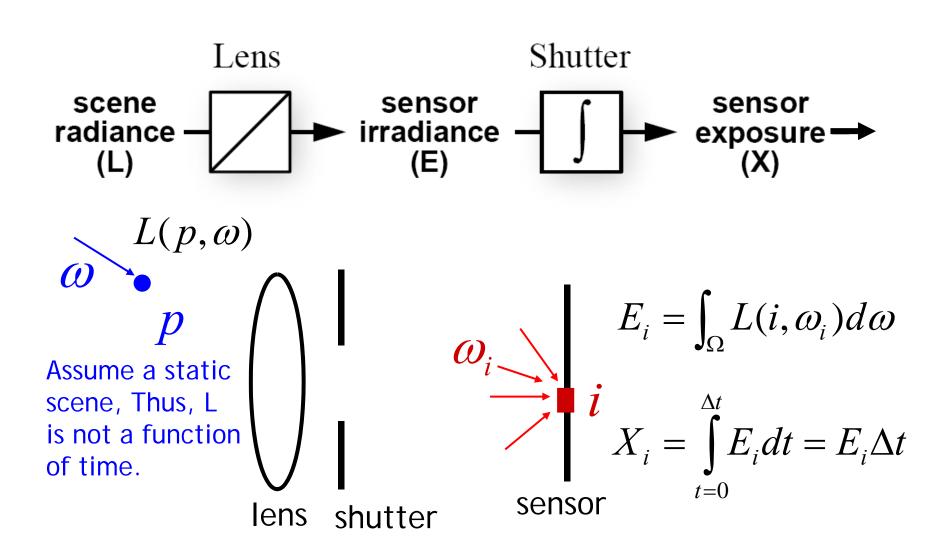
High dynamic range imaging

Digital Visual Effects Yung-Yu Chuang

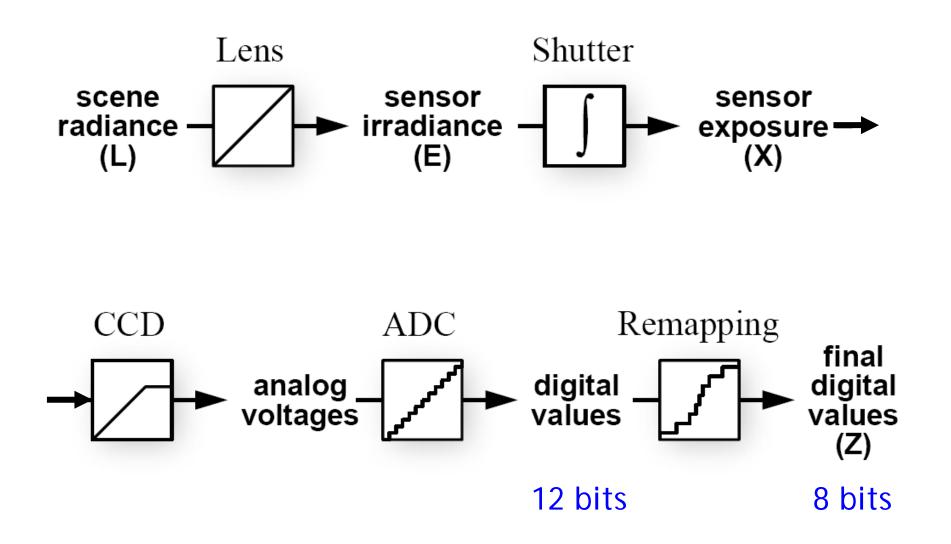
with slides by Fredo Durand, Brian Curless, Steve Seitz, Paul Debevec and Alexei Efros

- Camera is an imperfect device for measuring the radiance distribution of a scene because it cannot capture the full spectral content and dynamic range.
- Limitations in sensor design prevent cameras from capturing all information passed by lens.



