

# Focus Value

2014. 12. 31



熊育萱 / [bear8039@gmail.com](mailto:bear8039@gmail.com) / 0935334132

# Outline

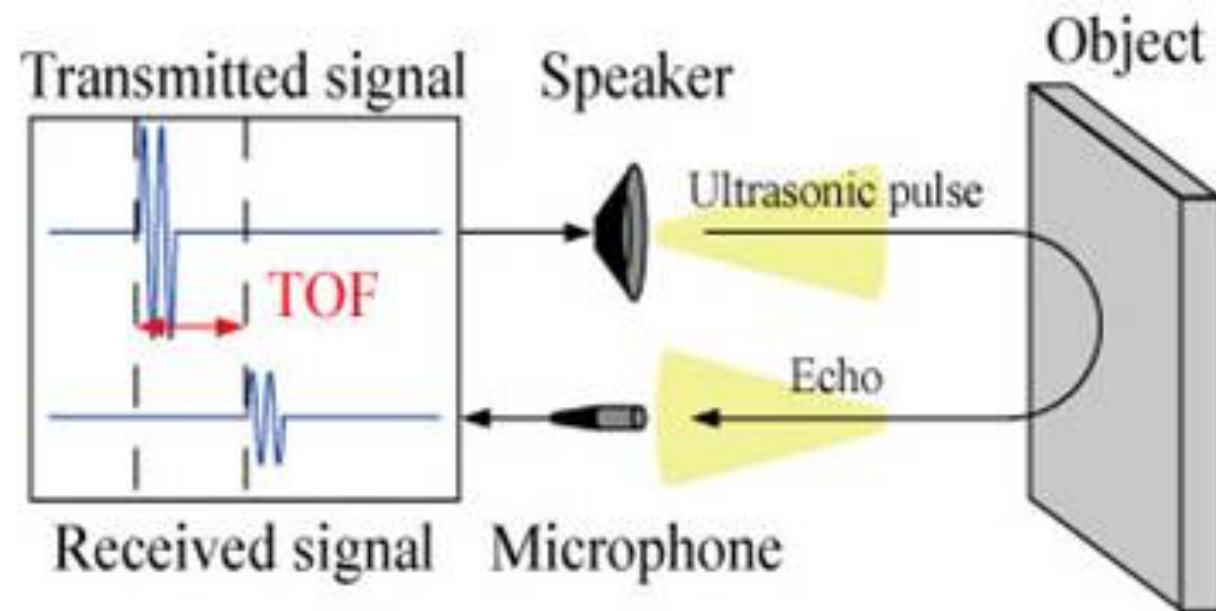
- Auto Focus
- Focus Formula
- Focus Value Curve
- Focus Value Curve Fitting

# **Auto Focus**

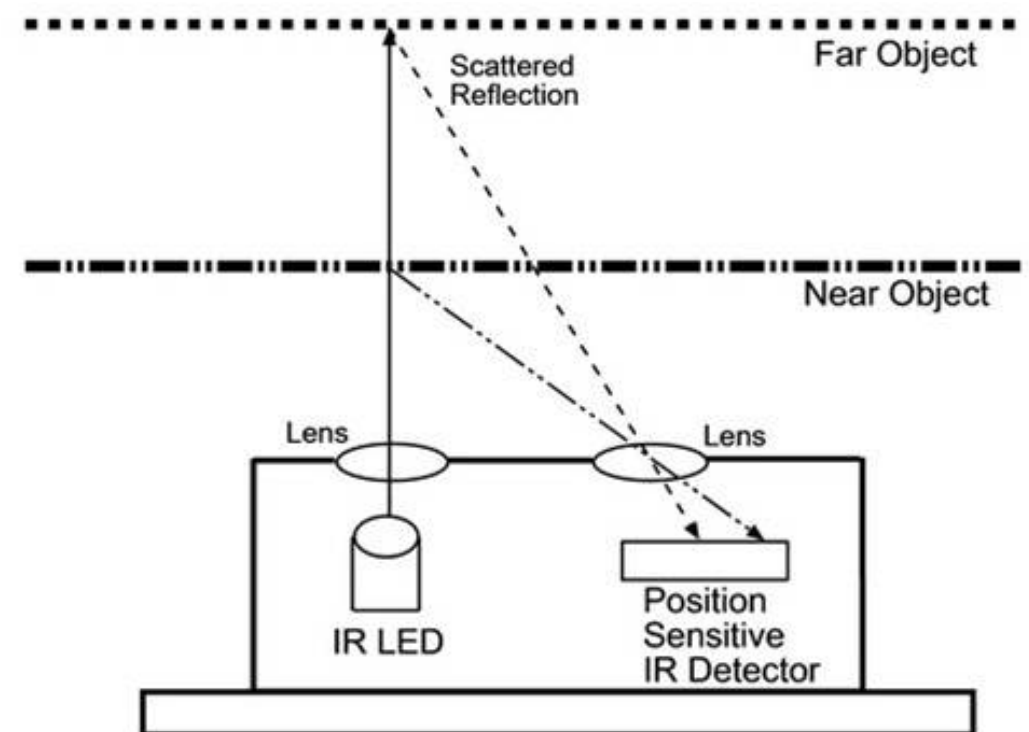
- Active Autofocus
- Passive Autofocus

# Active Autofocus

- Measure distance to the subject independently of the optical system, and subsequently adjust the optical system for correct focus.
- Ex: ultrasonic sound waves, infrared (IR) ray.



TOF: Time Of Flight  
LED: Light-Emitting Diode



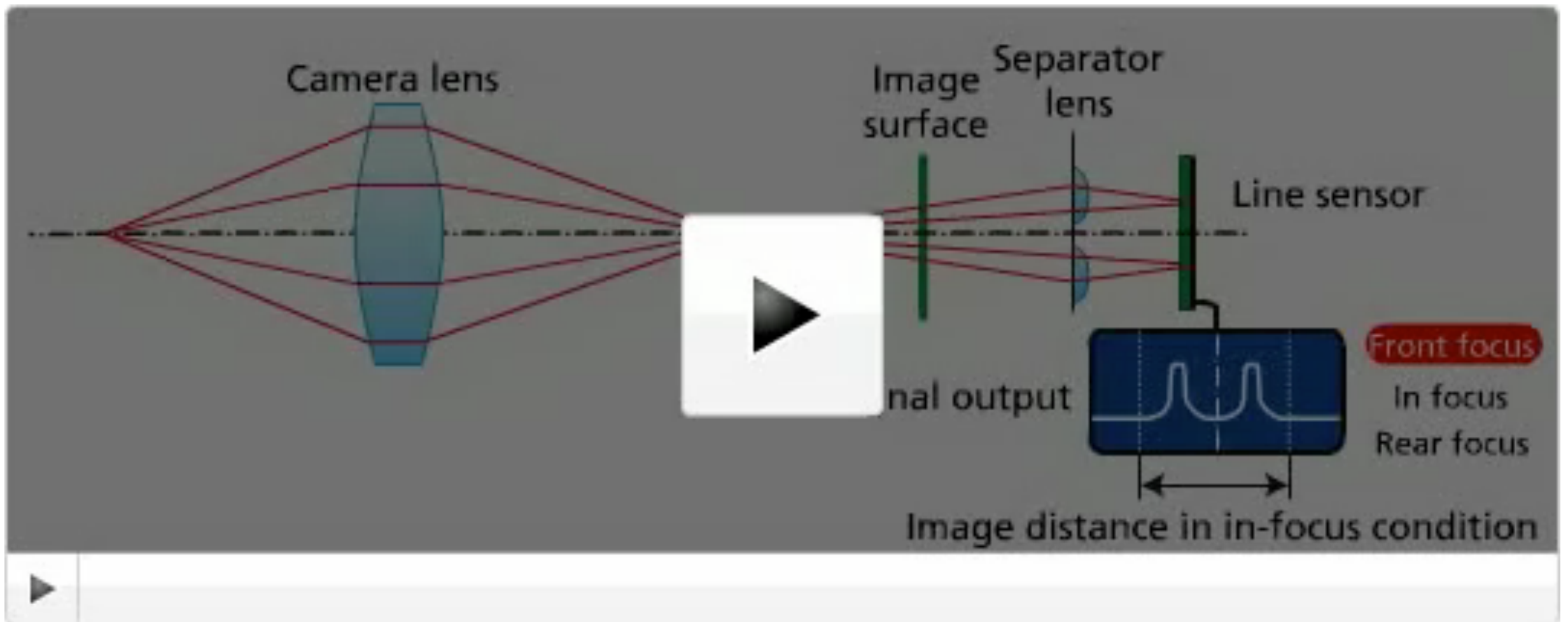


# Passive Autofocus

- Determine correct focus by performing passive analysis of the image that is entering the optical system.
- Can be achieved by phase detection or contrast measurement.

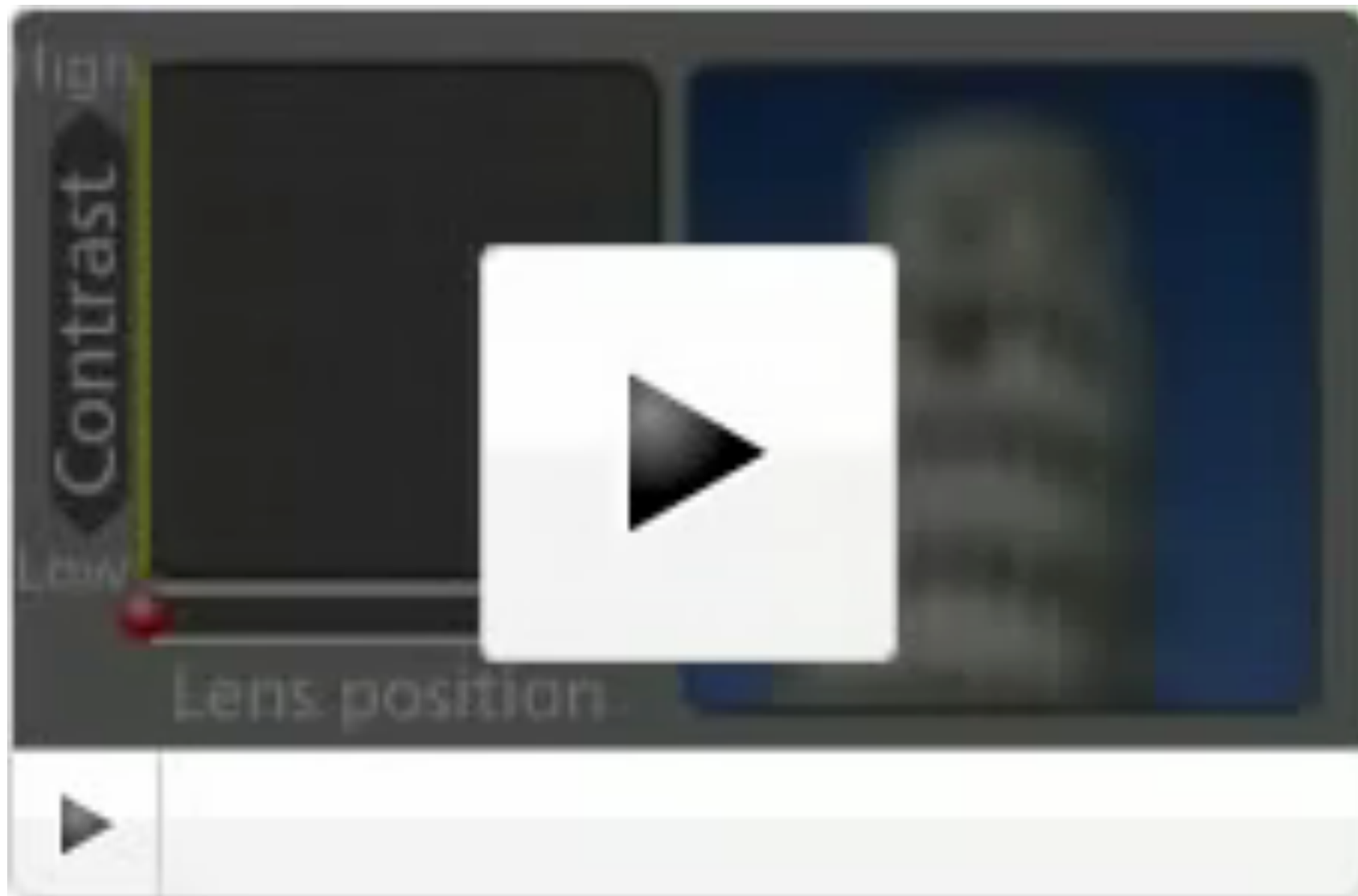
# Passive Autofocus

- Phase Detection:

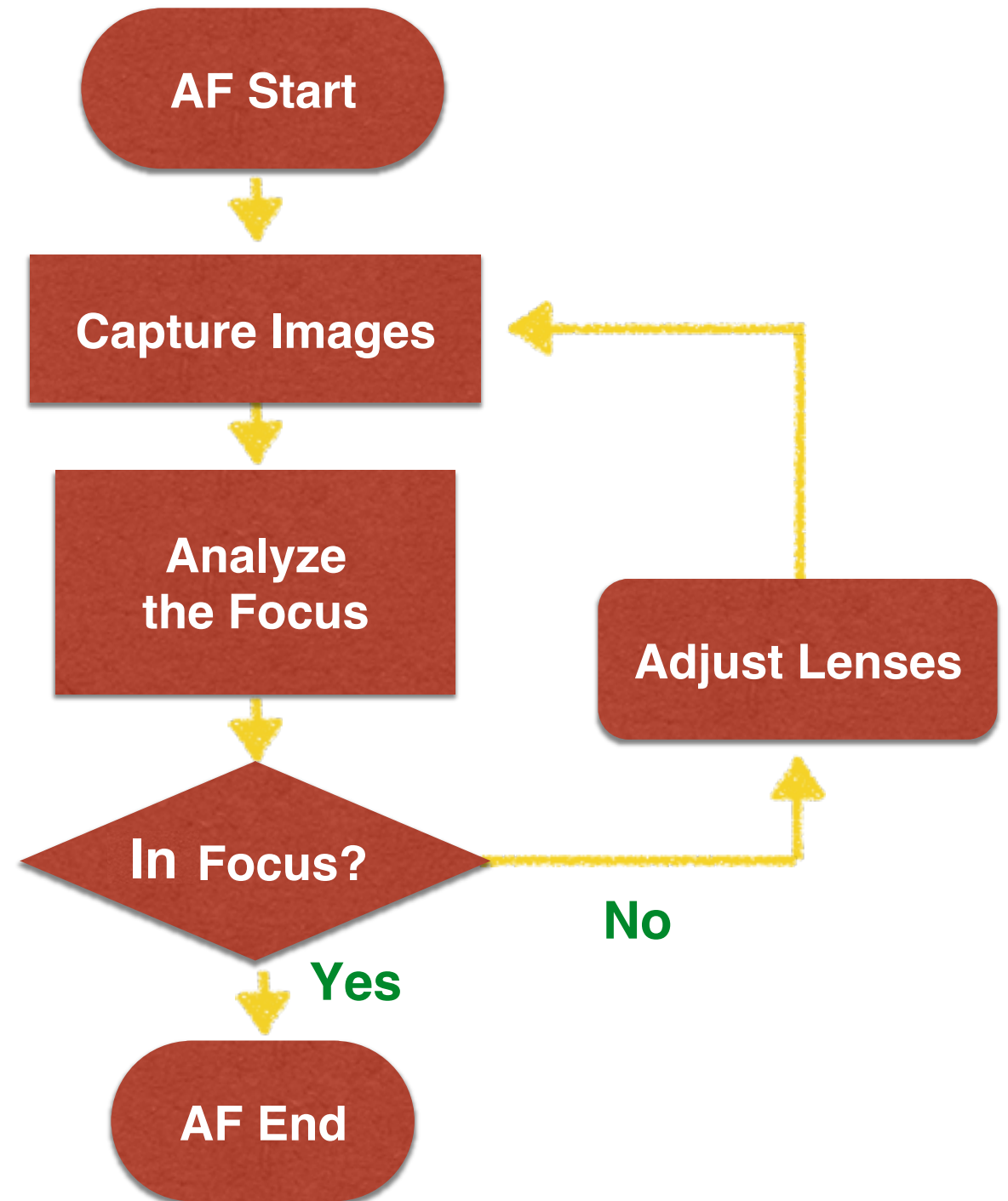
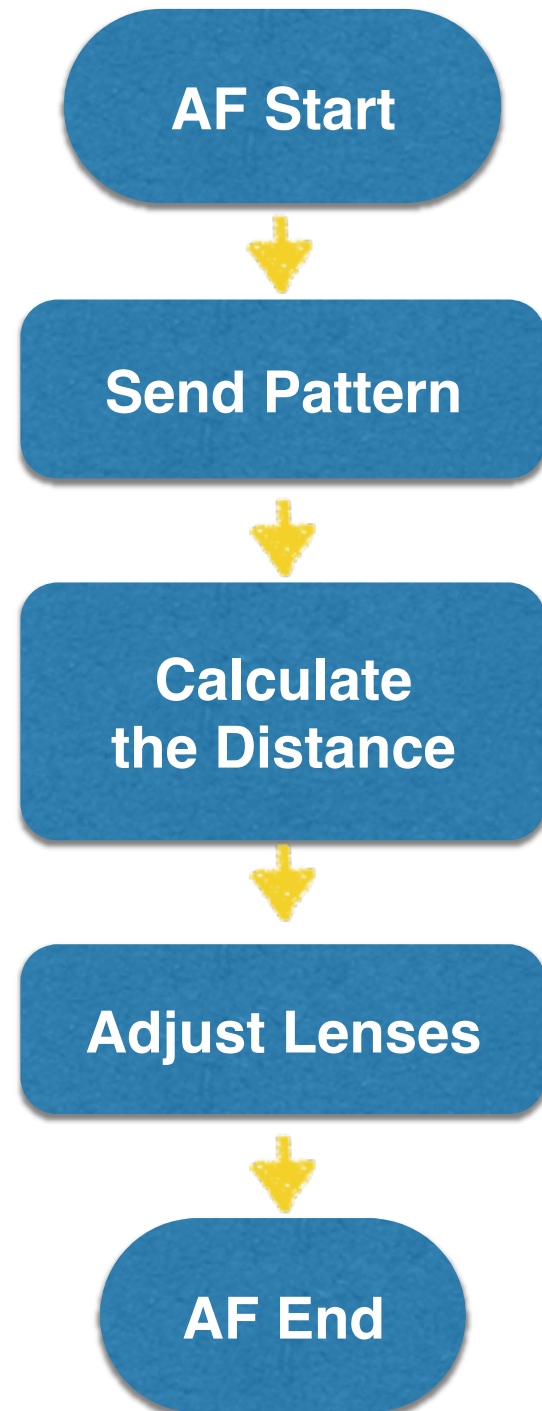


# Passive Autofocus

- Contrast Detection:



# Active / Passive



# Comparison of Active and Passive AutoFocus

	Advantages	Disadvantages
Active Autofocus	Fast	<ul style="list-style-type: none"><li>- High Cost</li><li>- Need space to place sensors</li></ul>
Passive Autofocus	Simple	<ul style="list-style-type: none"><li>- Mistake in darker or lighter scene</li></ul>

# Focus Formula

- Robert
- Prewitt
- Laplacian
- Sobel



# Robert

- Derived by first-order difference.

$$f'(x) = \lim_{\Delta x \rightarrow 0} \frac{f(x+\Delta x) - f(x)}{\Delta x} = f(x+1) - f(x)$$

- Simplest but sensitive for noise.

1			1
	-1	-1	

$$FV = \sum_{(r,c)} f(\underline{r},c) - f(r+1,c+1) + \sum_{(r,c)} f(r,c+1) - f(r+1,c)$$

# Prewitt

- One direction is calculated by first-order difference, another is average.
- Compared to Robert is relatively insensitive for noise.

