

Unbiased Risk Estimators Can Mislead: A Case Study of Learning with Complementary Labels

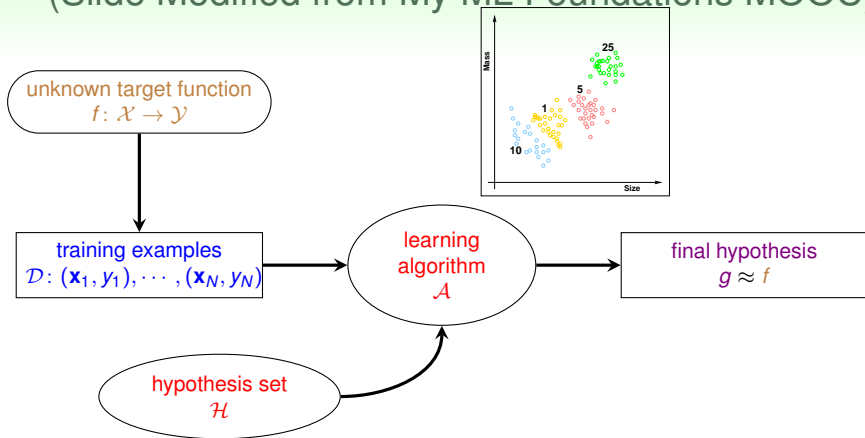
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ICML 2020 work done during Chou's internship at RIKEN AIP, Japan;
resulting M.S. thesis of Chou won the 2020 thesis award of TAAI

October 8, 2021, AI Forum, Taipei, Taiwan

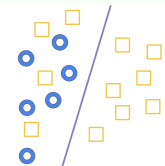
Supervised Learning

(Slide Modified from My ML Foundations MOOC)

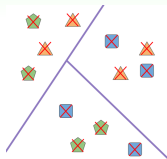


supervised learning:
every input vector \mathbf{x}_n with
its (possibly expensive) label y_n ,

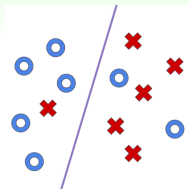
Weakly-supervised: Learning without True Labels y_n



(a) positive-unlabeled learning [EN08]



(b) learning with complementary labels [Ish+17]



(c) learning with noisy labels [Nat+13]

- positive-unlabeled: some of true $y_n = +1$ revealed
- complementary: 'not label' \bar{y}_n instead of true y_n
- noisy: noisy label y'_n instead of true y_n

weakly-supervised: a **realistic** and **hot** research direction to reduce labeling burden

[EN08] Learning classifiers from only positive and unlabeled data, KDD'08.

[Ish+17] Learning from complementary labels, NeurIPS'17.

[Nat+13] Learning with noisy labels, NeurIPS'13.

Motivation

popular weakly-supervised models [DNS15; Ish+19; Pat+17]

- derive **Unbiased Risk Estimators (URE)** as new loss
- theoretically, nice properties (unbiased, consistent, etc.) [Ish+17]
- practically, **sometimes bad performance** (overfitting)

our contributions: on Learning with Complementary Labels (LCL)

- analysis: **identify weakness** of URE framework
- algorithm: propose an **improved framework**
- experiment: demonstrate **stronger performance**

next: introduction to LCL

[DNS15] Convex formulation for learning from positive and unlabeled data, ICML'15.

[Ish+19] Complementary-Label Learning for Arbitrary Losses and Models, ICML'19.

[Pat+17] Making deep neural networks robust to label noise: A loss correction approach, CVPR'17.

Motivation behind Learning with Complementary Label

complementary label \bar{y}_n instead of true y_n

| True Label | Meerkat | Prairie Dog | Monkey |
|---------------------|---|---|--|
| |  |  |  |
| Complementary Label | Not "monkey" | Not "meerkat" | Not "prairie dog" |

Figure 1 of [Yu+18]

complementary label: **easier/cheaper** to obtain for some applications

Fruit Labeling Task (Image from AICup in 2020)



hard: true label

- orange ?
- mango ?
- cherry
- banana


easy: complementary label

- orange
- mango
- cherry
- banana ✗


complementary: **less labeling cost/expertise** required


Comparison

Ordinary (Supervised) Learning

training: $\{(\mathbf{x}_n = \text{, y_n = \text{mango})\} \rightarrow \text{classifier}$

Complementary Learning

training: $\{(\mathbf{x}_n = \text{, \bar{y}_n = \text{banana})\} \rightarrow \text{classifier}$

testing goal: $\text{classifier}(\text{)} \rightarrow \text{cherry}$

ordinary versus complementary: same goal via
different training data

Learning with Complementary Labels Setup

Given

N examples (input \mathbf{x}_n , complementary label \bar{y}_n) $\in \mathcal{X} \times \{1, 2, \dots, K\}$ in data set \mathcal{D} such that $\bar{y}_n \neq y_n$ for some hidden ordinary label $y_n \in \{1, 2, \dots, K\}$.