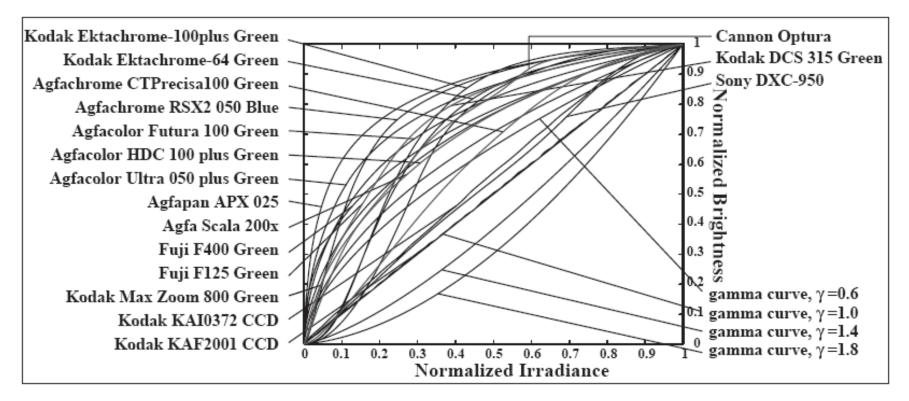






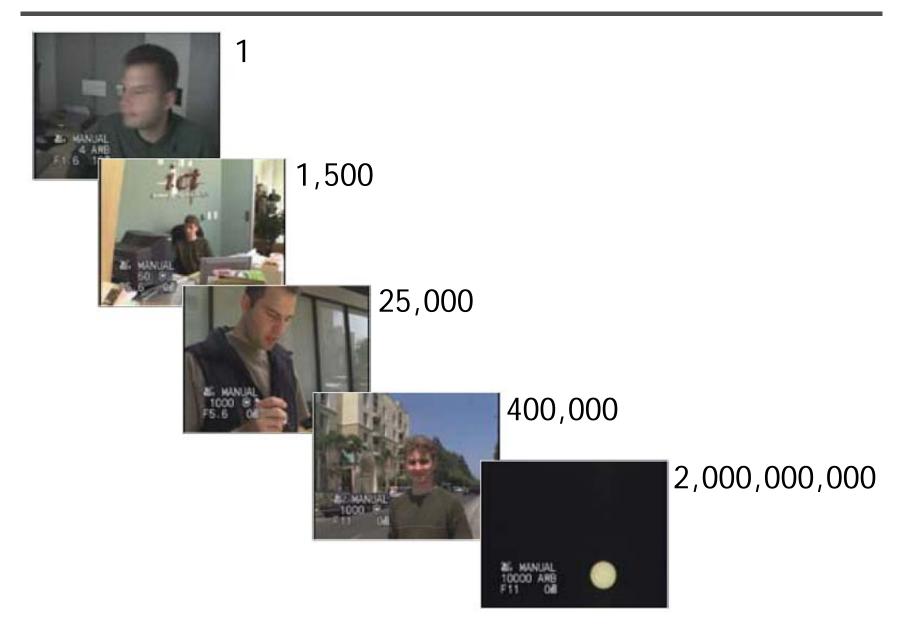
Real-world response functions

In general, the response function is not provided by camera makers who consider it part of their proprietary product differentiation. In addition, they are beyond the standard gamma curves.