-1		1
-1		1
-1		1

-1	-1	-1
1	1	1

$$\begin{aligned}
 FV = & \sum_{(r,c)} f(r-1,c+1)+f(r,c+1)+f(r+1,c+1) -f(r-1,c-1)-f(r,c-1)-f(r+1,c-1) \\
 & + \sum_{(r,c)} f(r+1,c-1)+f(r+1,c)+f(r+1,c+1) -f(r-1,c-1)-f(r-1,c)-f(r-1,c+1)
 \end{aligned}$$

# Sobel

- Improved from Prewitt. 

1	1
-1	-1

 × 

1	1
1	1
- The nearer pixels have the higher weight.

-1		1	-1	-2	-1
-2		2			
-1		1	1	2	1

$$\begin{aligned}
 FV = & \sum_{(r,c)} f(r-1,c+1) + 2 \times f(r,c+1) + f(r+1,c+1) - f(r-1,c-1) - 2 \times f(r,c-1) - f(r+1,c-1) \\
 & + \sum_{(r,c)} f(r+1,c-1) + 2 \times f(r+1,c) + f(r+1,c+1) - f(r-1,c-1) - 2 \times f(r-1,c) - f(r-1,c+1)
 \end{aligned}$$

# Laplacian

- Derived by second-order difference.

$$f''(x) = f'(x+1) - f'(x) = f(x+2) - 2 \times f(x+1) + f(x)$$

- Only use without noise.

	1	
1	-4	1
	1	

 or 

1	1	1
1	-8	1
1	1	1

$$FV = \sum_{(r,c)} f(r,c+1) + f(r+1,c) + f(r,c-1) + f(r-1,c) - 4 \times f(r,c)$$

