Image stitching

Digital Visual Effects Yung-Yu Chuang

with slides by Richard Szeliski, Steve Seitz, Matthew Brown and Vaclav Hlavac

Applications of image stitching

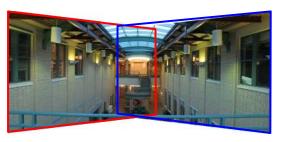
Digi<mark>VFX</mark>

- Video stabilization
- Video summarization
- Video compression
- Video matting
- Panorama creation

Image stitchingStitching = alignment + blending

/ geometrical registration photometric registration

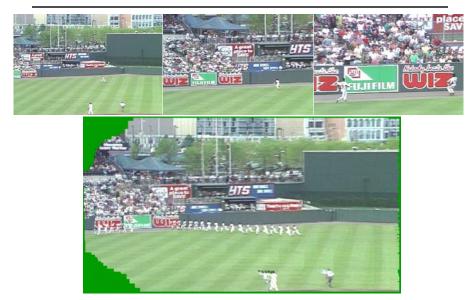




Video summarization

Digi<mark>VFX</mark>

DigiVFX

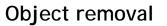


Video compression

DigiVFX









input video

Object removal

Digi<mark>VFX</mark>



background estimation

Panorama creation







Why panorama?

DigiVFX

- Are you getting the whole picture?
 - Compact Camera FOV = 50 x 35°



Why panorama?

- Are you getting the whole picture?
 - Compact Camera FOV = 50 x 35°
 - Human FOV = $200 \times 135^{\circ}$



Why panorama?

DigiVFX

- Are you getting the whole picture?
 - Compact Camera FOV = 50 x 35°
 - Human FOV = $200 \times 135^{\circ}$
 - Panoramic Mosaic = $360 \times 180^{\circ}$



Panorama examples

Digi<mark>VF</mark>X

- Similar to HDR, it is a topic of computational photography, seeking ways to build a better camera using either hardware or software.
- Most consumer cameras have a panorama mode
- Mars:

http://www.panoramas.dk/fullscreen3/f2_mars97.html

• Earth:

http://www.panoramas.dk/new-year-2006/taipei.html http://www.360cities.net/ http://maps.google.com.tw/



What can be globally aligned?



DigiVFX

mosaic projection plane

- In image stitching, we seek for a matrix to globally warp one image into another. Are any two images of the same scene can be aligned this way?
 - Images captured with the same center of projection
 - A planar scene or far-away scene

Mosaic as an image reprojection

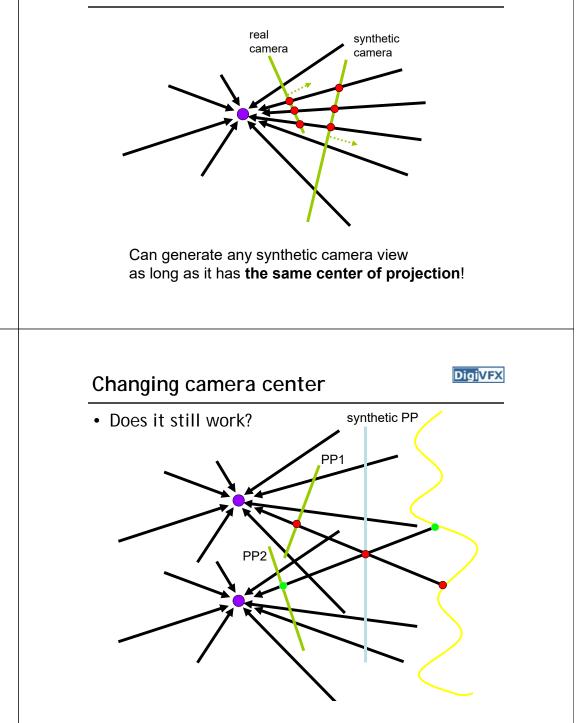
• The images are reprojected onto a common plane

• The mosaic is formed on this plane

• Mosaic is a synthetic wide-angle camera

A pencil of rays contains all views





What cannot

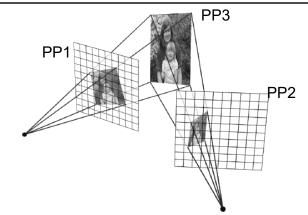
DigiVFX

• The scene with depth variations and the camera has movement



Planar scene (or a faraway one)





- PP3 is a projection plane of both centers of projection, so we are OK!
- This is how big aerial photographs are made

