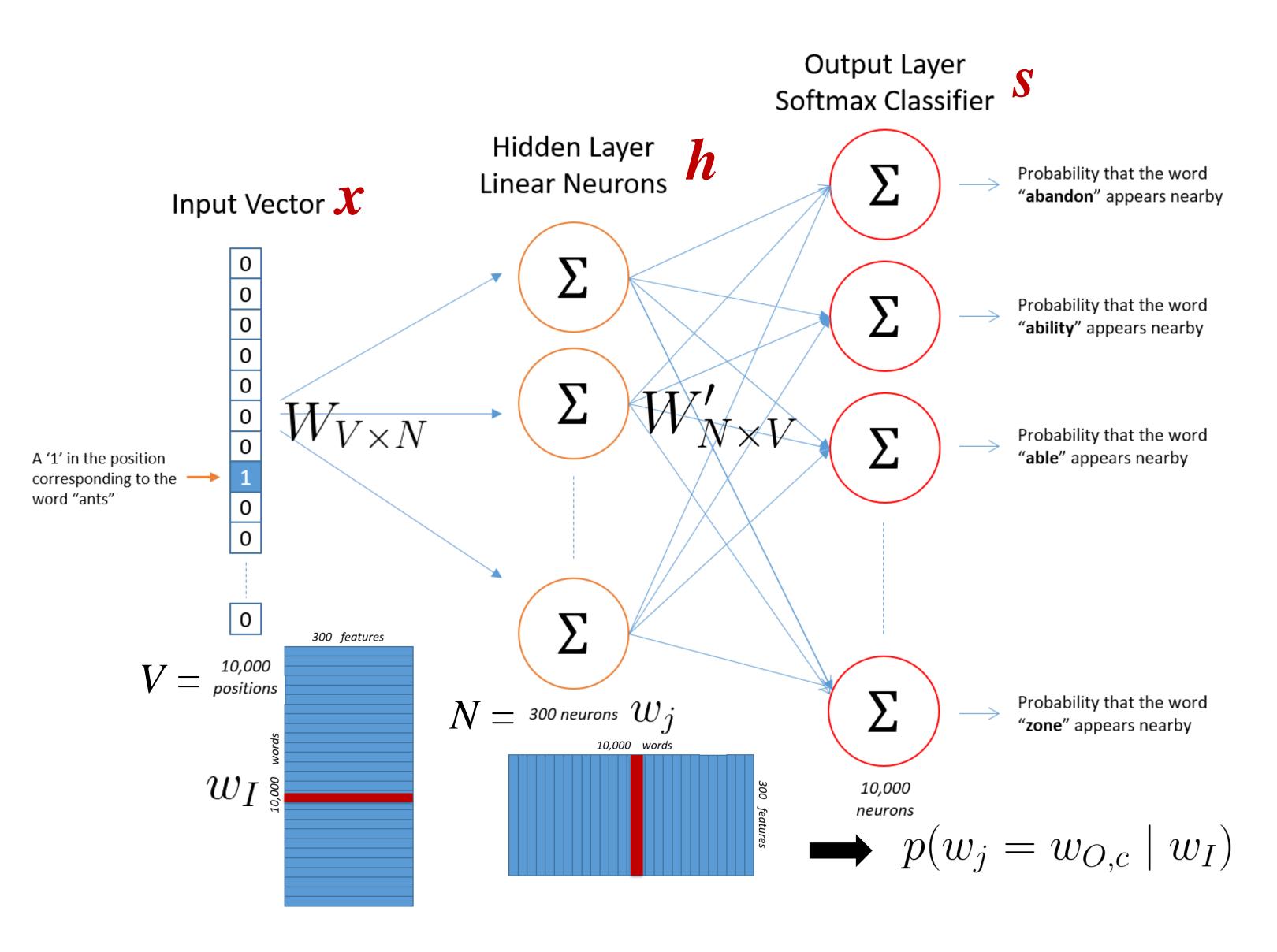


Output Layer

Probability that the word "able" appears nearby

Probability that the word "zone" appears nearby

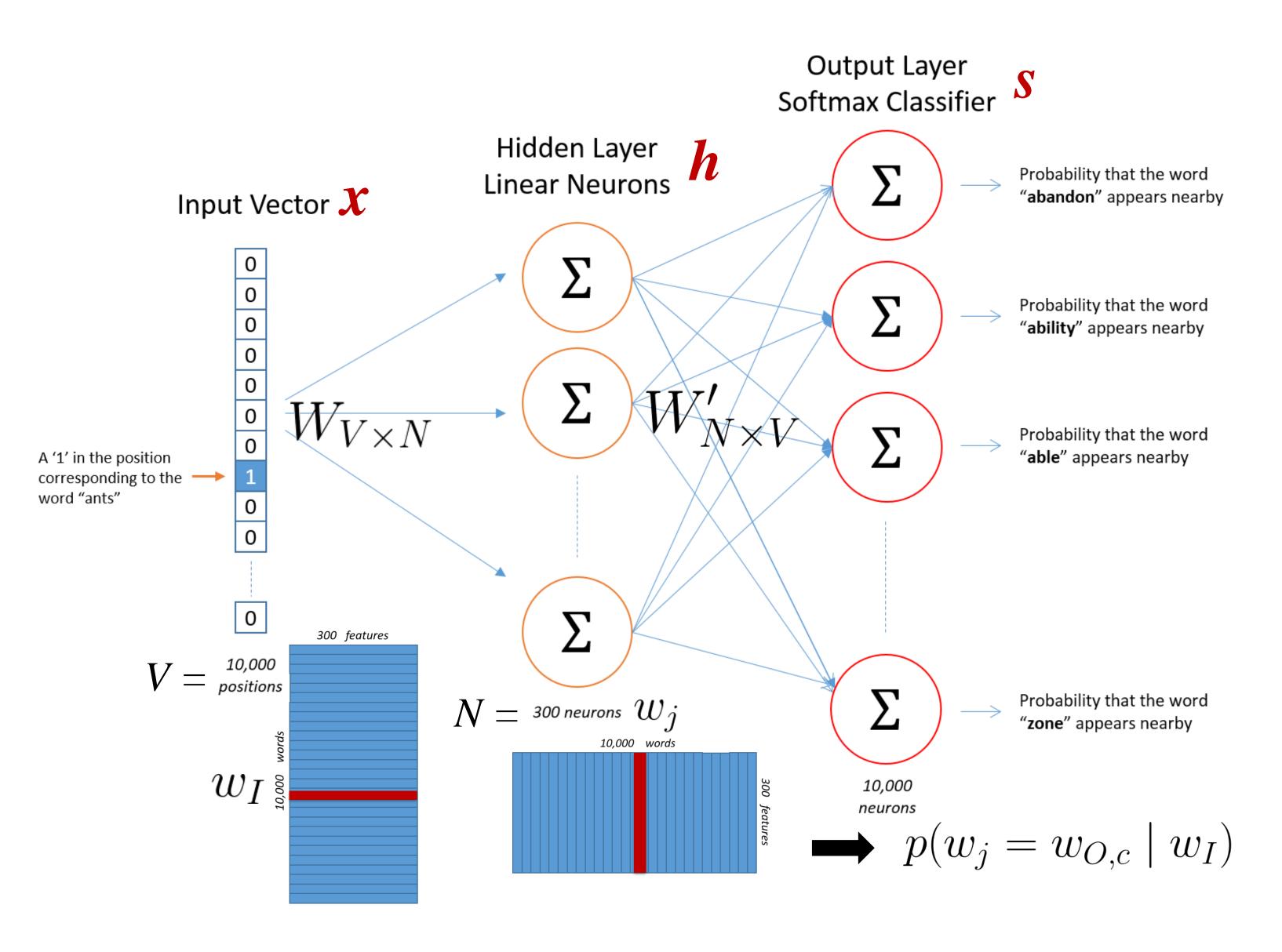
Word2Vec Skip-Gram Illustration 20



Word Embeddings Word2Vec Training



Word2Vec Skip-Gram Illustration



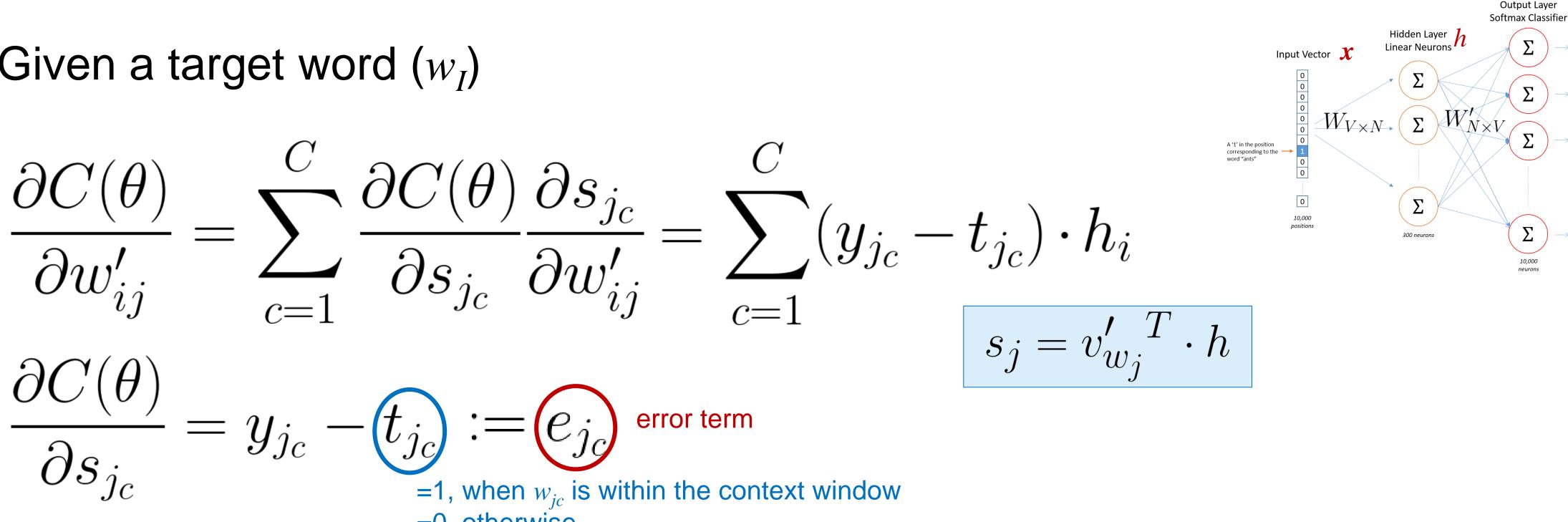


Given a target word (w_I)

 $C(\theta) = -\log p(w_{O,1}, w_{O,2}, \cdots, w_{O,C} \mid w_I)$ $= -\log \prod_{c=1}^{C} \frac{\exp(s_{j_c})}{\sum_{j'=1}^{V} \exp(s_{j'})}$ C $= -\sum s_{j_c} + C \log \sum \exp(s_{j'})$ c=1i'=1

SGD Update for W' 24

Given a target word (w_I)



=0, otherwise

$$w_{ij}^{\prime (t+1)} = w_{ij}^{\prime (t)} - \eta \cdot \sum_{c=1}^{C} (y_{j_c} - t_{j_c}) \cdot h_i$$