The world is high dynamic range





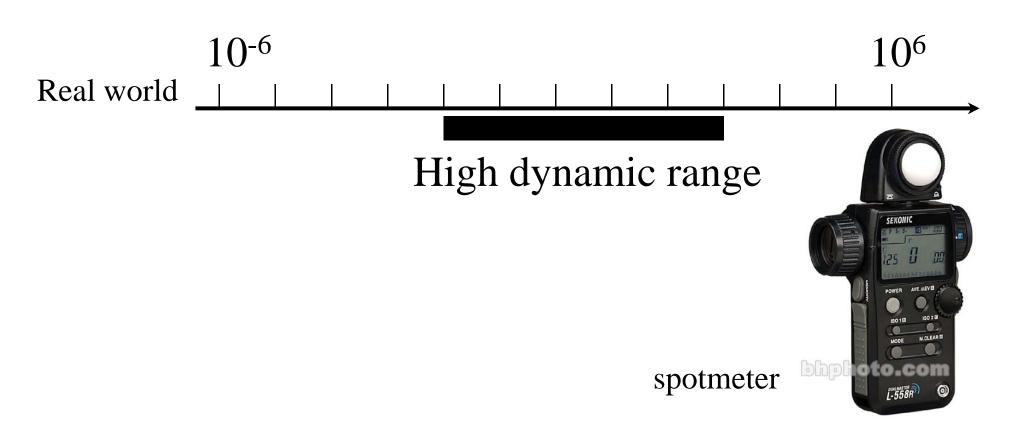
The world is high dynamic range



Real world dynamic range

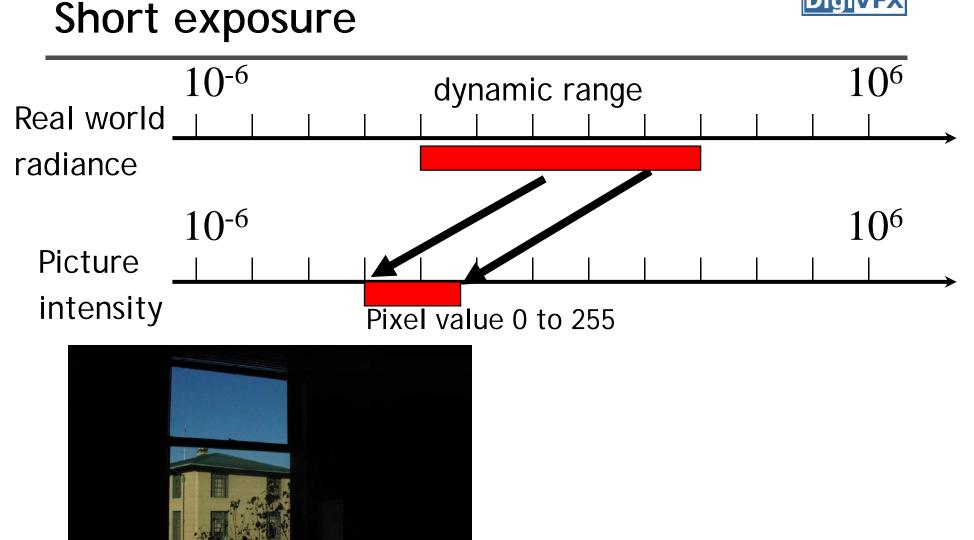


- Eye can adapt from ~ 10^{-6} to 10^{6} cd/m²
- Often 1 : 100,000 in a scene
- Typical 1:50, max 1:500 for pictures



