

Linked Lists

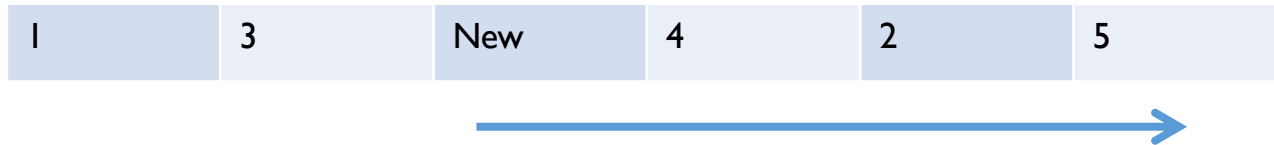
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2017/3/14

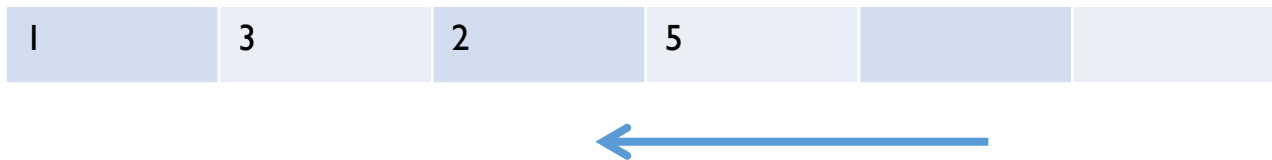
What's wrong with Arrays?



- Inserting a new element



- Deleting an existing element



- Time complexity= $O(??)$

Complexity for the array implementation

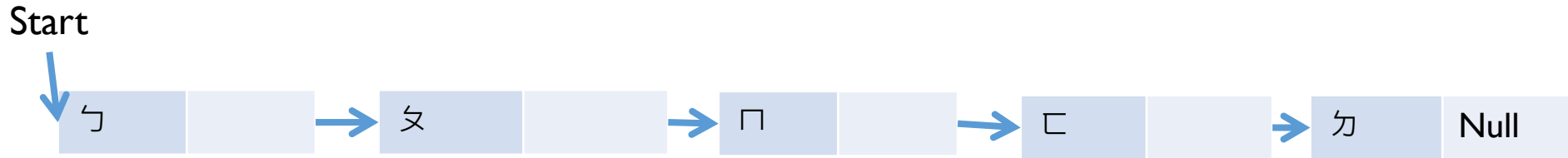
	Array	Dynamic Array (Expand to twice of the original space when full)	Linked List (What we are learning today)
Indexing (Get a particular element)			??
Insert/Delete at the head			??
Insert/Delete at the tail			??
Insert/Delete in the middle			??
Wasted space			??

New friend: Linked List

- How do we arrange the data, such
 1. We can arbitrarily change their order,
 2. But we still keep a record of their order?
- Answer:
- The order of the elements can be arbitrary,
- But, we store “which is the next” in addition to the data.

index	[0]	[1]	[2]	[3]	[4]
data	□	ㄨ	ㄣ	ㄣ	□
Which is the next	4	0	1	-1	3
head	1				

Conceptually, it looks like this:

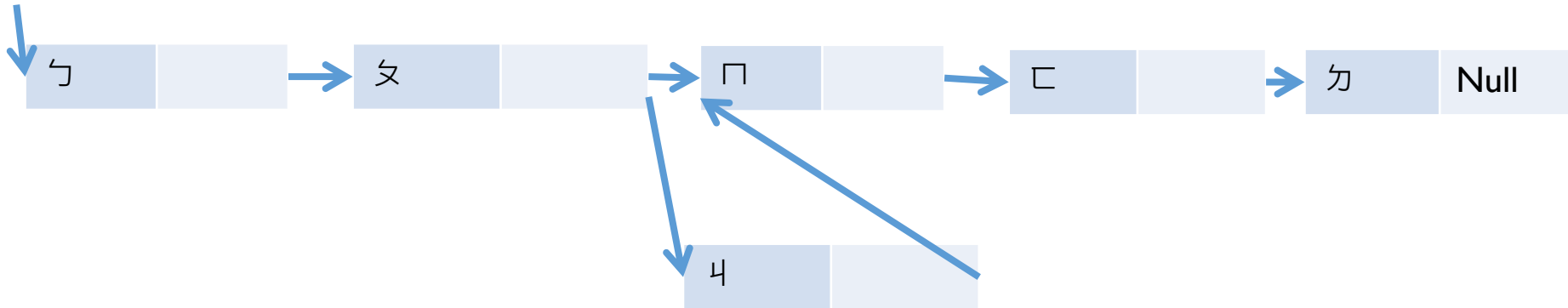


Actual implementation

index	[0]	[1]	[2]	[3]	[4]
data	ㄇ	ㄆ	ㄅ	ㄏ	ㄏ
Which is the next	4	0	1	-1	3
head	2				

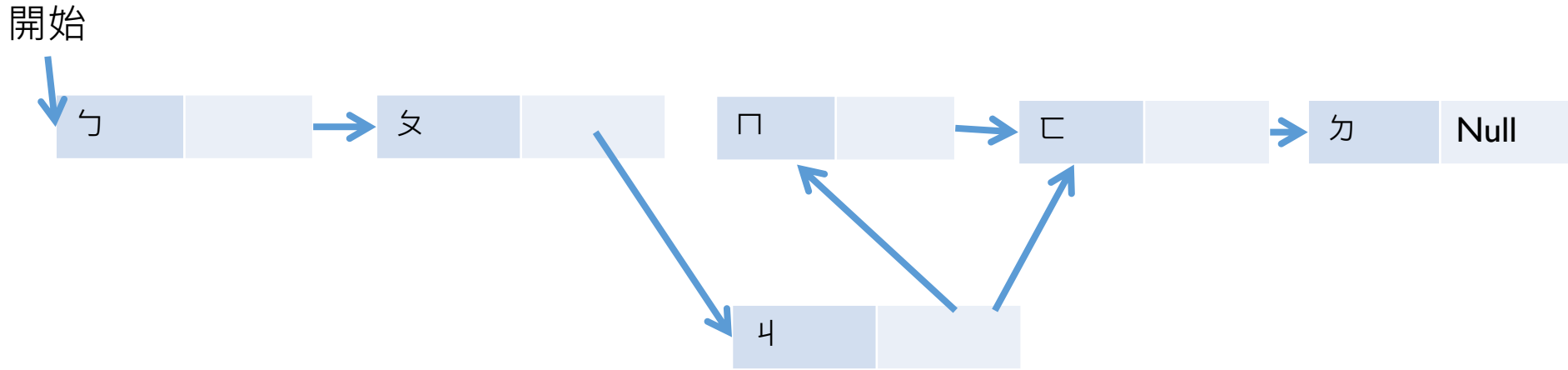
Add an additional element?

Start



index	[0]	[1]	[2]	[3]	[4]	[5]
data	ㄇ	ㄆ	ㄅ	ㄏ	ㄏ	4
Which is the next	4	5	1	-1	3	0
head	2					

Remove an existing element?



index	[0]	[1]	[2]	[3]	[4]	[5]
資料	冂	夕	勺	勹	匚	4
下一個是誰	4	5	1	-1	3	4
開始	2					

Code segments:

Struct and create a new node.

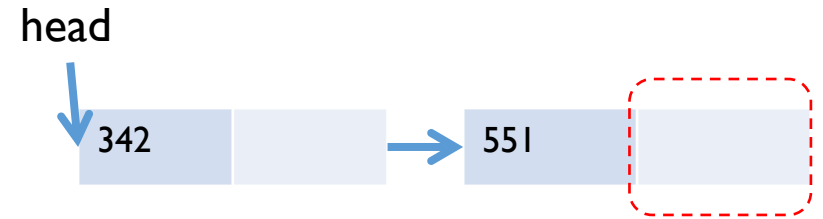
```
1 //Structure declaration for the list node
2 struct ListNode {
3 int data;
4 struct ListNode *next;
5 };
6
7 //Create a new node
8 struct ListNode *new;
9 new=(struct ListNode*)malloc(sizeof(struct listNode));
```


Code segments: accessing the structure members

- `new` is a pointer , pointing at a variable of type `struct ListNode`.
- How do we obtain the member `data` in this variable?
- Answer: by
- `(*new) .data`
- Or,
- `new->data`

- How about `next`?
- `(*new) .next`
- 或者,
- `new->next`

Code segments: accessing the next node



- Assume `head` points at the first node
- How do I get the value of `next` in the “551 node”?

```
1  struct ListNode {  
2  int data;  
3  struct ListNode *next;  
4  };
```

Create two nodes (Insert from the head)