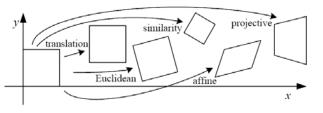
Motion models

Digi<mark>VFX</mark>

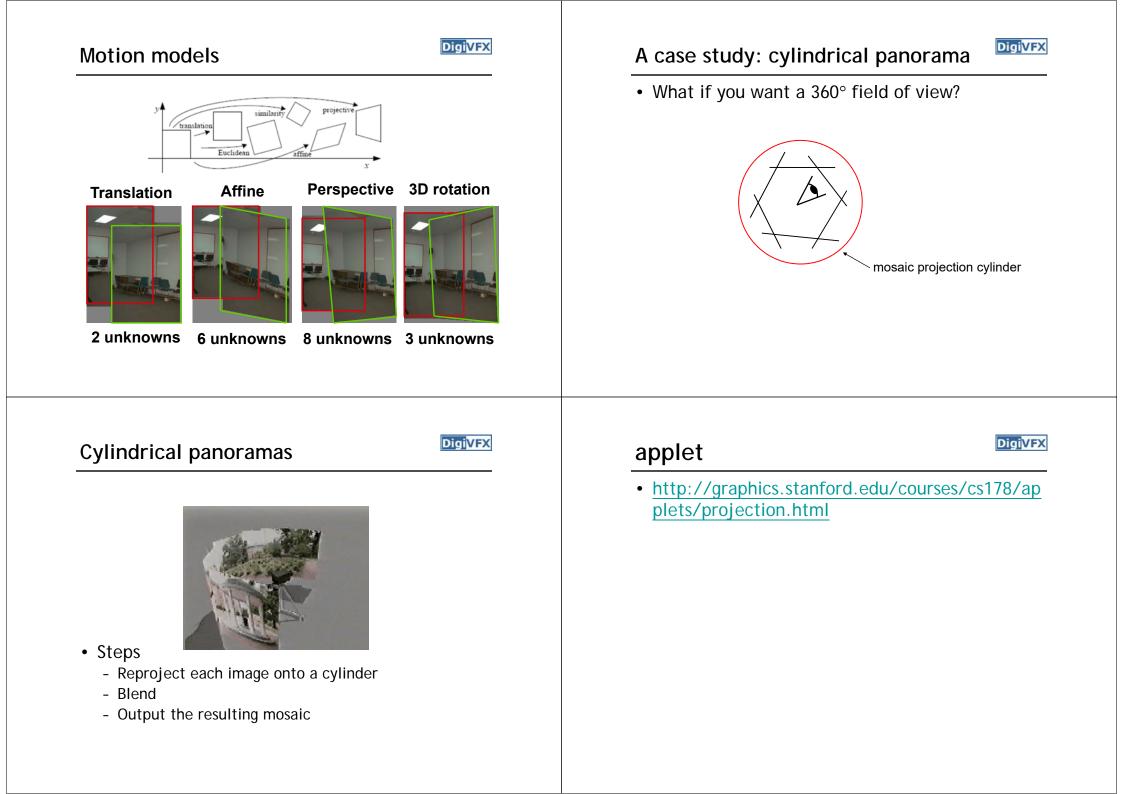
• Parametric models as the assumptions on the relation between two images.

2D Motion models

Digi<mark>VFX</mark>



Name	Matrix	# D.O.F.	Preserves:	Icon
translation	$igg[\left. I \right t igg]_{2 imes 3}$	2	orientation $+\cdots$	
rigid (Euclidean)	$\left[egin{array}{c c} m{R} & t \end{array} ight]_{2 imes 3}$	3	lengths $+\cdots$	\Diamond
similarity	$\left[\left. s \boldsymbol{R} \right \boldsymbol{t} \right]_{2 \times 3}$	4	angles $+\cdots$	\diamond
affine	$\left[egin{array}{c} oldsymbol{A} \end{array} ight]_{2 imes 3}$	6	$parallelism + \cdots$	\square
projective	$\left[egin{array}{c} ilde{m{H}} \end{array} ight]_{3 imes 3}$	8	straight lines	$\left[\right]$



Cylindrical panorama

DigiVFX

DigiVFX

- 1. Take pictures on a tripod (or handheld)
- 2. Warp to cylindrical coordinate
- 3. Compute pairwise alignments
- 4. Fix up the end-to-end alignment
- 5. Blending
- 6. Crop the result and import into a viewer

It is required to do radial distortion correction for better stitching results!