Probability that the word bandon" appears near

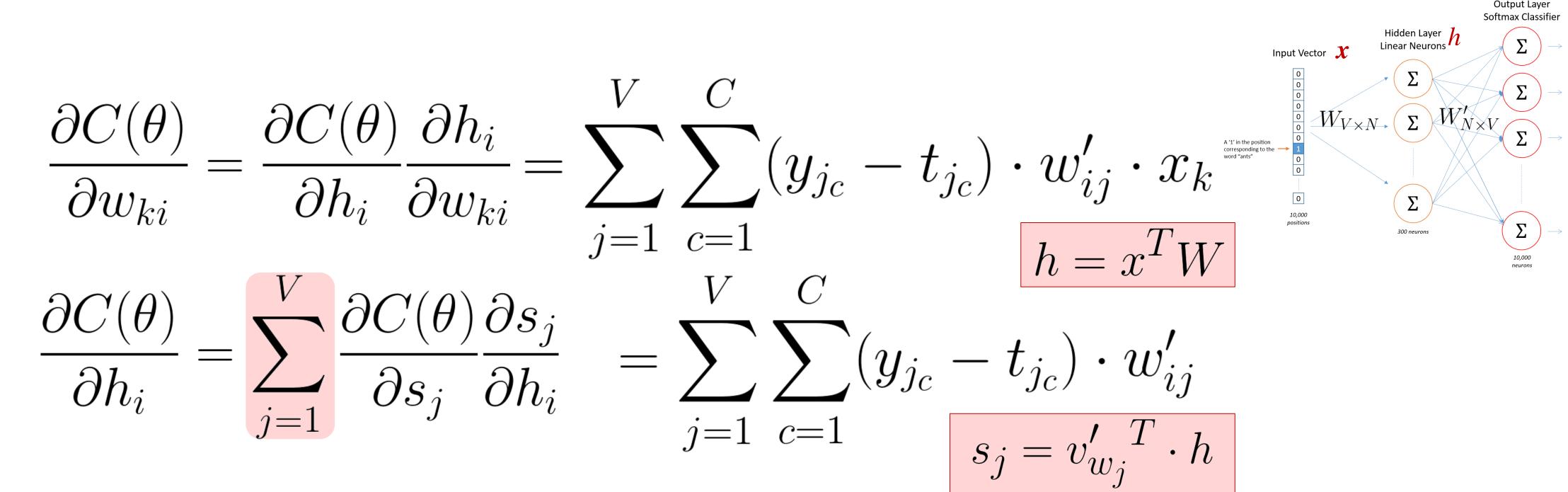
Probability that the word ability" appears near

Probability that the word "able" appears nearby

Probability that the word "zone" appears nearby



SGD Update for W



 $w_{ij}^{(t+1)} = w_{ij}^{(t)} - \eta \cdot \sum_{i=1}^{t} \sum_{j=1}^{t} w_{ij}^{(t)} - \eta \cdot \sum_{j=1}^{t} w_{ij}^{(t)} + \psi_{ij}^{(t)} + \psi$ *j*=

$$\sum_{i=1}^{C} \sum_{c=1}^{C} (y_{j_c} - t_{j_c}) \cdot w'_{ij} \cdot x_j$$



Probability that the word "**abandon"** appears nearby

Probability that the word "**ability**" appears nearby

Probability that the word "**able**" appears nearby

Probability that the word "zone" appears nearby

$$\begin{array}{l} \mathbf{5} \quad \mathbf{SGD Update} \\ w_{ij}^{\prime (t+1)} &= w_{ij}^{\prime (t)} - \eta \cdot \sum_{c=1}^{C} (y_{j_c} - t_{j_c}) \cdot h_i \\ w_{ij}^{\prime (t+1)} &= v_{w_j}^{\prime (t)} - \eta \cdot EI_j \cdot h \\ w_{ij}^{(t+1)} &= w_{ij}^{(t)} - \eta \cdot \sum_{j=1}^{V} \sum_{c=1}^{C} (y_{j_c} - t_{j_c}) \cdot w_{ij}^{\prime} \cdot x_j \\ w_{ij}^{(t+1)} &= w_{w_I}^{(t)} - \eta \cdot EH^T \\ v_{w_I}^{(t+1)} &= v_{w_I}^{(t)} - \eta \cdot EH^T \\ \end{array}$$

large vocabularies or large training corpora \rightarrow expensive computations

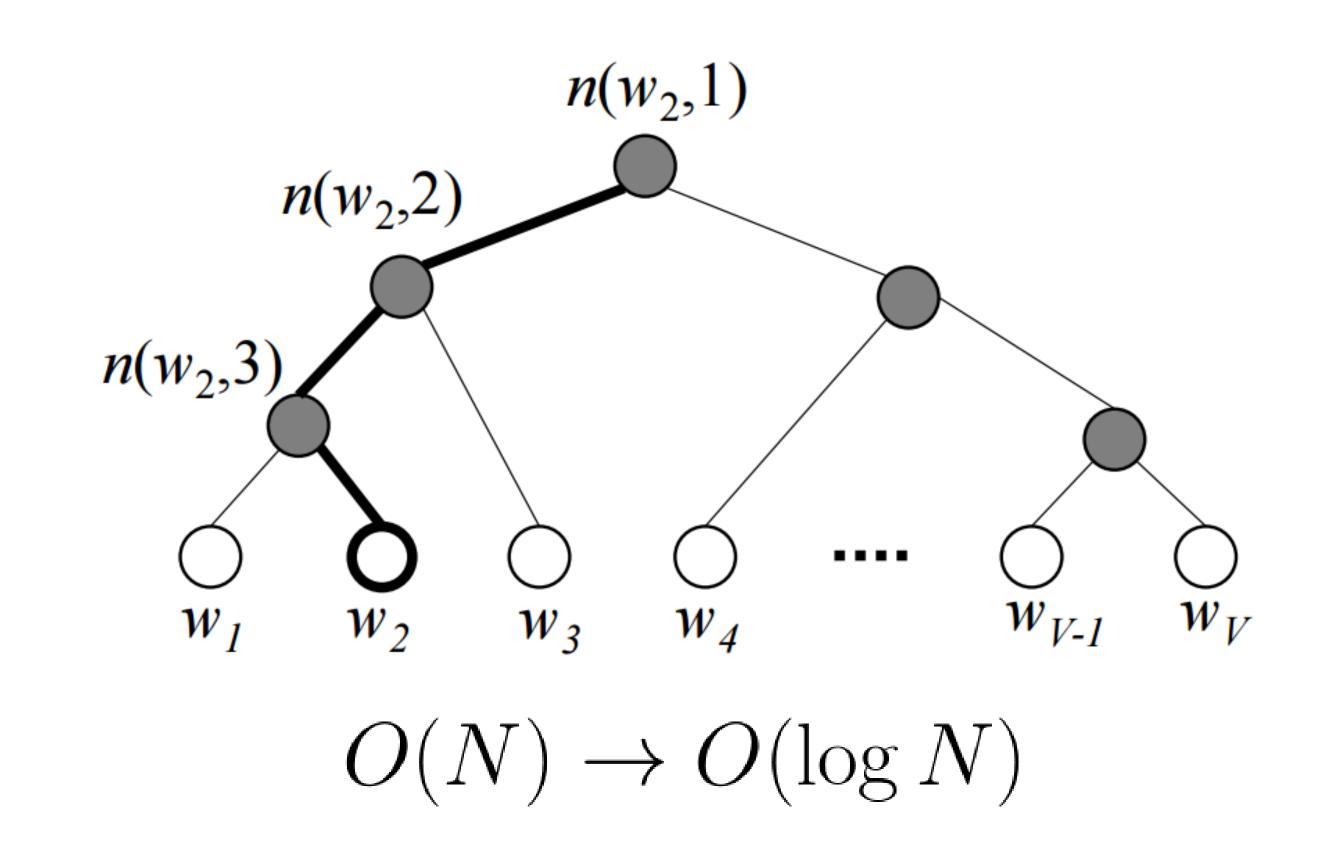
limit the number of output vectors that must be updated per training instance \rightarrow hierarchical softmax, sampling

Word Embeddings Negative Sampling





Idea: compute the probability of leaf nodes using the paths



Mikolov et al., "Distributed representations of words and phrases and their compositionality," in NIPS, 2013.

