

Queue

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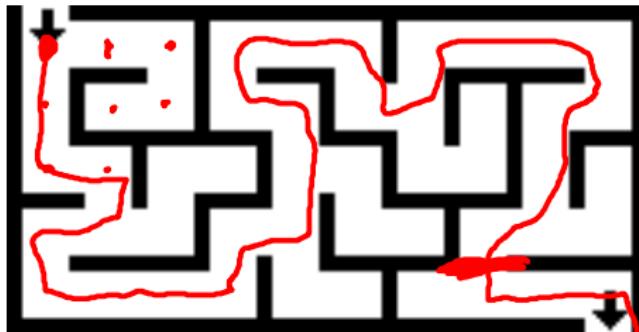
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What We Have Done

algorithm	data structure	
sequential search	array (or linked list)	✓
selection sort	array (or linked list)	✓
insertion sort	linked list (or array)	✓
binary search	ordered array	✓
polynomial merge	sparse array on linked list	✓
parenthesis matching	stack	✓
postfix evaluation	stack	
infix to postfix	stack)

next: another algorithm with stack (and more)

The Maze Problem



<http://commons.wikimedia.org/wiki/File:Maze01-01.png>

given a (2D) maze, is there a way out?



Recursive Algorithm

GET-OUT-RECURSIVE(m , $(0, 0)$)

Getting Out of Maze Recursively

GET-OUT-RECURSIVE(Maze m , Postion (i, j))

mark (i, j) as visited

for each unmarked (k, ℓ) reachable from (i, j) do

 if (k, ℓ) is an exit

 return TRUE

 end if

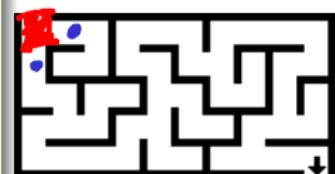
 if GET-OUT-RECURSIVE(m , (k, ℓ))

 return TRUE

 end if

end for

return FALSE



Recursion (Reading Assignment: Section 3.5, Remember?)

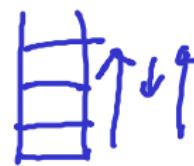
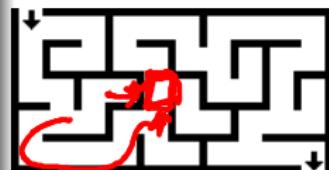
- a function call to itself
- be ware of **terminating conditions**
- can represent programming intentions clearly
- at the expense of **"space"** (why?)

From Recursion to Stack

Getting Out of Maze by Stack

GET-OUT-STACK(Maze m , Postion (i, j))

```
while stack not empty do
     $(i, j) \leftarrow$  pop from stack
    mark  $(i, j)$  as visited
    for each unmarked  $(k, \ell)$  reachable from  $(i, j)$  do
        if  $(k, \ell)$  is an exit
            return TRUE
        end if
        push  $(k, \ell)$  to stack [and mark  $(k, \ell)$  as todo]
    end for
end while
return FALSE
```



- similar result to recursive version, but conceptually different
 - recursive: one path on the system stack
 - stack: many positions-to-be-explored on the user stack

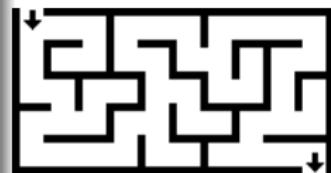
A General Maze Algorithm

Getting Out of Maze by Container

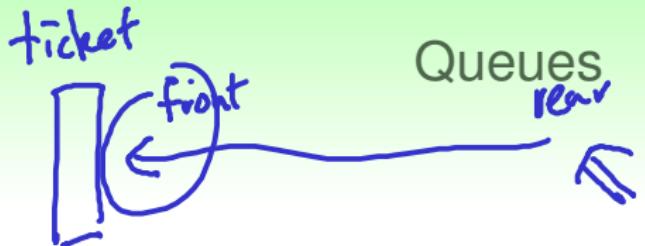
General

GET-OUT-CONTAINER(Maze m , Postion (i, j))

```
while container not empty do
     $(i, j) \leftarrow$  remove from container
    mark  $(i, j)$  as visited
    for each unmarked  $(k, \ell)$  reachable from  $(i, j)$  do
        if  $(k, \ell)$  is an exit
            return TRUE
        end if
        insert  $(k, \ell)$  to container [and mark  $(k, \ell)$  as todo]
    end for
end while
return FALSE
```



- if “random” remove from container: “random walk” to exit



Queue

- object: a container that holds some elements
- action: [constant-time] enqueue (to the rear), dequeue (from the front)
- first-in-first-out (FIFO): 買票, 印表機
- also very restricted data structure, but also important for computers

insert At Rear

remove from

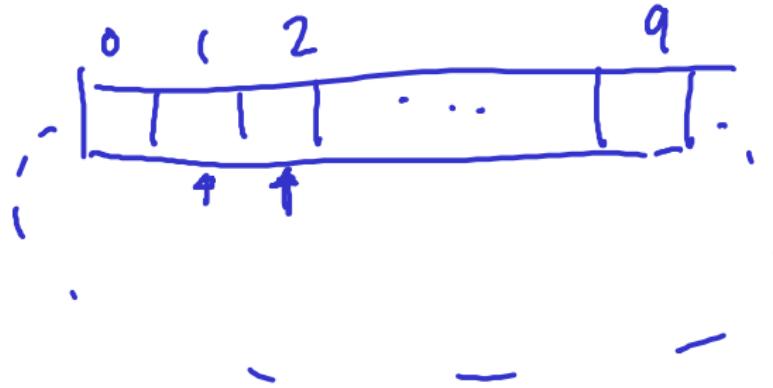
Front

stack : LIFO

Queues Implemented on Circular Array (5.2.4)

Reading Assignment

be sure to go ask the TAs or me if you are still confused



Reading Assignment

be sure to go ask the TAs or me if you are still confused

Maze From Stack to Queue

Getting Out of Maze by Queue

GET-OUT-QUEUE(Maze m , Position (i, j))

```
while queue not empty do
     $(i, j) \leftarrow \text{dequeue}$  from queue
    mark  $(i, j)$  as visited
    for each unmarked  $(k, \ell)$  reachable from  $(i, j)$  do
        if  $(k, \ell)$  is an exit
            return TRUE
        end if
        enqueue  $(k, \ell)$  to queue [and mark  $(k, \ell)$  as todo]
    end for
end while
return FALSE
```

- use of stack/queue: store the yet-to-be-explored positions
- stack version : first (lexicographically) way out (explore deeply)
—depth-first search DFS
- queue version : shortest way out (explore broadly) —breadth-first search BFS

