

Java Programming

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```
1 class Lecture4 {  
2  
3     "Arrays and More Data Structures"  
4  
5 }
```

Arrays

An array is an object which stores **multiple** values of the **same** type.

```
1 ...  
2 // Assume that T is any type and the size is known.  
3 T[] A = new T[size];  
4 ...
```

- We now proceed to explain Line 3 in two stages.

Stage 1: Array Creation

- We first focus on the RHS of Line 3.
- One array is allocated in the **heap** by invoking the **new** operator followed by **T** and **[]** surrounding its size,
- Then its starting address is returned and should be cached.
- Note that the size **cannot** be changed after allocation.¹

¹What if the array is full?! Stay tuned.

Stage 2: Reference

- We then declare one variable, say A in this case, to store the starting address of the array.
- I strongly emphasize that A is not the array, but the reference to the array!
- To understand the type correctly, one should read the type from right to left.
- For example, A is the reference to an array whose elements are of the \mathbf{T} type.
- Note that the array type is declared like $\mathbf{T}[]$ but without the size.

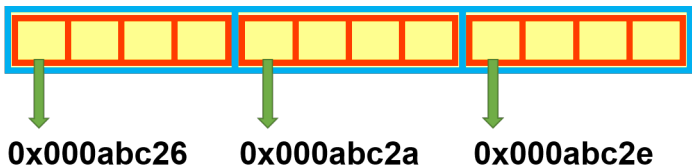
Zero-Based Array Indexing

- We access any array element by using its index, which starts from 0 but not 1.
- Explicitly, the first element is `A[0]`, followed by `A[1]`, `A[2]`, and so on. (Why?)
- So the last index of one array is $size - 1$.
- When the index is out of range, the program will fail due to the runtime exception **`ArrayIndexOutOfBoundsException`**.

Memory Allocation for Arrays

- An array is **allocated contiguously** in the memory.
- To fetch the second element, jump to the address stored by A and shift by 1 unit size of **T**, denoted by **A[1]**.
- For example,

```
1 ...  
2   int[] A = new int[3];  
3 ...
```



Zero-Based Array Indexing (Concluded)

- You now could explain why $A[0]$ denotes the first array element.
- Array index clearly acts as an **offset** from the starting address of the array!
- It is worth to mention that we can treat the whole memory as an array, indeed.
- This convention is applicable commonly among the mainstream languages!² (Why?)

²For example, C, C++, Java, JavaScript, and even Python. However, to the best of my knowledge, R and MATLAB manipulate arrays with the first index starting from 1. So it is just an option between choosing 0 and 1.

Array Initialization

- Every array is initialized implicitly once the array is created.
- Default values for different types are listed below:
 - 0 for all numeric types;
 - `\u0000` for `char` type;
 - `false` for `boolean` type;
 - `null` for all reference types.³
- An array can also be created by **enumerating** all elements without using the `new` operator, for example,

```
1 ...  
2     int[] A = { 10, 20, 30 }; // Syntax sugar.  
3 ...
```

³We will visit the keyword `null` in the chapter of OOP.

Arrays & Loops

We often use **for** loops to process array elements.

- Arrays have the attribute called `length`, which indicates the array capacity.
 - For example, `A.length`.
- So it is natural to use a **for** loop to manipulate arrays.

Examples

```
1 ...  
2 // Create an integer array of size 5.  
3 int[] A = new int[5];  
4  
5 // Generate 5 random integers ranging from 0 to 99.  
6 for (int i = 0; i < A.length; ++i) {  
7     A[i] = (int) (Math.random() * 100);  
8 }  
9  
10 // Display all elements of A: O(n).  
11 for (int i = 0; i < A.length; ++i) {  
12     System.out.printf("%d ", A[i]);  
13 }  
14 System.out.println();  
15 ...
```

- To show all elements, you need to iterate over the array by loops instead of simply printing A. (Why?)