Negative Sampling 29

Idea: only update a sample of output vectors

$$C(\theta) = -\log \sigma(v'_{w_O}{}^T v_{w_I}) + \sum_{w_j \in \mathcal{W}_{neg}} \log \sigma(v'_{w_j}{}^T v_{w_I})$$
$$v'_{w_j}{}^{(t+1)} = v'_{w_j}{}^{(t)} - \eta \cdot EI_j \cdot h$$
$$EI_j = \sigma(v'_{w_j}{}^T v_{w_I}) - t_j$$
$$V_{w_I}{}^{(t+1)} = v^{(t)}_{w_I} - \eta \cdot EH^T$$
$$EH = \sum_{w_j \in \{w_O\} \cup \mathcal{W}_{neg}} EI_j \cdot v'_{w_j}$$
$$w_j \in \{w_O\} \cup \mathcal{W}_{neg}$$

Mikolov et al., "Distributed representations of words and phrases and their compositionality," in NIPS, 2013.

Negative Sampling 30

- Sampling methods
 - Random sampling $w_i \in \{w_O\} \cup \mathcal{W}_{neg}$ 0
 - Ο

Idea: less frequent words sampled more often

Empirical setting: unigram model raised to the power of 3/4

Word	Probabi
is	
constitution	
bombastic	

Mikolov et al., "Distributed representations of words and phrases and their compositionality," in NIPS, 2013.

Distribution sampling: w_i is sampled from P(w) What is a good P(w)?

lity to be sampled for "neg"

 $0.9^{3/4} = 0.92$

 $0.09^{3/4} = 0.16$

 $0.01^{3/4} = 0.032$

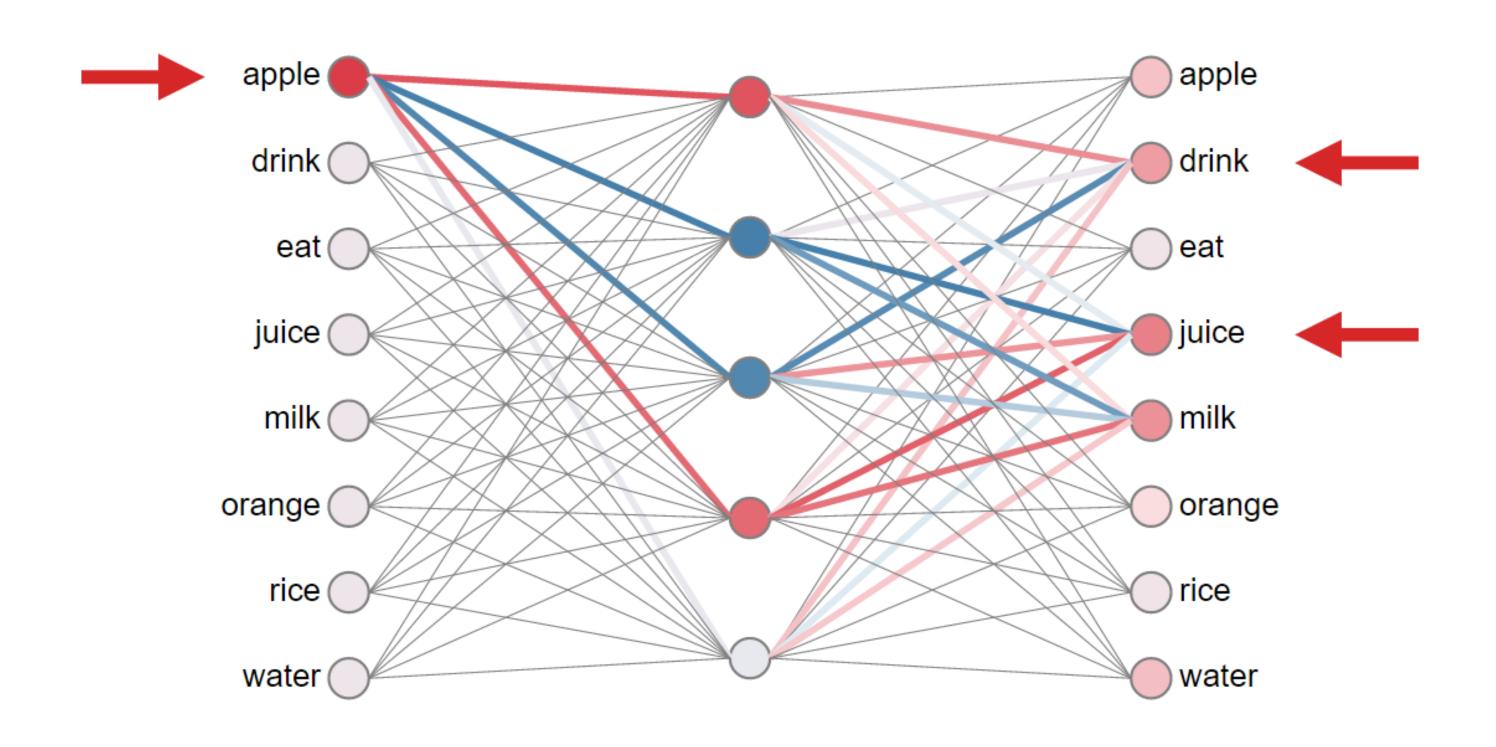


³¹ Word Embeddings Word2Vec Variants



Word2Vec Skip-Gram Visualization https://ronxin.github.io/wevi/

Skip-gram training data: e^water



apple|drink^juice,orange|eat^apple,rice|drink^juice,juice|drink^milk,milk|drink^rice,water|drink^mil k,juice|orange^apple,juice|apple^drink,milk|rice^drink,drink|milk^water,drink|water^juice,drink|juic



