

# High dynamic range imaging

Digital Visual Effects

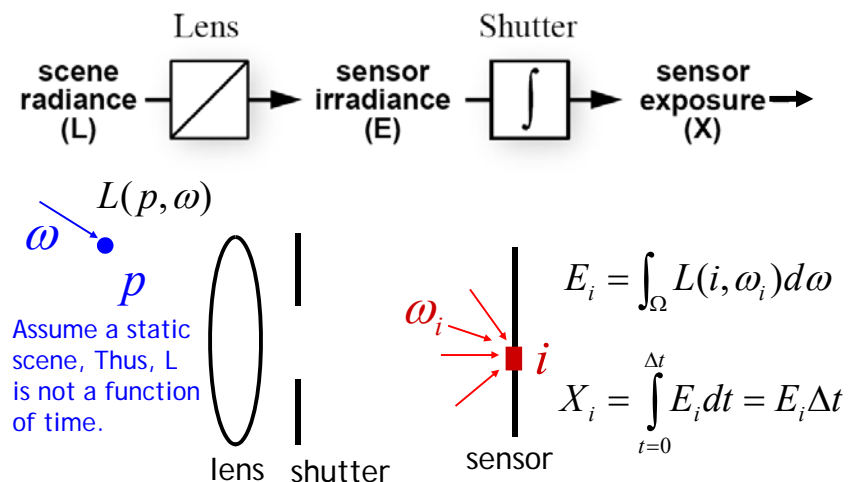
Yung-Yu Chuang

with slides by Fredo Durand, Brian Curless, Steve Seitz, Paul Debevec and Alexei Efros

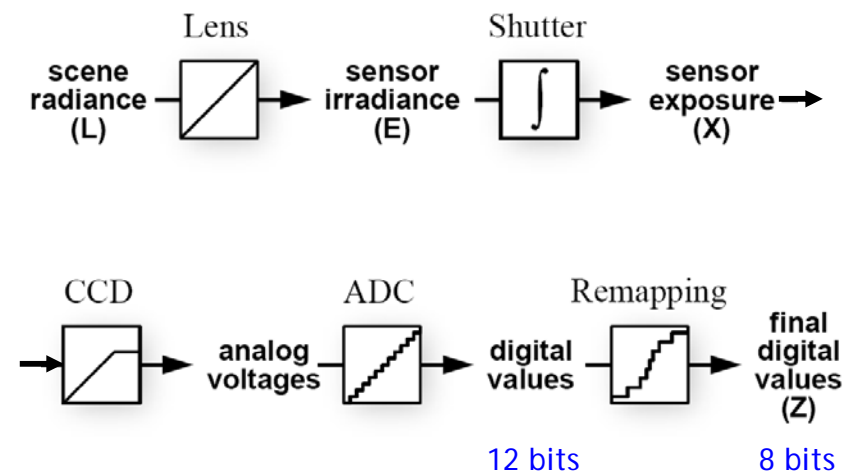
## Camera is an imperfect device

- Camera is an imperfect device for measuring the radiance distribution of a scene because it cannot capture the full spectral content and dynamic range.
- Limitations in sensor design prevent cameras from capturing all information passed by lens.

## Camera pipeline

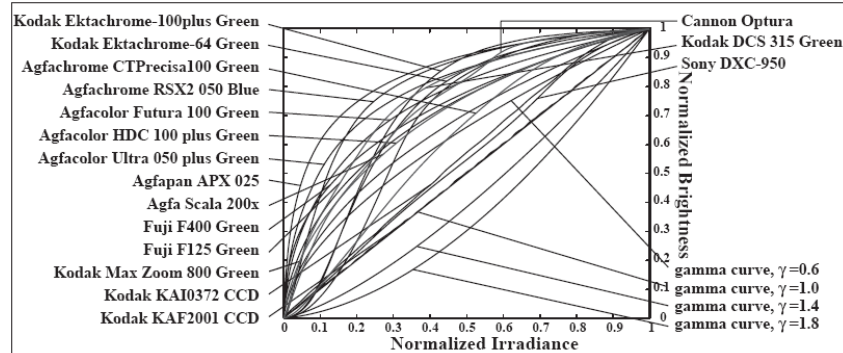


## Camera pipeline

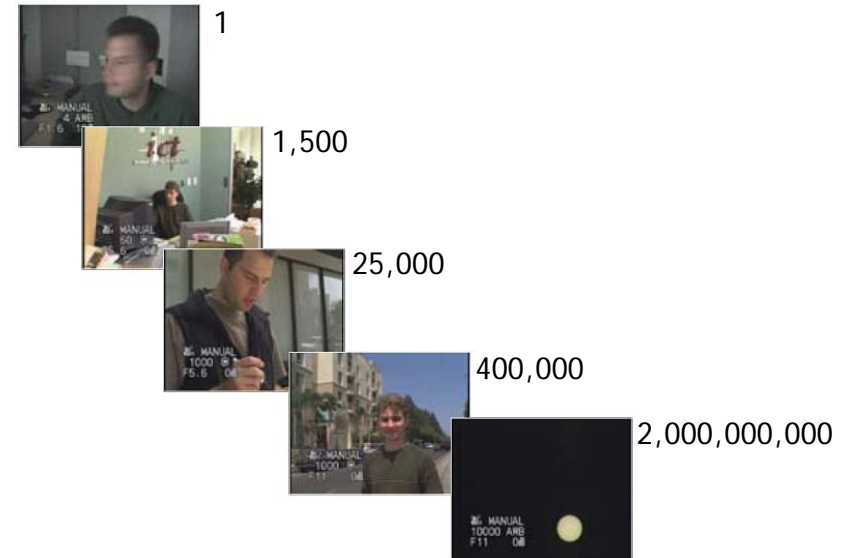


## Real-world response functions

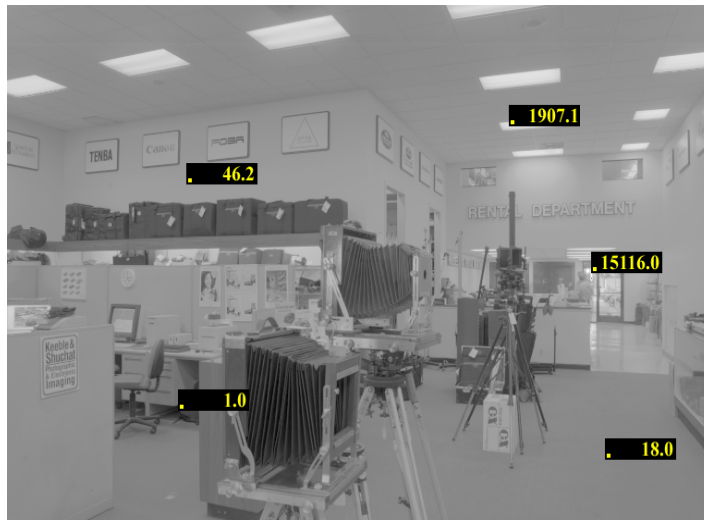
In general, the response function is not provided by camera makers who consider it part of their proprietary product differentiation. In addition, they are beyond the standard gamma curves.



## The world is high dynamic range

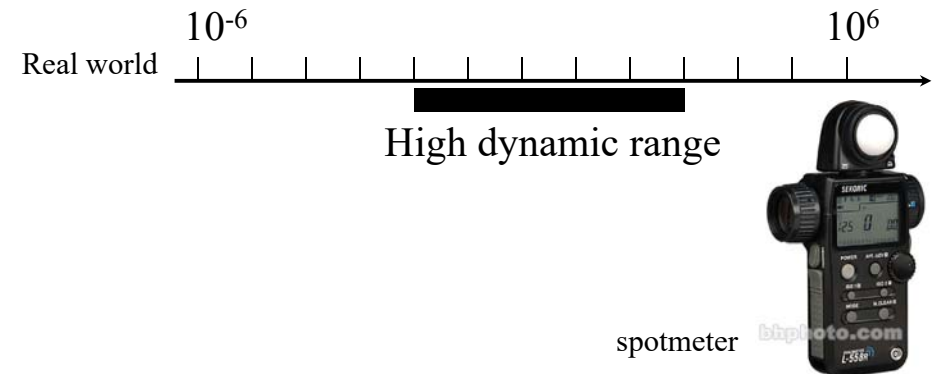


## The world is high dynamic range



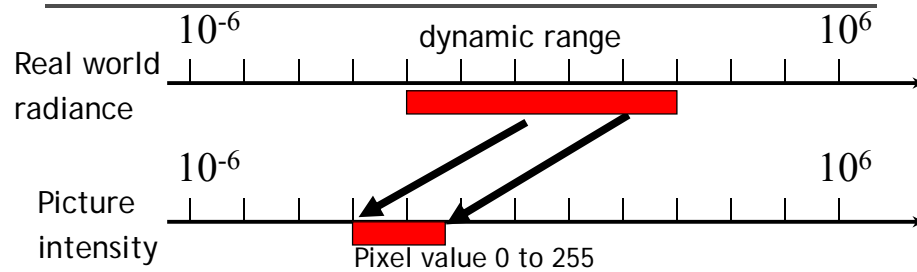
## Real world dynamic range

- Eye can adapt from  $\sim 10^{-6}$  to  $10^6$  cd/m<sup>2</sup>
- Often 1 : 100,000 in a scene
- Typical 1:50, max 1:500 for pictures