Taking pictures



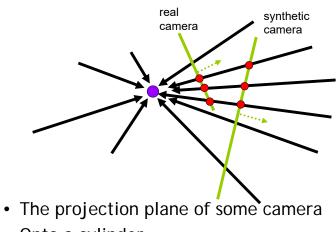


Kaidan panoramic tripod head

Translation model

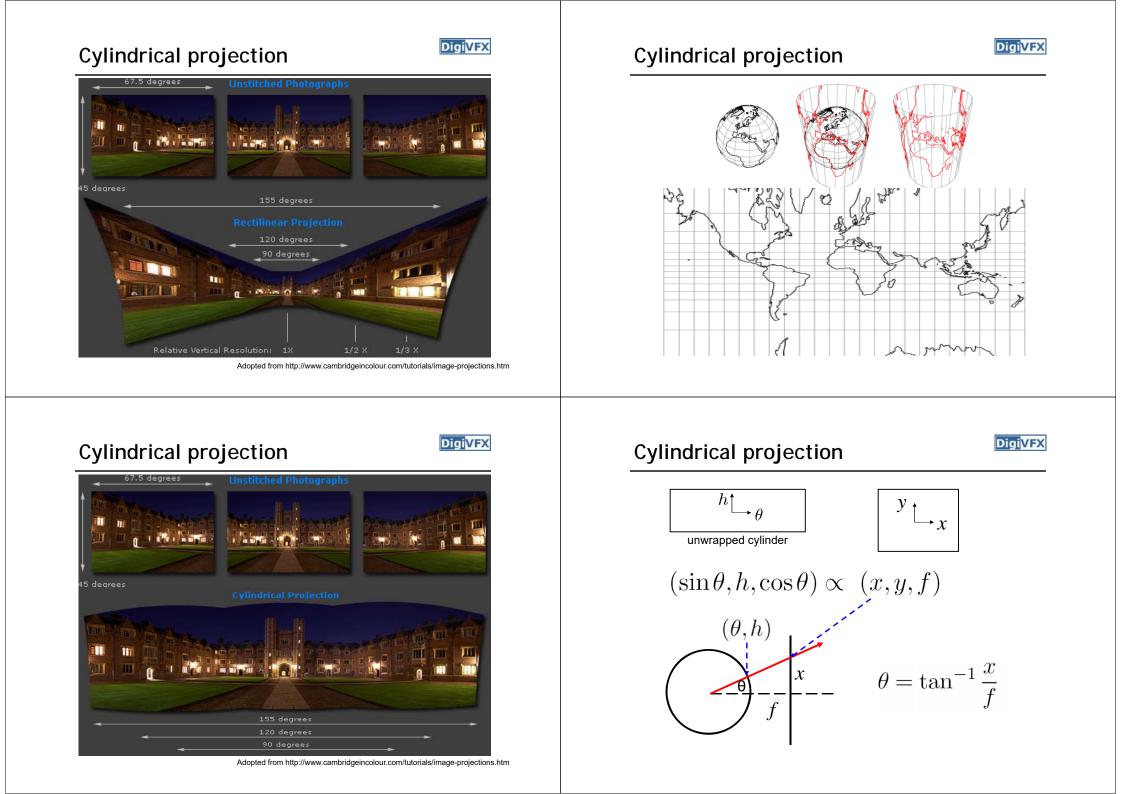


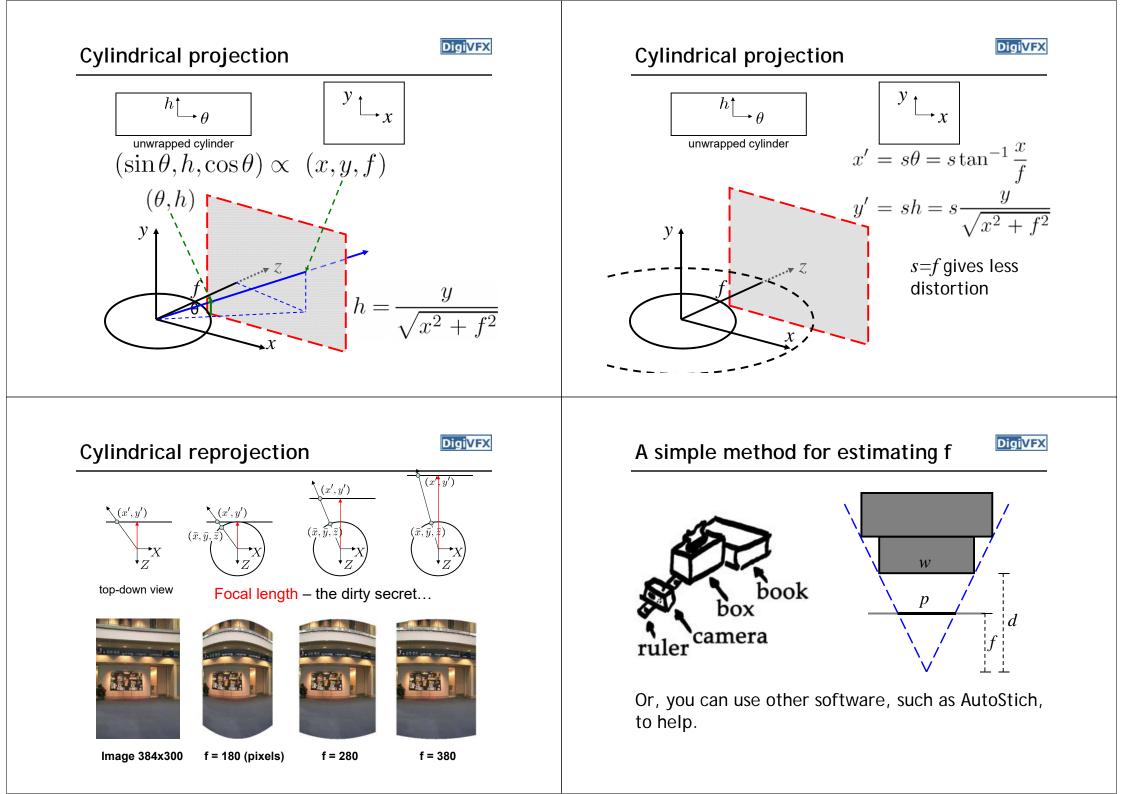
Where should the synthetic camera be