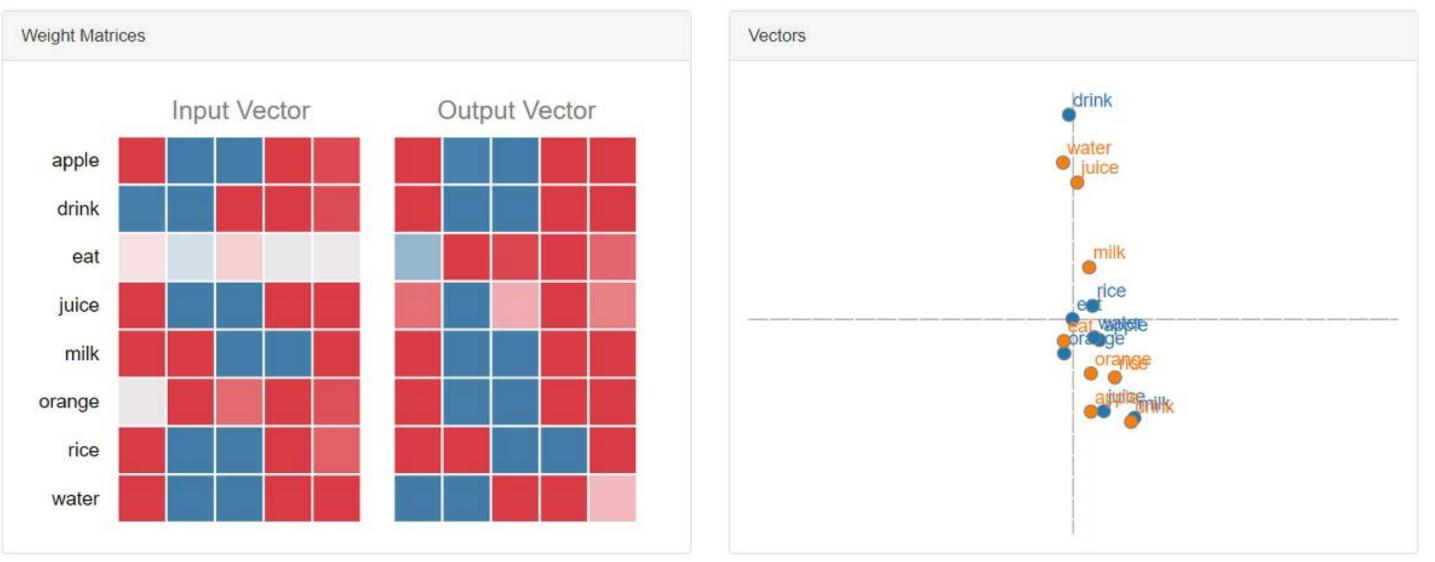


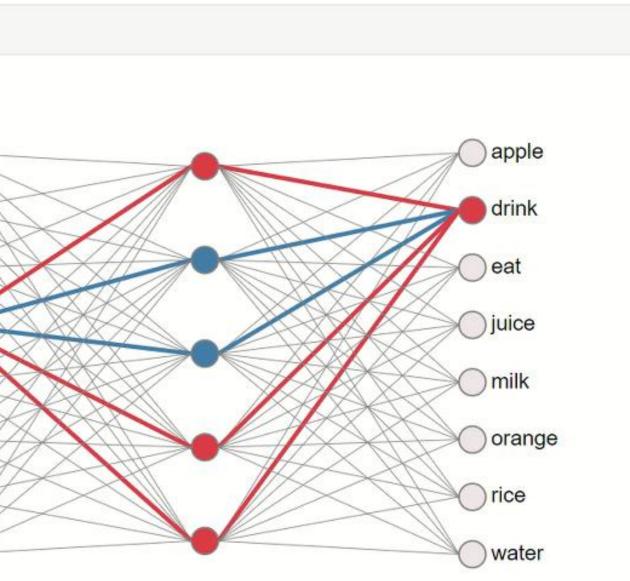


wevi: word embedding visual inspector

Everything you need to know about this tool - Source code

Control Panel	Neurons
Config:	
{"hidden_size":5,"random_state":1,"learning_rate":0 .2}	apple
Training data (context target):	drink
apple/drink^juice,orange/eat^apple,rice/drink^juice,j	eat
uice drink^milk,milk drink^rice,water drink^milk,juice orange^apple,juice apple^drink,milk rice^drink,drink milk^water,drink water^juice,drink juice^water	juice
Presets: Fruit and juice (Skip-gram) ▼	milk
Update and Restart Update Learning Rate	orange
Next 20 100 500 PCA	rice
	water





Word2Vec Variants

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2013)

 $p(w_{t-m}, \cdots w_{t-1}, w_t)$

- surrounding words (Mikolov+, 2013)
- $p(w_t \mid w_{t-m}, \cdots, w_{t-1}, w_{t+1}, \cdots, w_{t+m})$ contexts (Mikolov+, 2013)

$$p(w_{t+1} \mid w_t)$$

Practice the derivation by yourself!!

Mikolov et al., "Efficient estimation of word representations in vector space," in ICLR Workshop, 2013. Mikolov et al., "Linguistic regularities in continuous space word representations," in NAACL HLT, 2013.