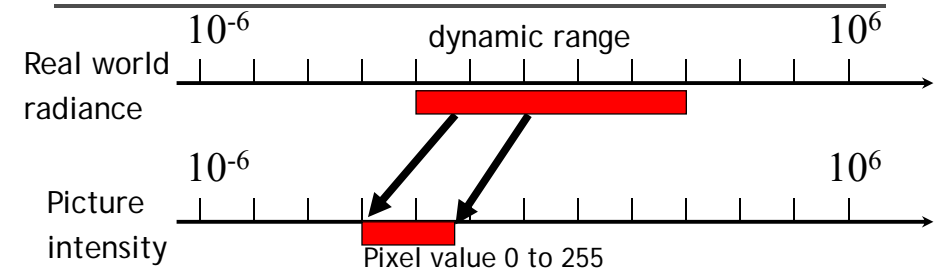
## Short exposure

DigiVFX



## Long exposure

DigiVFX



## Camera is not a photometer

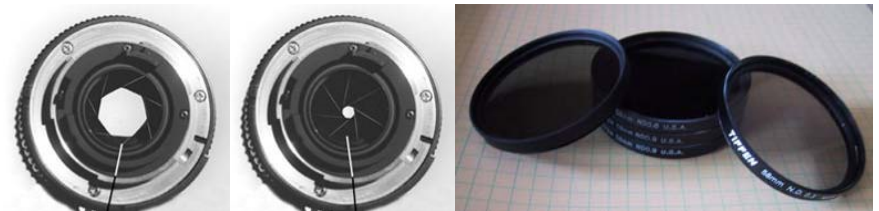
DigiVFX

- Limited dynamic range
  - ⇒ Perhaps use multiple exposures?
- Unknown, nonlinear response
  - ⇒ Not possible to convert pixel values to radiance
- Solution:
  - Recover response curve from multiple exposures, then reconstruct the *radiance map*

## Varying exposure

DigiVFX

- Ways to change exposure
  - Shutter speed
  - Aperture
  - Neutral density filters



## Shutter speed

DigiVFX

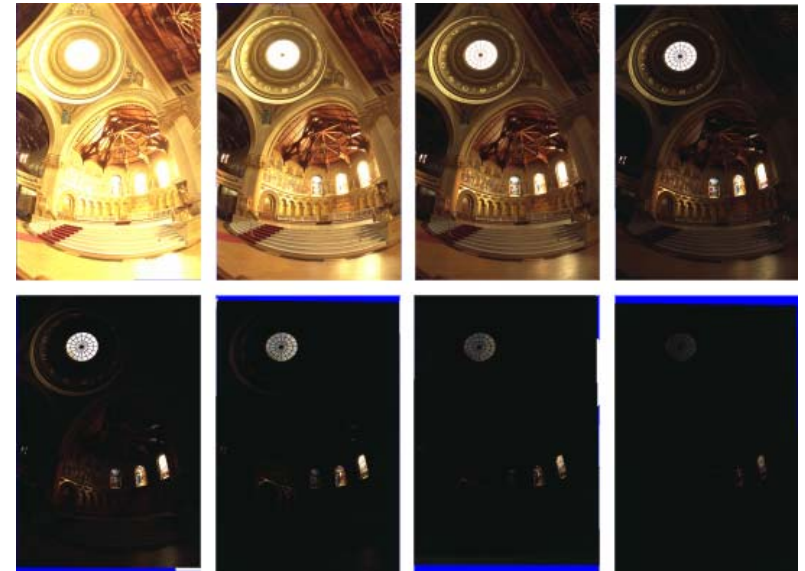
- Note: shutter times usually obey a power series - each "stop" is a factor of 2
- $\frac{1}{4}$ ,  $\frac{1}{8}$ ,  $\frac{1}{15}$ ,  $\frac{1}{30}$ ,  $\frac{1}{60}$ ,  $\frac{1}{125}$ ,  $\frac{1}{250}$ ,  $\frac{1}{500}$ ,  $\frac{1}{1000}$  sec

Usually really is:

$\frac{1}{4}$ ,  $\frac{1}{8}$ ,  $\frac{1}{16}$ ,  $\frac{1}{32}$ ,  $\frac{1}{64}$ ,  $\frac{1}{128}$ ,  $\frac{1}{256}$ ,  $\frac{1}{512}$ ,  $\frac{1}{1024}$  sec

## Varying shutter speeds

DigiVFX



## HDRI capturing from multiple exposures

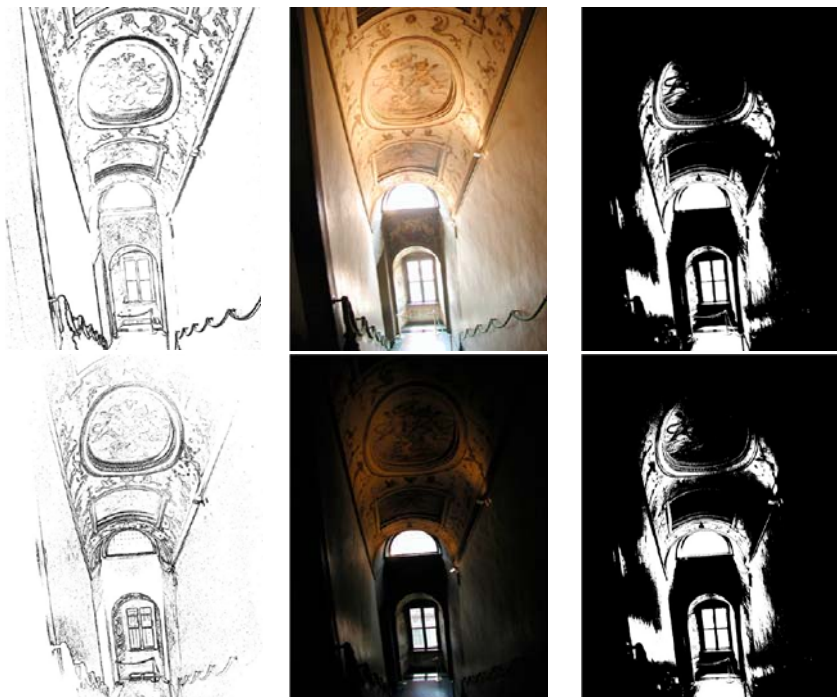
DigiVFX

- Capture images with multiple exposures
- Image alignment (even if you use tripod, it is suggested to run alignment)
- Response curve recovery
- Ghost/flare removal

## Image alignment

DigiVFX

- We will introduce a fast and easy-to-implement method for this task, called Median Threshold Bitmap (MTB) alignment technique.
- Consider only integral translations. It is enough empirically.
- The inputs are N grayscale images. (You can either use the green channel or convert into grayscale by  $Y = (54R + 183G + 19B) / 256$ )
- MTB is a binary image formed by thresholding the input image using the median of intensities.



## Why is MTB better than gradient?

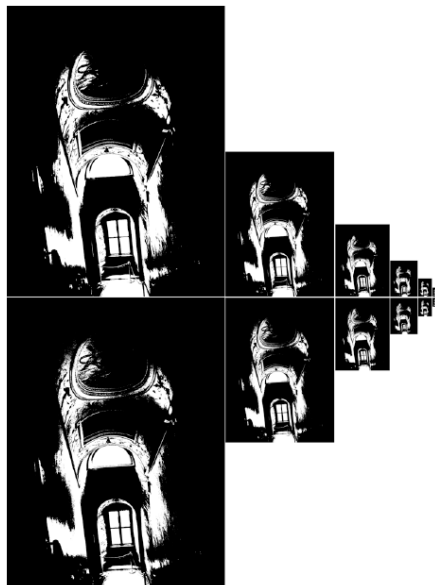
DigiVFX

- Edge-detection filters are dependent on image exposures
- Taking the difference of two edge bitmaps would not give a good indication of where the edges are misaligned.