Goal

a multi-class classifier $g(\mathbf{x})$ that **closely predicts** (0/1 error) the ordinary label y associated with some **unseen** inputs x

LCL model design: connecting
complementary & ordinary

Unbiased Risk Estimation for LCL

Ordinary Learning

- empirical risk minimization (ERM) on training data

risk: $\mathbb{E}_{(\mathbf{x}, y)}[\ell(y, g(\mathbf{x}))]$ **empirical risk:** $\mathbb{E}_{(\mathbf{x}_n, y_n) \in \mathcal{D}}[\ell(y_n, g(\mathbf{x}_n))]$

- loss ℓ : usually **surrogate** of 0/1 error

LCL [Ish+19]

- rewrite the loss ℓ to $\bar{\ell}$, such that

unbiased risk estimator: $\mathbb{E}_{(\mathbf{x}, \bar{y})}[\bar{\ell}(\bar{y}, g(\mathbf{x}))] = \mathbb{E}_{(\mathbf{x}, y)}[\ell(y, g(\mathbf{x}))]$

- LCL by minimizing **URE**

URE: **pioneer models** for LCL

Example of URE

Cross Entropy Loss

for $g(\mathbf{x}) = \operatorname{argmax}_{k \in \{1, 2, \dots, K\}} \mathbf{p}(k | \mathbf{x})$,

- ℓ_{CE} : derived by maximum likelihood as surrogate of 0/1

$$\text{risk: } R(g; \ell_{CE}) = \mathbb{E}_{(\mathbf{x}, y)} \underbrace{(-\log(\mathbf{p}(y | \mathbf{x})))}_{\ell_{CE}}$$

Complementary Learning [Ish+19]

$$\text{URE: } \bar{R}(g; \bar{\ell}) = \mathbb{E}_{(\mathbf{x}, \bar{y})} \left[\overbrace{\left((K-1) \log(\mathbf{p}(\bar{y} | \mathbf{x})) - \sum_{k=1}^K \log(\mathbf{p}(k | \mathbf{x})) \right)}^{\bar{\ell}} \right]$$

negative

under uniform \bar{y} assumption

ERM with URE: $\min_{\mathbf{p}} \bar{R}$ with \mathbb{E} taken on \mathcal{D}

URE overfits on single label

$$\ell = -\log(\mathbf{p}(y | \mathbf{x}))$$

$$\bar{\ell} = (K - 1) \log(\mathbf{p}(\bar{y} | \mathbf{x})) - \sum_{k=1}^K \log(\mathbf{p}(k | \mathbf{x}))$$

ordinary risk and URE very different

- $\ell > 0 \rightarrow$ ordinary risk non-negative
- small $\mathbf{p}(\bar{y} | \mathbf{x})$ (often) \rightarrow possibly very negative $\bar{\ell}$
empirical URE can be negative: only observing **some but not all** \bar{y}
- negative empirical URE **drags minimization** towards overfitting

practical remedy: [Ish+19]

NN-URE: constrain empirical URE to be non-negative

how can we avoid negative empirical URE?

Proposed Framework

Minimize Complementary 0/1

- Recall the goal: We minimize 0-1 loss instead of ℓ
- The unbiased estimator of R_{01}

$$\bar{R}_{01} : \mathbb{E}_{\bar{y}}[\bar{\ell}_{01}(\bar{y}, g(\mathbf{x}))] = \ell_{01}(y, g(\mathbf{x}))$$

- We denote $\bar{\ell}_{01}$ as the complementary 0-1 loss:

$$\bar{\ell}_{01}(\bar{y}, g(\mathbf{x})) = \mathbb{I}[\bar{y} \neq g(\mathbf{x})]$$

Surrogate Complementary Loss (SCL)

- Surrogate loss to optimize $\bar{\ell}_{01}$
- Unify previous work as surrogates of $\bar{\ell}_{01}$ [Yu+18; Kim+19]

[Yu+18] Learning with biased complementary labels, ECCV'18.

[Kim+19] NIN: Negative learning for noisy labels, ICCV'19.

Negative Risk Avoided

Unbiased Risk Estimator (URE)

URE loss $\bar{\ell}_{CE}$ [Ish+19] from cross-entropy ℓ_{CE} ,

$$\bar{\ell}_{CE}(\bar{y}, g(\mathbf{x})) = \underbrace{(K-1) \log(\mathbf{p}(\bar{y} | \mathbf{x}))}_{\text{negative loss term}} - \sum_{j=1}^K \log(\mathbf{p}(j | \mathbf{x}))$$

can go negative.

