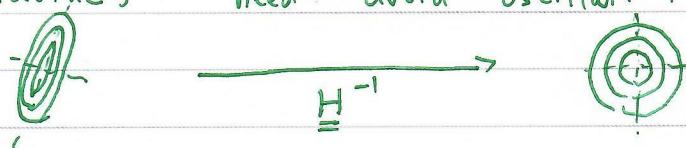


* difficulty in DL Optimization

- local min : not as bad as imagined
- saddle / local max : easily escapable (esp. w/ SGD)
- plateau : need larger η (learning rate) :
- ravines : need avoid oscillation



(Quasi-)Newton, but infeasible for DL usually

- slow computation of gradient : SGD on minibatch



"instable" estimate of gradient

* **running average estimate** of gradient from **SG**

$$\underline{v}_t = \beta \cdot \underline{v}_{t-1} + (1-\beta) \underline{\Delta}_t$$

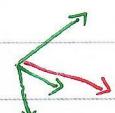
↓ current average ↓ previous average

→ stochastic gradient at t-th iteration

$$\text{update : } \underline{w}_t = \underline{w}_{t-1} - \eta \underline{v}_t$$

(SGD with) momentum

- stochastic instability cancels out



- pass ravine faster

* **oscillation** prevention by per-component learning rate

↑ larger gradient component
want: smaller step

$$\text{update : } \underline{w}_t = \underline{w}_{t-1} - \eta \underline{\Delta}_t \cdot / \text{"magnitude}(\underline{\Delta}_t)"$$

$\sqrt{\underline{\Delta}_t^T \underline{\Delta}_t + \epsilon}$

running average

$$\underline{v}_t = \beta \underline{v}_{t-1} + (1-\beta) (\underline{\Delta}_t \cdot * \underline{\Delta}_t)$$

RMS prop

* Adam = SGD + momentum + RMSProp (+ other tricks)

$$\underline{V}_t = \beta_1 \underline{V}_{t-1} + (1-\beta_1) \Delta_t$$

\downarrow
0.9

$$\underline{U}_t = \beta_2 \underline{U}_{t-1} + (1-\beta_2) (\Delta_t * \underline{V}_t)$$

\downarrow
0.999

$0.001 \leftarrow \frac{\eta}{\sqrt{t/N}} \text{ (decaying)}$

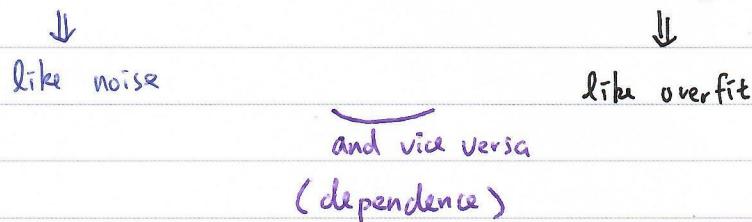
$$\underline{W}_t = \underline{W}_{t-1} - \frac{\eta_t}{\sqrt{\underline{U}_t + \epsilon}} * \underline{V}_t$$

\downarrow
 10^{-8}

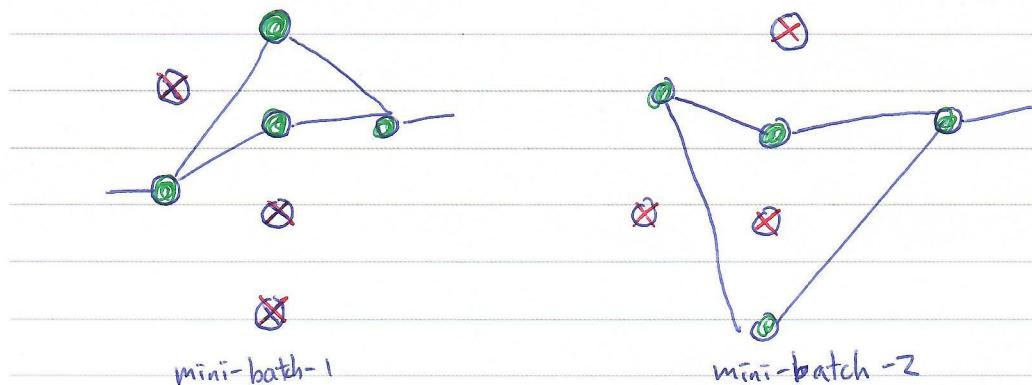
* difficulty in DL generalization

- co-adaptation :

(consistent mistakes from some neurons) corrected by fitting other neurons



* break the dependence : shut down neurons (randomly)



dropout : drop p
keep $(1-p)$ \Rightarrow many thin networks (combined)

↓ ↓

slows down convergence noise as regularization
but faster per-iteration like DAE

* dropout during testing

- full-net prediction w/o changing

$$E(S_i^{(l)}) = (1-p) S_i^{(l)}$$

in training in testing

- test-time "pseudo-" dropout

$$x_i^{(l)} = \theta((1-p) S_i^{(l)})$$

need to record p, less flexibility

for changing p per neuron
or dynamically

- inverted dropout

$$\text{training : dropout } \& \quad x_i^{(l)} = \theta(S_i^{(l)} / (1-p))$$

$$\text{testing : } x_i^{(l)} = \theta((1-p) S_i^{(l)} / (1-p))$$

$$= \theta(S_i^{(l)}) \quad \text{unchanged (usually preferred)}$$