# Focus Value Curve

- Robert
- Prewitt
- Sobel
- Laplacian
- Test

# Focus Formula

1	
	-1

+

	1
-1	

**Robert**

-1	-1	-1
1	1	1

+

-1		1
-1		1
-1		1

**Prewitt**

-1	-2	-1
1	2	1

+

-1		1
-2		2
-1		1

**Sobel**

	1	
1	-4	1
	1	

<sup>2</sup>

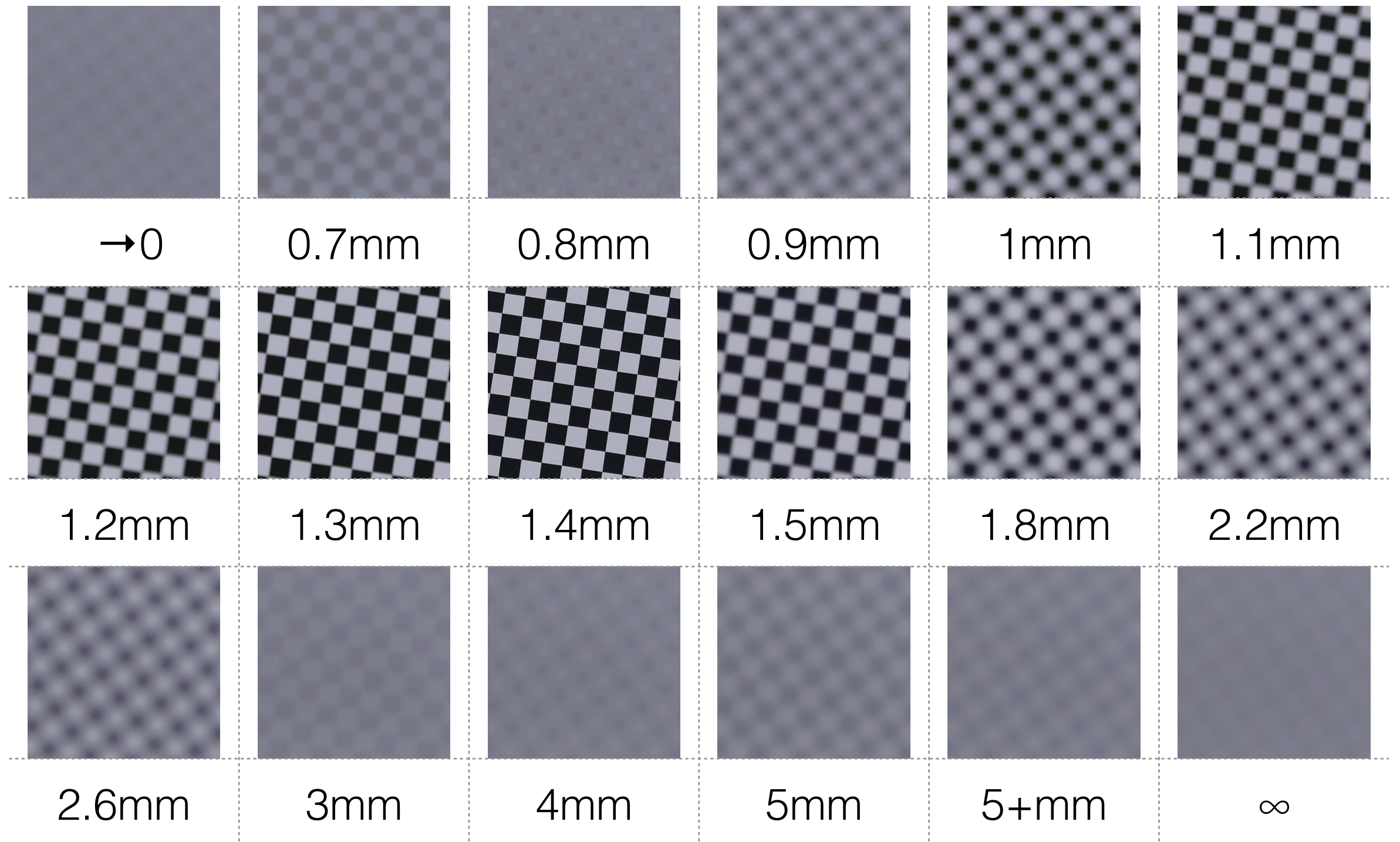
**Laplacian**

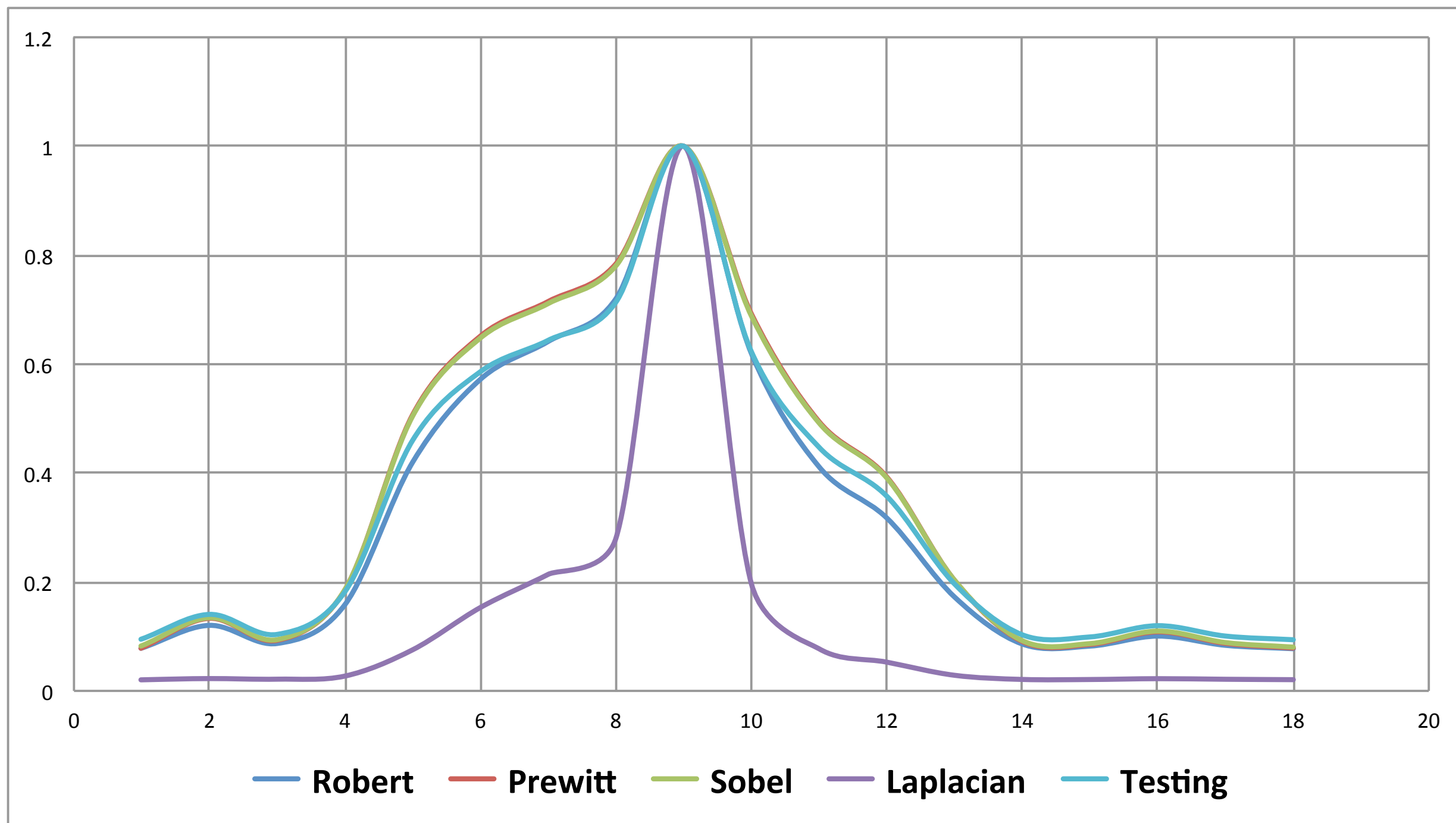
	a	
b	c	d
	e	

**$1a - c1 + 1b - c1 + 1d - c1 + 1e - c1$**



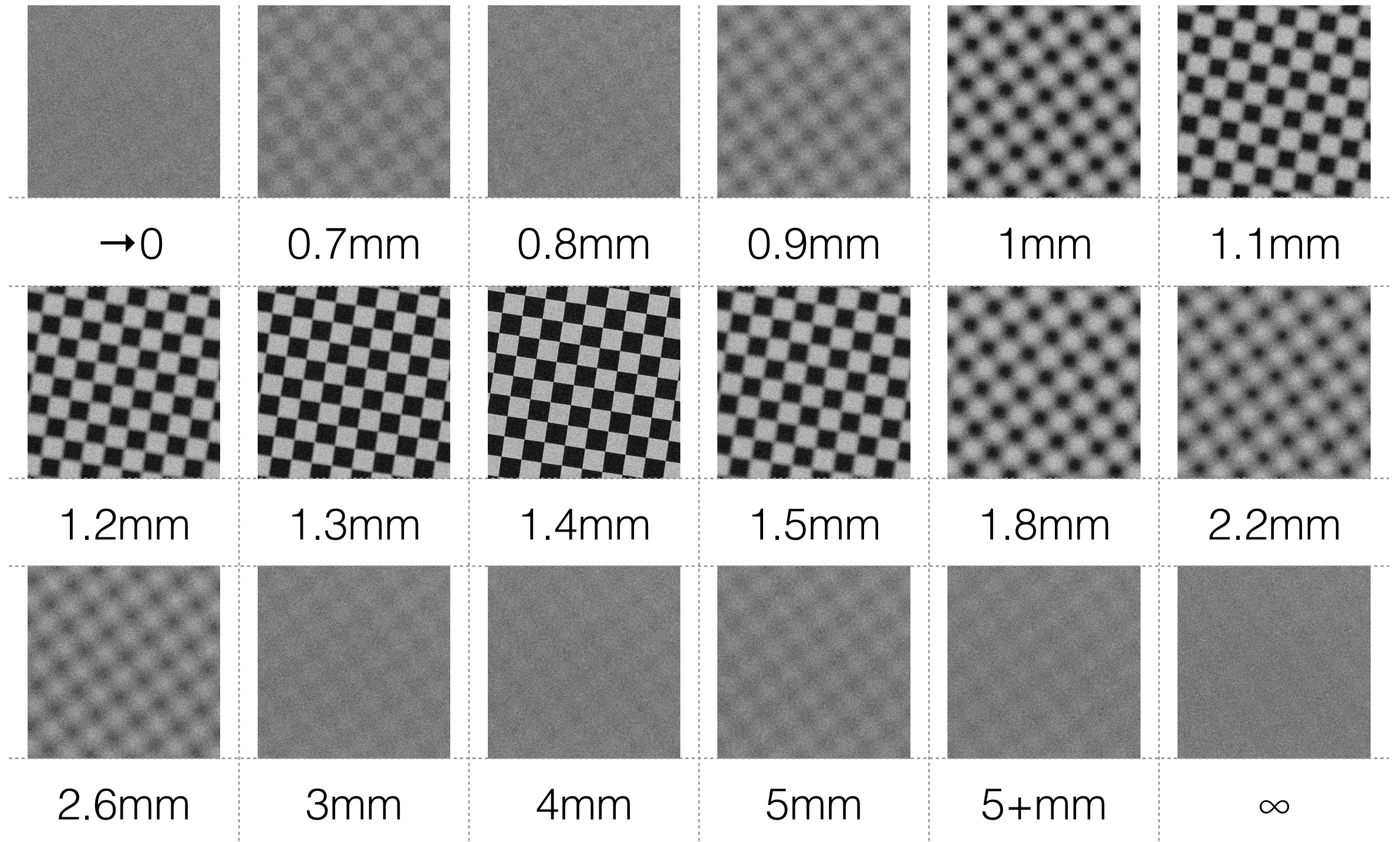
# 500x500 pixels

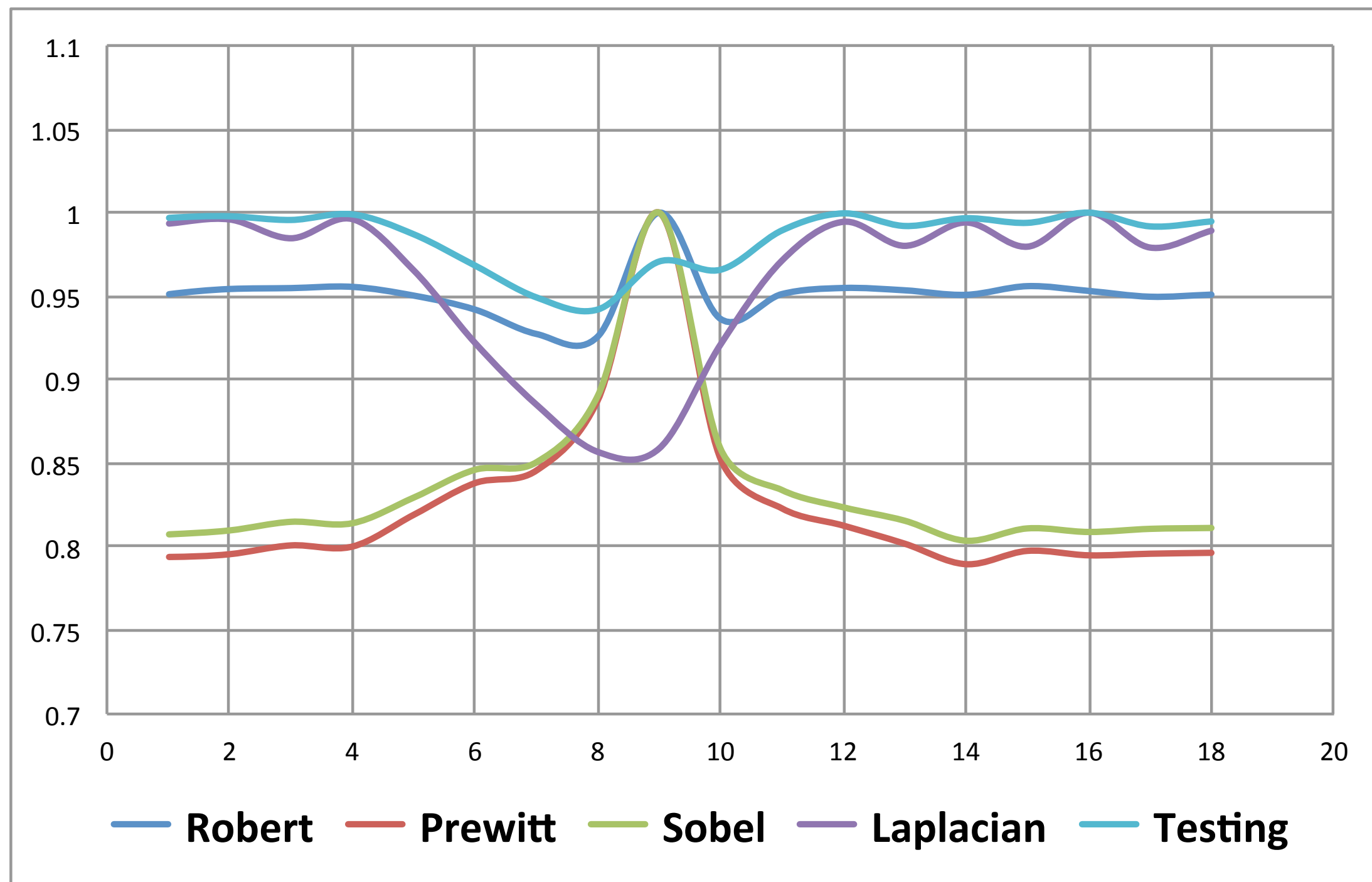




Original Image 500x500 pixels

# Add Gaussian Noise

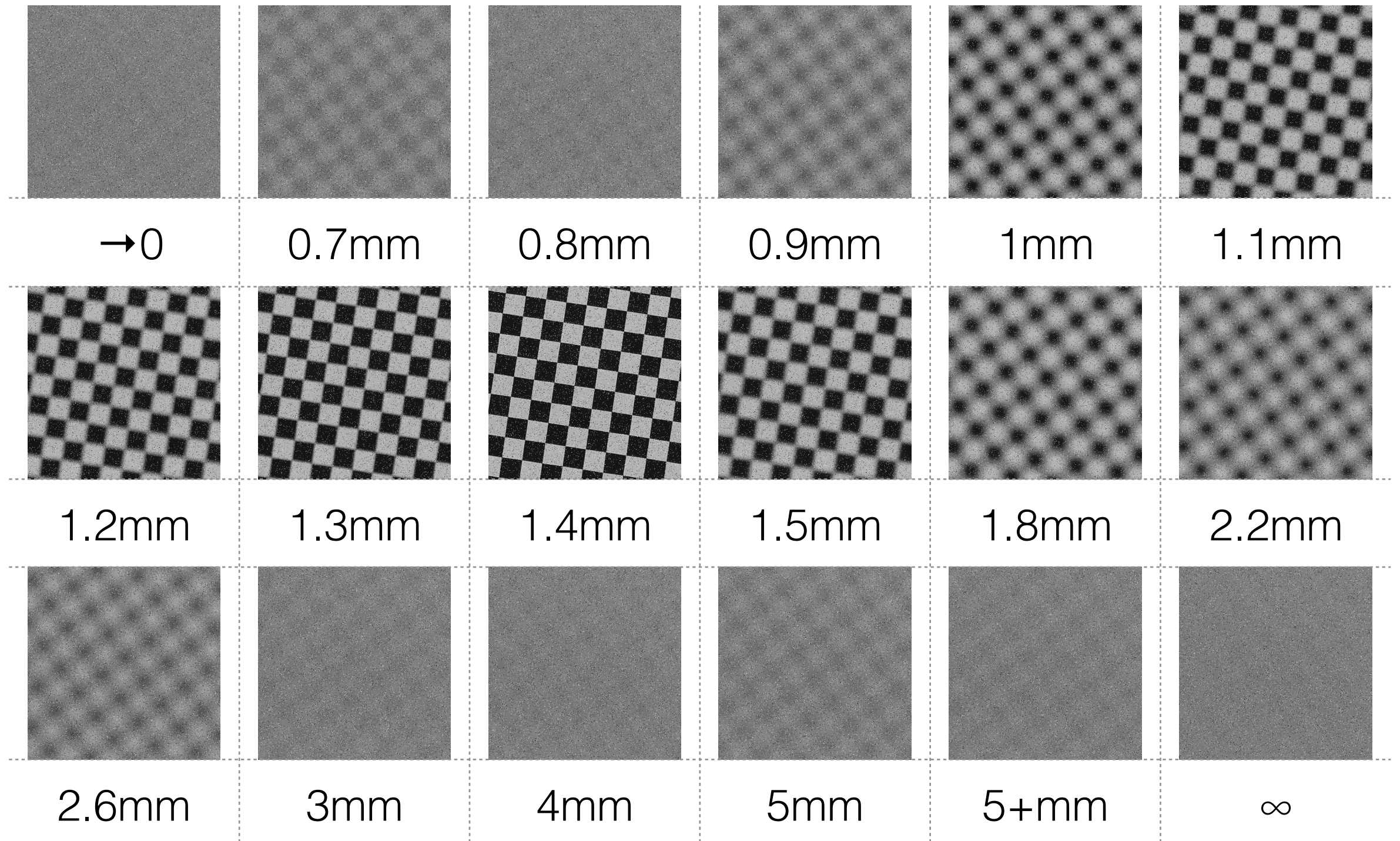


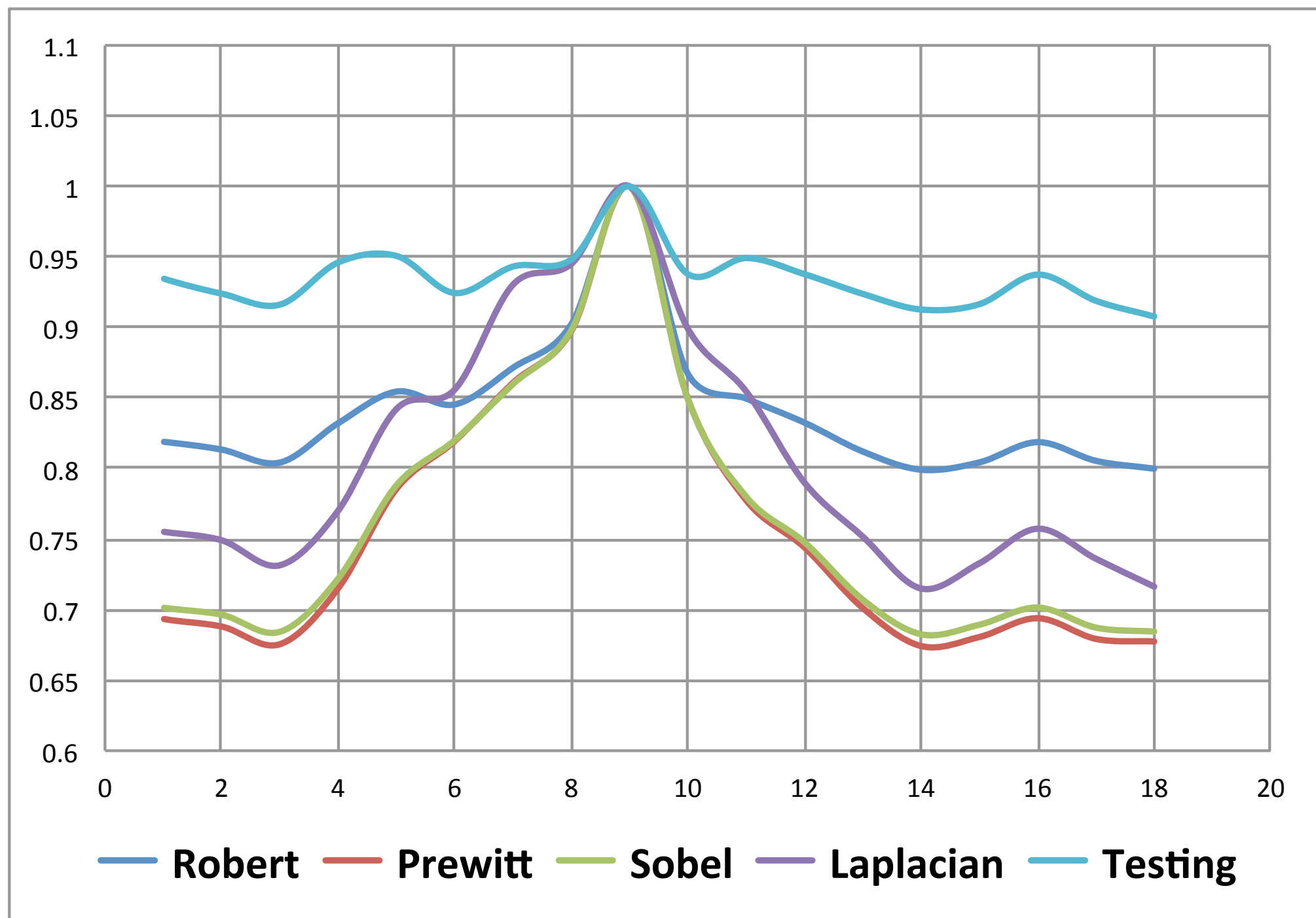


Add Gaussian Noise



# Add Salt and Pepper Noise (5%)



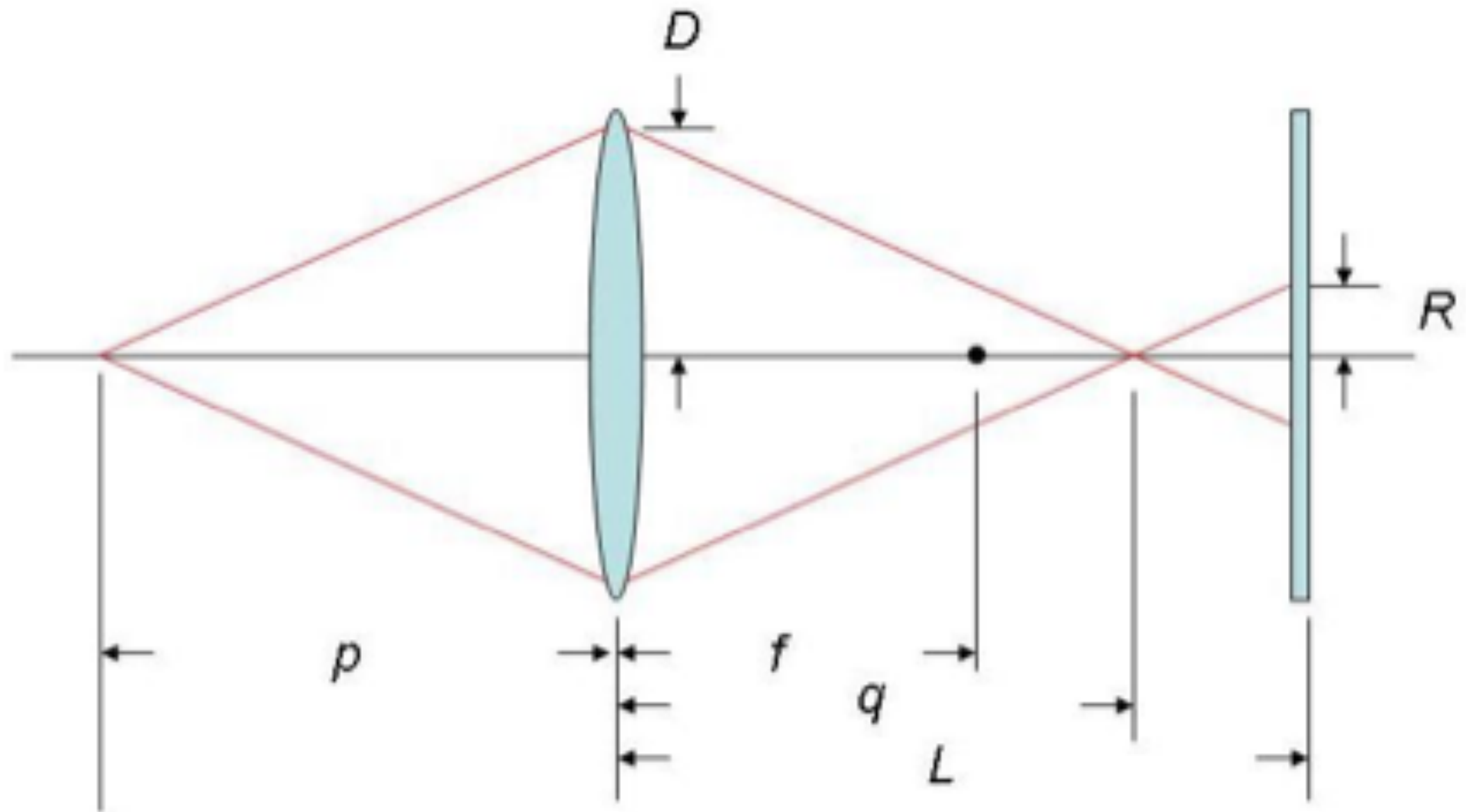


Add Salt and Pepper Noise (5%)



# Curve Fitting

$$FV = \frac{c_1}{k + |x - x_0|^2}$$



$R$ : Blur Circle Radius  
 $D$ : Aperture Length  
 $p$ : Object

$q$ : Focused Points  
 $f$ : Focus Length  
 $L$ : Distance between Lens  
 and Image Detector

$$FV = \frac{c_1}{k + |x - x_0|^2},$$

where

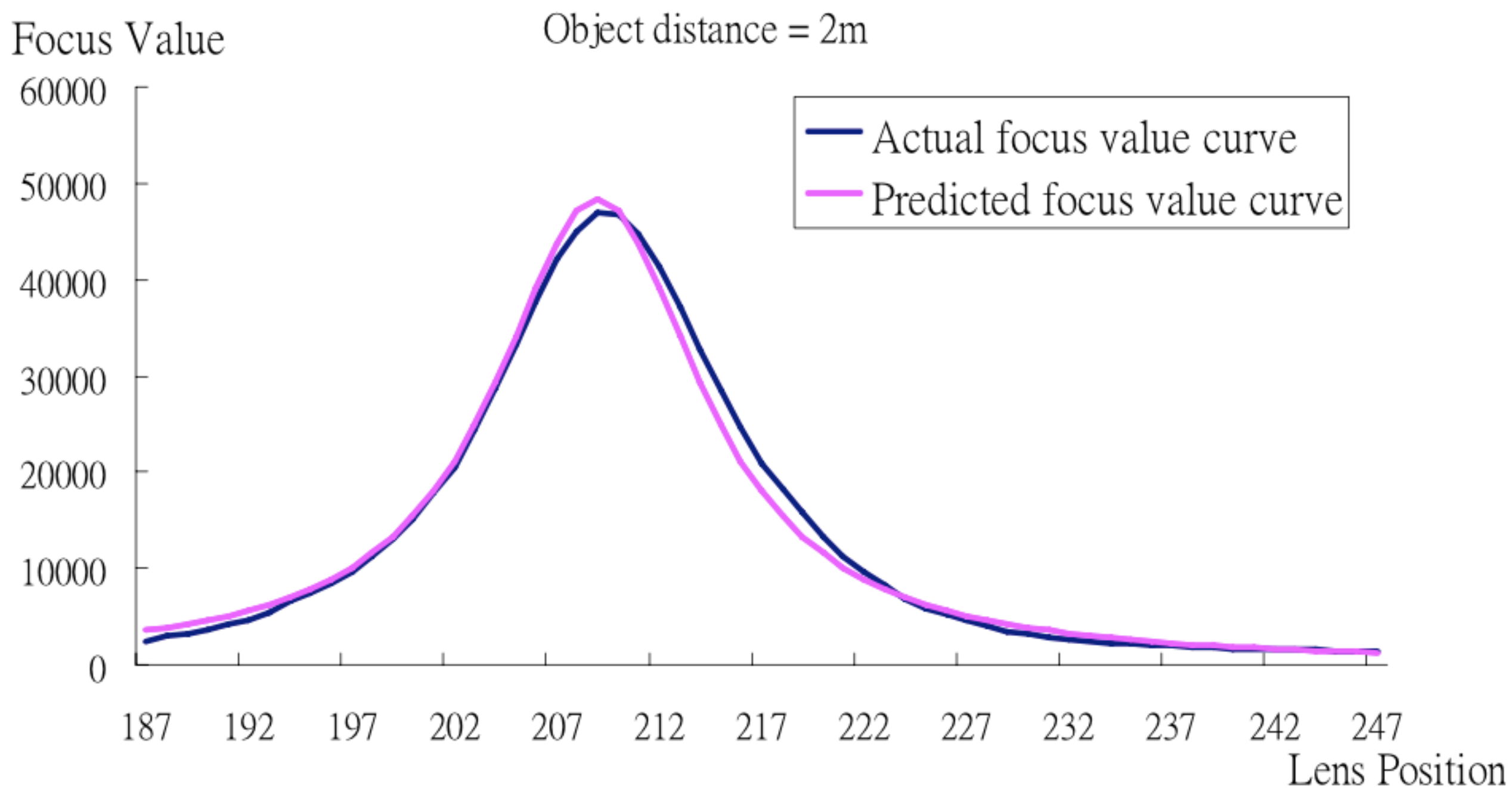
$c_1$ : a constant to fit parameter  $(\frac{q^2}{D^2})$

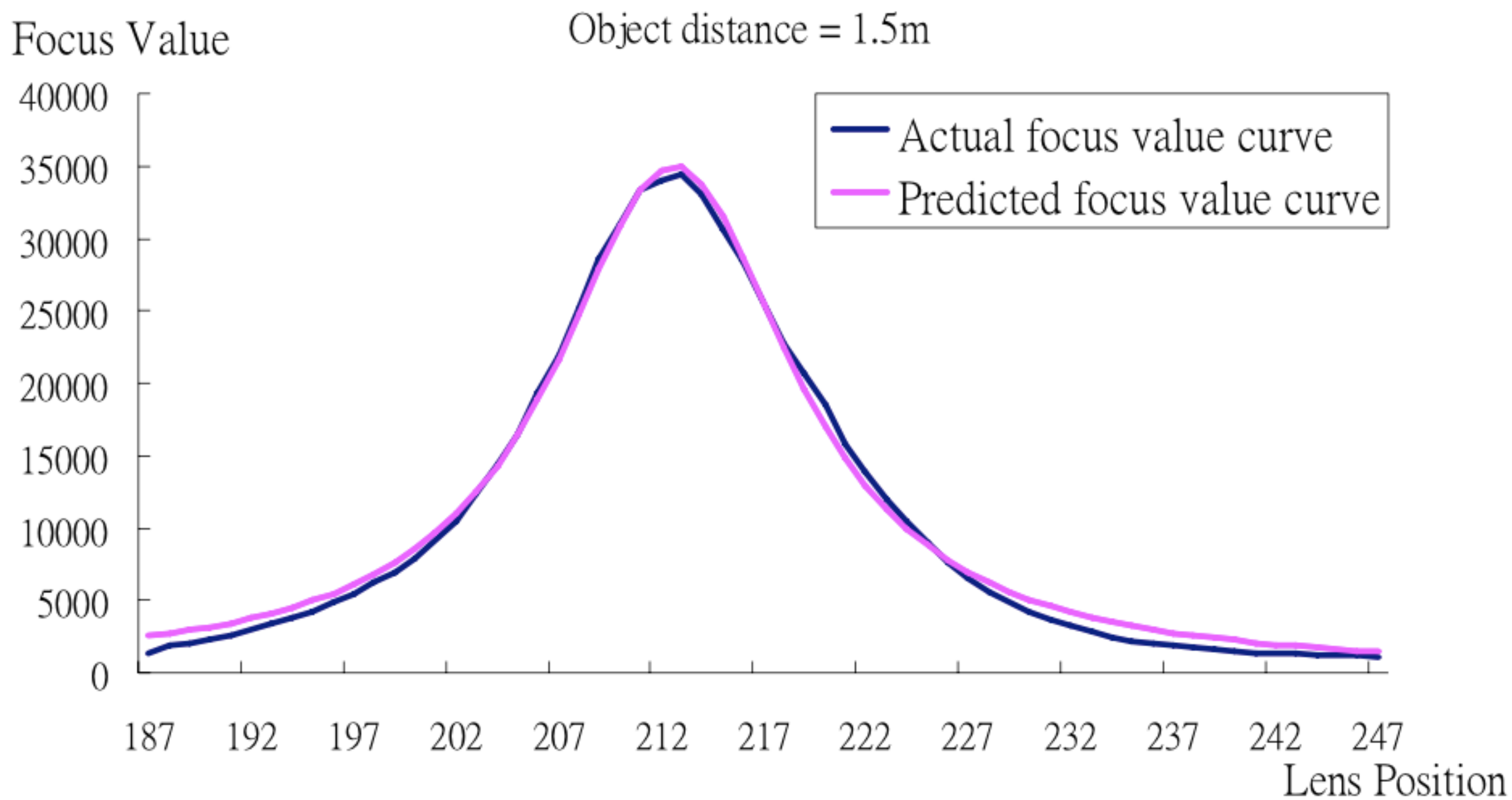
$x$ : to fit the lens position ( $L$ )

$x_0$ : to fit the best-focused lens position ( $q$ )

$k$ : a constant denoting minimum radius of CoC

CoC: Circle of Confusion





# Spatial Frequency Response

MTF: Modulation Transfer Function

熊育萱

bear8039@gmail.com

0935334132



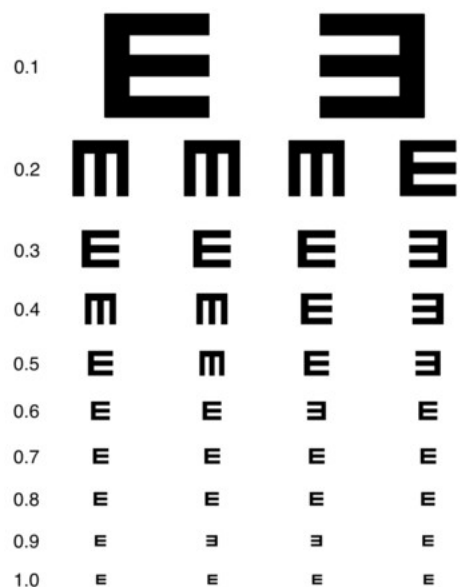
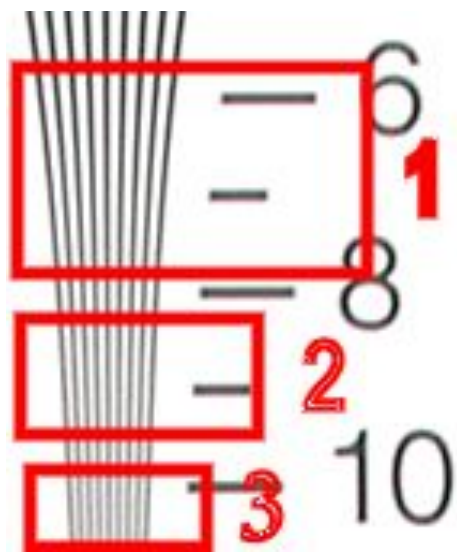
# Resolution Test

- Most important test part of digital imaging: “resolution” and “color.”
- Resolution test means that a measure is calculated at the transition point of image from clear to blurred. Limited to optical material and other factors, every shot and digital camera has a resolution limit.
- Resolution test uses scientific methods to calculate the resolution limit.

# Modulation Transfer Function

- MTF is the oldest method used by most people.
- The main idea of MTF is to use contrast to test the lens resolution. Users have to understand "spatial frequency."
- Spatial frequency: how often sinusoidal components of the structure repeat per unit of distance.

