Stacks, Queues, Deques

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A Simple Application: Parentheses Balancing

• in C, the following characters show up in pairs: (), [], {}, ""

```
good: {xxx(xxxxxx)xxxxx"xxxx"x}
bad: {xxx(xxxxxx)xxxxx"xxxx"x}
```

the LISP programming language

```
(append (pow (* (+ 3 5) 2) 4) 3)
```

how can we check parentheses balancing?

Stack Solution to Parentheses Balancing

inner-most parentheses pair \Longrightarrow top-most plate

'(': 堆盤子上去;')': 拿盤子下來

Parentheses Balancing Algorithm

```
for each c in the input do
  if c is a left character
    push c to the stack
  else if c is a right character
    pop d from the stack and check if match
  end if
end for
```

many more sophisticated use in compiler design

System Stack

- recall: function call ⇔ 拿新的草稿紙來算
- old (original) scrap paper: temporarily not used, 可以壓在下面

System Stack: 一疊草稿紙, each paper (stack frame) contains

- return address: where to return to the previous scrap paper
- local variables (including parameters): to be used for calculating within this function
- previous frame pointer: to be used when escaping from this function

some related issues: stack overflow? security attack?

Stacks Implemented on Array (5.1.4)

Reading Assignment

be sure to go ask the TAs or me if you are still confused

Stacks Implemented on Linked List (5.1.5)

Reading Assignment

be sure to go ask the TAs or me if you are still confused

Stack for Expression Evaluation (Supplementary)

$$a/b-c+d*e-a*c$$

- precedence: $\{*,/\}$ first; $\{+,-\}$ later
- steps
 - f = a/b
 - g = f c
 - h = d ∗ e
 - i = g + h
 - i = a * c
 - $\ell = i j$

Postfix Notation

same operand order, but put "operator" after needed operands

- —can "operate" immediately when seeing operator
- -no need to look beyond for precedence

Postfix from Infix (Usual) Notation

infix:

$$3 / 4 - 5 + 6 * 7 - 8 * 9$$

parenthesize:

$$3 / 4 - 5 + 6 * 7 - 8 * 9$$

• for every triple in parentheses, switch orders

remove parentheses

difficult to parenthesize efficiently

Evaluate Postfix Expressions

$$34/5 - 67 * +89 * -$$

- how to evaluate? left-to-right, "operate" when see operator
- 3, 4, $/ \Rightarrow 0.75$
- $0.75, 5, \Rightarrow -4.25$
- -4.25, 6, 7, * \Rightarrow -4.25, 42 (note: -4.25 stored for latter use)
- \bullet -4.25, 42, + \Rightarrow 37.75
- 37.75, 8, 9, * \Rightarrow 37.75, 72 (note: 37.75 stored for latter use)
- **●** 37.75, 72, ⇒ ...

stored where?

stack so closest operands will be considered first!

Stack Solution to Postfix Evaluation

Postfix Evaluation

```
for each token in the input do
  if token is a number
  push token to the stack
  else if token is an operator
  sequentially pop operands a_{t-1}, \cdots, a_0 from the stack
  push token(a_0, a_1, a_{t-1}) to the stack
  end if
  end for
  return the top of stack
```

matches closely with the definition of postfix notation

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One-Pass Algorithm for Infix to Postfix

infix ⇒ postfix efficiently?

at /, not sure of what to do (need later operands) so store

$$a/b - c + d * e - a * c$$

• at -, know that a / b can be a b / because - is of lower precedence

$$a/b - c + d * e - a * c$$

 at +, know that ? - c can be ? c - because + is of same precedence but {-, +} is left-associative

$$a/b - c + d * e - a * c$$

at *, not sure of what to do (need later operands) so store

$$a/b - c + d * e - a * c$$

stored where? stack so closest operators will be considered first!

Stack Solution to Infix-Postfix Translation

```
for each token in the input do
   if token is a number
    output token
   else if token is an operator
    while top of stack is of higher (or same) precedence do
    pop and output top of stack
   end while
   push token to the stack
   end if
end for
```

- here: infix to postfix with operator stack
 —closest operators will be considered first
- recall: postfix evaluation with operand stack
 —closest operands will be considered first
- mixing the two algorithms (say, use two stacks): simple calculator

Some More Hints on Infix-Postfix Translation

```
for each token in the input do
  if token is a number
   output token
  else if token is an operator
   while top of stack is of higher (or same) precedence do
      pop and output top of stack
   end while
   push token to the stack
  end if
end for
```

- for left associativity and binary operators
 - right associativity? same precedence needs to wait
 - unary/trinary operator? same
- parentheses? higest priority
 - at '(', cannot pop anything from stack
 - —like seeing '*' while having '+' on the stack
 - at ')', can pop until '(' —like parentheses matching

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