## Search for the optimal offset

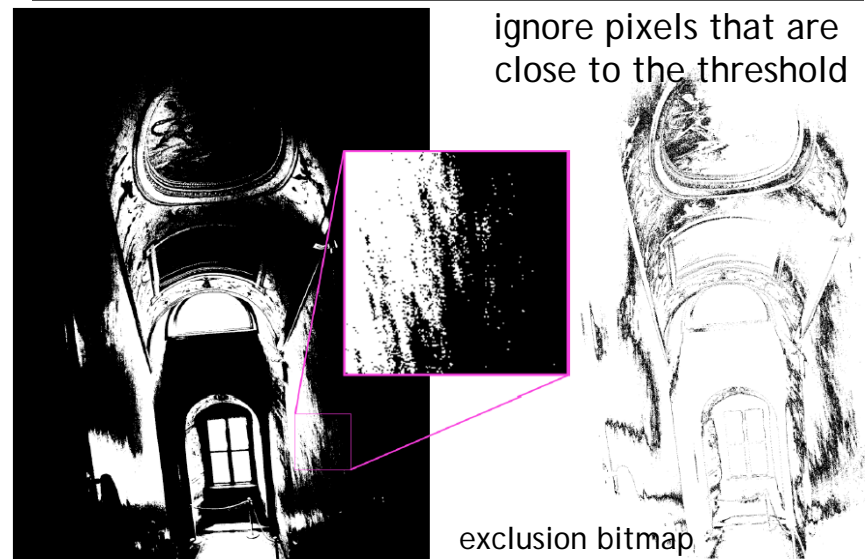
DigiVFX

- Try all possible offsets.
- Gradient descent
- Multiscale technique
- $\log(\text{max\_offset})$  levels
- Try 9 possibilities for the top level
- Scale by 2 when passing down; try its 9 neighbors



## Threshold noise

DigiVFX



## Efficiency considerations

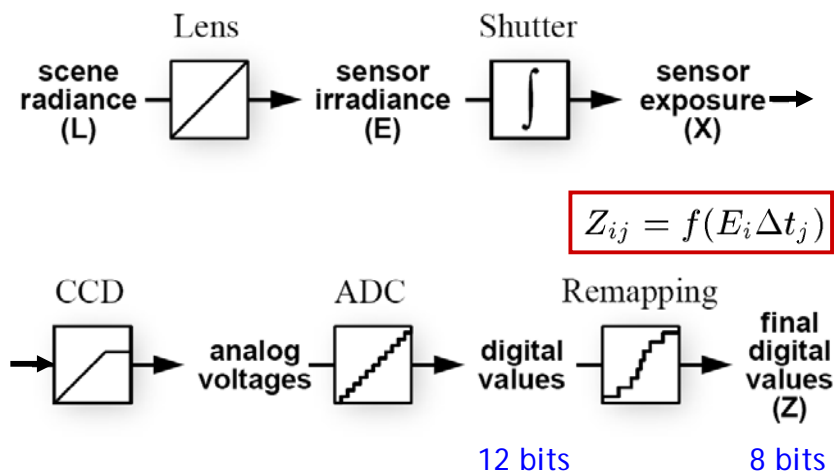
- XOR for taking difference
- AND with exclusion maps
- Bit counting by table lookup

## Results

Success rate = 84%. 10% failure due to rotation. 3% for excessive motion and 3% for too much high-frequency content.

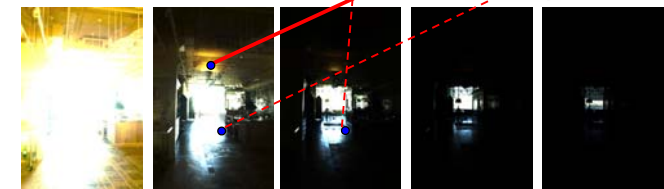
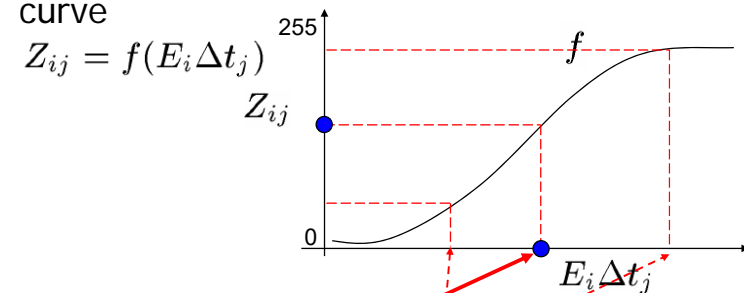


## Recovering response curve



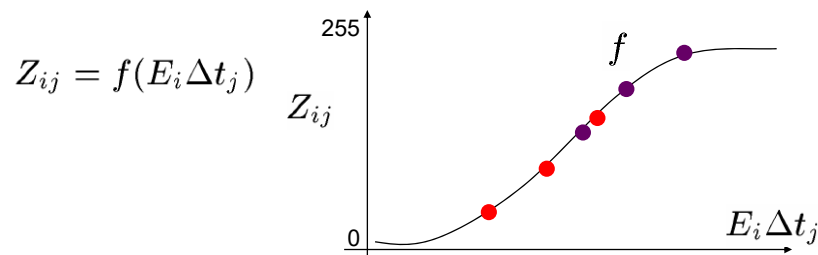
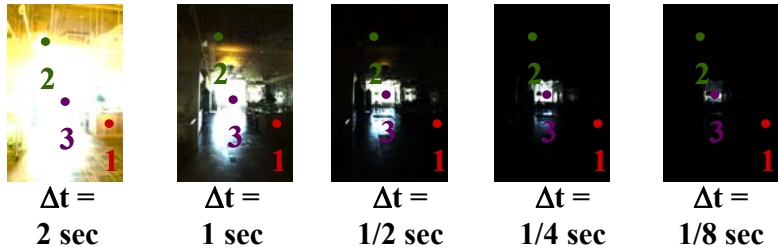
## Recovering response curve

- We want to obtain the inverse of the response curve



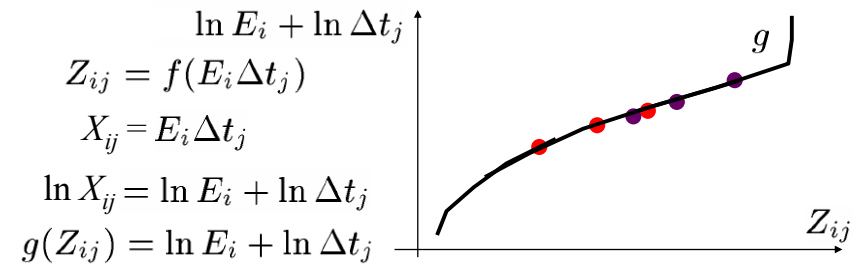
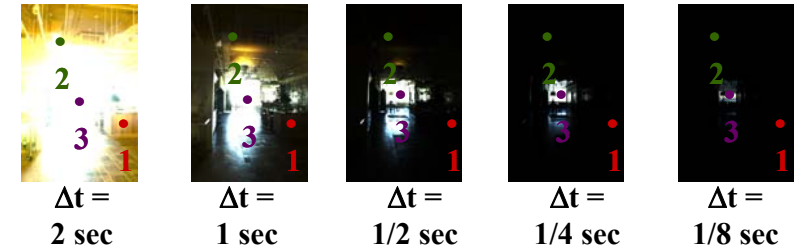
## Recovering response curve