# Spatial Frequency



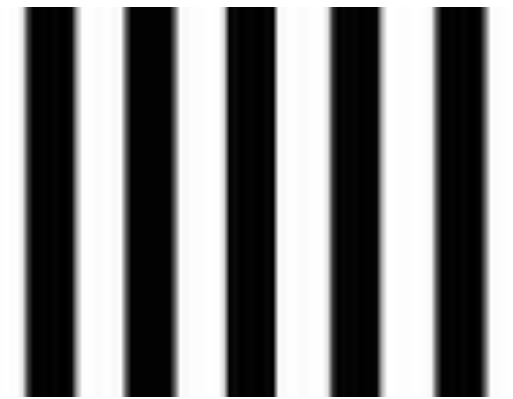
- Originally, sufficient contrast can easily identify the two lines.
- When the spatial frequency increases, that is, when the lines lie more closely, the contrast is gradually reduced.
- Finally, attenuation contrast to all turned gray, no longer distinguish between black and white stripes to, it means that the resolution of the lens has been to the limit.

# Contrast

Spatial  
frequency

**small**

[ 1 ]



100% of the contrast ratio, it may occur only under ideal conditions.

[ 2 ]



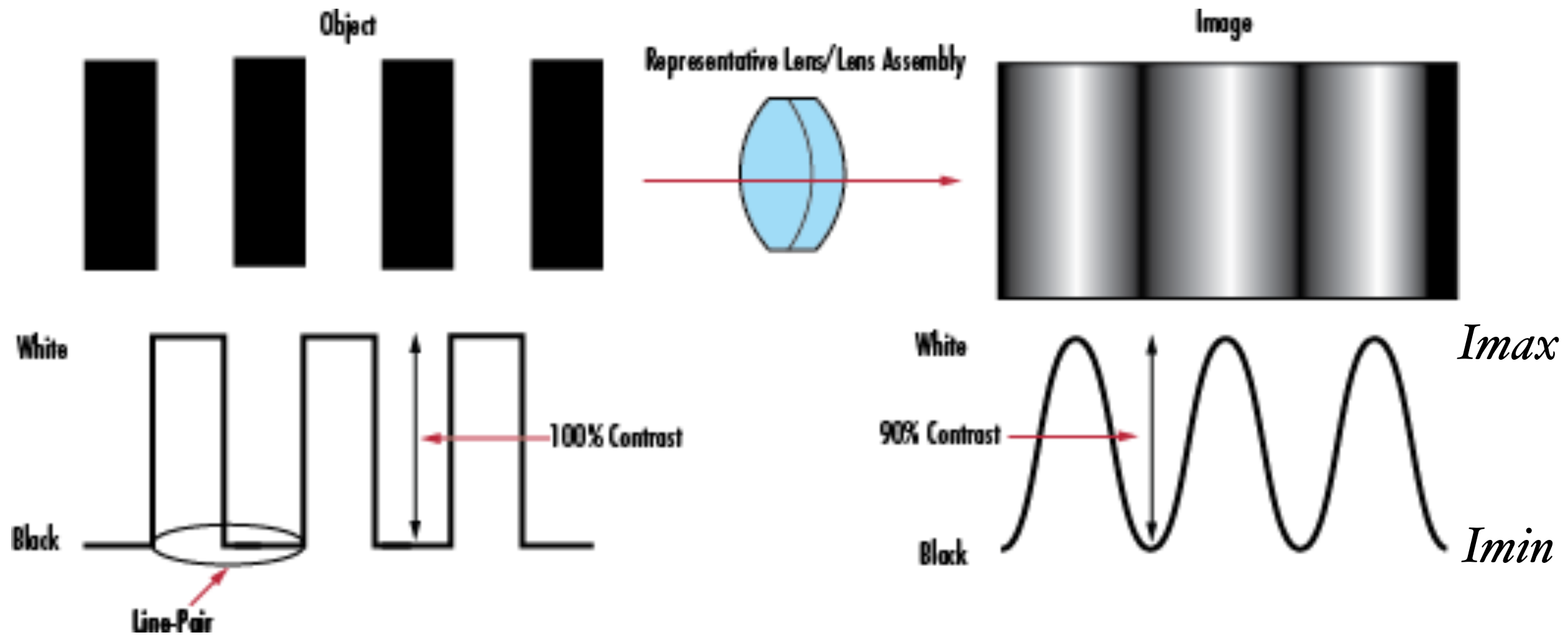
Resolution is poorer, but the contrast acceptable.

**large**

[ 3 ]

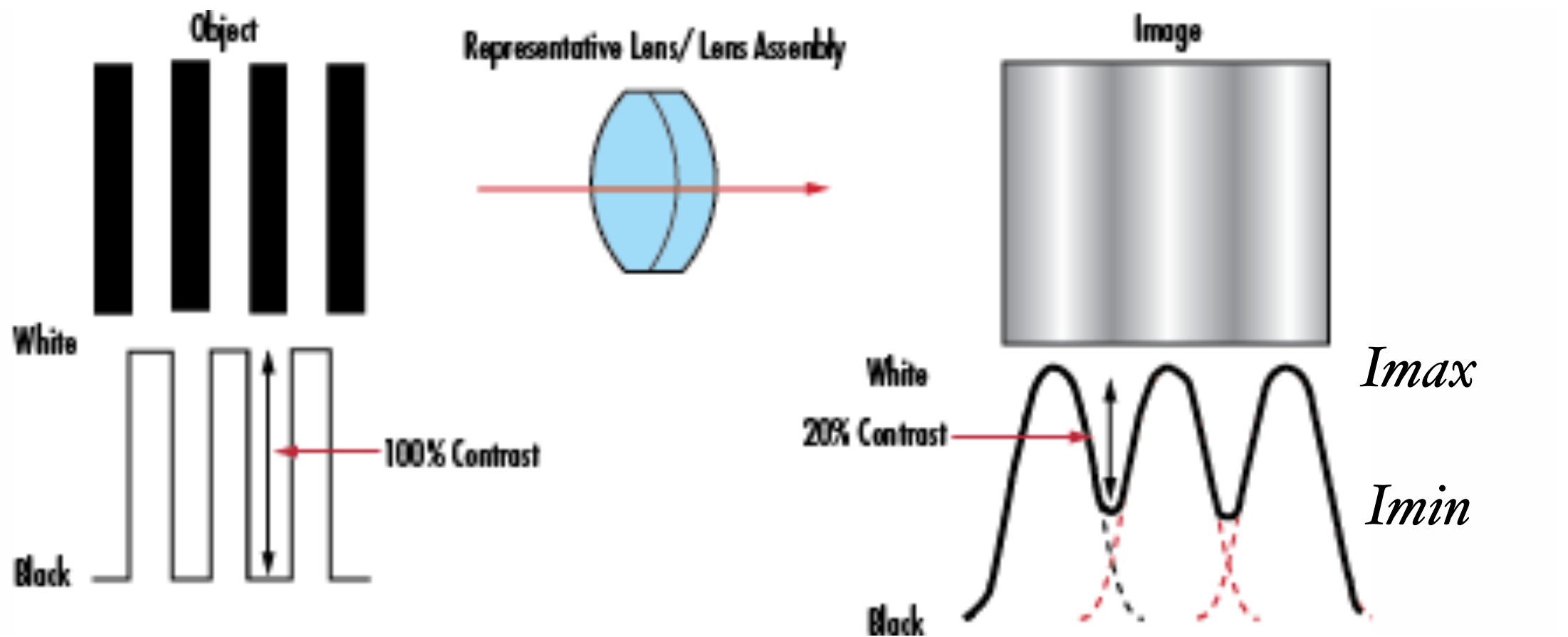


Both Resolution and contrast can not compare. (Lens has reached the limit.)



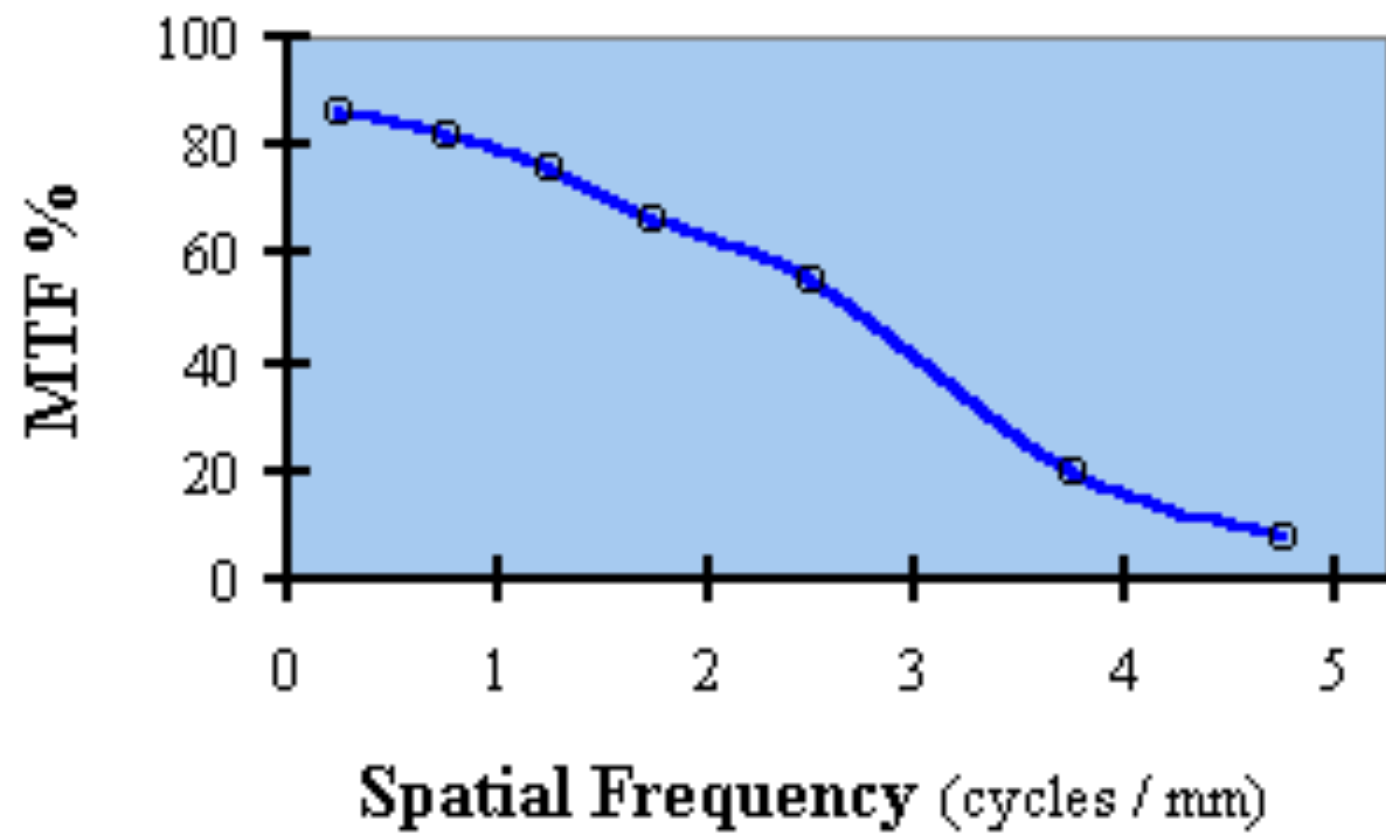
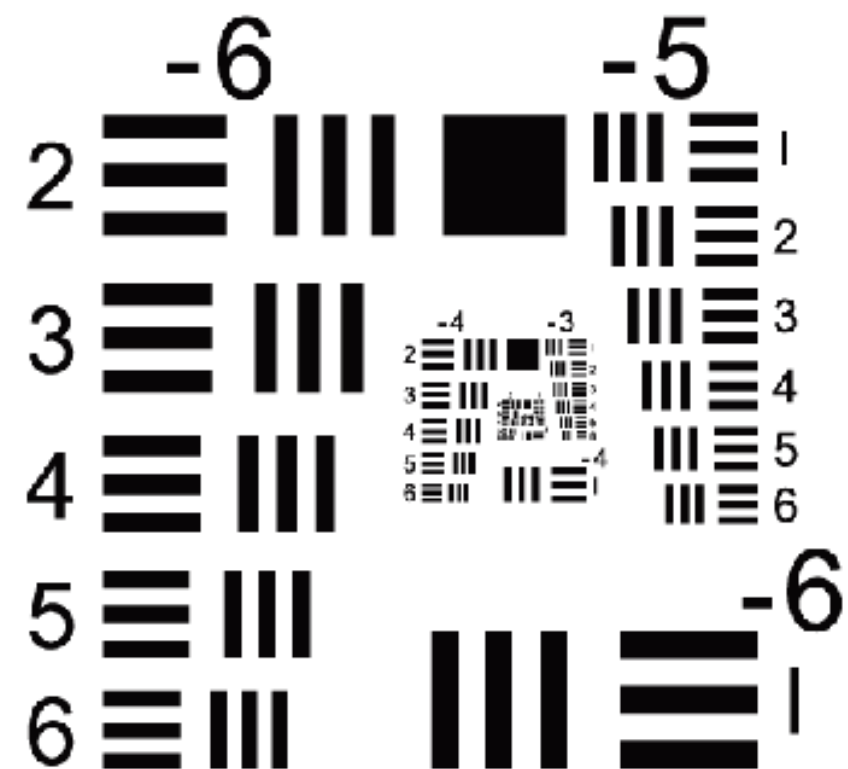
$$\text{Contrast} = \frac{I_{max} - I_{min}}{I_{max} + I_{min}}$$

$$\text{MTF} = \frac{\text{ContrastOut}}{\text{ContrastIn}}$$



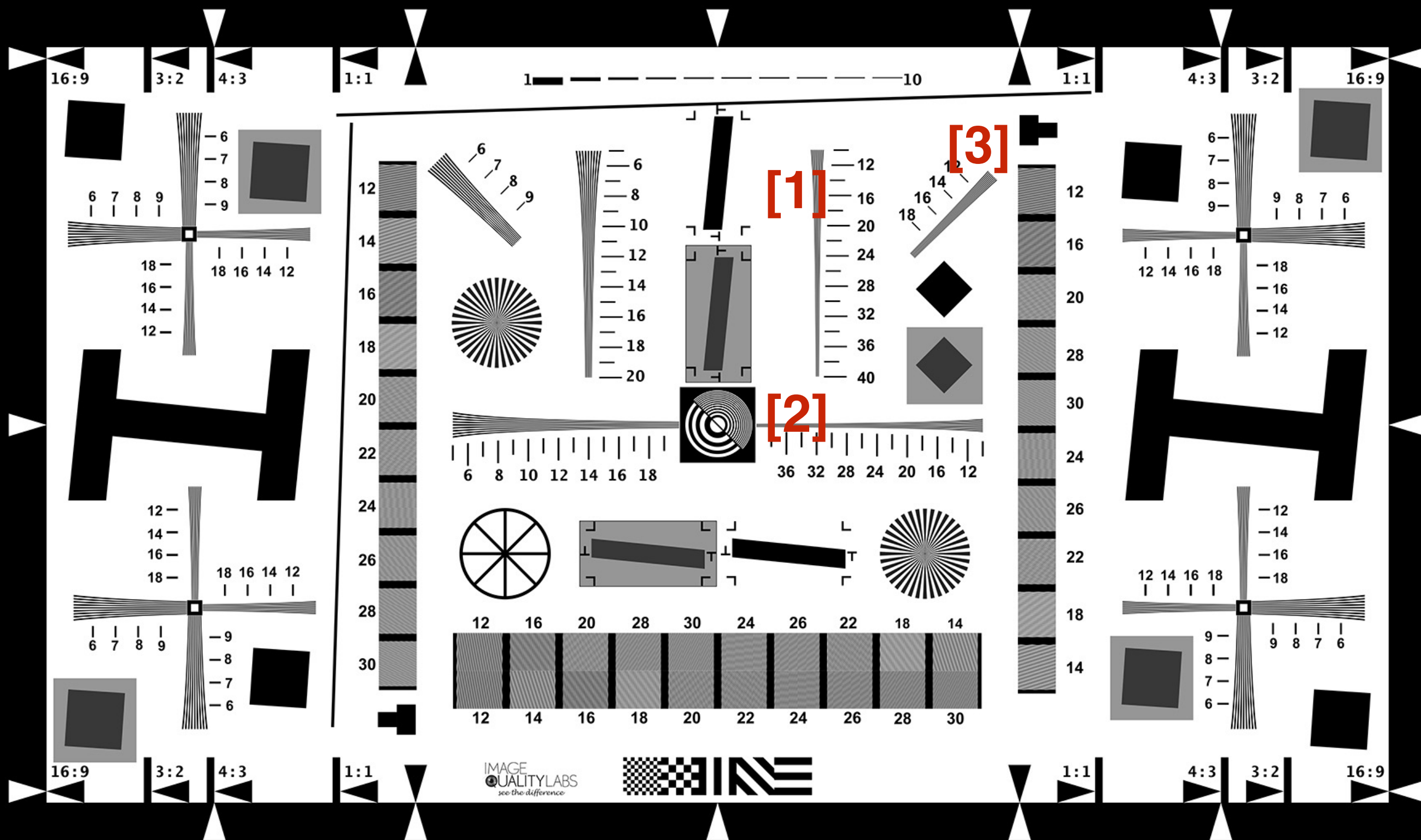
$$\text{Contrast} = \frac{I_{max} - I_{min}}{I_{max} + I_{min}}$$

