ABSTRACT

When digital image sensors are used to capture images or videos, captured colors will have obvious differences from the colors observed by human vision. This phenomenon results from the distinctions of response curves between digital image sensors and human vision so color restoration is an essential step when images are captured by digital image sensors. In real time image systems, such as digital still cameras or video camcorders, accurate color restoration is an arduous task because of highly changeable environmental illumination. This paper introduces a color restoration method to dynamically reproduce image colors. Our proposed method employs a two-step restoration procedure. White balance of captured images is the first step and is followed by image color correction in the second step. Our method is capable of accurate color restoration through empirical analysis and performs very fast due to low computation complexity.

Key Words: digital image sensor, color restoration, illumination, two-step restoration procedure.

I. INTRODUCTION

The color of an object is observed through the combination of image sensor sensitivity and object surface reflectance under various illuminations. Distinct sensor sensitivities will represent different image colors even under the same illumination. It is a great challenge to compensate for the differences of inconsistent responses between image sensors and human vision. Gray world assumptions (Forsyth, 1990; Funt et al., 1996; Finlayson et al., 1995; Barnard et al., 2002) and perfect reflector assumptions (Forsyth, 1990; Funt et al., 1996; Finlayson et al., 1995; Barnard et al., 2002) recover image colors by a diagonal matrix. This diagonal matrix can correct the unbalanced sensitivity for each channel of digital image sensors but it is not sufficient to restore the true color in real scenarios. Color Calibration (Chang and Reid, 1996; Vrhel and Trussel, 1999) corrects color discrepancies between standard color targets and devices. Least square approximation (LSA) (Wolf, 2003) uses a recursive algorithm to acquire an approximation solution and usually obtains satisfactory restoration results. They are hardly implemented in real time image systems because both methods need a standard color target in various scenarios. Prior information method (Hu et al., 2001) and neural network (Yin and Cooperstock, 2004) detect the color cast under different illuminations but they are limited because they rely on a great deal of prior information.

This paper introduces a fast and dynamic color restoration for real time image systems with digital image sensors. Our method recovers the unbalanced sensitivity for each channel of digital image sensors but it is not sufficient to restore the true color in real scenarios. Color Calibration (Chang and Reid, 1996; Vrhel and Trussel, 1999) corrects color discrepancies between standard color targets and devices. Least square approximation (LSA) (Wolf, 2003) uses a recursive algorithm to acquire an approximation solution and usually obtains satisfactory restoration results. They are hardly implemented in real time image systems because both methods need a standard color target in various scenarios. Prior information method (Hu et al., 2001) and neural network (Yin and Cooperstock, 2004) detect the color cast under different illuminations but they are limited because they rely on a great deal of prior information.

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Viggiano, 2001; Zhang, 2004) have explored the color relationship between digital image sensors and human vision. Here we give a brief review and define the notations as follows.

When an object with surface reflectance $R$ is lighted up under illumination $I$, the sensor response $P$ about this object can be described as

$$P_i = \int_{\lambda} I(\lambda)R(\lambda)S(\lambda)d\lambda \quad i = \{r, g, b\}, \quad (1)$$

where $S$ is image sensor sensitivity function and wavelength $\lambda$ should be integrated over visible spectrum $w$. Assume that sensor sensitivity $S$ is a Dirac delta function and therefore Eq. (1) can be rewritten to

$$P_i = I(\lambda_i)R(\lambda_i) \quad i = \{r, g, b\}. \quad (2)$$

Eq. (2) describes that the sensor response only correlates with environment illumination and object surface reflectance under narrow-band sensor sensitivity assumptions. It is obvious that each $RGB$ channel of sensor response can be transformed into an identical amount through one diagonal matrix transformation by

$$\begin{bmatrix}
I(\lambda_r)R(\lambda_r) \\
I(\lambda_g)R(\lambda_g) \\
I(\lambda_b)R(\lambda_b)
\end{bmatrix} = \begin{bmatrix}
I(\lambda_r)R(\lambda_r) & 0 & 0 \\
0 & 1 & 0 \\
0 & 0 & I(\lambda_b)R(\lambda_b)
\end{bmatrix} \\
\begin{bmatrix}
I(\lambda_r)R(\lambda_r) \\
I(\lambda_g)R(\lambda_g) \\
I(\lambda_b)R(\lambda_b)
\end{bmatrix}.$$

