# Image stitching

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# Applications of image stitching

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- Video stabilization
- Video summarization
- Video compression
- Video matting
- Panorama creation

# Image stitching • Stitching = alignment + blending f geometrical photometric registration registration





### Video summarization





## Video compression

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input video

## Object removal

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remove foreground

### Object removal





estimate background



### Object removal





#### background estimation

#### Panorama creation



### Why panorama?



- Are you getting the whole picture?
  - Compact Camera FOV = 50 x 35°



### Why panorama?



- Are you getting the whole picture?
  - Compact Camera FOV = 50 x  $35^{\circ}$
  - Human FOV =  $200 \times 135^{\circ}$



### Why panorama?

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- Are you getting the whole picture?
  - Compact Camera FOV = 50 x 35°
  - Human FOV =  $200 \times 135^{\circ}$
  - Panoramic Mosaic =  $360 \times 180^{\circ}$



#### Panorama examples

- Similar to HDR, it is a topic of computational photography, seeking ways to build a better camera using either hardware or software.
- Most consumer cameras have a panorama mode
- Mars:

http://www.panoramas.dk/fullscreen3/f2\_mars97.html

• Earth:

http://www.panoramas.dk/new-year-2006/taipei.html http://www.360cities.net/ http://maps.google.com.tw/

### What can be globally aligned?



- In image stitching, we seek for a matrix to globally warp one image into another. Are any two images of the same scene can be aligned this way?
  - Images captured with the same center of projection
  - A planar scene or far-away scene

## A pencil of rays contains all views





Can generate any synthetic camera view as long as it has **the same center of projection**!



#### Mosaic as an image reprojection



- The images are reprojected onto a common plane
- The mosaic is formed on this plane
- Mosaic is a synthetic wide-angle camera

### What cannot

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• The scene with depth variations and the camera has movement



#### Changing camera center

# synthetic PP



### Planar scene (or a faraway one)

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- PP3 is a projection plane of both centers of projection, so we are OK!
- This is how big aerial photographs are made

#### Motion models

• Parametric models as the assumptions on the relation between two images.

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## 2D Motion models



Name	Matrix	# D.O.F.	Preserves:	Icon
translation	$\left[ egin{array}{c c} I & t \end{array}  ight]_{2  imes 3}$	2	orientation $+\cdots$	
rigid (Euclidean)	$\left[ egin{array}{c c c c c c c c c c c c c c c c c c c $	3	$lengths + \cdots$	$\Diamond$
similarity	$\left[ \left  s \boldsymbol{R} \right  \boldsymbol{t} \right]_{2 \times 3}$	4	$angles+\cdots$	$\Diamond$
affine	$\left[ egin{array}{c} m{A} \end{array}  ight]_{2 imes 3}$	6	$parallelism + \cdots$	$\square$
projective	$\left[ \begin{array}{c}  ilde{H} \end{array}  ight]_{3 imes 3}$	8	straight lines	



### A case study: cylindrical panorama



• What if you want a 360° field of view?





### Cylindrical panoramas





- Steps
  - Reproject each image onto a cylinder
  - Blend
  - Output the resulting mosaic

### Cylindrical panorama



- 1. Take pictures on a tripod (or handheld)
- 2. Warp to cylindrical coordinate
- 3. Compute pairwise alignments
- 4. Fix up the end-to-end alignment
- 5. Blending
- 6. Crop the result and import into a viewer

It is required to do radial distortion correction for better stitching results!

### Taking pictures

applet

plets/projection.html





http://graphics.stanford.edu/courses/cs178/ap



Kaidan panoramic tripod head



#### Translation model



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# Where should the synthetic camera be



Onto a cylinder



 $\begin{tabular}{|c|c|c|c|c|} \hline \end{tabular} Descent for the second se$ 

Adopted from http://www.cambridgeincolour.com/tutorials/image-projections.htm





### Blending

• Why blending: parallax, lens distortion, scene motion, exposure difference

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## Blending







### Gradient-domain stitching





### Gradient-domain stitching



#### Panorama weaving

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Figure 1: Panorama Weaving on a challenging data-set (Nation, 12848 x 3821, 9 images) with moving objects during acquisition, registration issues and varying exposure. Our initial automatic solution (bottom, left) was computed in 4.6 seconds at full resolution for a result with lower seam energy than Graph Cuts. Additionally, we present a system for the interactive user exploration of the seam solution space (bottom, right), easily enabling: (a) the resolution of moving objects, (b) the hiding of registration artifacts (split pole) in low contrast areas (scooter) or (c) the fix of semantic notions for which automatic decisions can be unsatisfactory (stoplight colors are inconsistent after the automatic solve). The user editing session took only a few minutes. (top) the final, color-corrected panorama.