```
1 ...  
2     // Find maximum and minimum of A: O(n).  
3     int max = A[0];  
4     int min = A[0];  
5     for (int i = 1; i < A.length; ++i) {  
6         if (max < A[i]) max = A[i];  
7         if (min > A[i]) min = A[i];  
8     }  
9     ...
```

- How to find the locations of extreme values?⁴
- Can you find the 2nd maximum value in A ?
- Can you track and maintain a record of the first k maximum values in A ?

⁴See also [Arguments of Maxima](#) (argmax) and [Arguments of Minima](#) (argmin).

```

1 ...
2     // Sum of A: O(n) .
3     int sum = 0;
4     for (int i = 0; i < A.length; ++i) {
5         sum += A[i];
6     }
7 ...

```

- Calculate the following descriptive statistics:
 - the mean of A ;
 - the median⁵ of A ;
 - the mode⁶ of A .

⁵See <https://en.wikipedia.org/wiki/Median>.

⁶See [https://en.wikipedia.org/wiki/Mode_\(statistics\)](https://en.wikipedia.org/wiki/Mode_(statistics)).

Alternative Way: for-each Loops

- A **for**-each loop is designed to **iterate** over a collection of objects, such as arrays and other data structures, in strictly sequential fashion, from start to finish.

```
1 ...  
2     T[] A = { ... };  
3     for (T element : A) {  
4         // Loop body.  
5     }  
6 ...
```

Example

```
1 ...  
2     int s = 0;  
3     for (int i = 0; i < A.length; ++i) {  
4         s += A[i];  
5     }  
6 ...
```

```
1 ...  
2     int s = 0;  
3     for (int item : A) {  
4         s += item;  
5     }  
6 ...
```

- Short and sweet!
- You may consider using the for-each loop if you **iterate over all elements** and **the order of iteration is irrelevant**.

Exercise

```
1 ...  
2     String[] letters = { "A", "B", "C", "D", "E" };  
3  
4     for (String letter: letters) {  
5         System.out.printf("%s ", letter);  
6     }  
7     System.out.println();  
8 ...
```


More Examples (1/4): Cloning Arrays

- One might duplicate an array for some purpose, say a backup.
- For example,

```
1 ...  
2     int x = 1;  
3     int y = x; // You can say that y copies the value of x.  
4     x = 2;  
5     System.out.println(y); // Output 1.  
6  
7     int[] A = { 10, ... }; // Ignore the rest of elements.  
8     int[] B = A;  
9     A[0] = 100;  
10    System.out.println(B[0]); // Output?  
11 ...
```

- The result differs from our expectation. (Why?)
- This is called the **shallow copy**.

- To clone an array, you should create a new array and use loops to copy every element, one by one.

```
1 ...  
2     // Let A be an array to be copied.  
3     int[] B = new int[A.length];  
4     for (int i = 0; i < A.length; ++i) {  
5         B[i] = A[i];  
6     }  
7 ...
```

- This is called the **deep copy**.
- Alternatively, you may use the method **System.arraycopy()** for the same purpose.

```
1 ...  
2     // Assume that B is ready.  
3     System.arraycopy(A, 0, B, 0, A.length);  
4 ...
```

More Examples (2/4): Shuffle Algorithm

```
1 ...  
2     for (int i = 0; i < A.length; ++i) {  
3  
4         // Choose a random integer j.  
5         int j = (int) (Math.random() * A.length);  
6  
7         // Swap A[i] and A[j].  
8         int tmp = A[i];  
9         A[i] = A[j];  
10        A[j] = tmp;  
11  
12    }  
13 ...
```

- However, this naive algorithm is fundamentally broken!⁷
- How to swap by using XOR (that is, \wedge)?

⁷See <https://blog.codinghorror.com/the-danger-of-naivete/>.

Exercise

Write a program to deal the first 5 cards from a deck of 52 shuffled cards.

- As you can see, RNG produces only random numbers.
- How to shuffle nonnumerical objects?
- Simply label 52 cards by $0, 1, \dots, 51$.
- Shuffle these numbers!