Skip-gram: predicting surrounding words given the target word (Mikolov+,

$$w_{t+1}, \cdots, w_{t+m} \mid w_t)$$

CBOW (continuous bag-of-words): predicting the target word given the

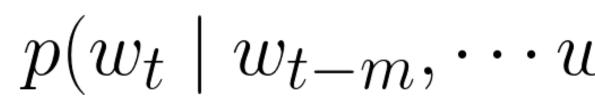
LM (Language modeling): predicting the next words given the proceeding

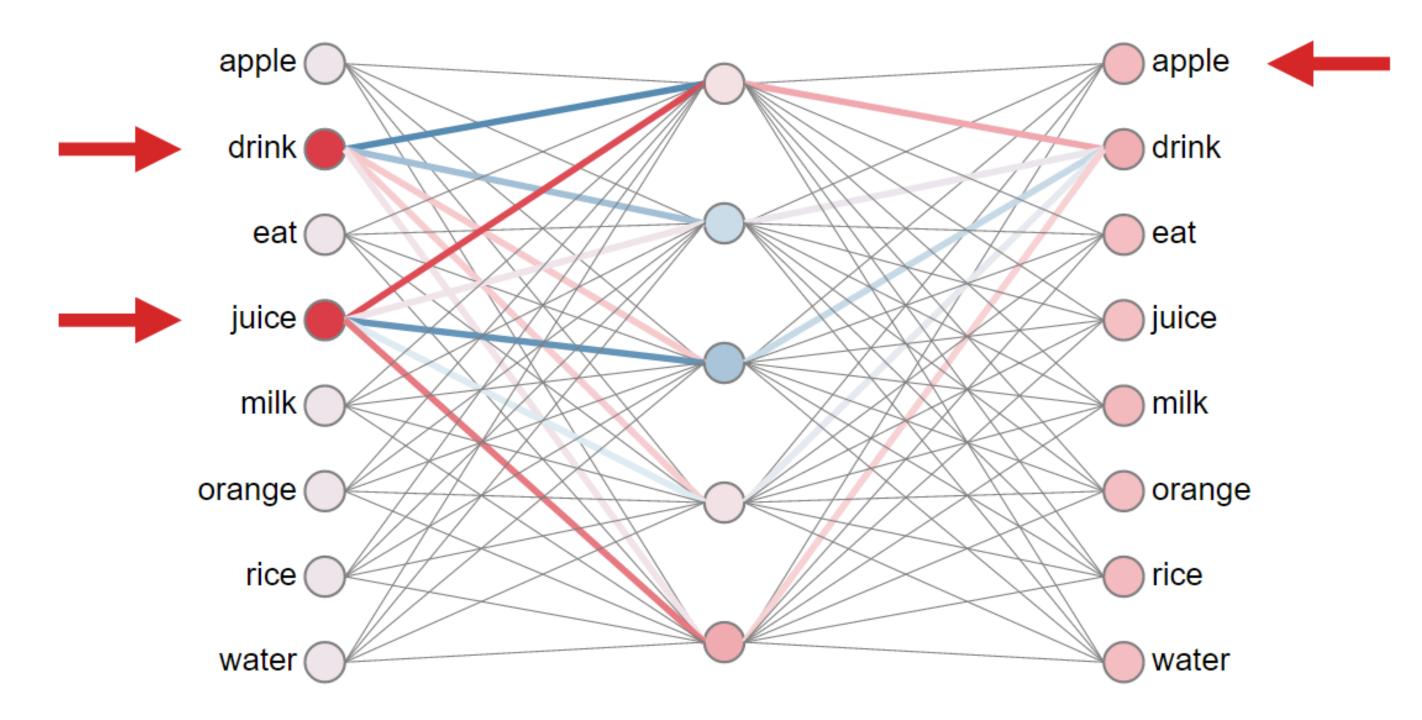






Goal: predicting the target word given the surrounding words

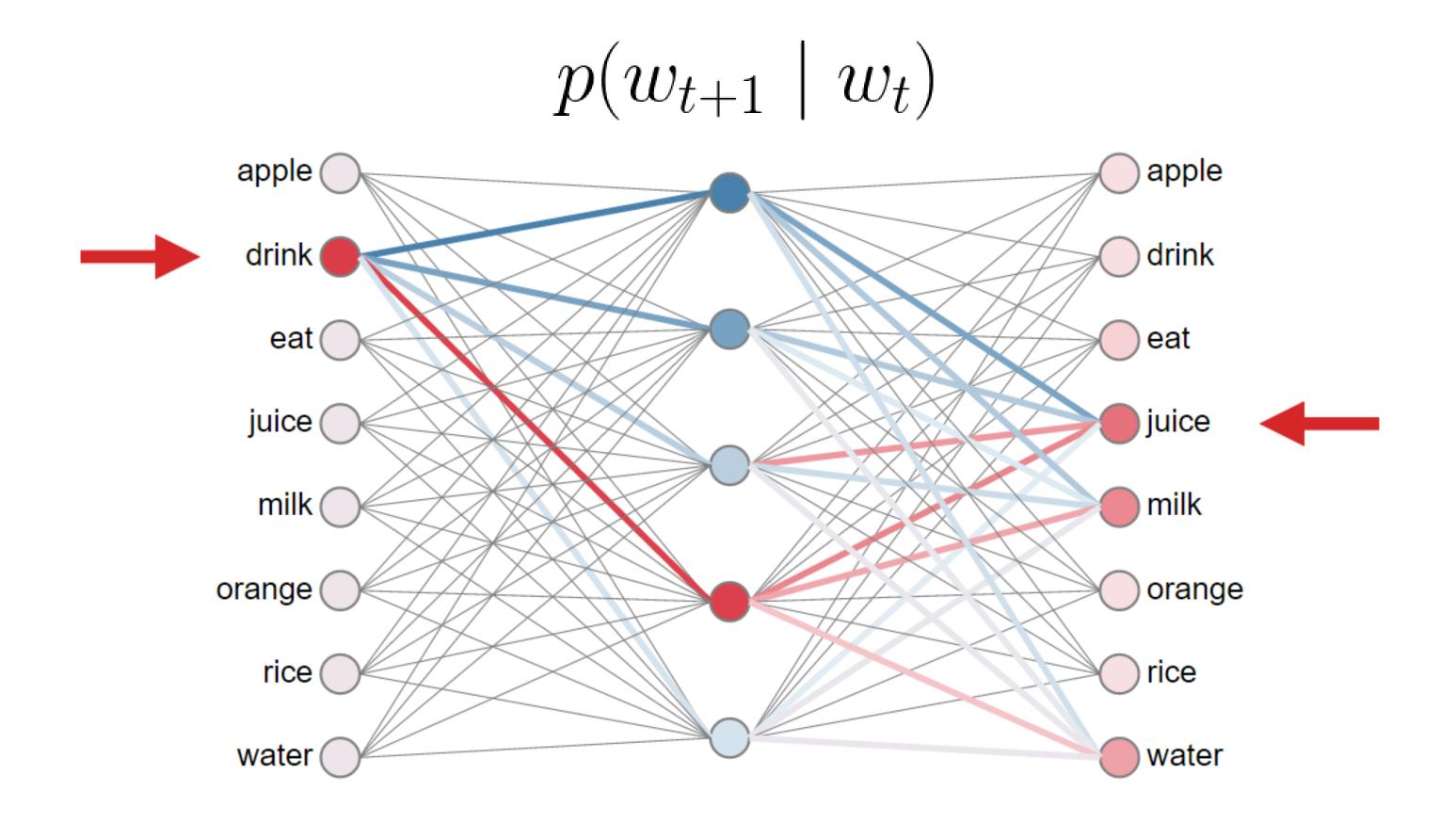




$$v_{t-1}, w_{t+1}, \cdots, w_{t+m}$$



• Goal: predicting the next words given the proceeding contexts







Count-based

- LSA, HAL (Lund & Burgess), COALS (Rohde et al), Hellinger-PCA (Lebret & Collobert)
- Pros \bigcirc
 - Fast training
 - Efficient usage of statistics
- Cons \bigcirc
 - Primarily used to capture word similarity
 - Disproportionate importance given to large counts

Combining the benefits from both worlds \rightarrow GloVe

Direct prediction

NNLM, HLBL, RNN, Skipgram/CBOW 0 (Bengio et al; Collobert & Weston; Huang et al; Mnih & Hinton; Mikolov et al; Mnih & Kavukcuoglu)

Pros \bigcirc

- Generate improved performance on other tasks
- Capture complex patterns beyond word similarity

Cons \bigcirc

- Benefits mainly from large corpus
- Inefficient usage of statistics





- Idea: ratio of co-occurrence probability can encode meaning
- P_{ij} is the probability that word w_i appears in the context of word w_i

$$P_{ij} = P(w_j$$

Relationship between the words w_i and w_j

	x = solid	x = gas	x = water	x = random
$P(x \mid ice)$	large	small	large	small
$P(x \mid \text{stream})$	small	large	large	small
$\frac{P(x \mid \text{ice})}{P(x \mid \text{stream})}$	large	small	~ 1	~ 1

Pennington et al., "GloVe: Global Vectors for Word Representation," in EMNLP, 2014.