• Onto a cylinder







Input images



Cylindrical warping



Blending

DigiVFX

DigiVFX

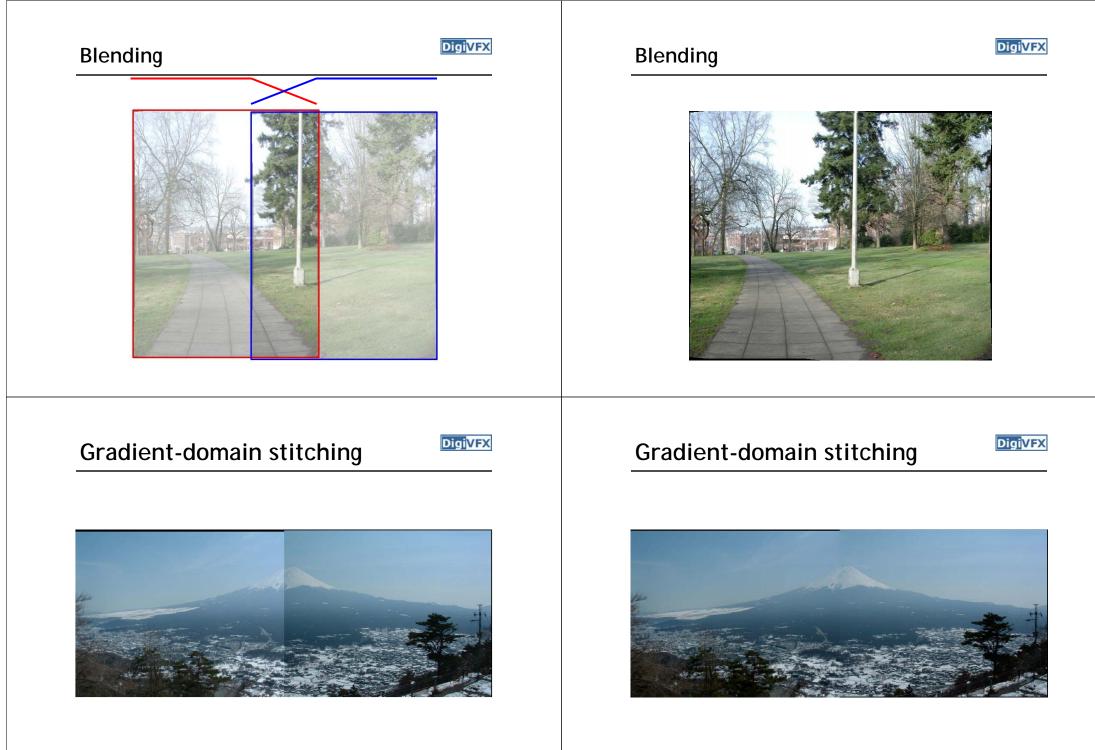
• Why blending: parallax, lens distortion, scene motion, exposure difference