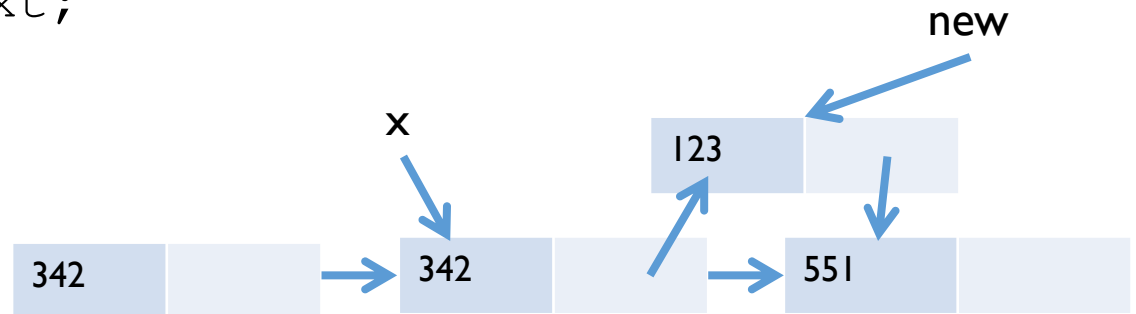
```
1  struct ListNode *head, *tmp;
2
3  tmp=(struct ListNode*)malloc(sizeof(struct ListNode));
4  if (tmp==NULL)
5      exit(-1); // exit program on error
6
7  tmp->data=551;
8  tmp->next=NULL;
9
10 head=tmp;
11 tmp=(struct ListNode*)malloc(sizeof(struct ListNode));
12
13 tmp->data=342;
14 tmp->next=head;
15
16 head=tmp;
```

Insert a new node after a certain node

```
1  struct ListNode *x;  
2  //Pointing at the node before the location to  
3  //be inserted  
4  
5  struct ListNode *new;  
6  
7  new=(struct ListNode*)malloc(sizeof(struct ListNode));  
8  new->data=123;
```

Do we process `new->next` first or `x->next` first?

```
1  new->next=x->next;  
2  x->next=new;
```

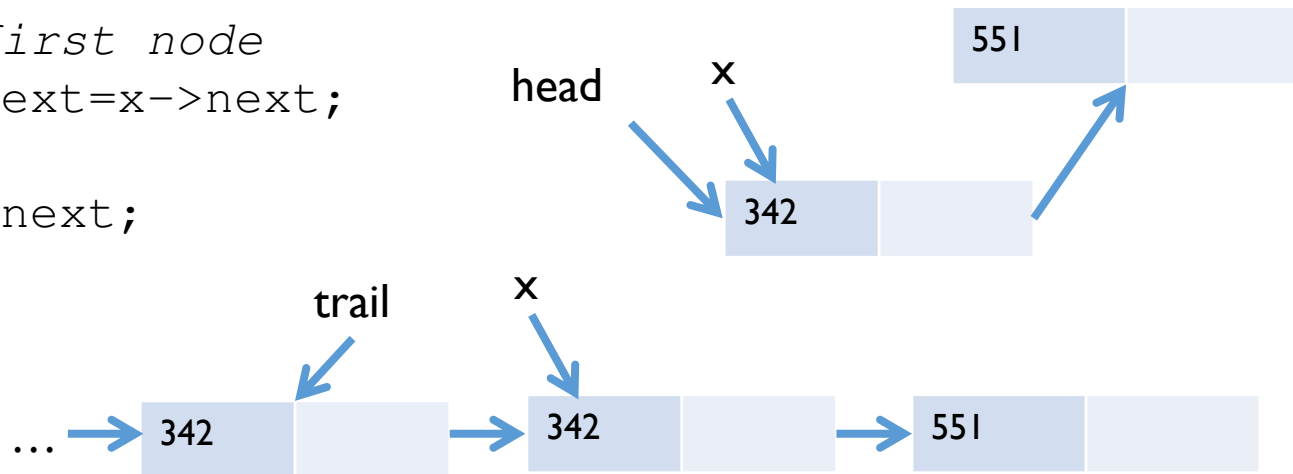


Deleting a node

```
1 struct ListNode *head; //Pointing at the head node
2 struct ListNode *x;
3 //Pointing at the node to be deleted
4 struct ListNode *trail;
5 //Pointing at the node before the node to be //deleted
```