```

1  ...
2      String[] suits = { "Club", "Diamond", "Heart", "Spade" };
3      String[] ranks = { "3", "4", "5", "6", "7", "8", "9",
4                          "10", "J", "Q", "K", "A", "2" };
5
6      int size = 52;
7      int[] deck = new int[size];
8      for (int i = 0; i < deck.length; i++)
9          deck[i] = i;
10
11     // Shuffle algorithm: correct version.
12     for (int i = 0; i < size - 1; i++) {
13         int j = (int) (Math.random() * (size - i)) + i;
14         int z = deck[i];
15         deck[i] = deck[j];
16         deck[j] = z;
17     }
18
19     for (int i = 0; i < 5; i++) {
20         String suit = suits[deck[i] / 13];
21         String rank = ranks[deck[i] % 13];
22         System.out.printf("%2s %-7s\n", rank, suit);
23     }
24     ...

```

More Examples (3/4): Sorting Problem

- In computer science, a sorting algorithm is an algorithm that puts elements of a list in a certain **order**.
- You may call **Arrays.sort(A)** to rearrange *A* in ascending order, for example,

```
1 import java.util.Arrays;
2
3 ...
4     int[] A = { 5, 2, 8 };
5     Arrays.sort(A); // Becomes { 2, 5, 8 }.
6
7     String[] B = { "www", "csie", "ntu", "edu", "tw" };
8     Arrays.sort(B); // Result?
9 ...
```

- Note that we sort strings in lexicographical (dictionary) order for most cases.

Exercise: Bubble Sort

```
1 ...  
2 // Bubble sort:  $O(n^2)$ .  
3 boolean swapped;  
4 do {  
5     swapped = false;  
6     for (int i = 0; i < A.length - 1; i++) {  
7         if (A[i] > A[i + 1]) {  
8             int tmp = A[i];  
9             A[i] = A[i + 1];  
10            A[i + 1] = tmp;  
11            swapped = true;  
12        }  
13    }  
14 } while (swapped);  
15 ...
```

- Try to implement [selection sort](#) and [insertion sort](#).⁸

⁸See <https://visualgo.net/en/sorting>.

More Examples (4/4): Searching Problem

- It is often to query one **key** for its corresponding **value**.
- For example, the program plans to find one client's credit card number.
- In this case, the client name is the query key and his/her credit card number is the value associated.

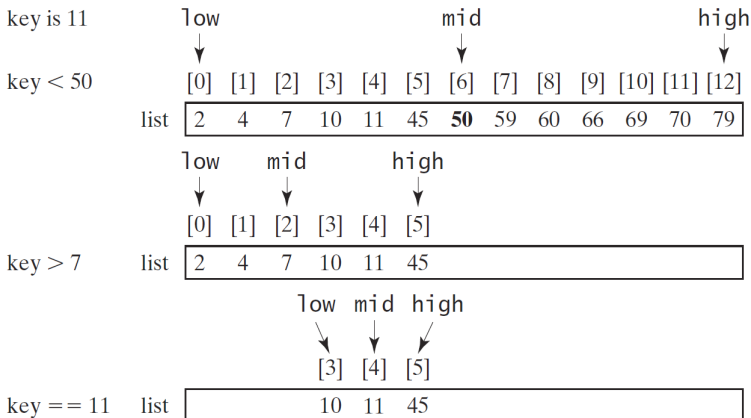
Solution 1: Linear Search

- **Linear search** compares the query key with all elements in sequential order.

```
1 ...  
2     // Linear search: O(n).  
3     int[] A = { ... };  
4     int founds = 0;  
5     for (int i = 0; i < A.length; i++) {  
6         if (A[i] == key) {  
7             System.out.printf("%d ", i);  
8             founds++;  
9         }  
10    }  
11    System.out.println("\nFounds: " + founds);  
12 ...
```

- Could we do better?

Solution 2: Binary Search (Revisited)