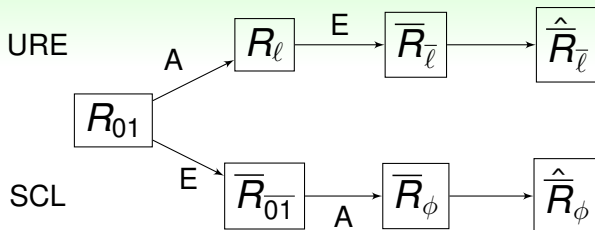
Surrogate Complementary Loss (SCL)

another loss [Kim+19], a surrogate $\bar{\ell}_{01}$

$$\phi_{NL}(\bar{y}, g(\mathbf{x})) = -\log(1 - \mathbf{p}(\bar{y} | \mathbf{x}))$$

remains non-negative.

Illustrative Difference between URE and SCE



URE: Ripple effect of errors

- Theoretical motivation [Ish+17]
- Estimation step (E) amplifies approximation error (A) in \bar{l}

SCL: 'Directly' minimize complementary likelihood

- Non-negative loss ϕ
- Practically prevents ripple effect

Classification Accuracy

Methods

- 1 Unbiased risk estimator (URE) [Ish+19]
- 2 Non-negative correction methods on URE (NN) [Ish+19]
- 3 Surrogate complementary loss (SCL)

Table: URE and NN are based on $\bar{\ell}$ rewritten from cross-entropy loss, while SCL is based on exponential loss $\phi_{\text{EXP}}(\bar{y}, g(\mathbf{x})) = \exp(\mathbf{p}_{\bar{y}})$.

| Data set + Model | URE | NN | SCL |
|--------------------|-------|-------|--------------|
| MNIST + Linear | 0.850 | 0.818 | 0.902 |
| MNIST + MLP | 0.801 | 0.867 | 0.925 |
| CIFAR10 + ResNet | 0.109 | 0.308 | 0.492 |
| CIFAR10 + DenseNet | 0.291 | 0.338 | 0.544 |

Gradient Analysis

Gradient Direction of URE

- Very diverged directions on each \bar{y} to maintain unbiasedness
- Low correlation to the target ℓ_{01}

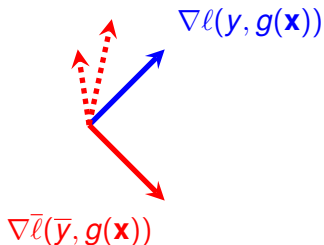


Figure: Illustration of URE

Gradient Direction of SCL

- Targets to minimum likelihood objective
- High correlation to the target $\bar{\ell}_{01}$

Gradient Estimation Error

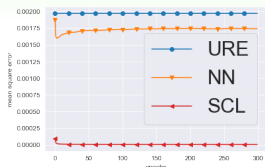
Bias-Variance Decomposition

$$\begin{aligned}\text{MSE} &= \mathbb{E}[(\mathbf{f} - \mathbf{c})^2] \\ &= \underbrace{\mathbb{E}[(\mathbf{f} - \mathbf{h})^2]}_{\text{Bias}^2} + \underbrace{\mathbb{E}[(\mathbf{h} - \mathbf{c})^2]}_{\text{Variance}}\end{aligned}$$

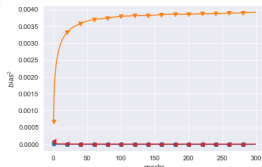
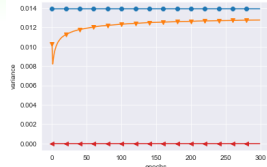
Gradient Estimation

- 1 Ordinary gradient $\mathbf{f} = \nabla \ell(y, g(\mathbf{x}))$
- 2 Complementary gradient $\mathbf{c} = \nabla \bar{\ell}(\bar{y}, g(\mathbf{x}))$
- 3 Expected complementary gradient \mathbf{h}

Bias-Variance Tradeoff



(a) MSE

(b) Bias²

(c) Variance

Findings

- SCL reduces variance by introducing small bias (towards \bar{y})

| | Bias | Variance | MSE |
|-----|-------|----------|-------|
| URE | 0 | Big | Big |
| SCL | Small | Small | Small |

Conclusion

Explain Overfitting of URE

- Unbiased method only do well in expectation
- Single fixed complementary label cause overfitting

Surrogate Complementary Loss (SCL)

- Minimum likelihood approach
- Avoids negative risk problem

Experiment Results

- SCL significantly outperforms other methods
- Introduce small bias for lower gradient variance

References



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