### Image series



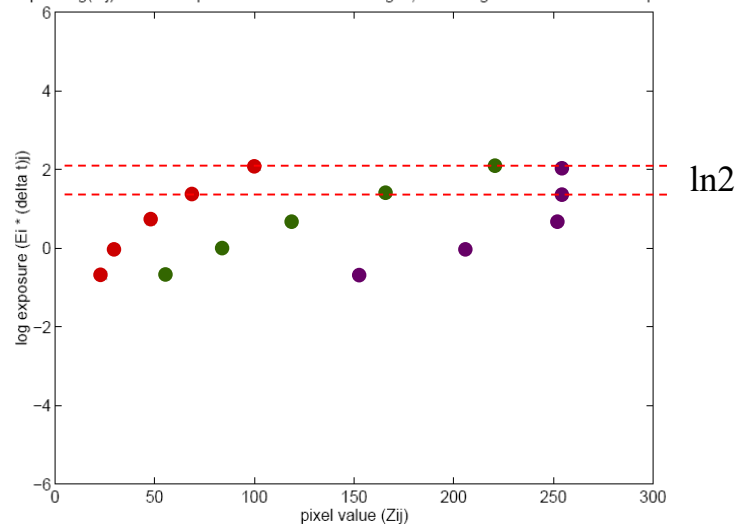
## Recovering response curve

### Image series



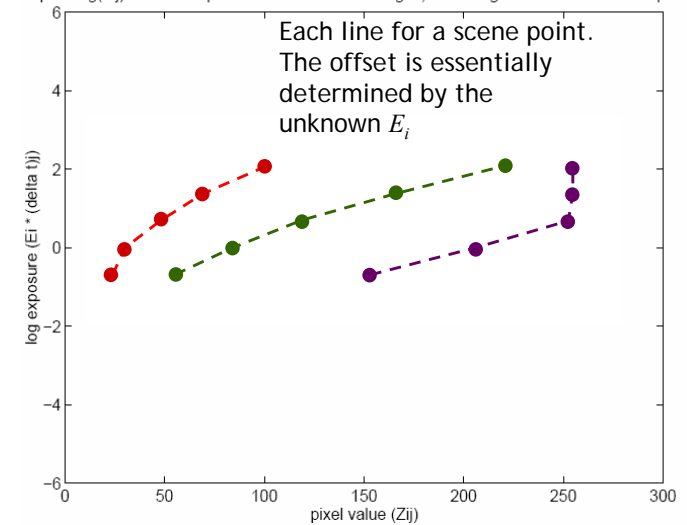
## Idea behind the math

plot of  $g(Z_{ij})$  from three pixels observed in five images, assuming unit radiance at each pixel

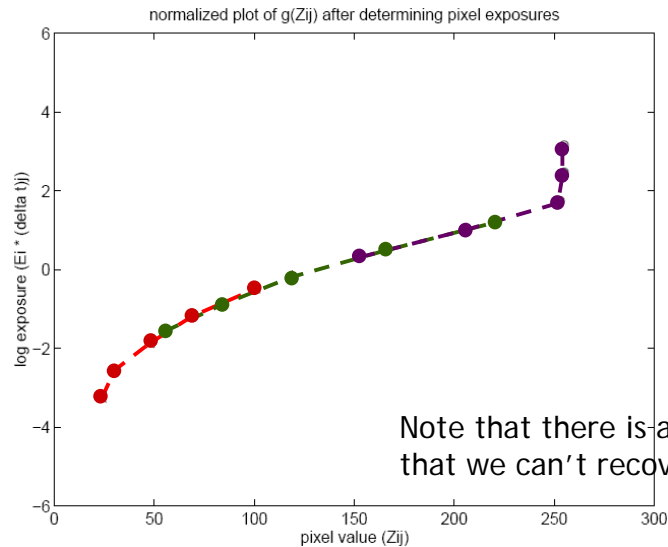


## Idea behind the math

plot of  $g(Z_{ij})$  from three pixels observed in five images, assuming unit radiance at each pixel



## Idea behind the math



## Basic idea

- Design an objective function
- Optimize it

## Math for recovering response curve

$$Z_{ij} = f(E_i \Delta t_j)$$

$f$  is monotonic, it is invertible

$$\ln f^{-1}(Z_{ij}) = \ln E_i + \ln \Delta t_j$$

let us define function  $g = \ln f^{-1}$

$$g(Z_{ij}) = \ln E_i + \ln \Delta t_j$$

minimize the following

$$\mathcal{O} = \sum_{i=1}^N \sum_{j=1}^P [g(Z_{ij}) - \ln E_i - \ln \Delta t_j]^2 + \lambda \sum_{z=Z_{min}+1}^{Z_{max}-1} g''(z)^2$$

$$g''(z) = g(z-1) - 2g(z) + g(z+1)$$

## Recovering response curve

- The solution can be only up to a scale, add a constraint

$$g(Z_{mid}) = 0, \text{ where } Z_{mid} = \frac{1}{2}(Z_{min} + Z_{max})$$

- Add a hat weighting function

$$w(z) = \begin{cases} z - Z_{min} & \text{for } z \leq \frac{1}{2}(Z_{min} + Z_{max}) \\ Z_{max} - z & \text{for } z > \frac{1}{2}(Z_{min} + Z_{max}) \end{cases}$$

$$\mathcal{O} = \sum_{i=1}^N \sum_{j=1}^P \{w(Z_{ij}) [g(Z_{ij}) - \ln E_i - \ln \Delta t_j]\}^2 + \lambda \sum_{z=Z_{min}+1}^{Z_{max}-1} [w(z)g''(z)]^2$$

## Recovering response curve

- We want  $N(P-1) > (Z_{max} - Z_{min})$   
If  $P=11$ ,  $N \sim 25$  (typically 50 is used)
- We prefer that selected pixels are well distributed and sampled from constant regions. They picked points by hand.
- It is an overdetermined system of linear equations and can be solved using SVD

## How to optimize?

$$\mathcal{O} = \sum_{i=1}^N \sum_{j=1}^P \{w(Z_{ij}) [g(Z_{ij}) - \ln E_i - \ln \Delta t_j]\}^2 + \lambda \sum_{z=Z_{min}+1}^{Z_{max}-1} [w(z)g''(z)]^2$$

## How to optimize?

$$\mathcal{O} = \sum_{i=1}^N \sum_{j=1}^P \{w(Z_{ij}) [g(Z_{ij}) - \ln E_i - \ln \Delta t_j]\}^2 + \lambda \sum_{z=Z_{min}+1}^{Z_{max}-1} [w(z)g''(z)]^2$$

1. Set partial derivatives to zero
- 2.

$$\min \sum_{i=1}^N (\mathbf{a}_i \mathbf{x} - \mathbf{b}_i)^2 \rightarrow \text{least-square solution of } \begin{bmatrix} \mathbf{a}_1 \\ \mathbf{a}_2 \\ \vdots \\ \mathbf{a}_N \end{bmatrix} \mathbf{x} = \begin{bmatrix} \mathbf{b}_1 \\ \mathbf{b}_2 \\ \vdots \\ \mathbf{b}_N \end{bmatrix}$$

## Sparse linear system

$$\begin{matrix} & 256 & n & & \\ \begin{matrix} n \times p \\ 1 \\ 254 \end{matrix} & \left[ \begin{array}{c} \\ \\ \\ \end{array} \right] & & \begin{bmatrix} g(0) \\ \vdots \\ g(255) \\ \ln E_1 \\ \vdots \\ \ln E_n \end{bmatrix} & = & \begin{bmatrix} \\ \\ \\ \end{bmatrix} \\ & & & & & \mathbf{Ax}=\mathbf{b} \end{matrix}$$

## Questions

- Will  $g(127)=0$  always be satisfied? Why or why not?
- How to find the least-square solution for an over-determined system?

## Least-square solution for a linear system

$$\underset{\substack{m \times n \quad n \\ m > n}}{\mathbf{A}} \mathbf{x} = \underset{m}{\mathbf{b}}$$

They are often mutually incompatible. We instead find  $\mathbf{x}$  to minimize the norm  $\|\mathbf{Ax} - \mathbf{b}\|$  of the residual vector  $\mathbf{Ax} - \mathbf{b}$ . If there are multiple solutions, we prefer the one with the minimal length  $\|\mathbf{x}\|$ .

## Least-square solution for a linear system

If we perform SVD on  $\mathbf{A}$  and rewrite it as

$$\mathbf{A} = \mathbf{U}\mathbf{\Sigma}\mathbf{V}^T$$

then  $\hat{\mathbf{x}} = \underset{\text{pseudo inverse}}{\mathbf{V}\mathbf{\Sigma}^+\mathbf{U}^T} \mathbf{b}$  is the least-square solution.

$$\mathbf{\Sigma}^+ = \begin{bmatrix} 1/\sigma_1 & & & 0 & \dots & 0 \\ & \ddots & & & & \\ & & 1/\sigma_r & & & \\ & & & 0 & & \\ & & & & \ddots & \\ & & & & & 0 & 0 & \dots & 0 \end{bmatrix}$$

## Proof

find  $\mathbf{x}$  使  $\|\mathbf{Ax} - \mathbf{b}\|$  最小

$$\|\mathbf{Ax} - \mathbf{b}\| = \|\mathbf{U}\mathbf{\Sigma}\mathbf{V}^T\mathbf{x} - \mathbf{b}\|$$

$$= \|\mathbf{U}(\mathbf{\Sigma}\mathbf{V}^T\mathbf{x} - \mathbf{U}^T\mathbf{b})\|$$

$$= \|\mathbf{\Sigma}\mathbf{V}^T\mathbf{x} - \mathbf{U}^T\mathbf{b}\|$$

$\mathbf{U}$  是 rotation  
不动长度

$$\text{令 } \mathbf{y} = \mathbf{V}^T\mathbf{x} \quad \mathbf{c} = \mathbf{U}^T\mathbf{b}$$