- Two possible conditions: x is/is not the head node

```
1 if (trail)
2 //x is not the first node
3     trail->next=x->next;
4 else
5     head=x->next;
6 free(x);
```



Examples: Traverse and Print

- Traverse (and print) linked list

```
1  struct ListNode *tmp;  
2  for(tmp=head; tmp!=NULL; tmp=tmp->next) {  
3      printf("%d", tmp->data);  
4  // you can do other processing here too  
5  }
```

Correct the code below: Find

- Find the location before a node with a particular data value

```
1  int a=123; //123 is the data to look for
2  struct ListNode *tmp;
3  for(tmp=head; tmp!=NULL; tmp=tmp->next) {
4      if (tmp->next->data==a)
5          break;
6      //when breaking, tmp is what we are looking for
7  }
8 }
```

- This code segment would crash in certain conditions. Correct it!

Comparison of complexity

	Array	Dynamic Array (Expand to twice of the original space when full)	Linked List
Indexing (Take a particular element)	$O(1)$	$O(1)$	
Insert/Delete at the head	$O(n)$, only feasible if not full	$O(n)$	
Insert/Delete at the tail	$O(1)$, only feasible if not full	$O(1)$, if not full $O(n)$, if full	
Insert/Delete in the middle	$O(n)$, only feasible if not full	$O(n)$	
Wasted space	0 (when full)	$O(n)$ (up to half of the space empty)	

Discussion

- When should we use array?
- When should we use linked list?
- Explain why.

Example: Stacks & Queues

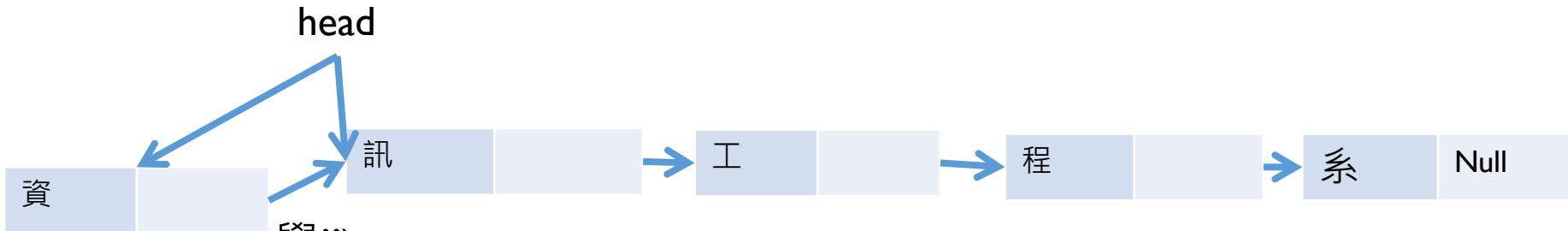
- 如果是一塊記憶體要放很多stack或queue
- 就很難做到很efficient
- 例如如果某一stack滿了, 就要把一堆資料往後擠
- 就不是 $O(1)$ 了 T_T

- 解決: 跟Linked List當朋友



Stack

- 要怎麼拿來當stack呢? (想想怎麼做主要的operation)
- push & pop
- 請一位同學來講解☺



- 例: push("學")
- head當作stack top
- 怎麼寫code?
- 那pop呢?