$$\text{MTF} = \frac{\text{ContrastOut}}{\text{ContrastIn}}$$



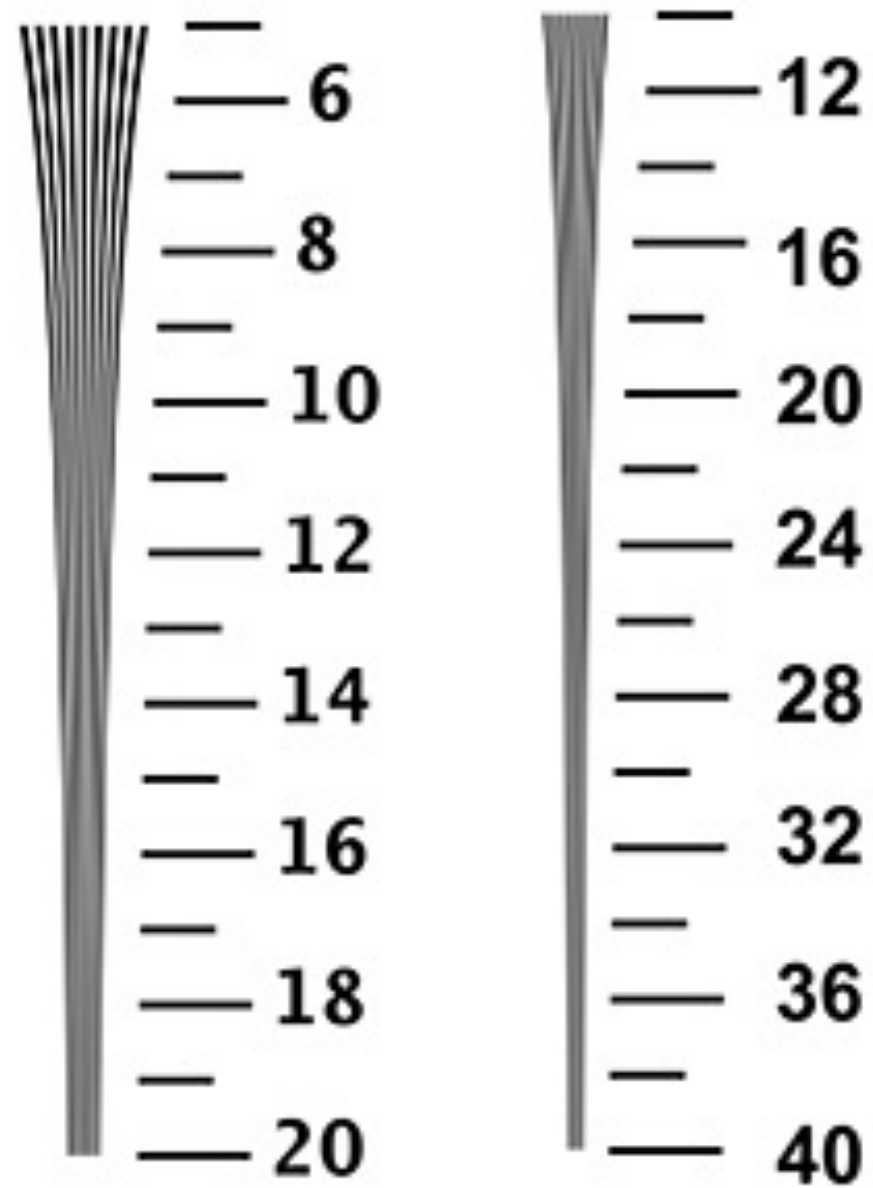
# PIMA / ISO 12233

VALUES IN 100X LINES PER PICTURE HEIGHT

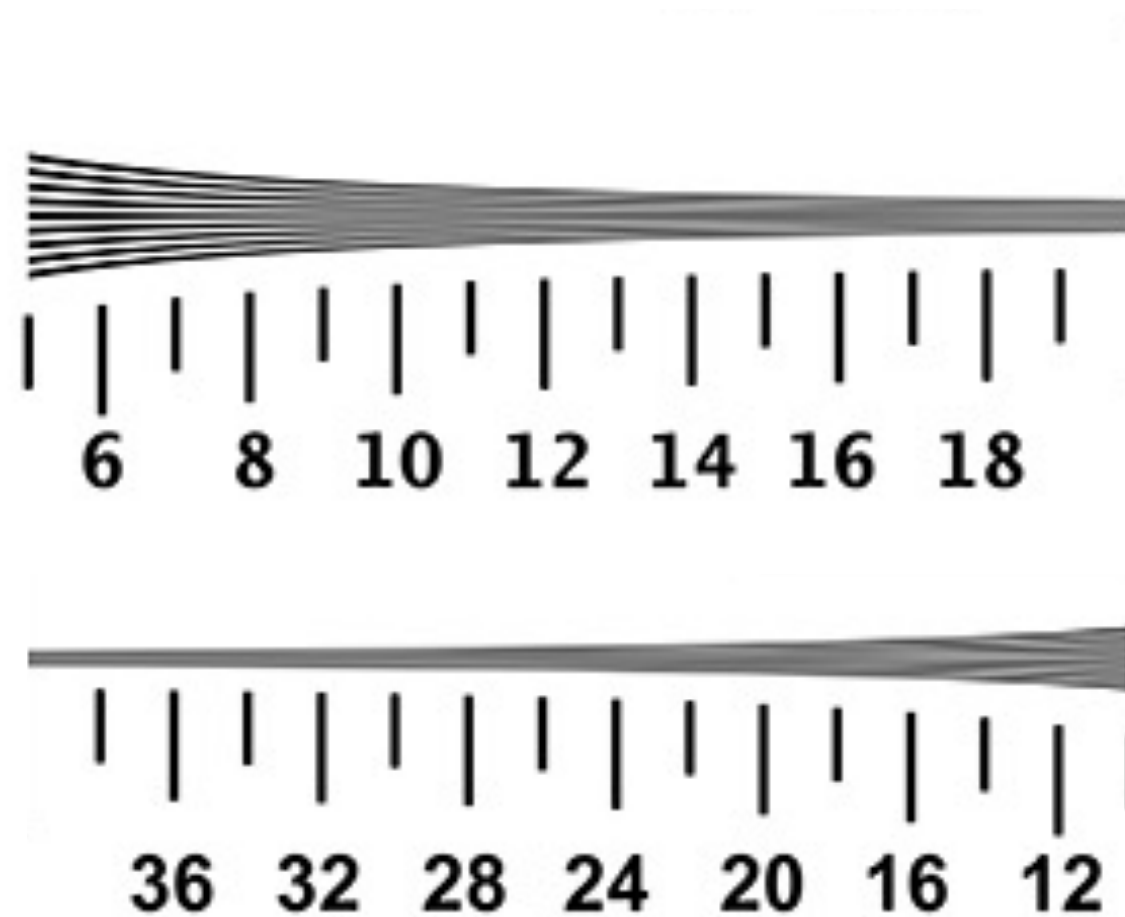


ISO: International Standards Organization  
PIMA: Photographic and Imaging Manufacturers Association

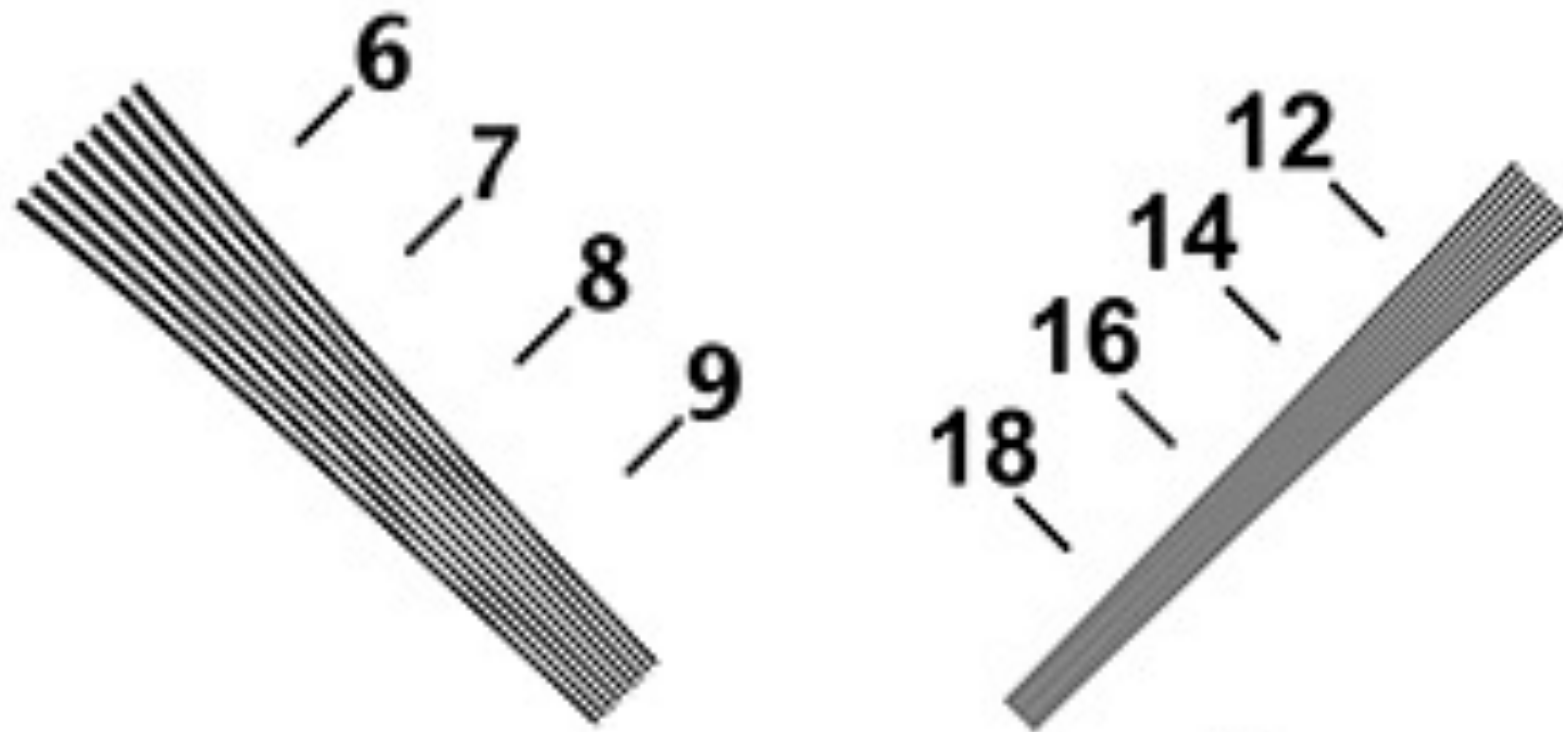




**[1] Vertical Resolution**



**[2] Horizontal Resolution**

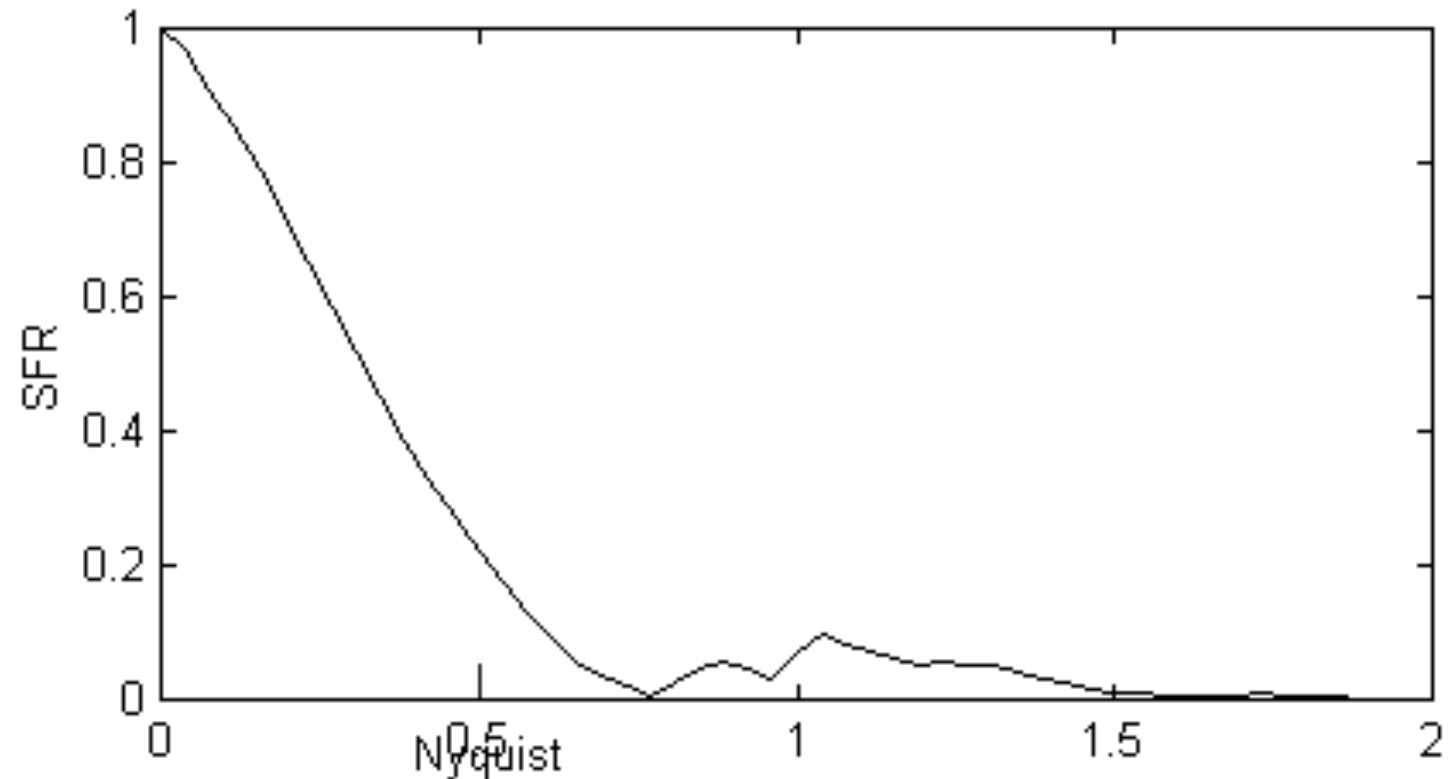
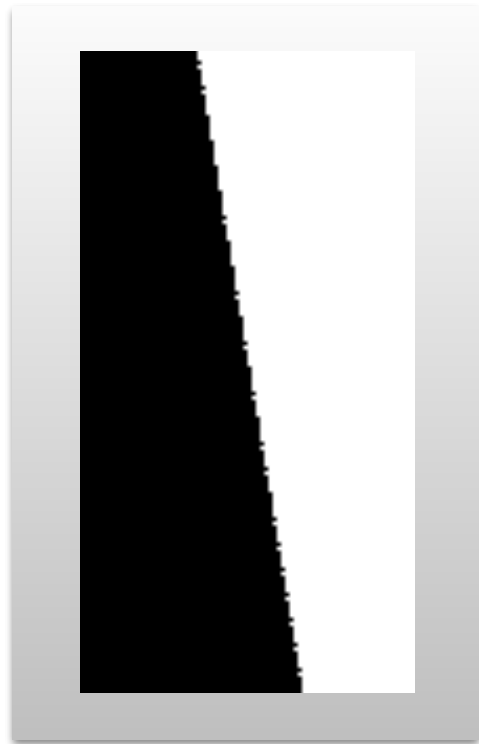


**[3] Diagonal Resolution**

# Spatial Frequency Response

- SFR is simplified version of MTF.
- MTF requires expensive sinusoidal patterns, and needs to convert large amounts of data. Therefore, PIMA developed this low-cost SFR as a substitute.
- SFR is mainly used to measure the spatial frequency and increases lines of a single image of the impact.

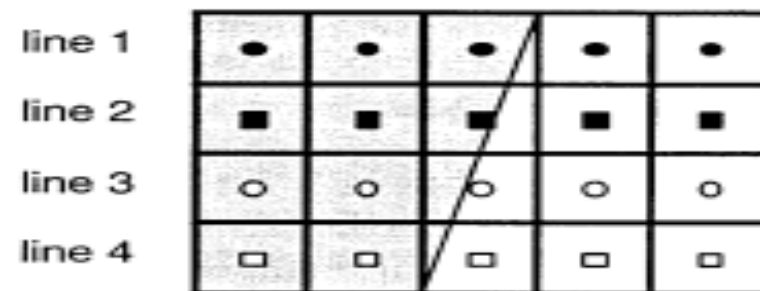
# Spatial Frequency Response



- SFR only needs one black and white slanted-edge, then can convert a value roughly equivalent to the MTF.

# Flowchart

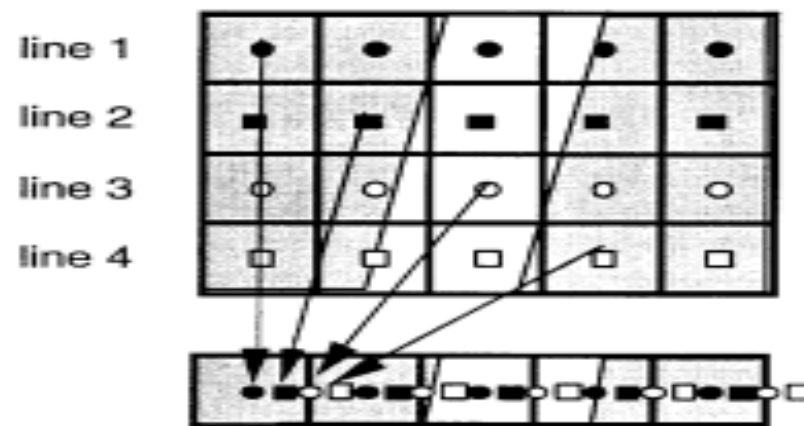
1) Digital image from camera, converted to a linear (reflectance) quantization characteristic.



2) Differentiate using discrete derivative



3) Calculate the best-fit line to the centroids of the first derivatives.



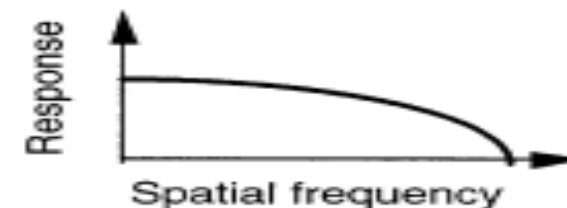
4) Create a single "composite" line by shifting the differentiated image data from lines 2,3, etc. by an amount calculated using the best-fit line and "binning" the data into four bins. Use an equal number of lines at each relative sampling phase, and delete any remaining lines at the bottom.



5) To reduce noise effects, window the curve using a Hamming window.

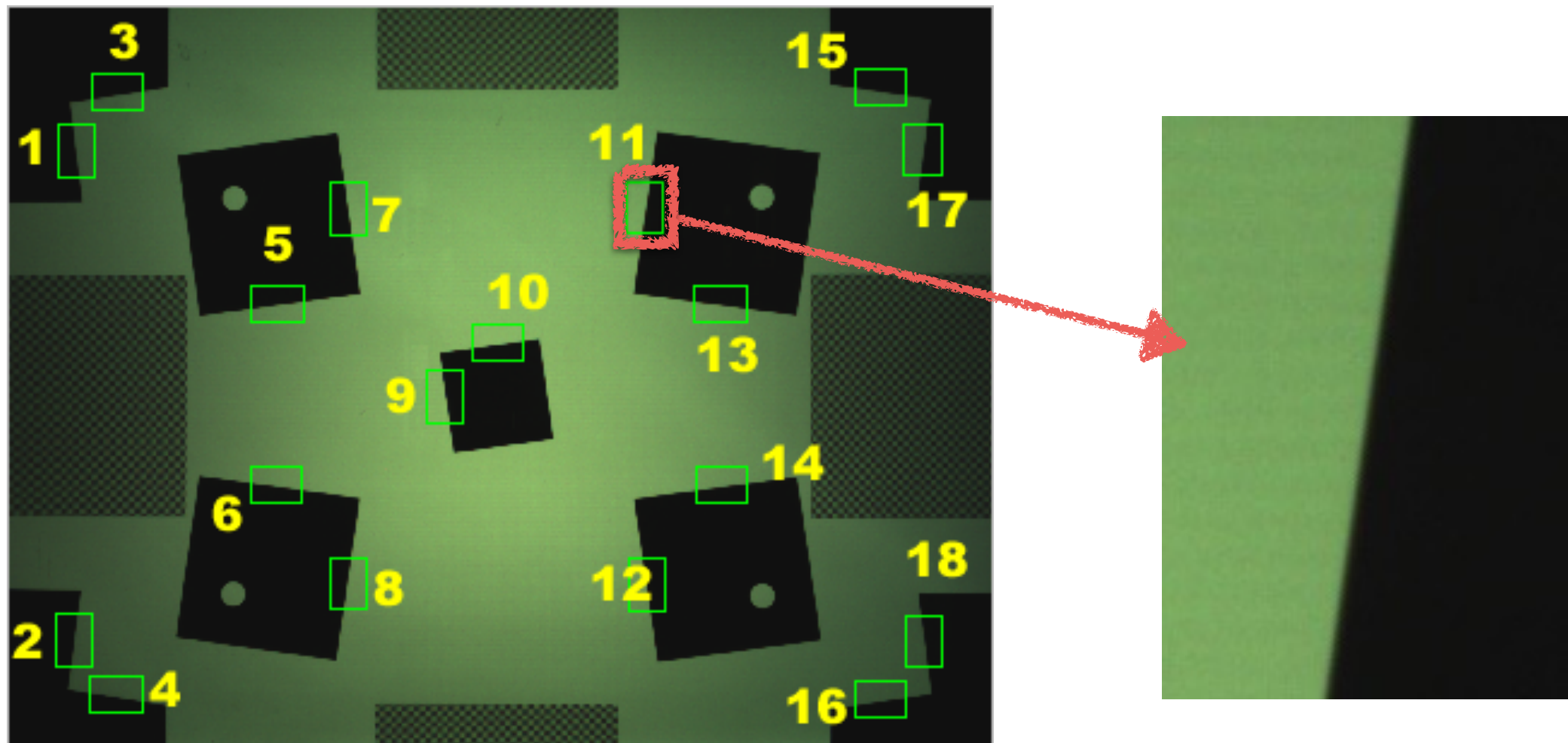


6) Calculate the Fourier transform of the windowed line spread curve.