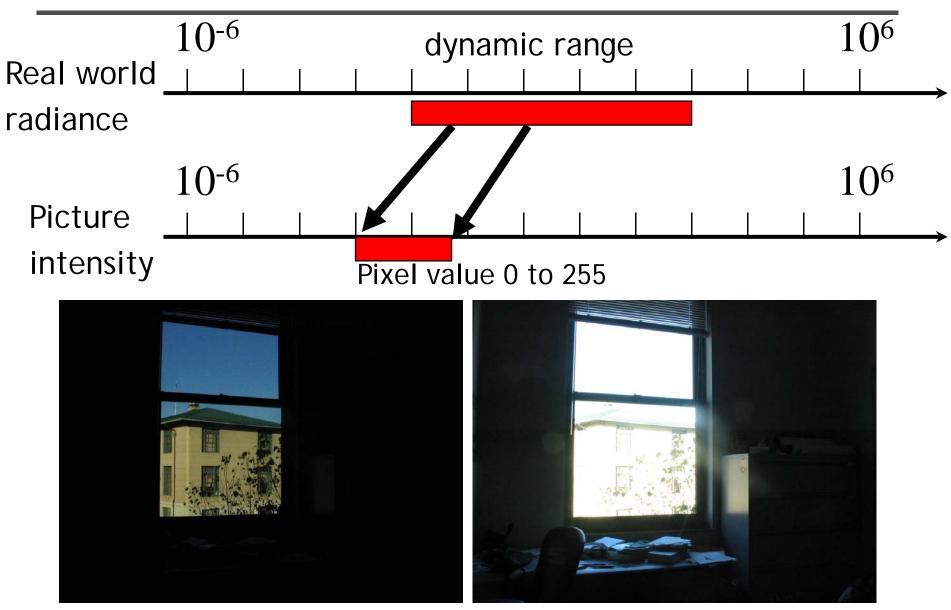








Long exposure



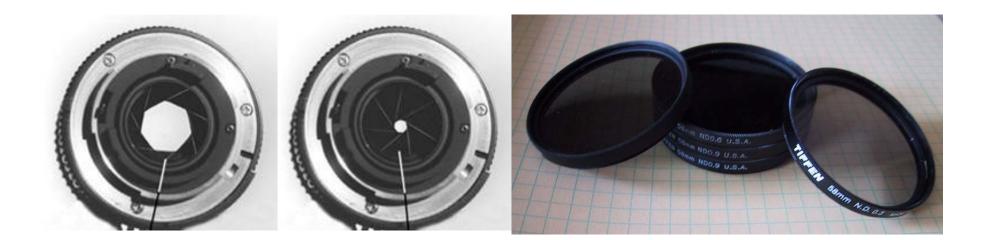


- Limited dynamic range
 - \Rightarrow Perhaps use multiple exposures?
- Unknown, nonlinear response
 - \Rightarrow Not possible to convert pixel values to radiance
- Solution:
 - Recover response curve from multiple exposures, then reconstruct the *radiance map*



Varying exposure

- Ways to change exposure
 - Shutter speed
 - Aperture
 - Neutral density filters





- Note: shutter times usually obey a power series – each "stop" is a factor of 2
- ¼, 1/8, 1/15, 1/30, 1/60, 1/125, 1/250, 1/500, 1/1000 sec

Usually really is:

¹/₄, 1/8, 1/16, 1/32, 1/64, 1/128, 1/256, 1/512, 1/1024 sec



Varying shutter speeds

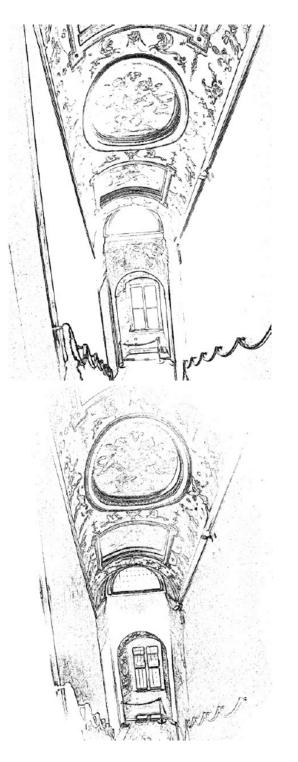


HDRI capturing from multiple exposures

- Capture images with multiple exposures
- Image alignment (even if you use tripod, it is suggested to run alignment)
- Response curve recovery
- Ghost/flare removal



- We will introduce a fast and easy-to-implement method for this task, called Median Threshold Bitmap (MTB) alignment technique.
- Consider only integral translations. It is enough empirically.
- The inputs are N grayscale images. (You can either use the green channel or convert into grayscale by Y=(54R+183G+19B)/256)
- MTB is a binary image formed by thresholding the input image using the median of intensities.









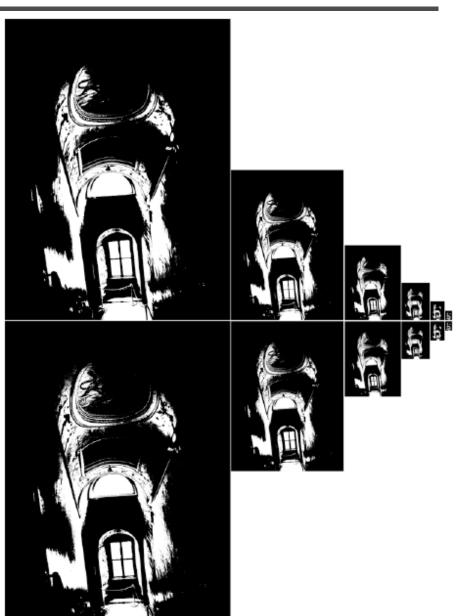
Why is MTB better than gradient?

- Edge-detection filters are dependent on image exposures
- Taking the difference of two edge bitmaps would not give a good indication of where the edges are misaligned.