#### Assembling the panorama





• Stitch pairs together, blend, then crop



### Problem: Drift

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- Error accumulation
  - small errors accumulate over time



- add displacement of  $(y_1 y_n)/(n 1)$  to each image after the first
- compute a global warp: y' = y + ax
- run a big optimization problem, incorporating this constraint
  - best solution, but more complicated
  - known as "bundle adjustment"

### End-to-end alignment and crop







# Rectangling panoramas







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(c) cropping

(d) our content-aware warping

video

## Rectangling panoramas







example: http://www.cs.washington.edu/education/courses/cse590ss/01wi/projects/project1/students/dougz/index.html

# Rectangling panoramas



### Viewer: texture mapped model





example: http://www.panoramas.dk/



### Cylindrical panorama

- DigiVFX
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#### Determine pairwise alignment?

- Feature-based methods: only use feature points to estimate parameters
- We will study the "Recognising panorama" paper published in ICCV 2003
- Run SIFT (or other feature algorithms) for each image, find feature matches.

### Determine pairwise alignment



- p'=Mp, where M is a transformation matrix, p and p' are feature matches
- It is possible to use more complicated models such as affine or perspective
- For example, assume M is a 2x2 matrix

$$\begin{pmatrix} x' \\ y' \end{pmatrix} = \begin{pmatrix} m_{11} & m_{12} \\ m_{21} & m_{22} \end{pmatrix} \begin{pmatrix} x \\ y \end{pmatrix}$$

• Find M with the least square error

$$\sum_{i=1}^n (Mp - p')^2$$

### Determine pairwise alignment

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$$\begin{pmatrix} x' \\ y' \end{pmatrix} = \begin{pmatrix} m_{11} & m_{12} \\ m_{21} & m_{22} \end{pmatrix} \begin{pmatrix} x \\ y \end{pmatrix} \qquad \qquad x_1 m_{11} + y_1 m_{12} = x_1' \\ x_1 m_{21} + y_1 m_{22} = y_1'$$

Overdetermined system

$$\begin{pmatrix} x_{1} & y_{1} & 0 & 0 \\ 0 & 0 & x_{1} & y_{1} \\ x_{2} & y_{2} & 0 & 0 \\ \vdots & \vdots & \vdots & \vdots \\ x_{n} & y_{n} & 0 & 0 \\ 0 & 0 & x_{n} & y_{n} \end{pmatrix} \begin{pmatrix} m_{11} \\ m_{12} \\ m_{21} \\ m_{22} \end{pmatrix} = \begin{pmatrix} x_{1} \\ y_{1} \\ x_{2} \\ \vdots \\ x_{n} \\ y_{n} \end{pmatrix}$$

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#### Normal equation

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Given an overdetermined system

 $\mathbf{A}\mathbf{x} = \mathbf{b}$ 

the normal equation is that which minimizes the sum of the square differences between left and right sides

 $\mathbf{A}^{\mathrm{T}}\mathbf{A}\mathbf{x} = \mathbf{A}^{\mathrm{T}}\mathbf{b}$ 

Why?



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$$\mathbf{A}\mathbf{x} - \mathbf{b} = \begin{bmatrix} \sum_{j=1}^{m} a_{1j} x_j \\ \vdots \\ \sum_{j=1}^{m} a_{ij} x_j \\ \vdots \\ \sum_{j=1}^{m} a_{nj} x_j \end{bmatrix} - \begin{bmatrix} b_1 \\ \vdots \\ b_i \\ \vdots \\ b_n \end{bmatrix} = \begin{bmatrix} \left(\sum_{j=1}^{m} a_{1j} x_j\right) - b_1 \\ \vdots \\ \left(\sum_{j=1}^{m} a_{nj} x_j\right) - b_i \\ \vdots \\ \left(\sum_{j=1}^{m} a_{nj} x_j\right) - b_n \end{bmatrix}^2$$
$$E(\mathbf{x}) = (\mathbf{A}\mathbf{x} - \mathbf{b})^2 = \sum_{i=1}^{n} \left[ \left(\sum_{j=1}^{m} a_{ij} x_j\right) - b_i \right]^2$$