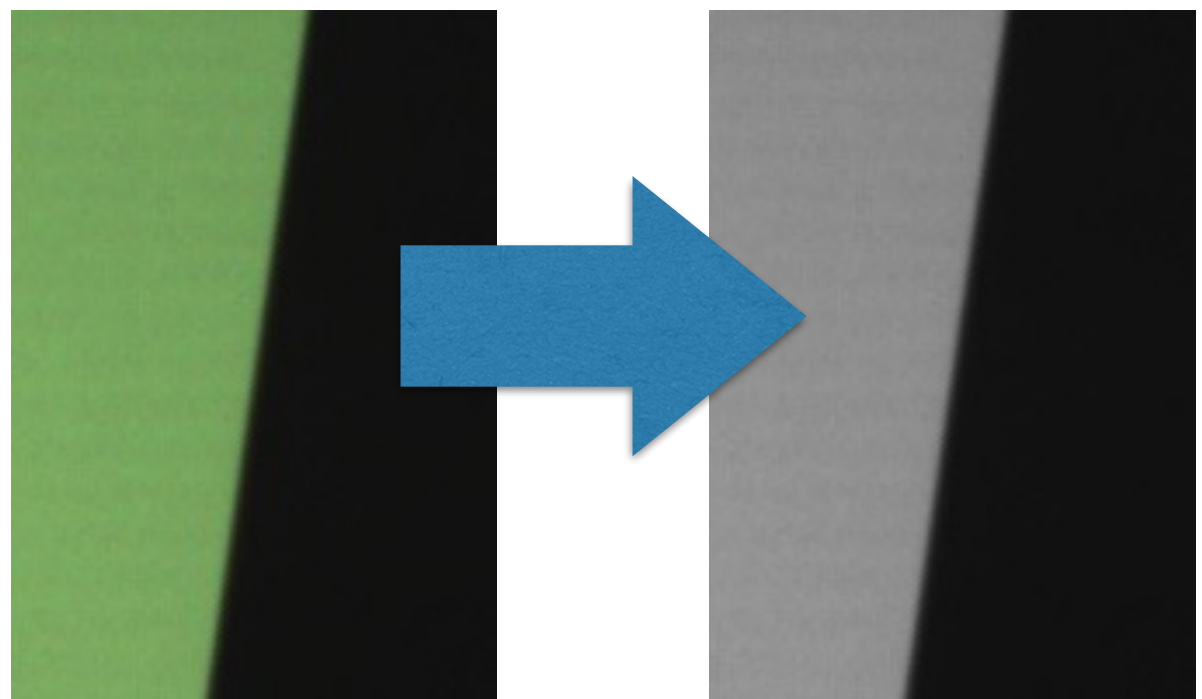
# Enter ROI

- Slanted-edge: Top-down, white to black



# RGB to Gray

- $\text{Gray} = R \cdot 0.299 + G \cdot 0.587 + B \cdot 0.114$
- Reduced 50% brightness
- Brightness between left and right must be at least 20% difference



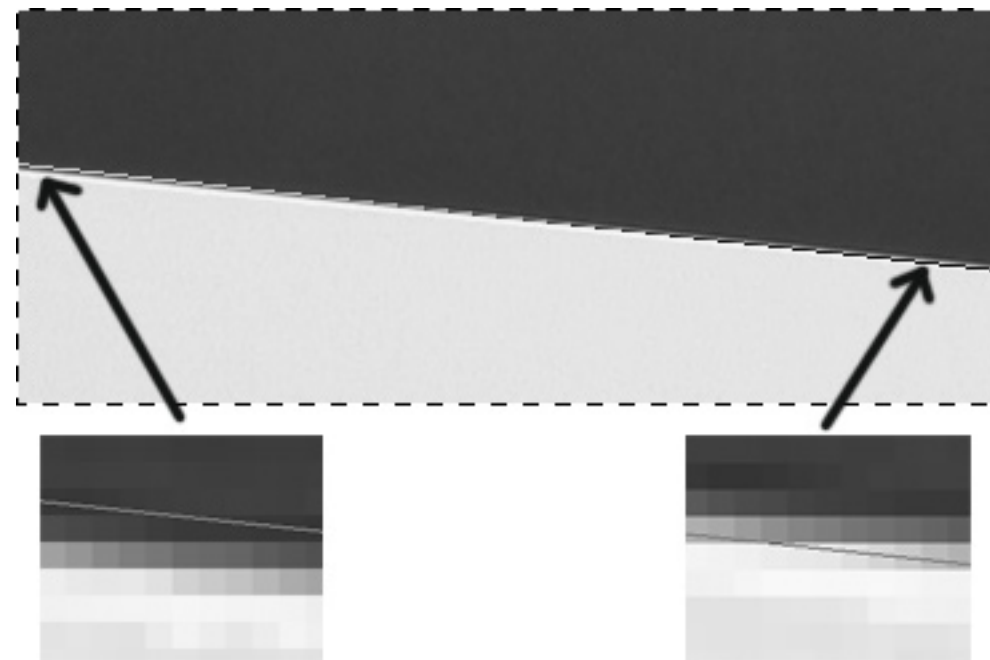


# Edge Detection and Align

- Minimizing edge detection errors is most critical for getting sensible results. It's the first step, and the most important too.
- The edge is usually detected by analyzing the line spread function for each pixel line. ISO 12233 mentions the use of the finite-difference schemes  $[-1, 0, 1]$  and  $[-1, 1]$ .

# Edge Detection and Align

- Edge detection errors may spoil the test results not only when "bad" images are tested, but even in very common cases



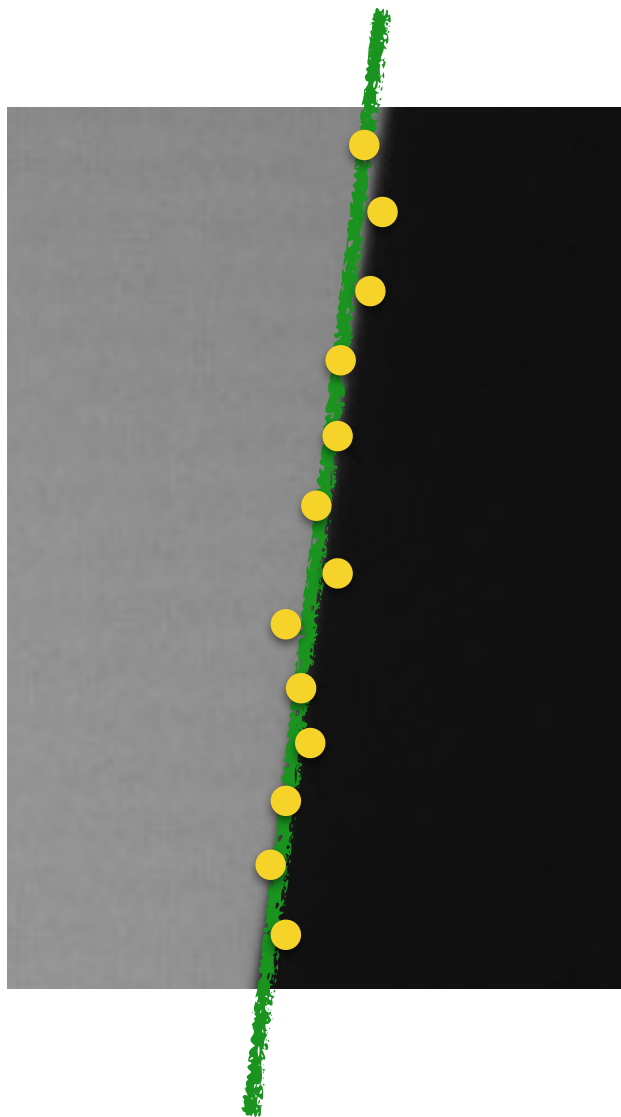
- ❑ An example of a slope calculation error when finding "pure" centroids.  
In this case, the results are meaningless.

# Edge Detection and Align

- Three options for edge detection:
  1. Centroid
  2. Centroid + Hamming
  3. Intensity based

# Edge Detection and Align

- Edge detector:  $[1 \ 0 \ -1]$

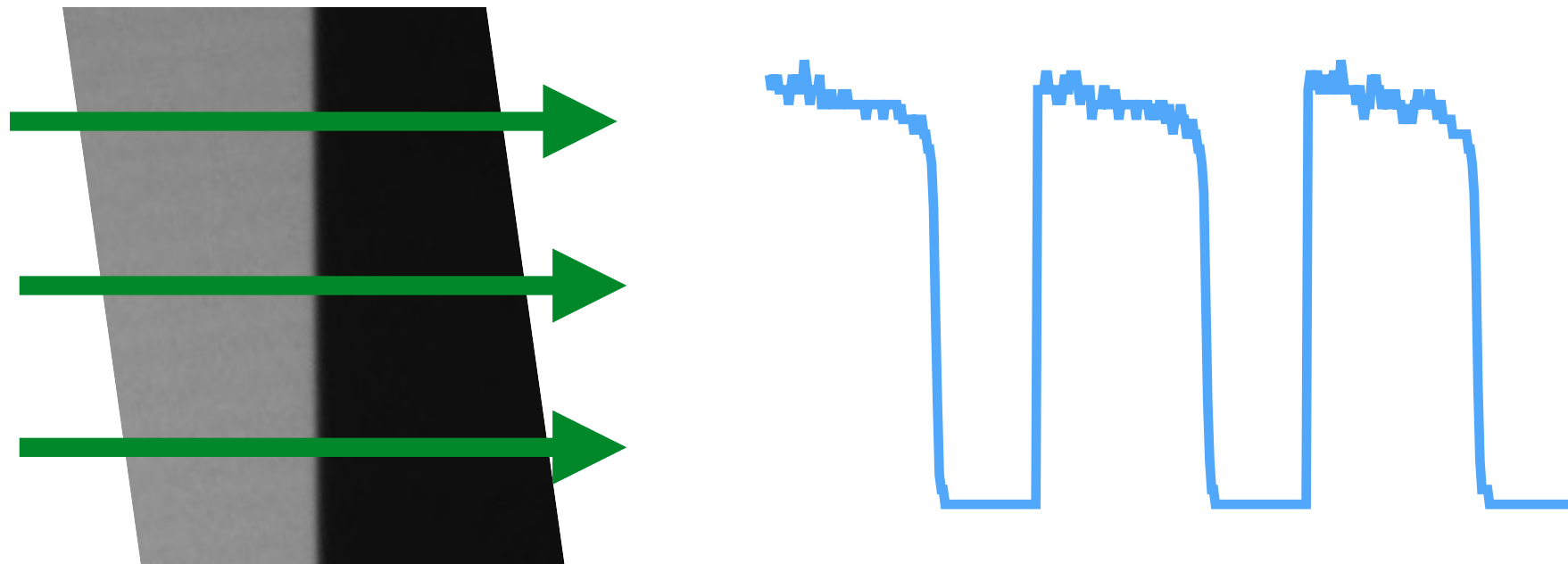


$$slope = \frac{\sum_{i=1}^n [(x_i - \bar{x}) \times (y_i - \bar{y})]}{\sum_{i=1}^n (x_i - \bar{x})^2}$$

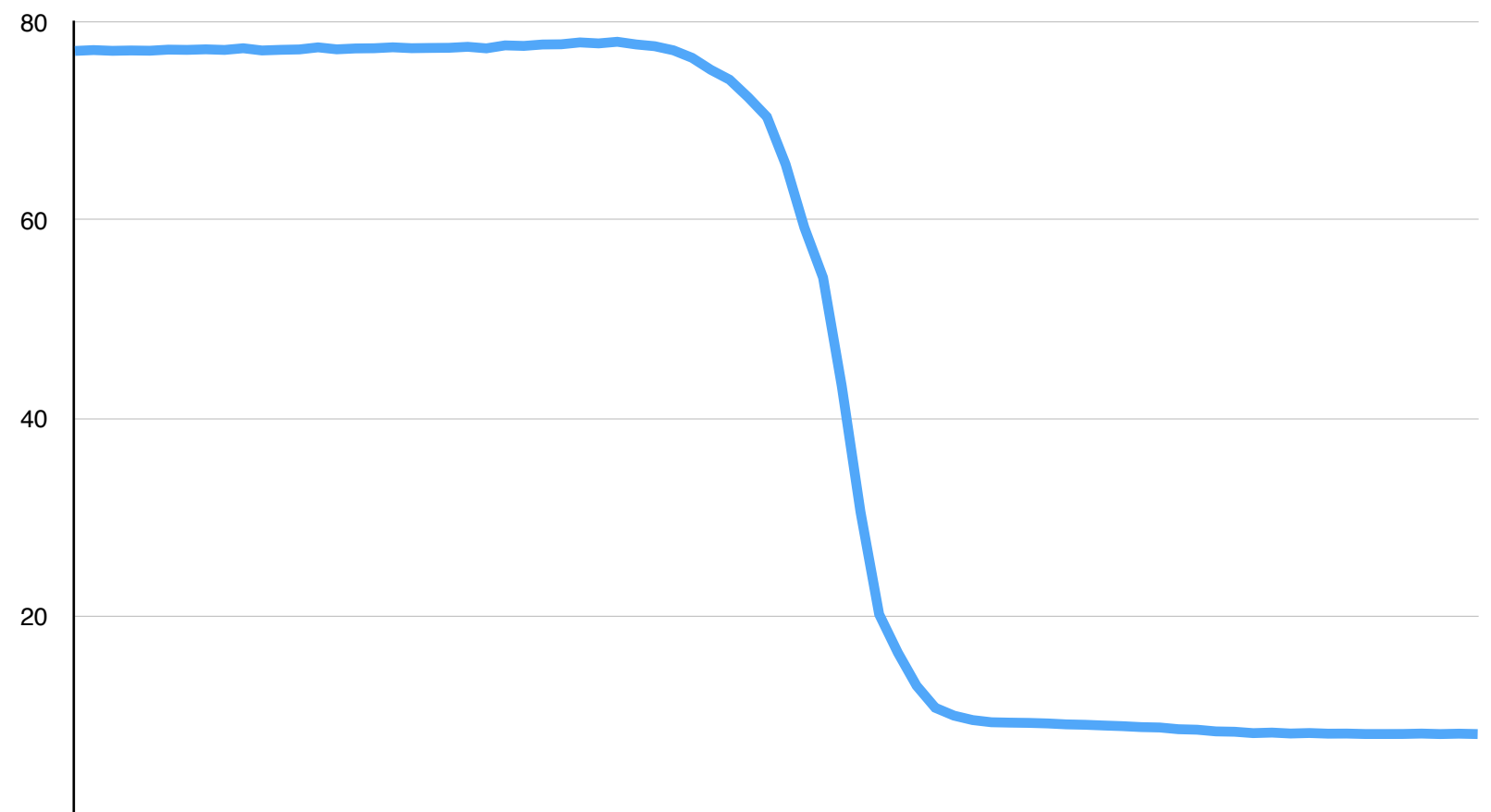
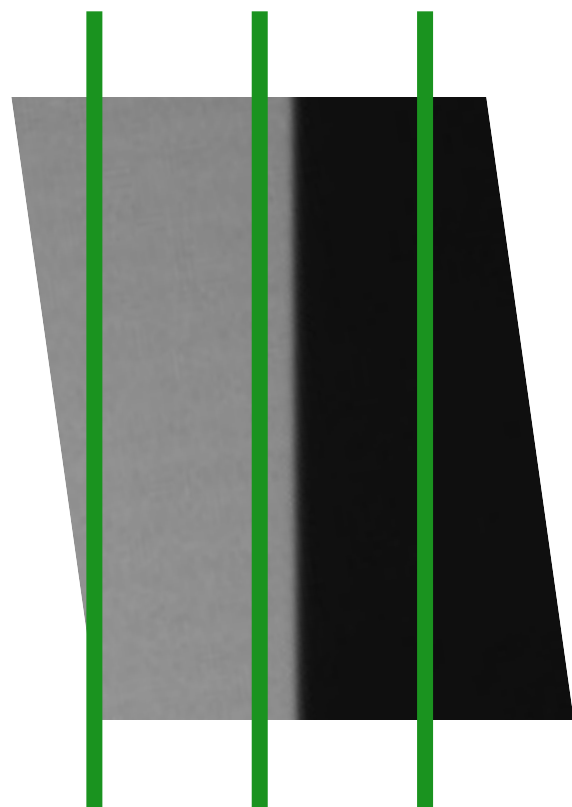
$$intercept = \bar{y} - slope \times \bar{x}$$

# Edge Spread Function

- At this step, the intensities for all lines are accumulated and averaged, with taking the displacement of the edge into consideration.