The determination of diagonal matrix is called white balance for environmental illumination. Gray world and perfect reflector assumptions are both well-known white balance algorithms to obtain the diagonal matrix under various illuminations. To simplify the notation, Eq. (3) can be described as

$$C_i = DP_i \quad i = \{r, g, b\}, \quad (4)$$

where $C$ represents the sensor response after white balance and $D$ denotes the diagonal matrix. Unfortunately the sensor sensitivity function is not the narrow-band Dirac delta function and usually covers broad-band wavelengths of light. So the sensor response after white balance will still have color discrepancies from human vision even when the diagonal matrix is accurately obtained. Fortunately some studies (Worthey and Brill, 1984; Finlayson et al., 1994; Finlayson and Funt, 1996) showed that the sensor response after white balance can have a good approximation with human vision through a $3 \times 3$ matrix correction. The relation between human vision response $X$ and white balanced sensor response $C$ is given by

$$X_i \equiv MC_i \quad i = \{r, g, b\}, \quad (5)$$

where $M$ is a $3 \times 3$ color correction matrix. From Eqs. (4) and (5), the image color can be restored well when the diagonal and color correction matrixes are both obtained correctly.

Some studies (Chang and Reid, 1996) skip the diagonal matrix calculation and directly compute the compound matrix $T$ as

$$T = MD. \quad (6)$$

In a static image system, the least square approximation (LSA) (Wolf, 2003) usually has a satisfactory result for compound matrix calculation. LSA mainly obtains an optimal transformation matrix $A$ with a minimum error between original vector $V$ and target vector $O$. The approximation can be defined as

$$O \equiv \tilde{O} = AV, \quad (7)$$

where $\tilde{O}$ is the result of original vector $V$ multiplied by the optimal transformation matrix $A$. For a $3 \times 3$ color correction matrix and three-channel sensor response, Eq. (7) will have nine linear equations. If over nine independent samples are used, the sets of Eq. (7) will be over-determined and the solution of LSA can be given by

$$O \equiv AV \Rightarrow V^TO \equiv AVV^T$$

$$\Rightarrow (V^TV)^{-1}V^TO \equiv (V^TV)^{-1}AVV^T$$

$$\Rightarrow A \equiv (V^TV)^{-1}V^TO. \quad (8)$$

In a dynamic image system, a standard color target is usually unavailable. Therefore our proposed method adopts a two-step method to restore image colors. The details of our method will be described in the following section.

**III. OUR PROPOSED METHOD**

For a real time image system, color rendition of image sensor depends on environmental illumination and sensor sensitivity functions. To precisely restore image colors, our proposed method will detect color temperatures of light sources and correct image colors close to human vision based on detected environmental color temperature. The algorithm flow is demonstrated in Fig. 1. At first, a calibration model is constructed under specific light sources. This calibration model is used to recognize the color temperatures
of environmental illumination and balance the sensitivity discrepancies of RGB channels. In the second step, image colors are corrected through the relationship between detected environment color temperature and calibration model. Our method does not rely on standard color targets. It will reduce computation complexity and perform excellent color restoration.

1. White Balance Algorithm

Image white balance aims at an accurate diagonal matrix acquisition in Eq. (4). Under various illuminations, RGB values of white colors are always consistent so white color is usually regarded as an indexed color for white balance adjustment. Our proposed white balance model is employed in the G/R-G/B color space. When white points are captured by an image sensor under various light sources, the locations of these white points in G/R-G/B coordinate can be represented in Fig. 2. These white-point locations in G/R-G/B coordinate are concentrated into a band, named the white-point color temperature band. This band is characteristic of a digital image sensor. The G/R-G/B coordinate depicts color temperature behavior of light sources. When color temperature of light source is higher, the blue component is stronger and the red component is weaker. On the contrary, when the color temperature of light source is lower, the blue component is weaker and the red component is stronger. Aside from color temperature coordinates, pixel luminance is an important factor in the G/R-G/B coordinates. Image sensor current noise is a zero-mean vibration and will be added into RGB channels when the raw image is output. Therefore, when pixel luminance is higher, noise effect is lower; when pixel luminance is lower, noise effect is relatively higher. It is concluded that white-points in a scene will be located in a band in the luminance-G/R-G/B three-dimensional color temperature coordinate.