Queue

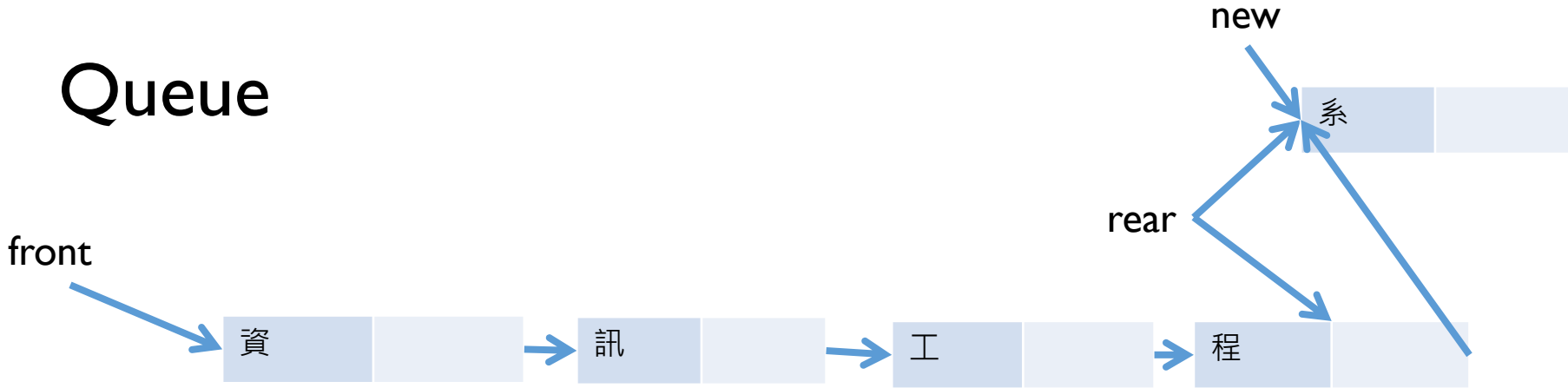
- 類似stack的作法
- 不過頭尾都要有一個指標
- 從頭拿, 從尾放



- 怎麼拿? (DeQueue)

```
struct ListNode* tmp;  
tmp=front;  
front=front->link;  
tmp_data=tmp->data;  
free(tmp);  
return tmp_data;
```

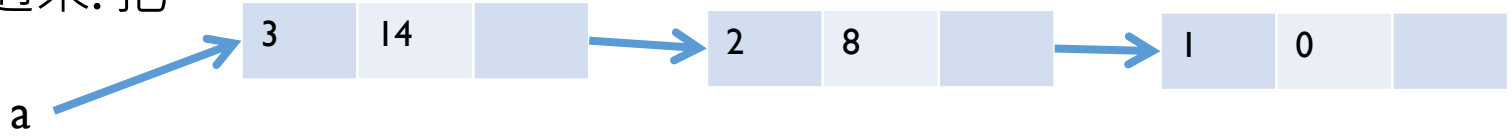
Queue



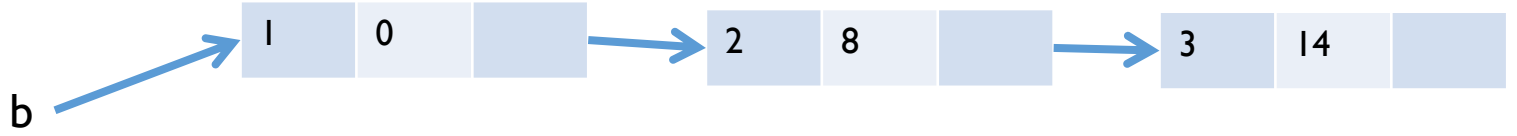
- 那怎麼放?
- 假設new是指到新的node
- `rear->next=new;`
- `new->next=NULL;`
- `rear=new;`

練習題2: 把linked list反過來

- 反過來: 把



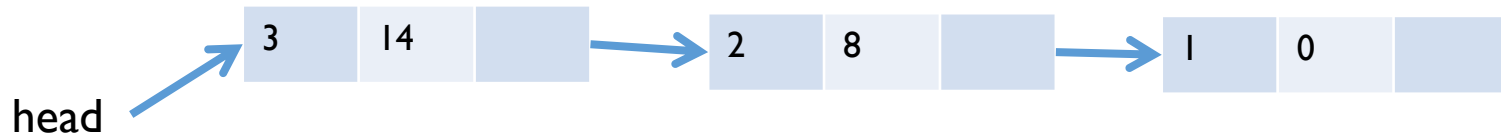
- 變成



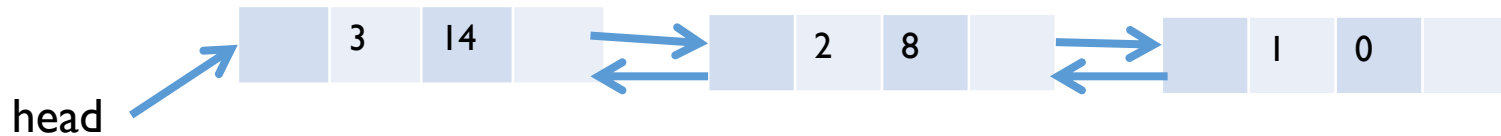
- 怎麼弄?