$$w_i) = X_{ij}/X_i$$



The relationship of w_i and w_j approximates the ratio of their co-occurrence probabilities with various w_k

$$F(w_i, w_j, \tilde{w}_k) = \frac{P_{ik}}{P_{jk}}$$

$$F(w_i - w_j, \tilde{w}_k) = \frac{P_{ik}}{P_{jk}}$$

$$F((v_{w_i} - v_{w_j})^T v'_{\tilde{w}_k}) = \frac{P_{ik}}{P_{jk}} \quad F(\cdot) = \exp(\cdot)$$

$$v_{w_i} \cdot v'_{\tilde{w}_k} = v_{w_i}^T v'_{\tilde{w}_k} = \log P(w_k \mid w_i)$$

Pennington et al., "GloVe: Global Vectors for Word Representation," in EMNLP, 2014.



$$v_{w_{i}} \cdot v_{\tilde{w}_{j}}' = v_{w_{i}}^{T} v_{\tilde{w}_{j}}' = \log P(w_{j} \mid w_{i}) \qquad P_{ij} = X_{ij}/X_{i}$$

$$= \log P_{ij} = \log(X_{ij}) - \log(X_{i})$$

$$v_{w_{i}}^{T} v_{\tilde{w}_{j}}' + b_{i} + \tilde{b}_{j} = \log(X_{ij})$$

$$C(\theta) = \sum_{i,j=1}^{V} f(P_{ij})(v_{w_{i}} \cdot v_{\tilde{w}_{j}}' - \log P_{ij})^{2}$$

$$C(\theta) = \sum_{i,j=1}^{V} f(X_{ij})(v_{w_{i}}^{T} v_{\tilde{w}_{j}}' + b_{i} + \tilde{b}_{j} - \log X_{ij})^{2}$$

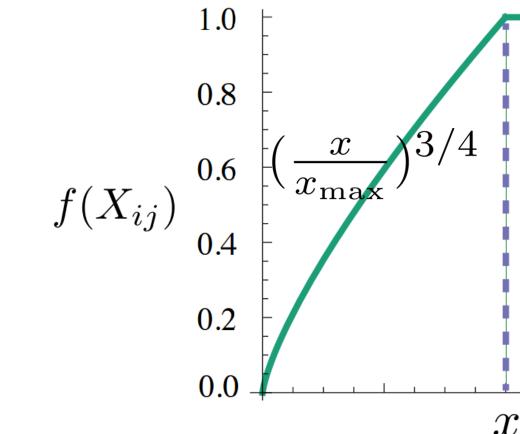
Pennington et al., "GloVe: Global Vectors for Word Representation," in EMNLP, 2014.

GIOVe – Weighted Least Squares Regression Model 42

 $C(\theta) = \sum f(X_{ij})(v_{w_i}^T v_{\tilde{w}_j}' + b_i + \tilde{b}_j - \log X_{ij})^2$ i, j=1

Weighting function should obey f(0) = 0

f(x) should be non-decreasing so that rare co-occurrences are not overweighted



fast training, scalable, good performance even with small corpus, and small vectors

Pennington et al., "GloVe: Global Vectors for Word Representation," in EMNLP, 2014.

o f(x) should be relatively small for large values of x, so that frequent co-occurrences are not overweighted