The calibration model of our white balance is to capture a white chart by image sensor under five specific light sources. In our experiments, these five light sources are often used color temperatures, 7500K, 6500K, 5000K, 4100K, and 3100K. The five locations in G/R-G/B coordinates are demonstrated in Fig. 3 and the five-point curve is called a white point color temperature curve (WPCTC). Let the five color temperature coordinates be \((x_1, y_1), (x_2, y_2), \ldots, (x_5, y_5)\) and define color temperature distance \(CTD(x_0, y_0, i)\) and minimum color temperature distance \(MCTD(x_0, y_0)\) as

\[
CTD(x_0, y_0, i) = \frac{m_i(x_0 - x_i) - (y_0 - y_i)}{m_i^2 + 1}, \quad i = 1, \ldots, 4,
\]

\[
MCTD(x_0, y_0) = \begin{cases} 
\sqrt{(x_0 - x_1)^2 + (y_0 - y_1)^2} & \text{if } x_0 < x_1 \text{ and } y_0 > y_1, \\
\sqrt{(x_0 - x_5)^2 + (y_0 - y_5)^2} & \text{if } x_0 > x_5 \text{ and } y_0 < y_5, \\
\text{Minimum}(CTD(i)) & \text{otherwise}
\end{cases}
\]
where \( m_i \) represents the slope between coordinates \((x_i, y_i)\) and \((x_i + 1, y_i + 1)\). Functions \( CTD(x_0, y_0, i) \) and \( MCTD(x_0, y_0) \) denote the four projection distances and shortest projection distance from an arbitrary pixel to each line of WPCTC. When the \( MCTD \) is calculated, the white-point detection mechanism can be expressed as

\[
\text{White Point} = \begin{cases} 
\text{Yes} & \text{if } MCTD \leq \text{distance threshold} \& \ L \geq \text{luminance threshold} \\
\text{No} & \text{otherwise}
\end{cases}
\quad (11)
\]

It shows that an image pixel is regarded as a white-point when pixel luminance (\( L \)) exceeds the luminance threshold and \( MCTD \) is under the distance threshold. Experiments show satisfactory results in most scenarios and sensors when the luminance and distance thresholds, 70 and 0.25, are used.

Our white balance method can be divided into three parts: white-point color temperature curve construction, white-point detection mechanism, and white balance adjustment. The detailed flow of our white balance is demonstrated in Fig. 4. First of all, \( G/R-G/B \) coordinates of the white chart under five light sources are calibrated for an image sensor and the WPCTC of this sensor is composed of these five \( G/R-G/B \) coordinates. WPCTC is the characteristic curve of a sensor and will not be reconstructed after the first calibration. The second step is the white-point detection mechanism. An image pixel is regarded as a white-point when it passes the examination of Eq. (11); then, corresponding pixel values of \( RGB \) channels are accumulated separately. If a pixel fails the examination, do nothing and the next image pixel enters the mechanism. The examination is repeated until all image pixels pass through the white point detection mechanism. The accumulated \( RGB \) pixel values of qualified white points in an image can be represented as

\[
R_a = \sum_{j=1}^{m} R_q, \quad G_a = \sum_{j=1}^{m} G_q, \quad B_a = \sum_{j=1}^{m} B_q \quad (12)
\]

Accumulated \( RGB \) pixel values of qualified white points in an image can be represented as

\[
D = \begin{bmatrix} 
G_a/R_a & 0 & 0 \\
0 & 1 & 0 \\
0 & 0 & G_a/B_a
\end{bmatrix}
\quad (13)
\]

2. Color Correction Algorithm

After white balance adjustment, the diagonal matrix \( D \) is calculated. The next step is to obtain the color correction matrix \( M \) for further color restoration. From Eqs. (2), (4) and (5), we know that the diagonal and color correction matrixes will alter with the illumination on an object. This implies that the color correction matrix will change with the diagonal matrix.