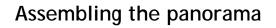
Blending



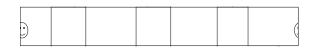






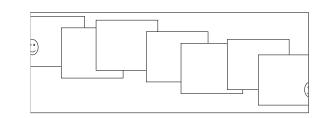


DigiVFX

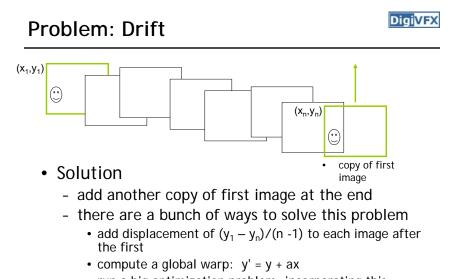


• Stitch pairs together, blend, then crop





- Error accumulation
 - small errors accumulate over time



- run a big optimization problem, incorporating this constraint
 - best solution, but more complicated
 - known as "bundle adjustment"

End-to-end alignment and crop







DigiVFX DigiVFX Rectangling panoramas Rectangling panoramas DABBARILLING N ODDDDDDDDDD (a) input panorama nanananan (c) cropping (d) our content-aware warping video DigiVFX **DigiVFX** Rectangling panoramas Viewer: panorama



example: http://www.cs.washington.edu/education/courses/cse590ss/01wi/projects/project1/students/dougz/index.html

Viewer: texture mapped model



example: http://www.panoramas.dk/

365-GB panorama (biggest on the earth)



Mont Blanc / Canon 70D / 70,000 images / videovideoweb2-week shooting / 2-month processingLondon

Cylindrical panorama



DigiVFX

- 1. Take pictures on a tripod (or handheld)
- 2. Warp to cylindrical coordinate
- 3. Compute pairwise alignments
- 4. Fix up the end-to-end alignment
- 5. Blending
- 6. Crop the result and import into a viewer

Determine pairwise alignment?



- Feature-based methods: only use feature points to estimate parameters
- We will study the "Recognising panorama" paper published in ICCV 2003
- Run SIFT (or other feature algorithms) for each image, find feature matches.

Determine pairwise alignment

- Digi<mark>VFX</mark>
- p'=Mp, where M is a transformation matrix, p and p' are feature matches
- It is possible to use more complicated models such as affine or perspective
- For example, assume M is a 2x2 matrix

$$\begin{pmatrix} x' \\ y' \end{pmatrix} = \begin{pmatrix} m_{11} & m_{12} \\ m_{21} & m_{22} \end{pmatrix} \begin{pmatrix} x \\ y \end{pmatrix}$$

• Find M with the least square error

$$\sum_{i=1}^n (Mp - p')^2$$

Normal equation

DigiVFX

Given an overdetermined system

 $\mathbf{A}\mathbf{x} = \mathbf{b}$

the normal equation is that which minimizes the sum of the square differences between left and right sides

$$\mathbf{A}^{\mathrm{T}}\mathbf{A}\mathbf{x} = \mathbf{A}^{\mathrm{T}}\mathbf{b}$$

Why?

Determine pairwise alignment

$$\begin{pmatrix} x' \\ y' \end{pmatrix} = \begin{pmatrix} m_{11} & m_{12} \\ m_{21} & m_{22} \end{pmatrix} \begin{pmatrix} x \\ y \end{pmatrix} \qquad \qquad x_1 m_{11} + y_1 m_{12} = x_1' \\ x_1 m_{21} + y_1 m_{22} = y_1'$$

Overdetermined system

$$\begin{pmatrix} x_{1} & y_{1} & 0 & 0 \\ 0 & 0 & x_{1} & y_{1} \\ x_{2} & y_{2} & 0 & 0 \\ \vdots & \vdots & \vdots & \vdots \\ x_{n} & y_{n} & 0 & 0 \\ 0 & 0 & x_{n} & y_{n} \end{pmatrix} \begin{pmatrix} m_{11} \\ m_{12} \\ m_{21} \\ m_{22} \end{pmatrix} = \begin{pmatrix} x_{1}' \\ y_{1}' \\ x_{2}' \\ \vdots \\ x_{n}' \\ y_{n}' \end{pmatrix}$$