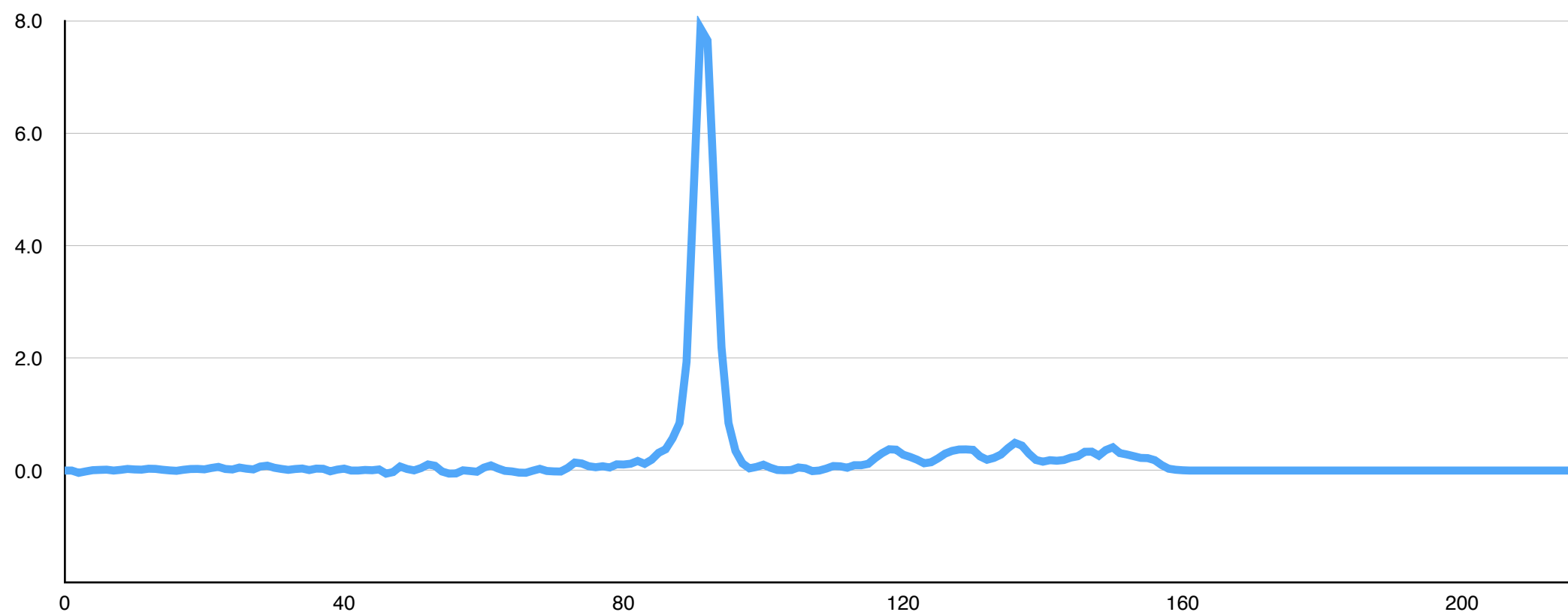
# Edge Spread Function



□ Average intensity of each column

# Line Spread Function

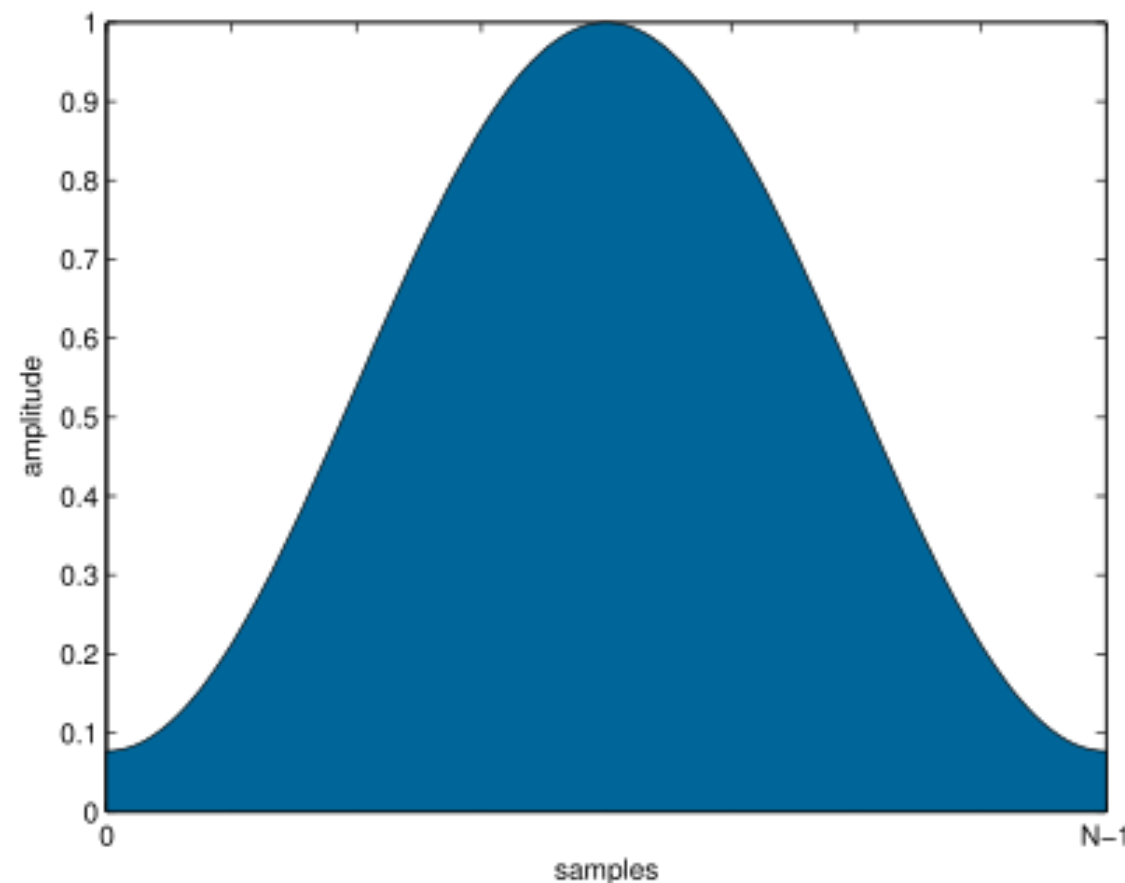
- LSF is the first derivative of ESF by  $[-1 \ 0 \ 1]$ .
- Two difference schemes:  $[-1, 0, 1]$  and  $[-1, 1]$ .





# Hamming Window

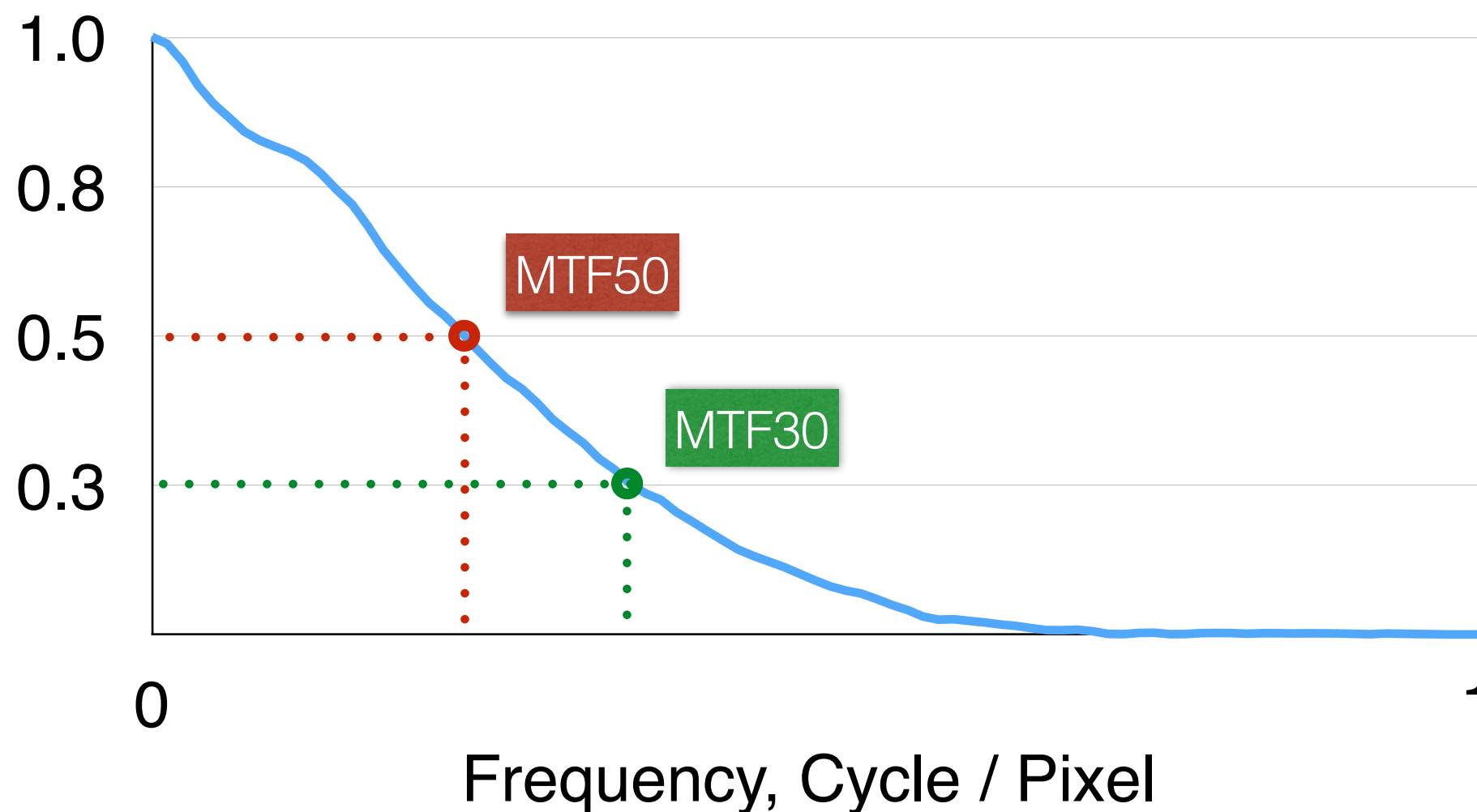
- After the LSF is calculated, the Hamming window is applied to the LSF.



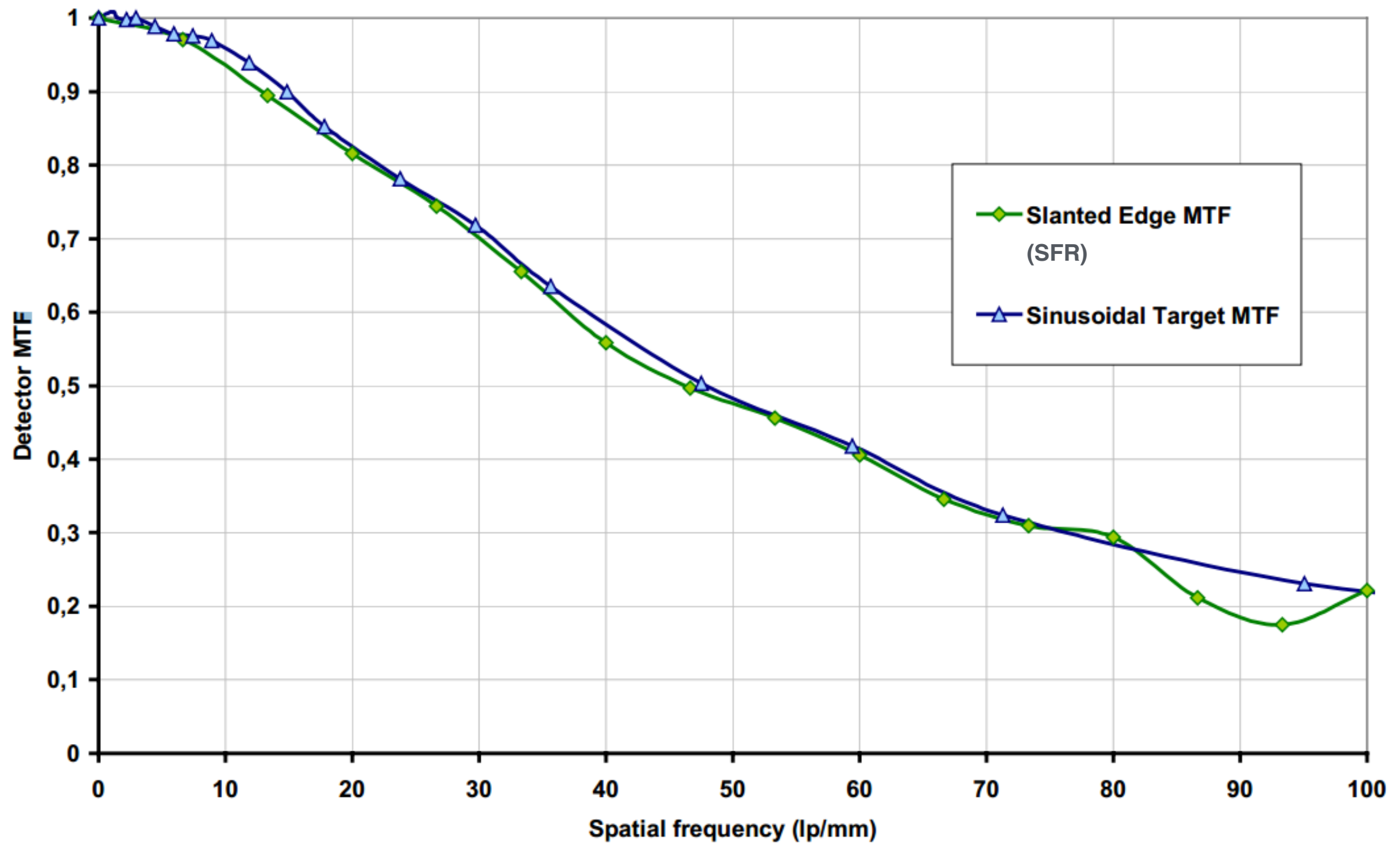
$$\square \quad w(n) = 0.53836 - 0.46164 \cos\left(\frac{2\pi n}{N-1}\right)$$

# Discrete Fourier Transform

- The SFR is an absolute value of the Fourier transform of the LSF.



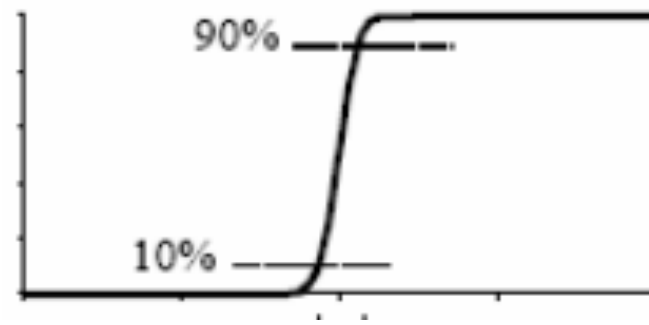
# SFR vs MTF



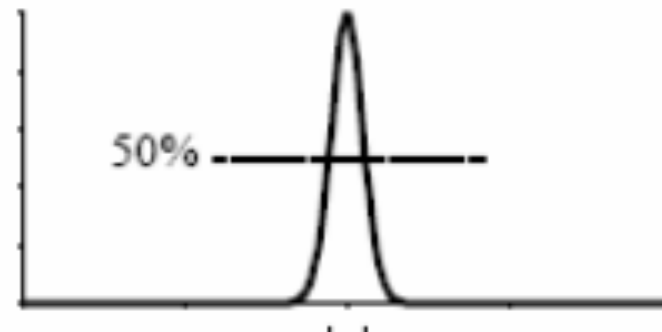
# Smooth

- ESF Avg  
[0.1, 0.1, 0.1, 0.1, 0.1, 0.1, 0.1, 0.1, 0.1, 0.1]

- ESF 10%~90%



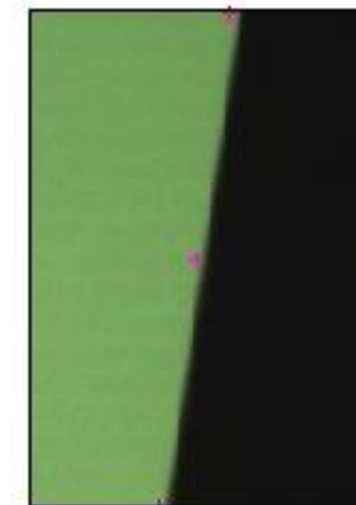
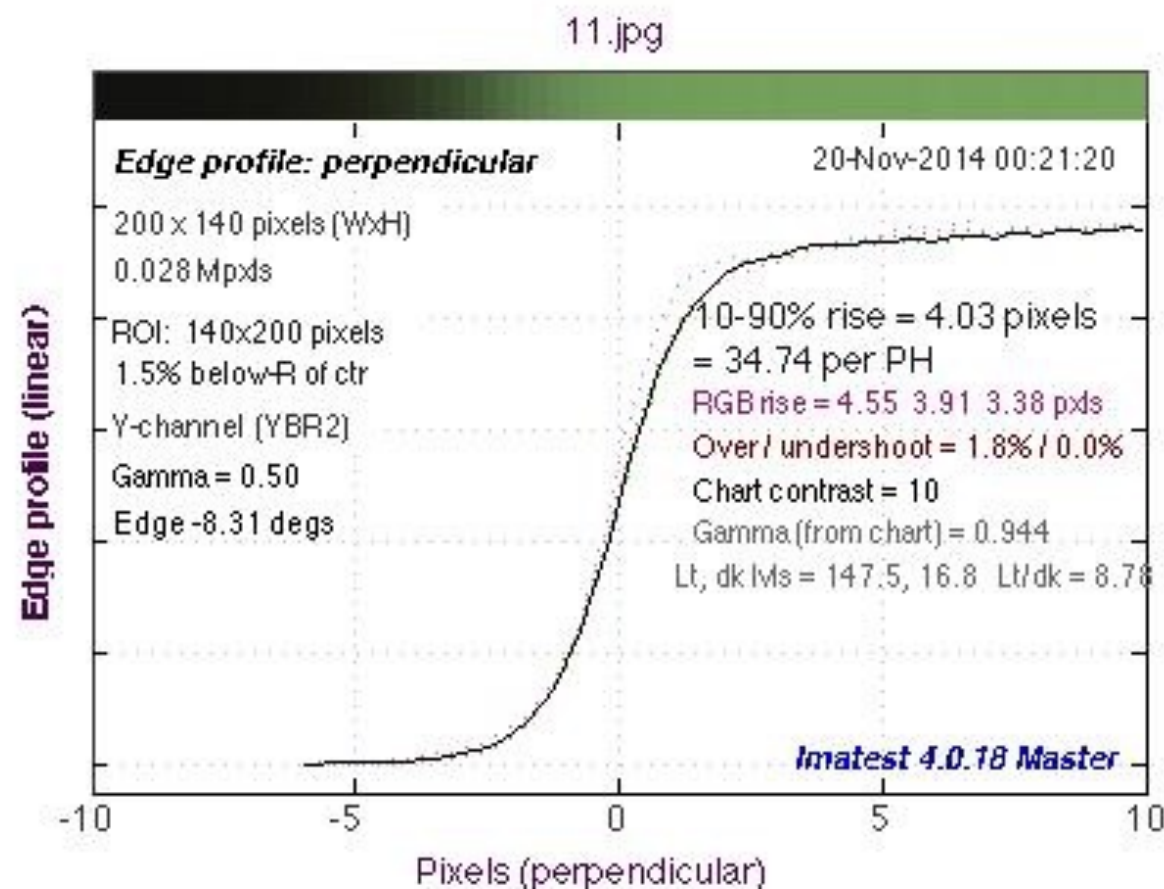
- LSF 50%(↑)



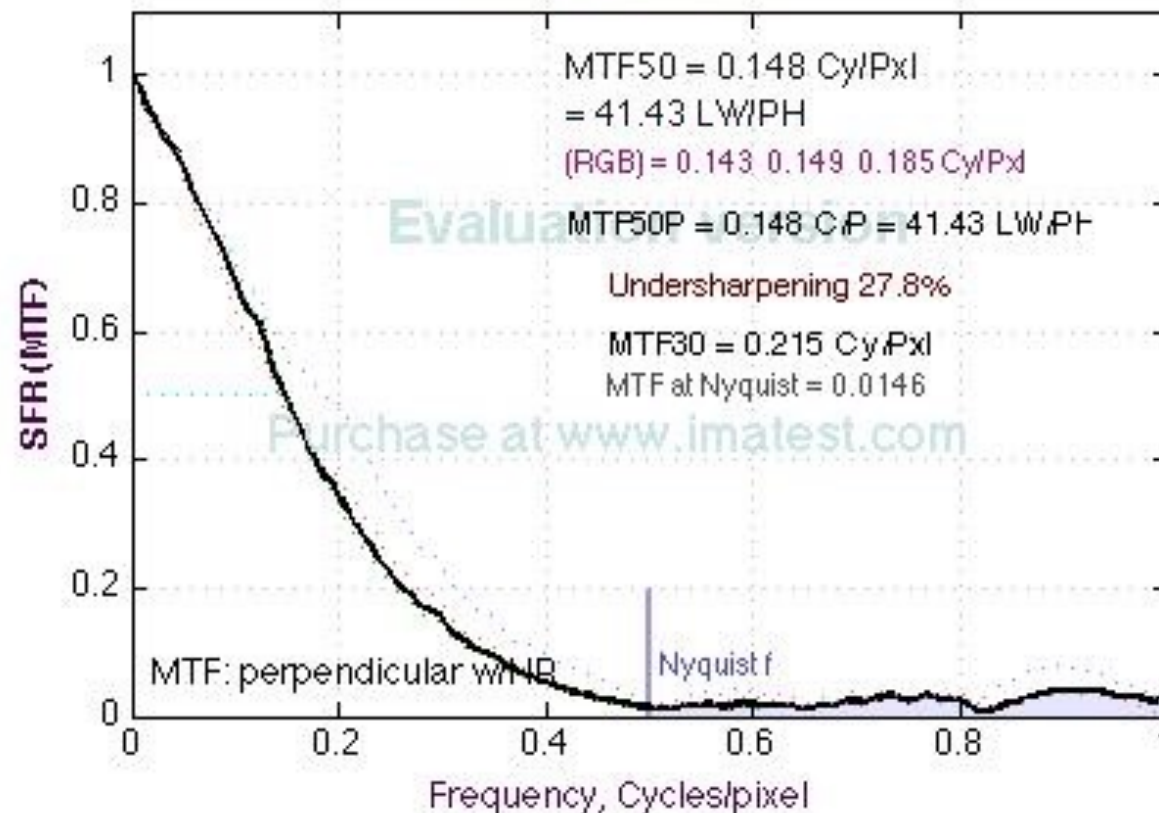


# Imatest

- Imatest is a good software for digital imaging testing.
- Imatest covers SFR, color, and noise concurrently for printers, scanners, etc. Complete the test content.
- System is built on the well-known mathematical computing platform “Matlab” with high reliability.