Let the five color correction matrixes \( M_1, M_2, \ldots, M_5 \) be the approximation solution of Eq. (5) under five specific illuminations in the WPCTC construction. These five matrixes can be easily calculated through least square approximation. Let white balance ratios, \( \left( G_a/R_a, G_a/B_a \right) \), be the color temperature coordinates of current environmental illumination. We can acquire an arbitrary color correction matrix under various illuminations by

\[
M = \alpha M_j + (1 - \alpha) M_{j + 1} \quad (14)
\]

where \( j \) and \( j + 1 \) denote two consecutive nodes in WPCTC which are close to the environmental color temperature coordinate, \( \left( G_a/R_a, G_a/B_a \right) \), and \( \alpha \) represents the distance weight between the environmental
color temperature coordinate and these two coordinates. The distance weight is defined as

\[ \alpha = \frac{CTD_{j+1}}{CTD_j + CTD_{j+1}}. \]  

(15)

Eqs. (14) and (15) show that color temperature coordinates of different light sources are spatially closer and corresponding color correction matrixes will be quantitatively more similar.

In a real time image system, the frequently changing environmental illumination always makes color restoration difficult. In our proposed method, color correction matrix is obtained through the color temperature distance between environmental illumination and calibrated color temperature coordinates. Although there is no standard color target for color correction matrix calculation, the acquired matrix from Eqs. (14) and (15) will be very close to the approximation result by LSA. Experiments in the following section will demonstrate the color behavior between LSA and our method.

IV. EXPERIMENTAL RESULTS

1. Algorithm Simulation

To evaluate our method, we prepare unprocessed raw images from digital still cameras under various illuminations. Unprocessed raw images can be used to compare various color restoration algorithms. Because LSA is considered as an accurate method in static color reproduction, here we compare LSA with our method with the same raw images. The root mean squared errors (RMSE) in Eq. (16) between restored images and standard color chart, GretagMacbeth ColorChecker, are used for quantitative evaluation.

\[ RMSE = \sqrt{\frac{1}{N}[(R_r - R_s)^2 + (G_r - G_s)^2 + (B_r - B_s)^2]}, \]

(16)

where \( N \) is the total number of pixels. The restored image in \( RGB \) color space is described as \( (R_r, G_r, B_r) \) and standard color chart in \( RGB \) color space is described as \( (R_s, G_s, B_s) \). Fig. 5 demonstrates RMSE between standard color target and restored images using LSA and our method. Besides restored images, the RMSE between standard color target and raw images are also shown in this figure. The RMSE data in Fig. 5 represent accumulated errors from number 13 to 19 blocks of GretagMacbeth ColorChecker under various illuminations. LSA restores image colors by least squared approximation between each raw image and standard color in GretagMacbeth ColorChecker. So it performs excellent color restoration. Based on the same raw images, our method employs the familiar LSA performance with the two-step restoration procedure. Fig. 6 demonstrates one set of these compared images. The unprocessed raw image is displayed in Fig. 6(a). It is clear that image colors are very greenish in the raw image because the green channel in the digital image sensor usually has a broader range and a higher sensitivity in the three \( RGB \) channels. Fig. 6(b) shows the raw image after our white balance. Our method will detect environmental illumination and adjust the diagonal matrix based on environmental information. The unbalanced colors in the raw image have been recovered but image colors are not restored accurately yet. Fig. 6(c) shows the final result of our method. The color correction matrix is determined, dynamically, based on the relation between current and reference calibrated illuminations. Therefore image colors are restored excellently and are similar to the restored colors produced by LSA in Fig. 6(d). Besides, although colors from sensors are device-dependent, the transformed colors are compared in the device-independent sRGB color space.

