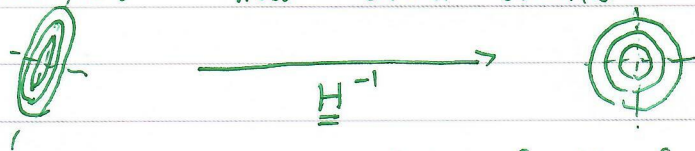


* difficulty in DL Optimization

- local min : not as bad as imagined
- saddle / local max : easily escapable (esp. w/ SGD)
- plateau : need larger η (learning rate)
- ravines : need avoid oscillation



(Quasi-)Newton, but infeasible for DL usually

◦ slow computation of gradient : SGD on minibatch

↓
"unstable" estimate of gradient

* running average estimate of gradient from SG

$$\boxed{V_t} = \beta \cdot \boxed{V_{t-1}} + (1-\beta) \boxed{\Delta_t}$$

↓
current average
↓
previous average

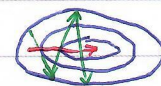
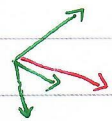
↘ stochastic gradient at t-th iteration

update : $\underline{W}_t = \underline{W}_{t-1} - \eta \underline{V}_t$

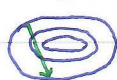
(SGD with) momentum

◦ stochastic instability cancels out

◦ pass ravine faster



* oscillation prevention by per-component learning rate



↑ larger gradient component
want: smaller step

update : $\underline{W}_t = \underline{W}_{t-1} - \eta \frac{\Delta_t \cdot \text{"magnitude"}(\Delta_t)}{\sqrt{\mu_t + \epsilon}}$

running average

$$\underline{\mu}_t = \beta \underline{\mu}_{t-1} + (1-\beta) (\Delta_t \cdot \Delta_t)$$

RMS prop

* dropout during testing

- full-net prediction w/o changing

$$\underset{\text{in training}}{E(S_i^{(l)})} = (1-p) \underset{\text{in testing}}{S_i^{(l)}}$$

- test-time "pseudo-dropout"

$$x_i^{(l)} = \theta \left(\underbrace{(1-p)}_{\text{need to record } p, \text{ less flexibility}} S_i^{(l)} \right)$$

need to record p , less flexibility

- inverted dropout

training : dropout & $x_i^{(l)} = \theta \left(S_i^{(l)} / (1-p) \right)$

testing : $x_i^{(l)} = \theta \left(\underbrace{(1-p)}_{\text{for changing } p \text{ per neuron or dynamically}} S_i^{(l)} / \underbrace{(1-p)}_{\text{or dynamically}} \right)$

$$= \theta \left(S_i^{(l)} \right) \quad \text{unchanged (usually preferred)}$$