Normal equation

$$E(\mathbf{x}) = (\mathbf{A}\mathbf{x} - \mathbf{b})^2$$

$$\begin{bmatrix} a_{11} & \dots & a_{1m} \\ \vdots & & \vdots \\ \vdots & & \vdots \\ a_{n1} & \dots & a_{nm} \end{bmatrix} \begin{bmatrix} x_1 \\ \vdots \\ x_m \end{bmatrix} = \begin{bmatrix} b_1 \\ \vdots \\ \vdots \\ \vdots \\ b_n \end{bmatrix}$$

*n*X*m*, *n* equations, *m* variables

Normal equation

$$E(\mathbf{x}) = (\mathbf{A}\mathbf{x} - \mathbf{b})^2 = \sum_{i=1}^n \left[ \left( \sum_{j=1}^m a_{ij} x_j \right) - b_i \right]^2$$
$$0 = \frac{\partial E}{\partial x_1} = \sum_{i=1}^n 2 \left[ \left( \sum_{j=1}^m a_{ij} x_j \right) - b_i \right] a_{i1}$$
$$= 2 \sum_{i=1}^n a_{i1} \sum_{j=1}^m a_{ij} x_j - 2 \sum_{i=1}^n a_{i1} b_i$$
$$0 = \frac{\partial E}{\partial \mathbf{x}} = 2 (\mathbf{A}^T \mathbf{A} \mathbf{x} - \mathbf{A}^T \mathbf{b}) \rightarrow \mathbf{A}^T \mathbf{A} \mathbf{x} = \mathbf{A}^T \mathbf{b}$$



#### Normal equation

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 $(\mathbf{A}\mathbf{x} - \mathbf{b})^2$ 

### Normal equation

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$$(\mathbf{A}\mathbf{x} - \mathbf{b})^{2}$$
  
=  $(\mathbf{A}\mathbf{x} - \mathbf{b})^{T} (\mathbf{A}\mathbf{x} - \mathbf{b})$   
=  $((\mathbf{A}\mathbf{x})^{T} - \mathbf{b}^{T})(\mathbf{A}\mathbf{x} - \mathbf{b})$   
=  $(\mathbf{x}^{T}\mathbf{A}^{T} - \mathbf{b}^{T})(\mathbf{A}\mathbf{x} - \mathbf{b})$   
=  $\mathbf{x}^{T}\mathbf{A}^{T}\mathbf{A}\mathbf{x} - \mathbf{b}^{T}\mathbf{A}\mathbf{x} - \mathbf{x}^{T}\mathbf{A}^{T}\mathbf{b} + \mathbf{b}^{T}\mathbf{b}$   
=  $\mathbf{x}^{T}\mathbf{A}^{T}\mathbf{A}\mathbf{x} - (\mathbf{A}^{T}\mathbf{b})^{T}\mathbf{x} - (\mathbf{A}^{T}\mathbf{b})^{T}\mathbf{x} + \mathbf{b}^{T}\mathbf{b}$   
 $\frac{\partial E}{\partial \mathbf{x}} = 2\mathbf{A}^{T}\mathbf{A}\mathbf{x} - 2\mathbf{A}^{T}\mathbf{b}$ 

#### Determine pairwise alignment



- p'=Mp, where M is a transformation matrix, p and p' are feature matches
- For translation model, it is easier.

$$E = \sum_{i=1}^{n} \left[ \left( m_1 + x_i - x_i^{'} \right)^2 + \left( m_2 + y_i - y_i^{'} \right)^2 \right]$$

 $0 = \frac{\partial E}{\partial m_1}$ 

• What if the match is false? Avoid impact of outliers.

#### RANSAC

- RANSAC = Random Sample Consensus
- An algorithm for robust fitting of models in the presence of many data outliers
- Compare to robust statistics
- Given N data points x<sub>i</sub>, assume that majority of them are generated from a model with parameters Θ, try to recover Θ.







# **RANSAC** for Homography



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### RANSAC for Homography



# **RANSAC** for Homography





### Applications of panorama in VFX



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- Background plates
- Image-based lighting

### Troy (image-based lighting)



http://www.cgnetworks.com/story\_custom.php?story\_id=2195&page=4

### Spiderman 2 (background plate)



#### Reference

- Richard Szeliski, <u>Image Alignment and Stitching: A Tutorial</u>, Foundations and Trends in Computer Graphics and Computer Vision, 2(1):1-104, December 2006.
- R. Szeliski and H.-Y. Shum. <u>Creating full view panoramic image</u> mosaics and texture-mapped models, SIGGRAPH 1997, pp251-258.
- M. Brown, D. G. Lowe, <u>Recognising Panoramas</u>, ICCV 2003.