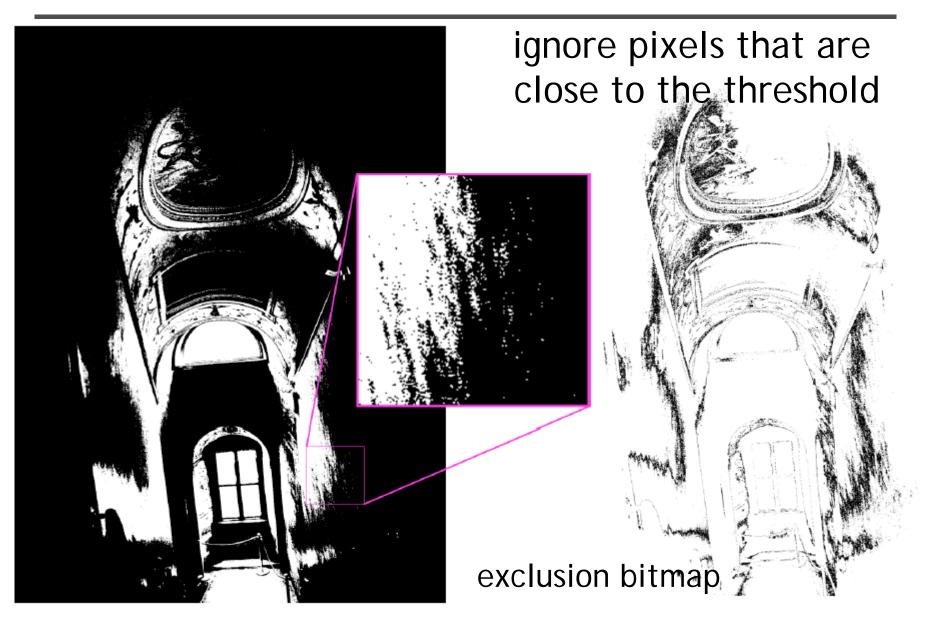
Search for the optimal offset

- Try all possible offsets.
- Gradient descent
- Multiscale technique
- log(max_offset) levels
- Try 9 possibilities for the top level
- Scale by 2 when passing down; try its 9 neighbors



Threshold noise





Efficiency considerations



- XOR for taking difference
- AND with exclusion maps
- Bit counting by table lookup

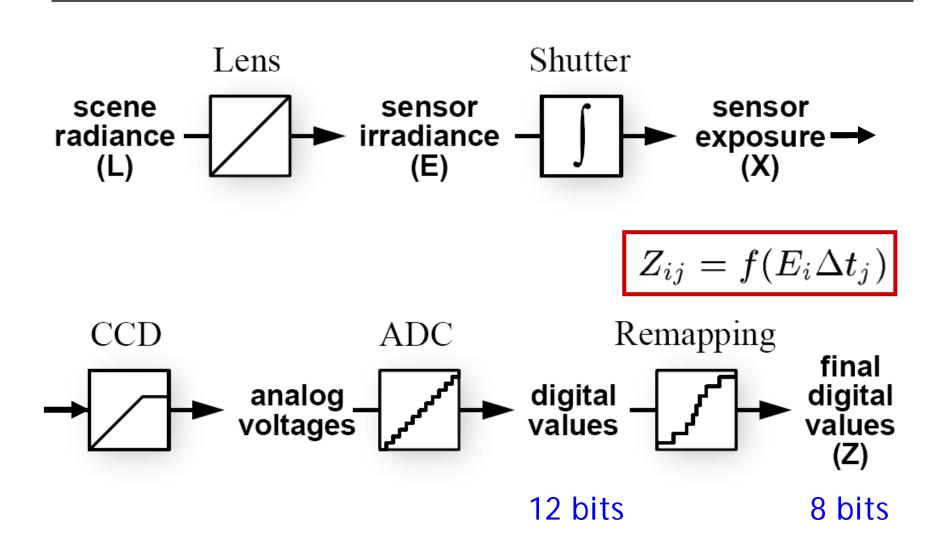
Results



Success rate = 84%. 10% failure due to rotation. 3% for excessive motion and 3% for too much high-frequency content.