则相当于求  $\mathbf{y}$  使  $\|\mathbf{\Sigma}\mathbf{y} - \mathbf{c}\|$  最小

$$\begin{pmatrix} \sigma_1 & & & 0 \\ & \ddots & & \\ & & \sigma_r & \\ & & & \ddots \\ 0 & & & & 0 \end{pmatrix} \begin{pmatrix} y_1 \\ \vdots \\ y_r \\ \vdots \\ y_n \end{pmatrix} = \begin{pmatrix} c_1 \\ \vdots \\ c_r \\ \vdots \\ c_n \end{pmatrix}$$

## Proof

$$\Rightarrow y_i = \frac{c_i}{\sigma_i} \quad i=1 \dots r \quad y_i = 0 \quad i=r+1 \dots n$$

$$\Rightarrow \tilde{y} = \begin{pmatrix} \cancel{1/\sigma_1} & \dots & 0 \\ & \ddots & \\ 0 & \dots & 1/\sigma_r & \dots & 0 \end{pmatrix} \begin{pmatrix} c_1 \\ \vdots \\ c_r \\ \vdots \\ c_n \end{pmatrix} = \Sigma^+ C$$

$$\Rightarrow \tilde{y} = V^T \tilde{x} = \Sigma^+ C = \Sigma^+ U^T b$$

$$\Rightarrow \tilde{x} = V \Sigma^+ U^T b$$

## Libraries for SVD

- Matlab
- GSL
- Boost
- LAPACK
- ATLAS

## Matlab code

```
%
% gsolve.m - Solve for imaging system response function
%
% Given a set of pixel values observed for several pixels in several
% images with different exposure times, this function returns the
% imaging system's response function g as well as the log film irradiance
% values for the observed pixels.
%
% Assumes:
%
%   Zmin = 0
%   Zmax = 255
%
% Arguments:
%
%   Z(i,j) is the pixel values of pixel location number i in image j
%   B(j)   is the log delta t, or log shutter speed, for image j
%   l      is lambda, the constant that determines the amount of smoothness
%   w(z)   is the weighting function value for pixel value z
%
% Returns:
%
%   g(z)   is the log exposure corresponding to pixel value z
%   lE(i)  is the log film irradiance at pixel location i
%
```

## Matlab code

```
function [g,lE]=gsolve(Z,B,l,w)

n = 256;
A = zeros(size(Z,1)*size(Z,2)+n+1,n+size(Z,1));
b = zeros(size(A,1),1);

k = 1;                                %% Include the data-fitting equations
for i=1:size(Z,1)
    for j=1:size(Z,2)
        wij = w(Z(i,j)+1);
        A(k,Z(i,j)+1) = wij; A(k,n+1) = -wij; b(k,1) = wij * B(j);
        k=k+1;
    end
end

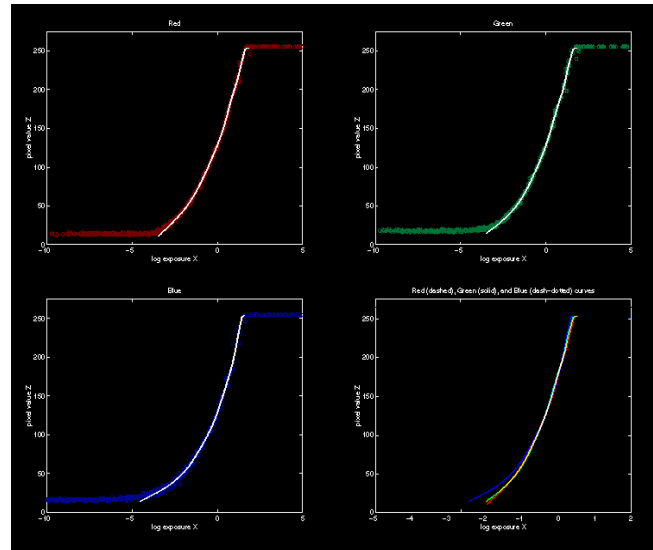
A(k,129) = 1;                          %% Fix the curve by setting its middle value to 0
k=k+1;

for i=1:n-2                             %% Include the smoothness equations
    A(k,i)=l*w(i+1); A(k,i+1)=-2*l*w(i+1); A(k,i+2)=l*w(i+1);
    k=k+1;
end

x = A\b;                                %% Solve the system using SVD

g = x(1:n);
lE = x(n+1:size(x,1));
```

## Recovered response function



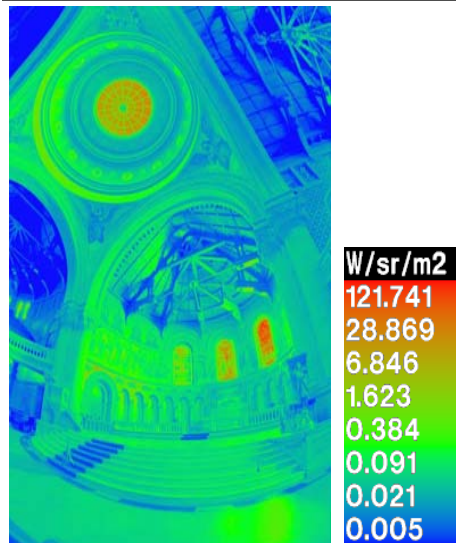
## Constructing HDR radiance map

$$\ln E_i = g(Z_{ij}) - \ln \Delta t_j$$

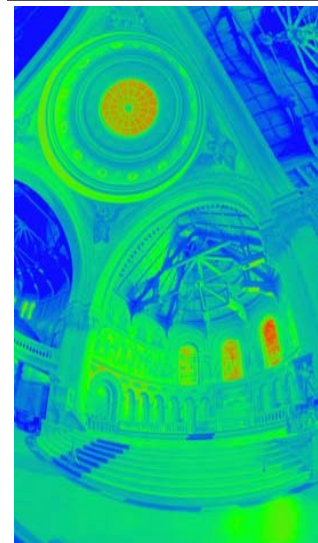
combine pixels to reduce noise and obtain a more reliable estimation

$$\ln E_i = \frac{\sum_{j=1}^P w(Z_{ij})(g(Z_{ij}) - \ln \Delta t_j)}{\sum_{j=1}^P w(Z_{ij})}$$

## Reconstructed radiance map



## What is this for?



- Human perception
- Vision/graphics applications

## Automatic ghost removal

DigiVFX



before



after

## Weighted variance

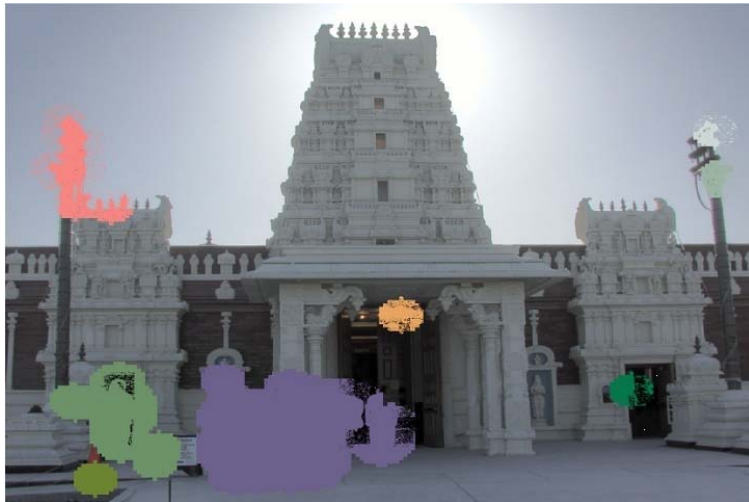
DigiVFX



Moving objects and high-contrast edges render high variance.