```

1  ...
2      int idx = -1; // Why?
3      int high = A.length - 1, low = 0, mid;
4      while (high > low && idx < 0) {
5          mid = low + (high - low) / 2; // Why?
6          if (A[mid] < key)
7              low = mid + 1;
8          else if (A[mid] > key)
9              high = mid - 1;
10         else
11             idx = mid;
12     }
13
14     if (idx > -1)
15         System.out.printf("%d: %d\n", key, idx);
16     else
17         System.out.printf("%d: not found\n", key);
18     ...

```

- It can be shown that binary search runs in $O(\log n)$ time.
- However, binary search works only for **ordered** data!

Discussions

| Scenario / Operation | Insert | Search |
|--------------------------|----------|-------------|
| Immutable unsorted array | N/A | $O(n)$ |
| Immutable sorted array | N/A | $O(\log n)$ |
| Mutable unsorted array | $O(1)^*$ | $O(n)$ |
| Mutable sorted array | $O(n)$ | $O(\log n)$ |

*: insert by attaching behind the array.

- Assume that the data is immutable (unchangeable).
- We sort the data once for all and the binary search works well.
- What if the data may be changed all the time?
- Is it possible to make it run in $O(1)$ time for both operations?⁹

⁹See https://en.wikipedia.org/wiki/Hash_table.

Short Introduction to Data Structures

- A data structure is a particular way of **organizing** data in a program so that it can perform **efficiently**.¹⁰
- **The choice for data structures depends on applications.**
- As an alternative to arrays, **linked lists**¹¹ are used to store data in the way different from arrays.
- You will see plenty of data structures in the future.¹²
 - For example, trees, graphs, tables, and more.
- You could also find a huge number of questions about data structures on [LeetCode](https://leetcode.com/).

¹⁰See <http://bigocheatsheet.com/>.

¹¹See https://en.wikipedia.org/wiki/Linked_list.

¹²See [Introduction to Collections](#) by Oracle and [Java Collections Framework](#) from Wikipedia.

Beyond 1D Arrays

- 2D or higher dimensional arrays are widely used in various applications.
 - For example, RGB images are stored as 3D arrays.
- We can create 2D **T**-type arrays simply by adding one more [] with its size.
- For example,

```
1 ...  
2     int rows = 4; // Row size.  
3     int cols = 3; // Column size.  
4     T[][] M = new T[rows][cols];  
5 ...
```

- It is similar to create 3D or higher-dimensional arrays.

| | [0] | [1] | [2] | [3] | [4] |
|-----|-----|-----|-----|-----|-----|
| [0] | 0 | 0 | 0 | 0 | 0 |
| [1] | 0 | 0 | 0 | 0 | 0 |
| [2] | 0 | 0 | 0 | 0 | 0 |
| [3] | 0 | 0 | 0 | 0 | 0 |
| [4] | 0 | 0 | 0 | 0 | 0 |

`matrix = new int[5][5];`

(a)

| | [0] | [1] | [2] | [3] | [4] |
|-----|-----|-----|-----|-----|-----|
| [0] | 0 | 0 | 0 | 0 | 0 |
| [1] | 0 | 0 | 0 | 0 | 0 |
| [2] | 0 | 7 | 0 | 0 | 0 |
| [3] | 0 | 0 | 0 | 0 | 0 |
| [4] | 0 | 0 | 0 | 0 | 0 |

`matrix[2][1] = 7;`

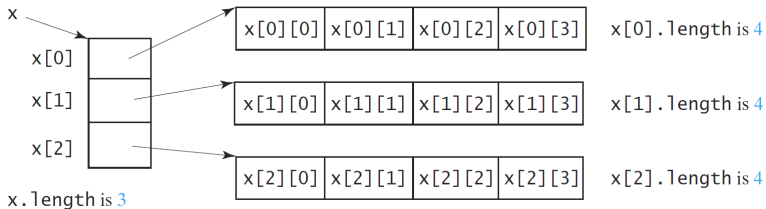
(b)

| | [0] | [1] | [2] |
|-----|-----|-----|-----|
| [0] | 1 | 2 | 3 |
| [1] | 4 | 5 | 6 |
| [2] | 7 | 8 | 9 |
| [3] | 10 | 11 | 12 |

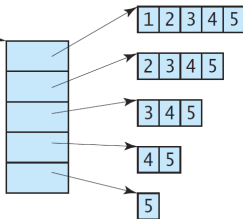
```
int[][] array = {
    {1, 2, 3},
    {4, 5, 6},
    {7, 8, 9},
    {10, 11, 12}
};
```

(c)

Memory Allocation for 2D Arrays



