

# Theory of Computation

## Homework 2

Due: 9:10, 2009/10/27

**Problem 1.** We call a boolean function  $f : \{0, 1\}^k \rightarrow \{0, 1\}$  symmetric if  $f(x_1, x_2, \dots, x_k)$  depends only on  $\sum_{i=1}^k x_i$ . How many symmetric boolean functions of  $k$  variables are there?

**Problem 2.** It is known that the language

$$\{M : M \text{ halts on all inputs}\}$$

is undecidable. Prove or disprove that the following restricted language

$$L_{1000} = \{M : M \text{ halts on all inputs and } M \text{ is at most 1000 bits long}\}$$

is undecidable.