## Region masking

DigiVFX



Thresholding; dilation; identify regions;

## Best exposure in each region

DigiVFX



## Lens flare removal

DigiVFX

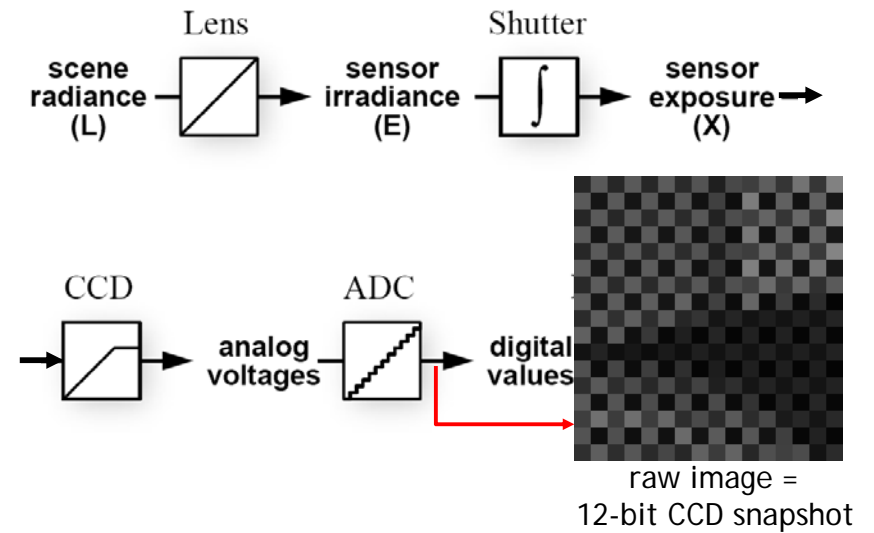


before

after

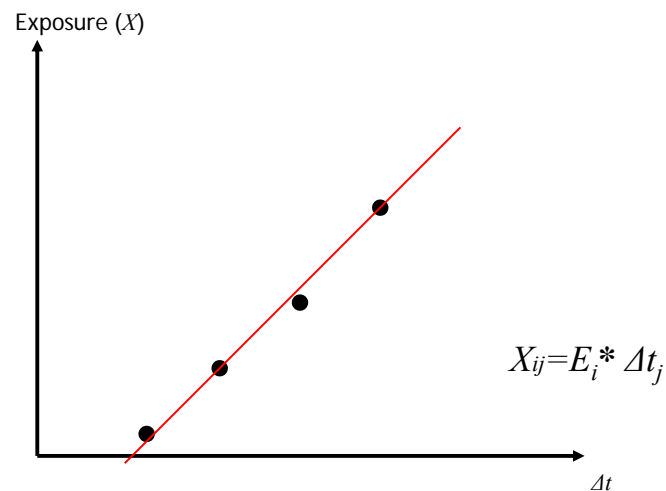
## Easier HDR reconstruction

DigiVFX



## Easier HDR reconstruction

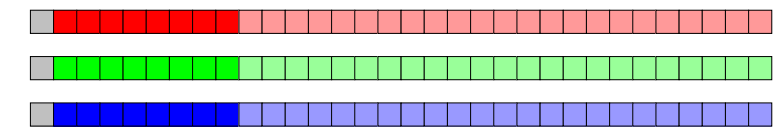
DigiVFX



## Portable floatMap (.pfm)

DigiVFX

- 12 bytes per pixel, 4 for each channel

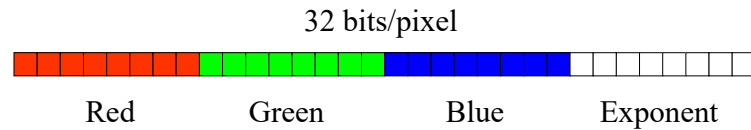


Text header similar to Jeff Poskanzer's .ppm image format:

```
PF
768 512
1
<binary image data>
```

Floating Point TIFF similar

## Radiance format (.pic, .hdr, .rad)



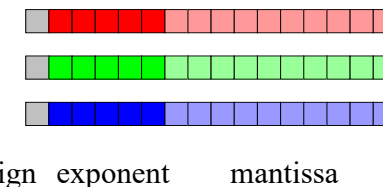
$$\begin{aligned}
 (145, 215, 87, 149) &= (145, 215, 87, 103) = \\
 (145, 215, 87) * 2^{(149-128)} &= (145, 215, 87) * 2^{(103-128)} = \\
 1190000 \ 1760000 \ 713000 & \quad 0.00000432 \ 0.00000641 \ 0.00000259
 \end{aligned}$$

Ward, Greg. "Real Pixels," in Graphics Gems IV, edited by James Arvo, Academic Press, 1994

## ILM's OpenEXR (.exr)



- 6 bytes per pixel, 2 for each channel, compressed



- Several lossless compression options, 2:1 typical
- Compatible with the "half" datatype in NVidia's Cg
- Supported natively on GeForce FX and Quadro FX

- Available at <http://www.openexr.net/>

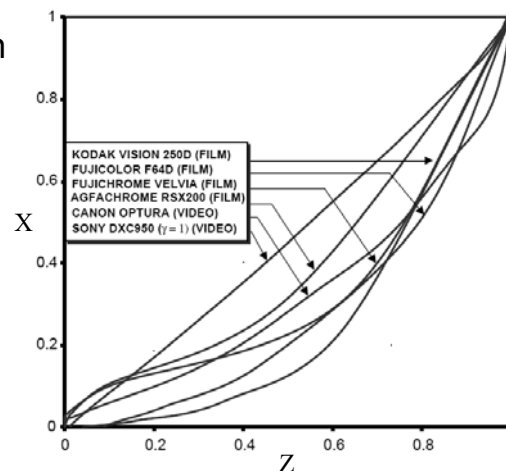
## Radiometric self calibration



- Assume that any response function can be modeled as a high-order polynomial

$$X = g(Z) = \sum_{m=0}^M c_m Z^m$$

- No need to know exposure time in advance. Useful for cheap cameras



## Mitsunaga and Nayar



- To find the coefficients  $c_m$  to minimize the following

$$\mathcal{E} = \sum_{i=1}^N \sum_{j=1}^P \left[ \sum_{m=0}^M c_m Z_{ij}^m - R_{j,j+1} \sum_{m=0}^M c_m Z_{i,j+1}^m \right]^2$$

A guess for the ratio of

$$\frac{X_{ij}}{X_{i,j+1}} = \frac{E_i \Delta t_j}{E_i \Delta t_{j+1}} = \frac{\Delta t_j}{\Delta t_{j+1}}$$

## Mitsunaga and Nayar

- Again, we can only solve up to a scale. Thus, add a constraint  $f(1)=1$ . It reduces to  $M$  variables.
- How to solve it?

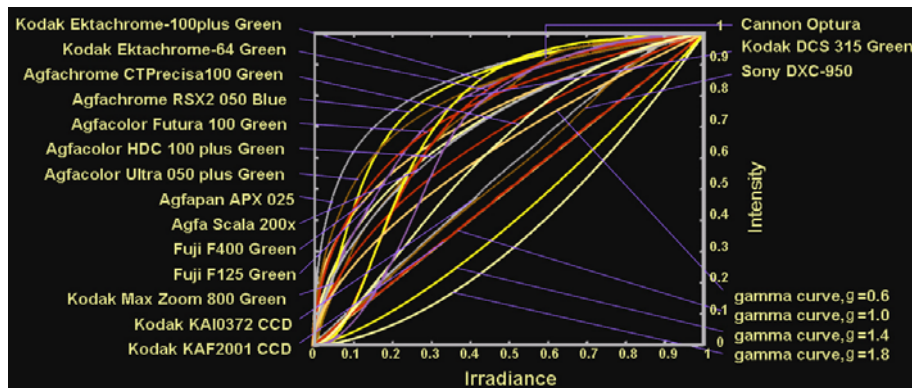
## Mitsunaga and Nayar

- We solve the above iteratively and update the exposure ratio accordingly

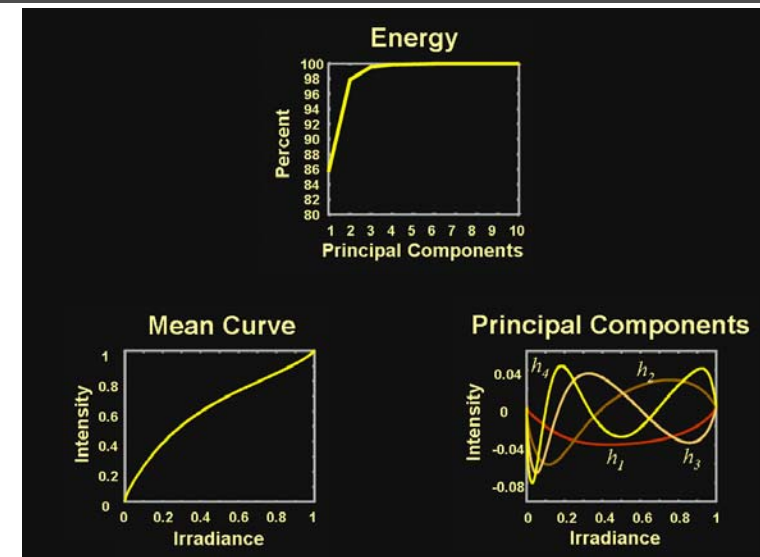
$$R_{j,j+1}^{(k)} = \frac{1}{N} \frac{\sum_{m=0}^M c_m^{(k)} Z_{ij}^m}{\sum_{m=0}^M c_m^{(k)} Z_{i,j+1}^m}$$

- How to determine  $M$ ? Solve up to  $M=10$  and pick up the one with the minimal error. Notice that you prefer to have the same order for all channels. Use the combined error.