Singly v.s. doubly linked list

Singly linked list:



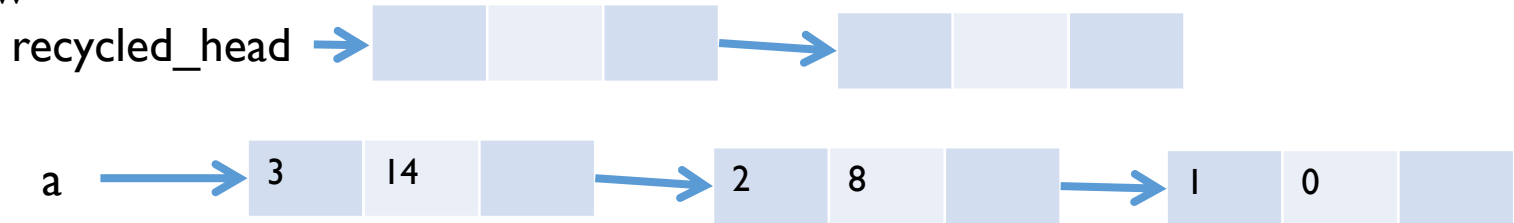
Doubly linked list:



- When do you need to use doubly linked list?
- Singly linked list: can only traverse forward, not backward
- (go all the way back to the head)
- When we need to frequently traverse backward: use doubly linked list
- Trade-offs:
 - Space for two pointers (instead of one) (see: <http://goo.gl/qifrq2>)
 - Additional time to process the pointers when inserting, deleting.

Recycling

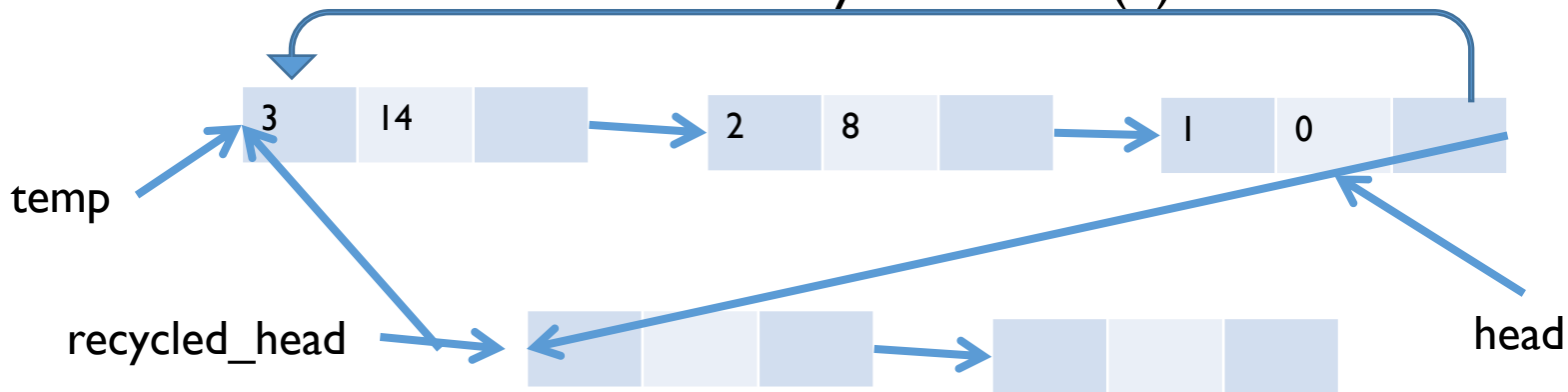
- Return the memory occupied by the nodes to the system when done. (Why?)
- $O(n)$ time to return all the nodes
- Alternative: recycling! Collect all “deleted nodes”, and use them when necessary.
- Goal: $O(1)$ time for both delete and new (from recycled nodes)
- How



- Key: slow to find the tail (obviously, not $O(1)$ time operation)
- Can we avoid using the tail pointer?

Sol: Circular List

- head pointer points at the tail.
- The tail node's next pointer points to the head node (instead of setting it as NULL).
- Easy to connect the entire list with another list!
Place the entire list to the recycled list= $O(1)$!!



- We can also have doubly circular linked list!

Let's review!

- The types of linked lists that we introduced today:
 - Singly linked list
 - Circular
 - Non-circular (chain)
 - Doubly linked list
 - Circular
 - Non-circular (chain)

(If time permits) Practice Problems

- Given a (singly) linked list of unknown length, design an algorithm to find the n -th node from the tail of the linked list. Your algorithm is allowed to traverse the linked list only once.

- Reverse a given singly linked list using the original link nodes.