2. Practical Implementation

To further observe real scenarios using our method, we implemented our method in a prototype camera. This prototype camera has the full functions and capabilities of digital cameras, including a six mega pixel image sensor, image signal processing, optical zoom lens, and so on. It can output uncorrected raw images, intermediate images after white balance, and final restored results. Figs. 7, 8, and 9 demonstrate some scenarios captured by our prototype camera. Figs. 7(a), 8(a), and 9(a) show unprocessed raw images. These raw images are all greenish due to the higher sensitivity of the green channel. Figs. 7(b), 8(b), and 9(b) display the intermediate images after our white balance. Image colors are balanced by diagonal matrix compensations. Because red, green, and blue channels of digital image sensors are not impulse functions, restored image colors using only
Fig. 6  (a) Unprocessed raw image from digital image sensor.  (b) image is recovered after white balance by our method.  (c) image is restored after color correction by our method.  (d) image is restored by LSA

Fig. 7  (a) Raw image, (b) intermediate image after our white balance and (c) final result

Fig. 8  (a) Raw image, (b) intermediate image after our white balance and (c) final result
diagonal matrix compensations have discrepancies from true colors. Figs. 7(c), 8(c), and 9(c) show the final results of our method. Restored colors are very similar to true colors because color correction matrices are obtained based on the information concerning current and reference calibrated color temperatures.

V. CONCLUSIONS

This paper introduces a dynamic color restoration method for real time image systems with digital image sensors. Our method restores image colors by a two-step procedure and it can dynamically detect highly changeable environmental color temperatures. The first step is white balance recovery and color correction is the second step. Our white balance locates the environmental color temperature and compensates for the unbalanced colors based on detected environmental information. The color correction step will refer to the detected environmental color temperature and obtain a corresponding color correction matrix. Image colors are accurately restored by our method according both to objective and subjective experimental results.

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NOMENCLATURE

<table>
<thead>
<tr>
<th>Symbol</th>
<th>Description</th>
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<tbody>
<tr>
<td>A</td>
<td>optimal transformation matrix</td>
</tr>
<tr>
<td>B_s</td>
<td>accumulated pixel value of blue channel</td>
</tr>
<tr>
<td>B_q</td>
<td>pixel value of blue channel of qualified white point</td>
</tr>
<tr>
<td>B_r</td>
<td>pixel value of blue channel of restored image</td>
</tr>
<tr>
<td>B_s</td>
<td>pixel value of blue channel of standard color chart</td>
</tr>
<tr>
<td>C</td>
<td>sensor response after white balance</td>
</tr>
<tr>
<td>CTD(x_0, y_0, i)</td>
<td>color temperature distance of an arbitrary pixel (x_0, y_0)</td>
</tr>
<tr>
<td>D</td>
<td>diagonal matrix</td>
</tr>
<tr>
<td>G_a</td>
<td>accumulated pixel value of green channel</td>
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<td>G_q</td>
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<td>pixel value of green channel of restored image</td>
</tr>
<tr>
<td>G_s</td>
<td>pixel value of green channel of standard color chart</td>
</tr>
<tr>
<td>I</td>
<td>illumination</td>
</tr>
<tr>
<td>j and j + 1</td>
<td>two consecutive nodes in WPCTC</td>
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<tr>
<td>M</td>
<td>color correction matrix</td>
</tr>
<tr>
<td>MCTD(x_0, y_0)</td>
<td>minimum color temperature distance of an arbitrary pixel (x_0, y_0)</td>
</tr>
<tr>
<td>m</td>
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</tr>
<tr>
<td>m_i</td>
<td>slope between coordinates (x_i, y_i) and (x_i + 1, y_i + 1)</td>
</tr>
<tr>
<td>N</td>
<td>total number of pixels</td>
</tr>
<tr>
<td>O</td>
<td>target vector</td>
</tr>
<tr>
<td>Ô</td>
<td>result of target vector multiplied by the optimal transformation matrix</td>
</tr>
<tr>
<td>P</td>
<td>sensor response</td>
</tr>
<tr>
<td>R</td>
<td>surface reflectance</td>
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<td>RMSE</td>
<td>root mean squared errors</td>
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<tr>
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<tr>
<td>R_r</td>
<td>pixel value of red channel of restored image</td>
</tr>
<tr>
<td>R_s</td>
<td>pixel value of red channel of standard color chart</td>
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<tr>
<td>S</td>
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<td>T</td>
<td>compound matrix</td>
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<tr>
<td>X</td>
<td>human vision response</td>
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Greek Symbols

<table>
<thead>
<tr>
<th>Symbol</th>
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</tr>
</thead>
<tbody>
<tr>
<td>α</td>
<td>distance weight</td>
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<td>λ</td>
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REFERENCES


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