## Space of response curves



## Space of response curves



$$Z_{ij} = f(E_i \Delta t_j)$$

$$g(Z_{ij}) = f^{-1}(Z_{ij}) = E_i \Delta t_j$$

Given  $Z_{ij}$  and  $\Delta t_j$ , the goal is to find both  $E_i$  and  $g(Z_{ij})$

Maximum likelihood

$$\Pr(E_i, g \mid Z_{ij}, \Delta t_j) \propto \exp\left(-\frac{1}{2} \sum_{ij} w(Z_{ij}) (g(Z_{ij}) - E_i \Delta t_j)^2\right)$$

$$\hat{g}, \hat{E}_i = \arg \min_{g, E_i} \sum_{ij} w(Z_{ij}) (g(Z_{ij}) - E_i \Delta t_j)^2$$

$$\hat{g}, \hat{E}_i = \arg \min_{g, E_i} \sum_{ij} w(Z_{ij}) (g(Z_{ij}) - E_i \Delta t_j)^2$$

repeat

assuming  $g(Z_{ij})$  is known, optimize for  $E_i$

assuming  $E_i$  is known, optimize for  $g(Z_{ij})$

until converge

$$\hat{g}, \hat{E}_i = \arg \min_{g, E_i} \sum_{ij} w(Z_{ij}) (g(Z_{ij}) - E_i \Delta t_j)^2$$

repeat

assuming  $g(Z_{ij})$  is known, optimize for  $E_i$

assuming  $E_i$  is known, optimize for  $g(Z_{ij})$

until converge

$$\hat{g}, \hat{E}_i = \arg \min_{g, E_i} \sum_{ij} w(Z_{ij}) (g(Z_{ij}) - E_i \Delta t_j)^2$$

repeat

assuming  $g(Z_{ij})$  is known, optimize for  $E_i$

assuming  $E_i$  is known, optimize for  $g(Z_{ij})$

until converge

$$E_i = \frac{\sum_j w(Z_{ij}) g(Z_{ij}) \Delta t_j}{\sum_j w(Z_{ij}) \Delta t_j^2}$$

$$\hat{g}, \hat{E}_i = \arg \min_{g, E_i} \sum_{ij} w(Z_{ij}) (g(Z_{ij}) - E_i \Delta t_j)^2$$

repeat

assuming  $g(Z_{ij})$  is known, optimize for  $E_i$

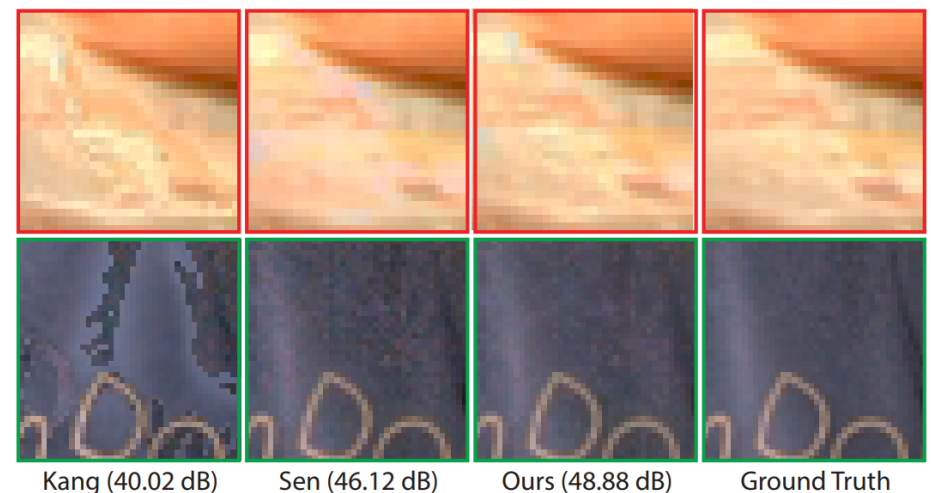
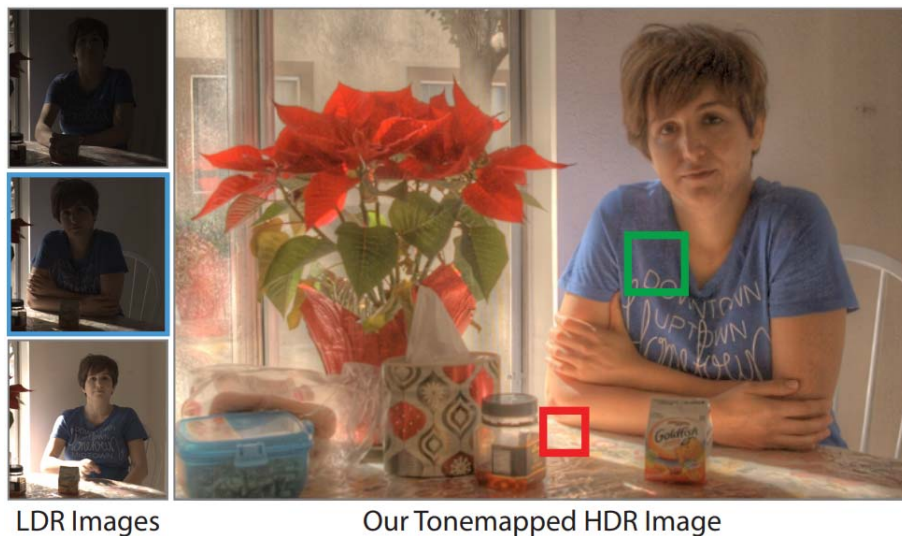
assuming  $E_i$  is known, optimize for  $g(Z_{ij})$

until converge

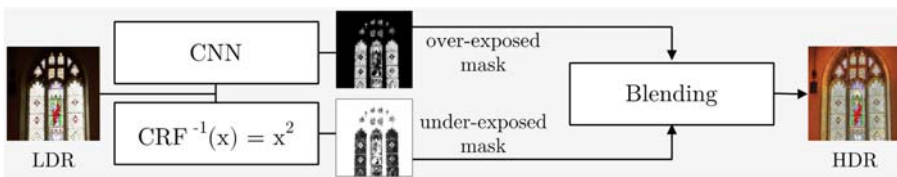
$$g(m) = \frac{1}{|E_m|} \sum_{ij \in E_m} E_i \Delta t_j$$

normalize so that

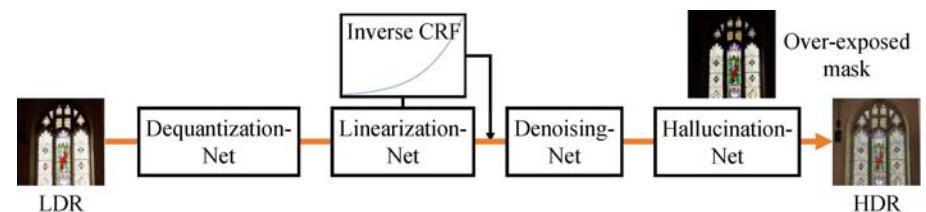
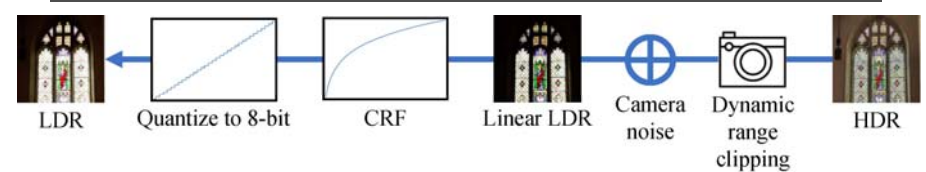
$$g(128) = 1$$