Normal equation

Digi<mark>VFX</mark>

$$E(\mathbf{x}) = (\mathbf{A}\mathbf{x} - \mathbf{b})^2$$

$$\begin{bmatrix} a_{11} & \dots & a_{1m} \\ \vdots & & \vdots \\ \vdots & & \vdots \\ a_{n1} & \dots & a_{nm} \end{bmatrix} \begin{bmatrix} x_1 \\ \vdots \\ x_m \end{bmatrix} = \begin{bmatrix} b_1 \\ \vdots \\ \vdots \\ \vdots \\ b_n \end{bmatrix}$$

nxm, *n* equations, *m* variables

Digi<mark>VFX</mark>

DigiVFX

Normal equation

$$\mathbf{A}\mathbf{x} - \mathbf{b} = \begin{bmatrix} \sum_{j=1}^{m} a_{1j} x_j \\ \vdots \\ \sum_{j=1}^{m} a_{ij} x_j \\ \vdots \\ \sum_{j=1}^{m} a_{nj} x_j \end{bmatrix} - \begin{bmatrix} b_1 \\ \vdots \\ b_i \\ \vdots \\ b_n \end{bmatrix} = \begin{bmatrix} \left(\sum_{j=1}^{m} a_{1j} x_j\right) - b_1 \\ \vdots \\ \left(\sum_{j=1}^{m} a_{nj} x_j\right) - b_i \\ \vdots \\ \left(\sum_{j=1}^{m} a_{nj} x_j\right) - b_n \end{bmatrix}^2$$
$$E(\mathbf{x}) = (\mathbf{A}\mathbf{x} - \mathbf{b})^2 = \sum_{i=1}^{n} \left[\left(\sum_{j=1}^{m} a_{ij} x_j\right) - b_i \right]^2$$

Normal equation

$$E(\mathbf{x}) = (\mathbf{A}\mathbf{x} - \mathbf{b})^2 = \sum_{i=1}^n \left[\left(\sum_{j=1}^m a_{ij} x_j \right) - b_i \right]^2$$
$$0 = \frac{\partial E}{\partial x_1} = \sum_{i=1}^n 2 \left[\left(\sum_{j=1}^m a_{ij} x_j \right) - b_i \right] a_{i1}$$
$$= 2 \sum_{i=1}^n a_{i1} \sum_{j=1}^m a_{ij} x_j - 2 \sum_{i=1}^n a_{i1} b_i$$

$$0 = \frac{\partial E}{\partial \mathbf{x}} = 2(\mathbf{A}^{\mathrm{T}}\mathbf{A}\mathbf{x} - \mathbf{A}^{\mathrm{T}}\mathbf{b}) \rightarrow \mathbf{A}^{\mathrm{T}}\mathbf{A}\mathbf{x} = \mathbf{A}^{\mathrm{T}}\mathbf{b}$$

Digi<mark>VFX</mark>

 $(\mathbf{A}\mathbf{x}-\mathbf{b})^2$

Normal equation

Normal equation

$$\frac{(\mathbf{A}\mathbf{x} - \mathbf{b})^{2}}{= (\mathbf{A}\mathbf{x} - \mathbf{b})^{T} (\mathbf{A}\mathbf{x} - \mathbf{b})} \\
= ((\mathbf{A}\mathbf{x})^{T} - \mathbf{b}^{T}) (\mathbf{A}\mathbf{x} - \mathbf{b}) \\
= (\mathbf{x}^{T}\mathbf{A}^{T} - \mathbf{b}^{T}) (\mathbf{A}\mathbf{x} - \mathbf{b}) \\
= \mathbf{x}^{T}\mathbf{A}^{T}\mathbf{A}\mathbf{x} - \mathbf{b}^{T}\mathbf{A}\mathbf{x} - \mathbf{x}^{T}\mathbf{A}^{T}\mathbf{b} + \mathbf{b}^{T}\mathbf{b} \\
= \mathbf{x}^{T}\mathbf{A}^{T}\mathbf{A}\mathbf{x} - (\mathbf{A}^{T}\mathbf{b})^{T}\mathbf{x} - (\mathbf{A}^{T}\mathbf{b})^{T}\mathbf{x} + \mathbf{b}^{T}\mathbf{b} \\
= \frac{\partial E}{\partial \mathbf{x}} = 2\mathbf{A}^{T}\mathbf{A}\mathbf{x} - 2\mathbf{A}^{T}\mathbf{b}$$



DigiVFX

Determine pairwise alignment



DigiVFX

How bia?

Smaller is better

- p'=Mp, where M is a transformation matrix, p and p' are feature matches
- For translation model, it is easier.

$$E = \sum_{i=1}^{n} \left[\left(m_1 + x_i - x_i^{'} \right)^2 + \left(m_2 + y_i - y_i^{'} \right)^2 \right]$$

 $0 = \frac{\partial E}{\partial m_1}$

RANSAC algorithm

(1) draw *n* samples randomly

number of inlier points c

Output Θ with the largest c

Run k times:

• What if the match is false? Avoid impact of outliers.

