

# Theory of Computation

## Homework 4

Due: 2014/12/9

**Problem 1** Show that VALIDITY is coNP-complete.

**Problem 2** Recall that the Jacobi symbol is given by  $(a|m) = \prod_i^k (a|p_i)$  for any odd integer  $m = p_1 p_2 \dots p_k$ ,  $m > 1$ , and  $\gcd(a, m) = 1$ . Show that  $(-1|m) = (-1)^{(m-1)/2}$  for any odd integer  $m$ . (You may use the Legendre symbol  $(a|p) = a^{\frac{p-1}{2}}$  for any odd prime  $p$  and  $a \not\equiv 0 \pmod{p}$ .)