0.0 / 1

 x_{\max}





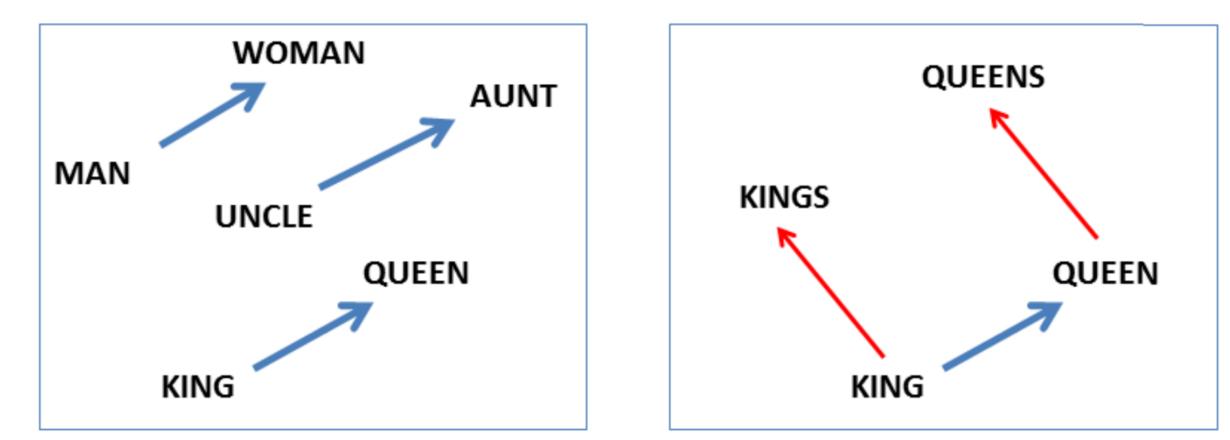
43 Word Vector Evaluation

Intrinsic Evaluation – Word Analogies 44

Word linear relationship w_A : w_B

$$x = \arg \max_{x} \frac{(v_{w_B} - v_{w_A} + v_{w_C})^T v_{w_x}}{\|v_{w_B} - v_{w_A} + v_{w_C}\|}$$

Syntactic and Semantic example questions [link]



Issue: what if the information is there but not linear

$$= w_C : w_x$$

Intrinsic Evaluation – Word Analogies

- Word linear relationship $w_A : w_B = w_C : w_x$
- Syntactic and Semantic example questions [link]

city---in---state

45

Chicago : Illinois = Houston : Texas Chicago : Illinois = Philadelphia : Pennsylvania Chicago : Illinois = Phoenix : Arizona Chicago : Illinois = Dallas : Texas Chicago : Illinois = Jacksonville : Florida Chicago : Illinois = Indianapolis : Indiana Chicago : Illinois = Aus8n : Texas Chicago : Illinois = Detroit : Michigan Chicago : Illinois = Memphis : Tennessee Chicago : Illinois = Boston : Massachusetts

Issue: different cities may have same name

 $= w_C : w_x$ uestions [link]

capital---country
Abuja : Nigeria = Accra : Ghana
Abuja : Nigeria = Algiers : Algeria
Abuja : Nigeria = Amman : Jordan
Abuja : Nigeria = Ankara : Turkey
Abuja : Nigeria = Antananarivo : Madagascar
Abuja : Nigeria = Apia : Samoa
Abuja : Nigeria = Ashgabat : Turkmenistan
Abuja : Nigeria = Asmara : Eritrea
Abuja : Nigeria = Astana : Kazakhstan

Issue: can change with time

ar

46 Intrinsic Evaluation – Word Analogies

- Word linear relationship $w_A : w_B = w_C : w_x$
- Syntactic and Semantic example questions [link]

superlative

- bad : worst = big : biggest
- bad : worst = bright : brightest
- bad : worst = cold : coldest
- bad : worst = cool : coolest
- bad : worst = dark : darkest
- bad : worst = easy : easiest
- bad : worst = fast : fastest
- bad : worst = good : best
- bad : worst = great : greatest

 $= w_C : w_x$ uestions [link]

past tense

dancing : danced = decreasing : decreased

- dancing : danced = describing : described
- dancing : danced = enhancing : enhanced
- dancing : danced = falling : fell
- dancing : danced = feeding : fed
- dancing : danced = flying : flew
- dancing : danced = generating : generated
- dancing : danced = going : went
- dancing : danced = hiding : hid
- dancing : danced = hiding : hit

Intrinsic Evaluation – Word Correlation

Comparing word correlation with human-judged scores

Human-judged word correlation [link]

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Word 1	Word 2	Human-Judged Score
tiger	cat	7.35
tiger	tiger	10.00
book	paper	7.46
computer	internet	7.58
plane	car	5.77
professor	doctor	6.62
stock	phone	1.62

Ambiguity: synonym or same word with different POSs

Extrinsic Evaluation – Subsequent Task 48

Goal: use word vectors in neural net models built for subsequent tasks

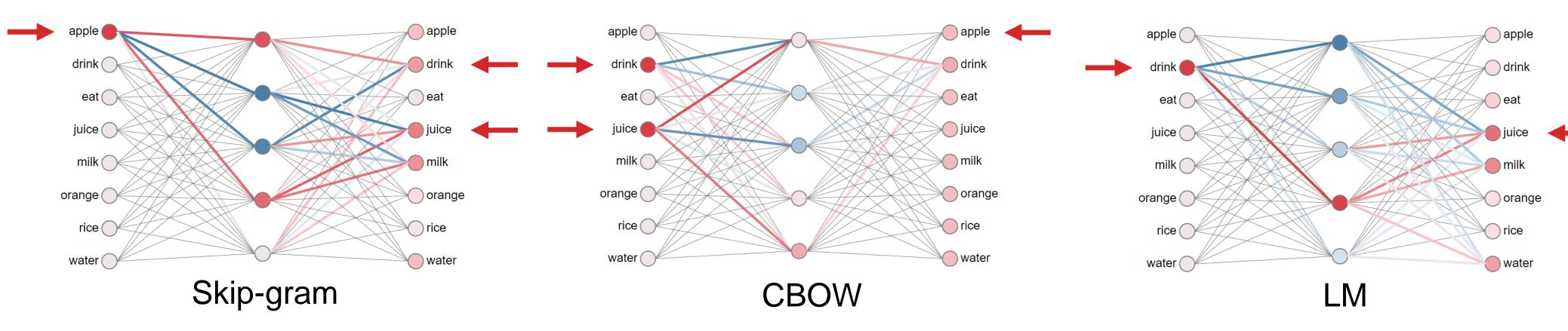
Benefit

- Ability to also classify words accurately Ex. countries cluster together a classifying location words should be possible with word vectors
- Incorporate any information into them other tasks Ο
 - Ex. project sentiment into words to find most positive/negative words in corpus



Concluding Remarks 49

Low dimensional word vector word2vec \bigcirc



- GloVe: combining count-based and direct learning 0
- Word vector evaluation
 - Intrinsic: word analogy, word correlation 0
 - Extrinsic: subsequent task 0