– How many times?

its distance to the fitted model, count the

How to define?

Depends on the problem.

(2) fit parameters Θ with these *n* samples (3) for each of other *N*-*n* points, calculate

RANSAC

- RANSAC = Random Sample Consensus
- An algorithm for robust fitting of models in the presence of many data outliers
- Compare to robust statistics
- Given N data points x_i, assume that majority of them are generated from a model with parameters Θ, try to recover Θ.

How to determine k

Digi<mark>VFX</mark>

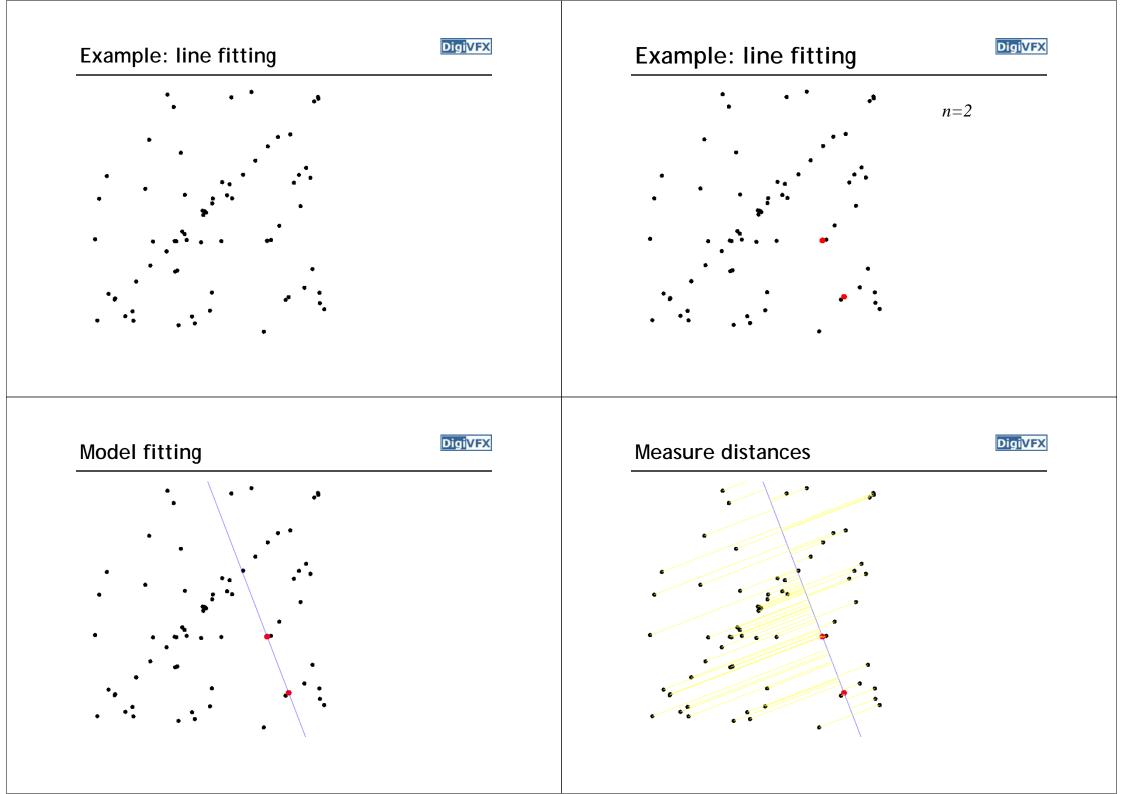
DIGIVEX

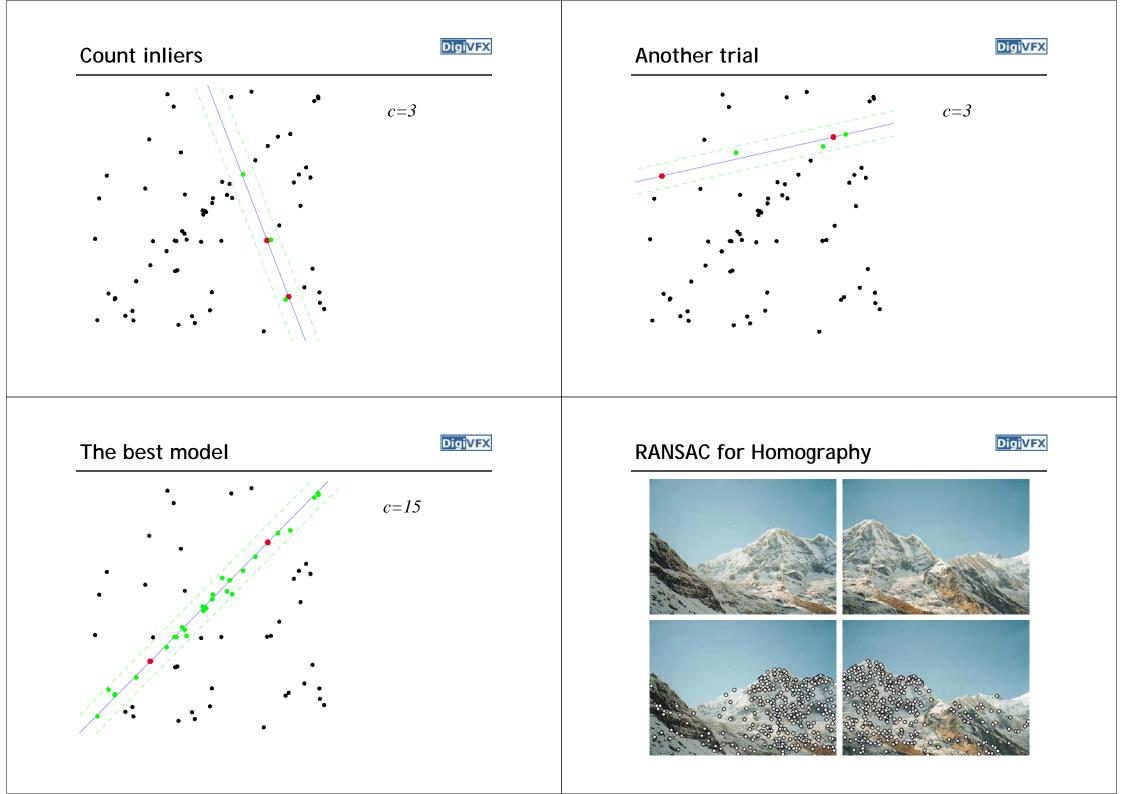
p: probability of real inliers*P*: probability of success after k trials

$$P = 1 - (1 - p^{n})^{k}$$
n samples are all inliers
a failure
failure after k trials
$$k = \frac{\log(1 - P)}{\log(1 - p^{n})}$$
 for $P = 0.99$
$$\frac{n p k}{3 0.5 35}$$

$$\frac{1}{6 0.6 97}$$

