

# Theory of Computation

homework 1

Due: 9/29/2015

**Problem 1** The TM on p. 30 of the slides halts with a “yes” if the input string contains two consecutive 1’s; otherwise, it halts at “no”. That program assumes the input alphabet  $\Sigma = \{0, 1, \sqcup, \triangleright\}$ . Now, write a TM program for the same problem when  $\Sigma = \{0, 1, 2, \sqcup, \triangleright\}$ .

**Problem 2** Explain why the following Turing machine does not decide the language of polynomials with integer coefficients which have integer roots: The input represents a polynomial over variables  $x_1, \dots, x_n$  with integer coefficients.

1. Examine all possible integer values of  $x_1, \dots, x_n$ .
2. Evaluate the polynomial on all of them.
3. If any of them evaluates to 0, accept; else reject.