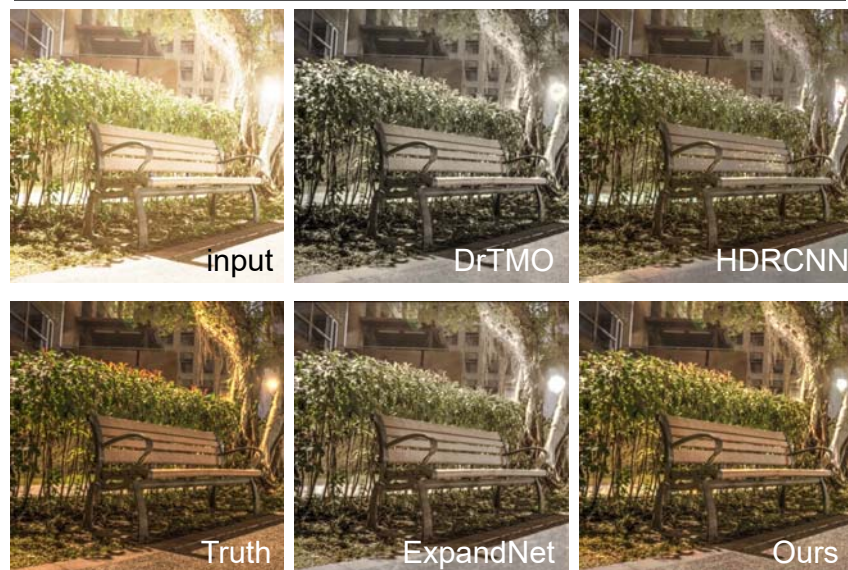
## Deep single-image HDR reconstruction DigiVFX



## Learning to reverse the pipeline DigiVFX



## Comparison DigiVFX



## Input DigiVFX



## Result

DigiVFX



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## Input

DigiVFX



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## Result

DigiVFX



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## HDR Video

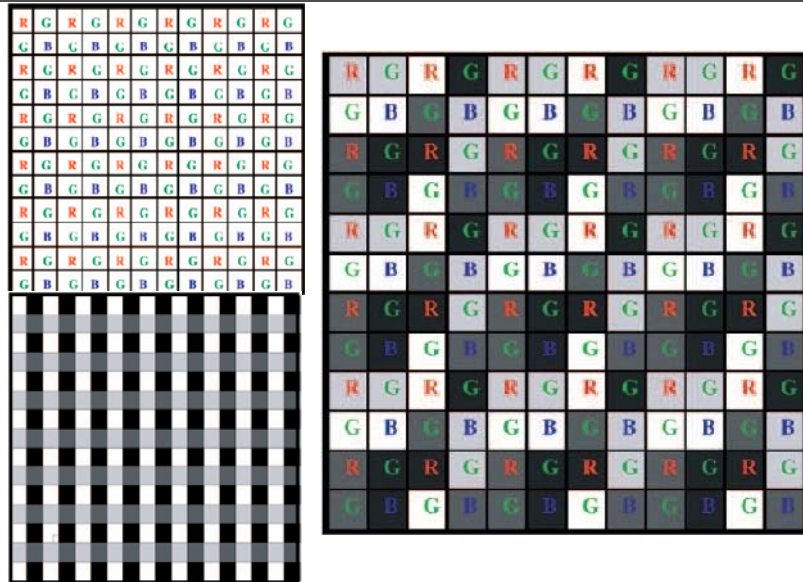
DigiVFX

- High Dynamic Range Video  
Sing Bing Kang, Matthew Uyttendaele, Simon Winder, Richard Szeliski  
SIGGRAPH 2003

[video](#)

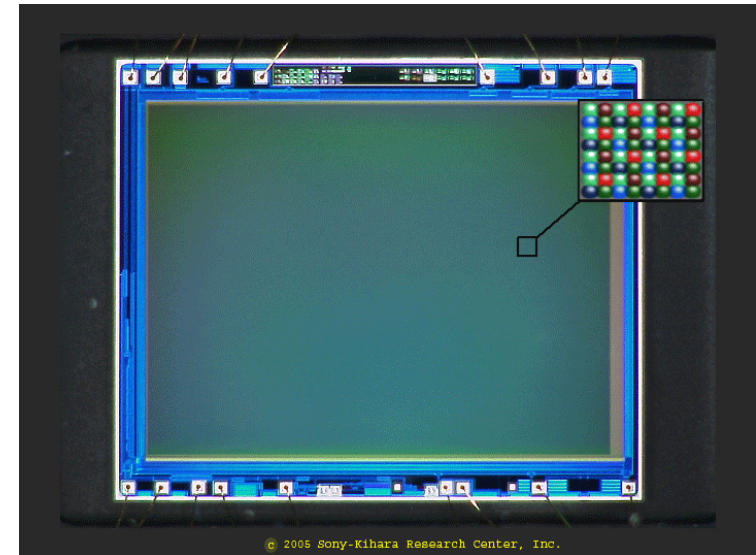
## Assorted pixel

DigiVFX



## Assorted pixel

DigiVFX



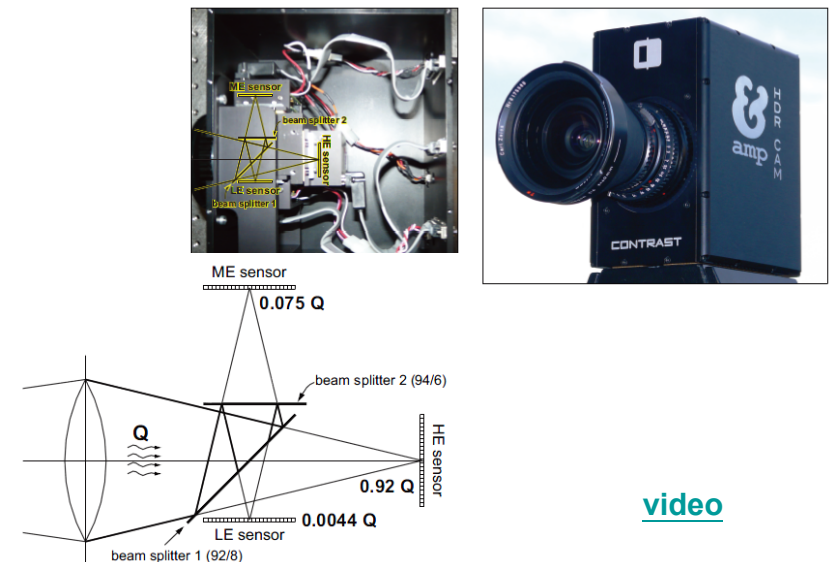
## Assorted pixel

DigiVFX



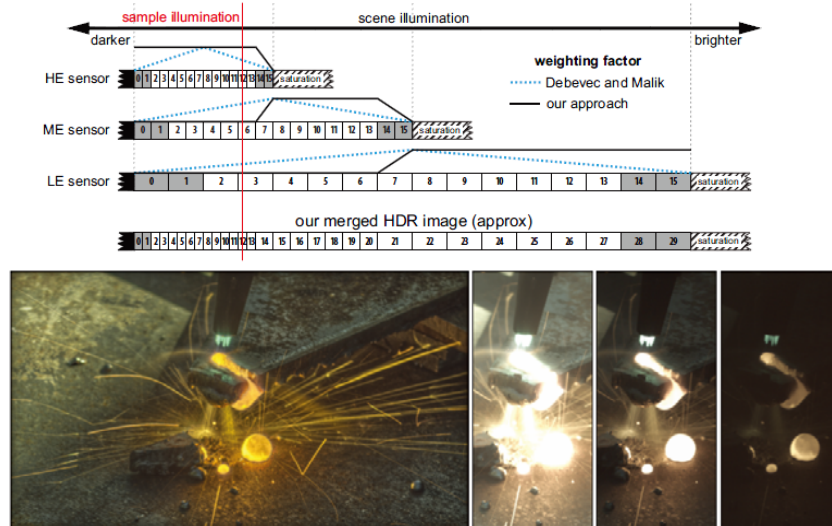
## A Versatile HDR Video System

DigiVFX



# A Versatile HDR Video System

DigiVFX



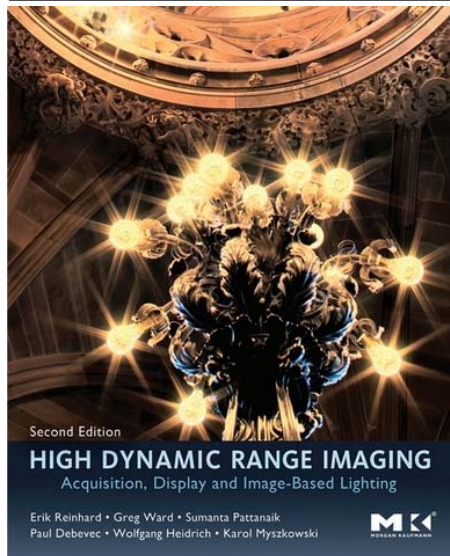
# HDR becomes common practice

DigiVFX

- Many cameras has bracket exposure modes
- For example, since iPhone 4, iPhone has HDR option. But, it could be more exposure blending rather than true HDR.

## References

DigiVFX



## References

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