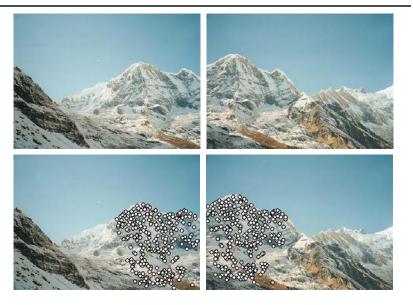
$$\frac{1}{6 0.5 293}$$





RANSAC for Homography





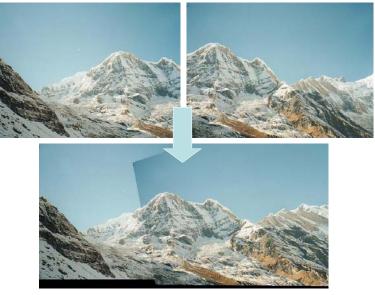
Tools for image stitching

DigiVFX

- Hugin
- Image Composite Editor
- AutoStitch
- Google photo
- ...

RANSAC for Homography

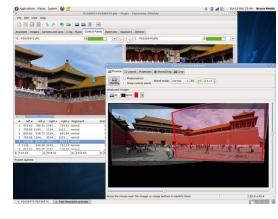




Applications of panorama in VFX



- Background plates
- Image-based lighting



Troy (image-based lighting)





http://www.cgnetworks.com/story_custom.php?story_id=2195&page=4

Spiderman 2 (background plate)





Reference

DigiVFX

- Richard Szeliski, <u>Image Alignment and Stitching: A Tutorial</u>, *Foundations and Trends in Computer Graphics and Computer Vision*, 2(1):1-104, December 2006.
- R. Szeliski and H.-Y. Shum. <u>Creating full view panoramic image</u> mosaics and texture-mapped models, SIGGRAPH 1997, pp251-258.
- M. Brown, D. G. Lowe, <u>Recognising Panoramas</u>, ICCV 2003.