ROI: 140x200 pixels  
 LR T B = 1 140 1 200



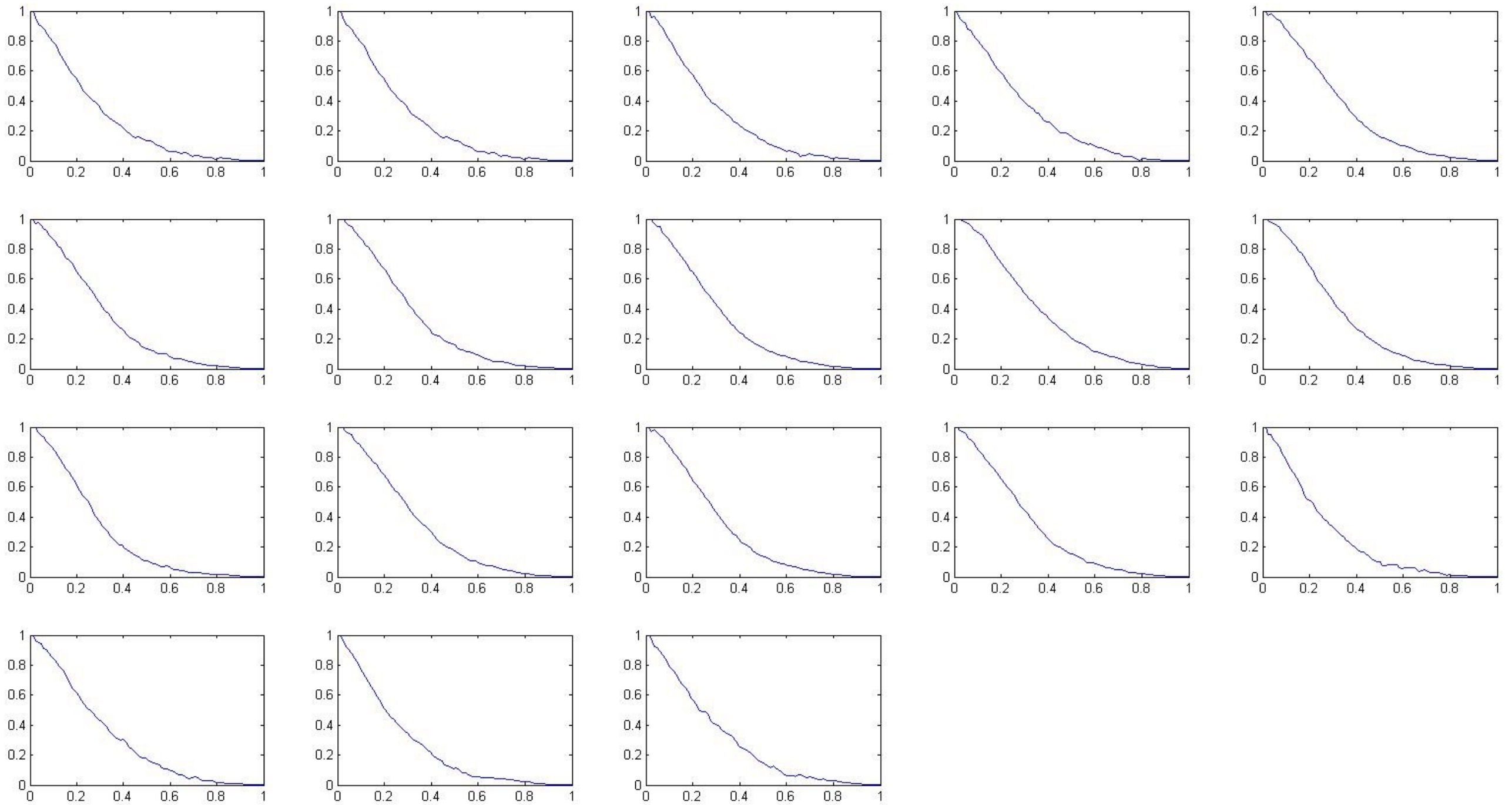
Edge angle = -8.31 degs  
 Estm. chart contrast = 77.1

Selected EXIF data



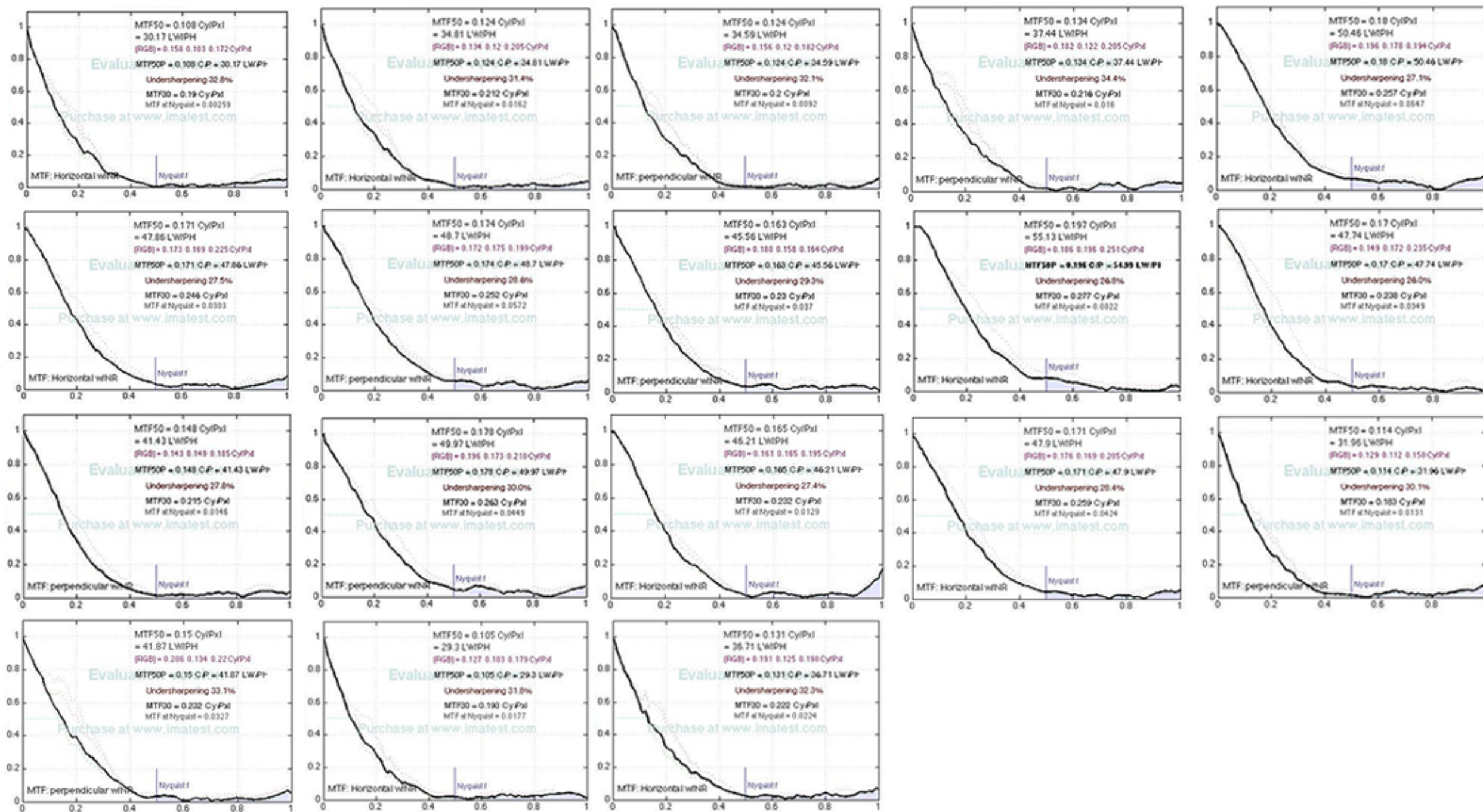
EXIF: Exchangeable Image File Format

# MySFR



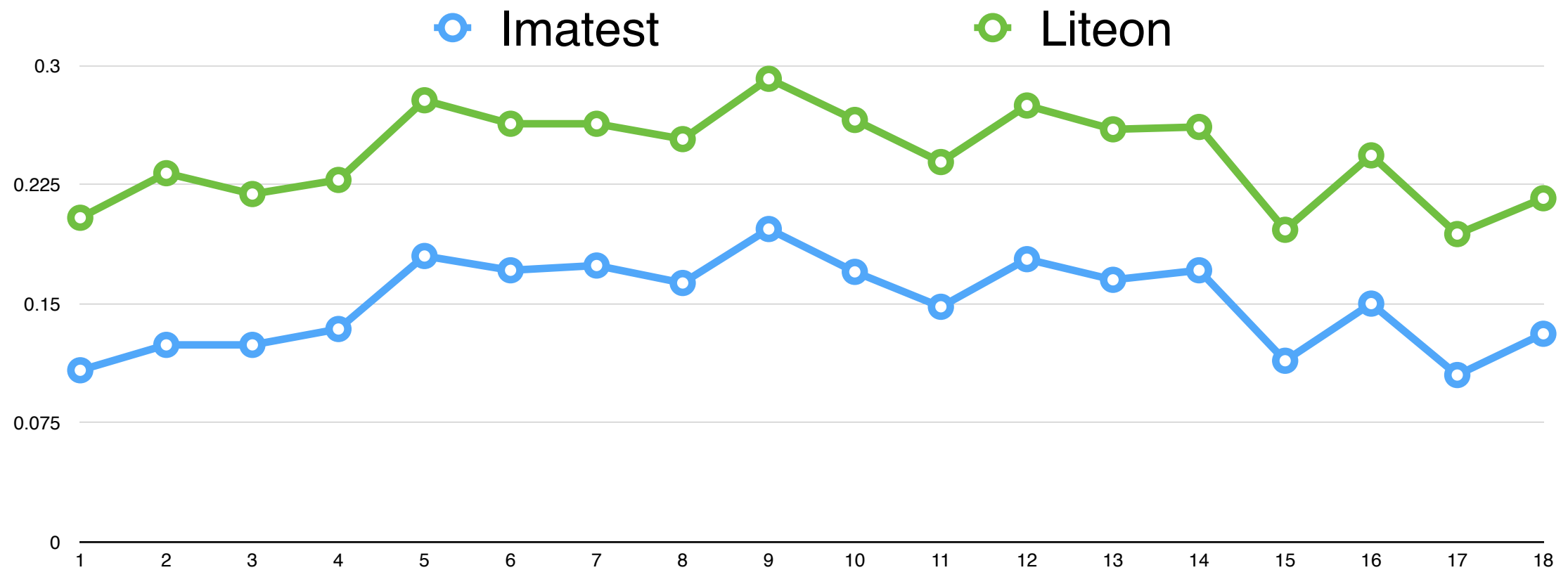


# Imatest MTF



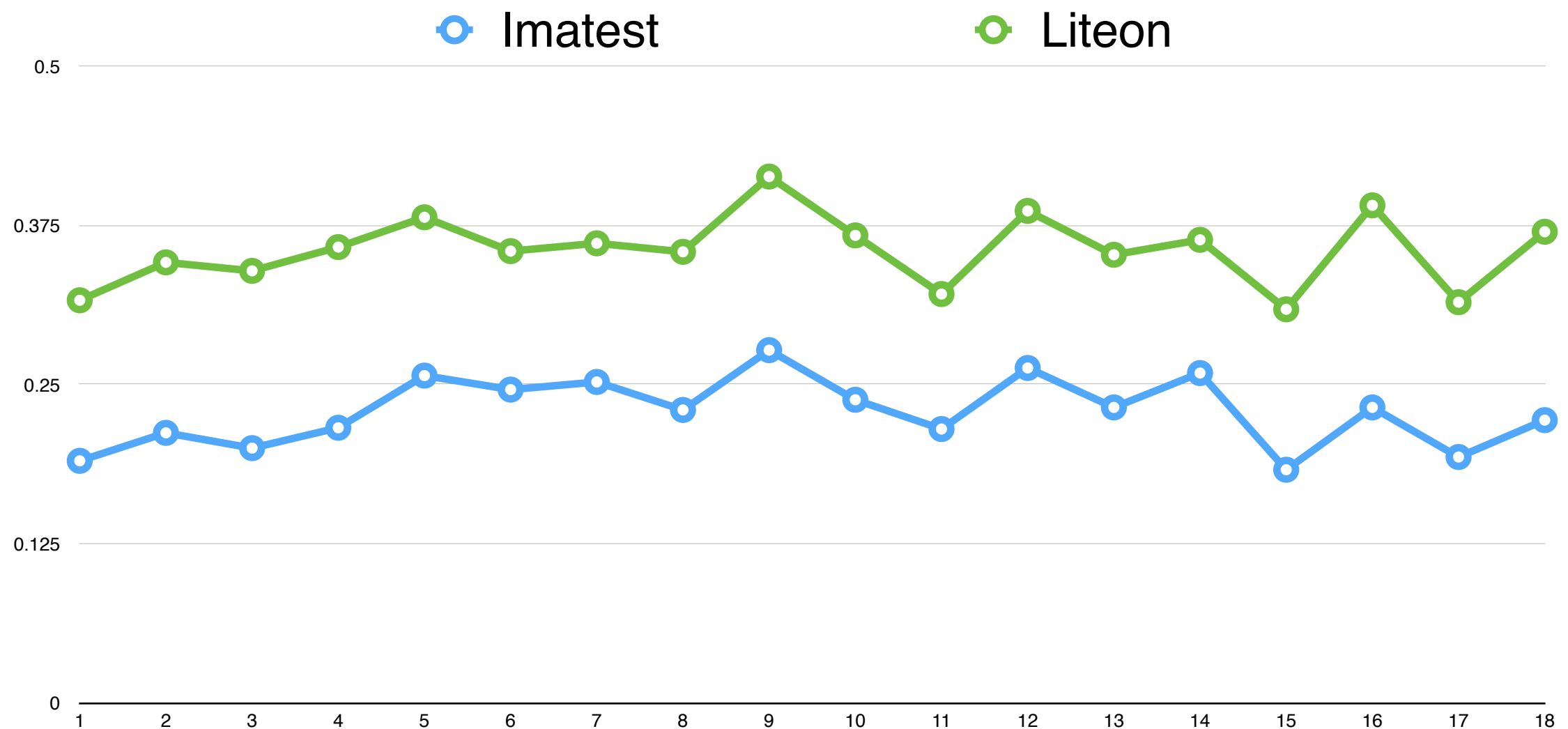
# Accuracy

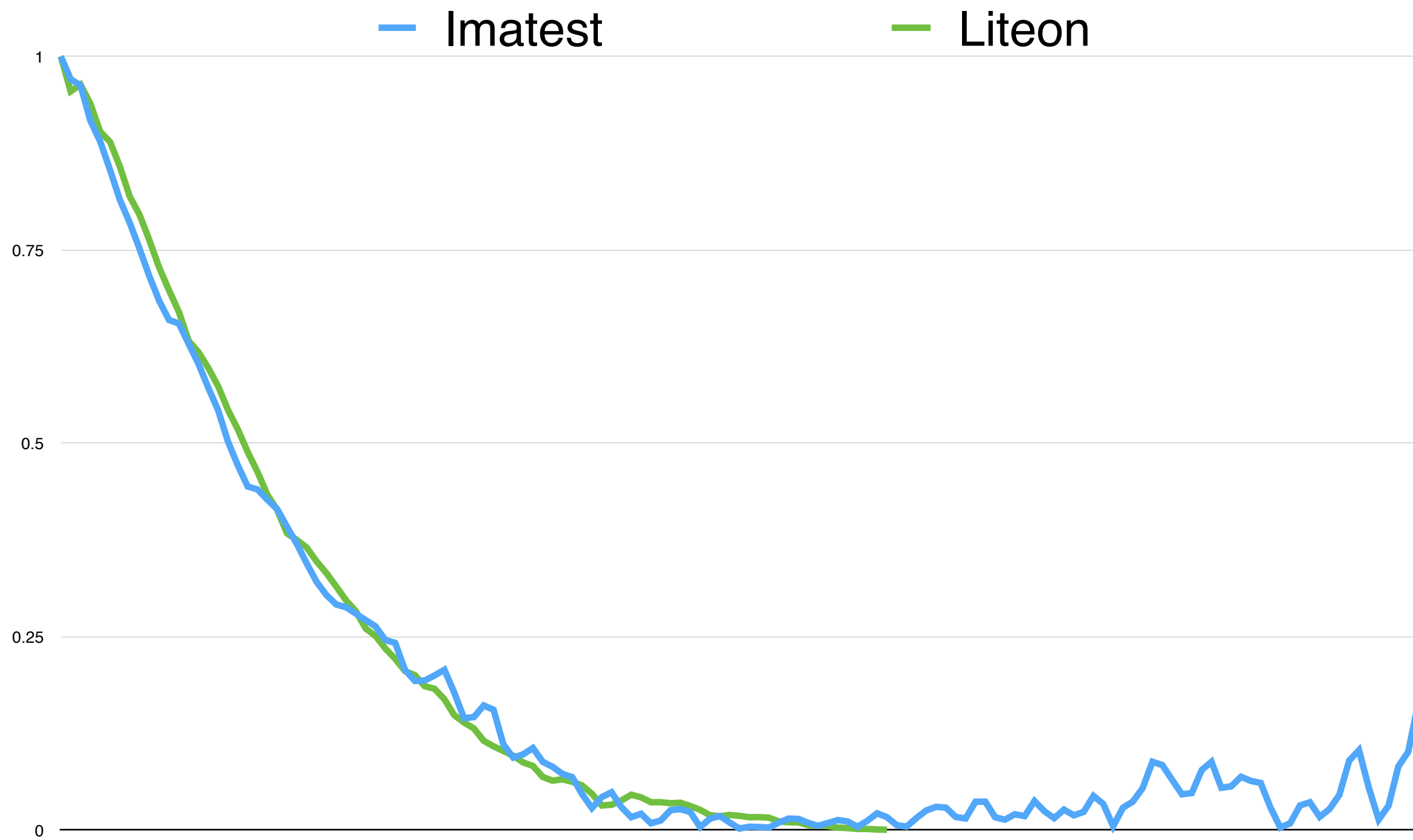
- Our result compared with Imatest has about 9% difference at MTF50.



# Accuracy

- Our result compared with Imatest has about 12% difference at MTF30.





# Reference

- <http://www.edmundoptics.com/technical-resources-center/optics/modulation-transfer-function/>
- Chiu, L.-C. & Fuh, C.-S. (2010), "An Efficient Auto Focus Method for Digital Still Camera Based on Focus Value Curve Prediction Model.", J. Inf. Sci. Eng. 26 (4) , 1261-1272 .
- Estriebeau, Magali and Magnan, Pierre "Fast MTF measurement of CMOS imagers using ISO 12233 slanted-edge methodology." (2004) In: SPIE Optical System Design 2003, 30 Sept 2003, Saint-Etienne, France .
- Greer PB, van Doorn T. "Evaluation of an algorithm for the assessment of the MTF using an edge method." Med Phys. 2000 Sep; 27(9):2048-59.
- I. A. Cunningham and A. Fenster "A method for modulation transfer function determination from edge profiles with correction for finite-element differentiation." Med. Phys. 14, 533 (1987).