```
int[][] triangleArray = {  
    {1, 2, 3, 4, 5},  
    {2, 3, 4, 5},  
    {3, 4, 5},  
    {4, 5},  
    {5}  
};
```



Example: 2D Arrays & Loops¹³

```
1 ...
2     int[][] A = { { 10, 20, 30 }, { 40, 50 }, { 60 } };
3
4     // Conventional for loop.
5     for (int i = 0; i < A.length; i++) {
6         for (int j = 0; j < A[i].length; j++)
7             System.out.printf("%3d", A[i][j]);
8         System.out.println();
9     }
10
11    // For-each loop.
12    for (int[] row : A) {
13        for (int item : row)
14            System.out.printf("%3d", item);
15        System.out.println();
16    }
17 ...
```

¹³Thanks to a lively discussion on January 31, 2016.

Exercise: Matrix Multiplication

Let $A_{m \times n}$ and $B_{n \times q}$ be two matrices for $m, n, q \in \mathbb{N}$. Write a program to calculate $C = AB$.

- Let a_{ik} and b_{kj} be elements of A and B , respectively.
- For $k = 1, 2, \dots, n$, use the formula

$$c_{ij} = \sum_{k=1}^n a_{ik} b_{kj}$$

for $i = 1, 2, \dots, m$ and for $j = 1, 2, \dots, q$.

- Following the formula, it takes $O(n^3)$ time. (Why?)

Digression: ArrayList

```
1 ...
2     int[] A = new int[3]; // The size should be known in advance.
3     A[0] = 100;
4     A[1] = 200;
5     A[2] = 300;
6     for (int item : A)
7         System.out.printf("%d ", item);
8     System.out.println();
9
10    ArrayList<Integer> B = new ArrayList<>(); // Size?
11    B.add(100);
12    B.add(200);
13    B.add(300);
14    System.out.println(B); // Short and sweet!
15 ...
```

- Arrays are the simplest form of data structures but not convenient to use.
- For example, resizing arrays can be costly when you frequently move data to a newly created, larger array. (Why?)
- So it is advisable to use **ArrayList**<E>, where E is the **type parameter**.
- Using angle brackets < · > in Java is called the **generics** starting from JDK5 in 2004.

Digression: Generics

- Generics are widely used in data structures, like **Stack**<T>, **Map**<K, V>, **Graph**<V, E>, etc.¹⁴
- To use **ArrayList**<E> correctly, we need to replace E with **Integer**, which is the wrapper class¹⁵ for **int** values.
- Be aware that only reference types can substitute the type parameters.
- This technique is also utilized in C++ and C#.

¹⁴See also [Generics](#) by Oracle. Stay tuned in Java Programming 2.

¹⁵See [The Numbers Classes](#).

Case Study: Order Reversing

- How to rearrange an input array in reverse order?
- Let A be an integer array.
- The first attempt is to create another array with same size and **copy** each element from A to B .

```
1 ...  
2     int[] A = { 1, 2, 3, 4, 5 };  
3     int[] B = new int[A.length];  
4     for (int i = 0; i < A.length; i++) {  
5         B[A.length - 1 - i] = A[i];  
6     }  
7     A = B; // Why?  
8 ...
```

Another Attempt

```
1 ...  
2     int[] A = { 1, 2, 3, 4, 5 };  
3     for (int i = 0; i < A.length / 2; i++) {  
4         int j = A.length - 1 - i;  
5         int tmp = A[i];  
6         A[i] = A[j];  
7         A[j] = tmp;  
8     }  
9 ...
```

| Approach | Time Complexity | Space Complexity |
|-------------|-----------------|------------------|
| 1st attempt | $O(n)$ | $O(n)$ |
| 2nd attempt | $O(n)$ | $O(1)$ |

- The second is better in both time¹⁶ and space.
- This is an **in-place** algorithm.

¹⁶It runs in only half time of the first attempt.