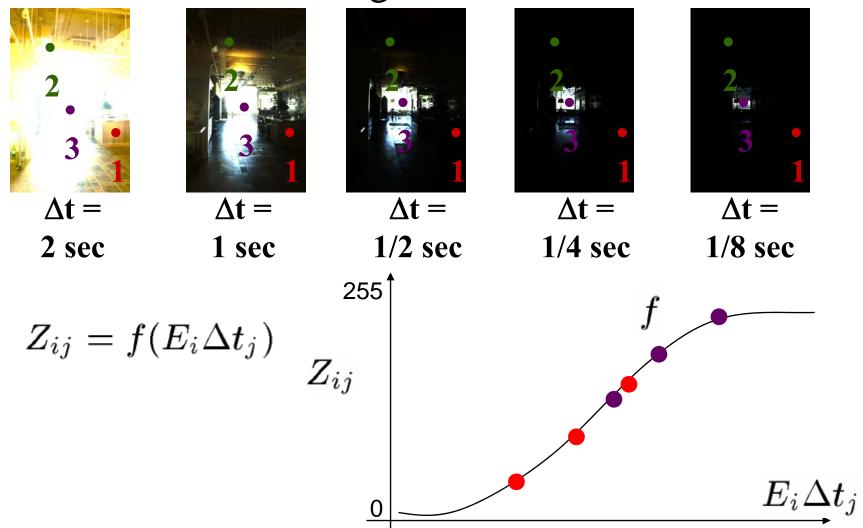


• We want to obtain the inverse of the response curve 255 $Z_{ij} = f(E_i \Delta t_j)$ Z_{ij} 0 $E_i \Delta t_j$

Recovering response curve



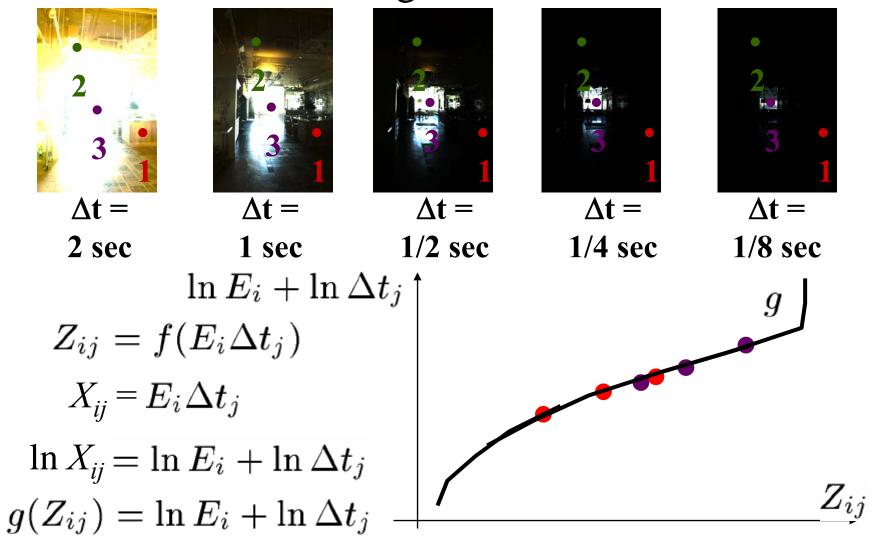
Image series



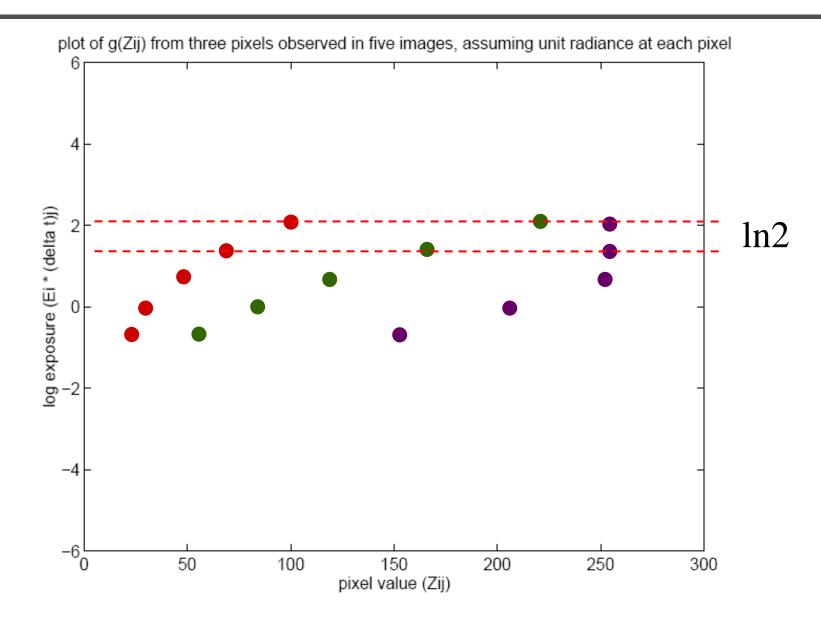
Recovering response curve



Image series

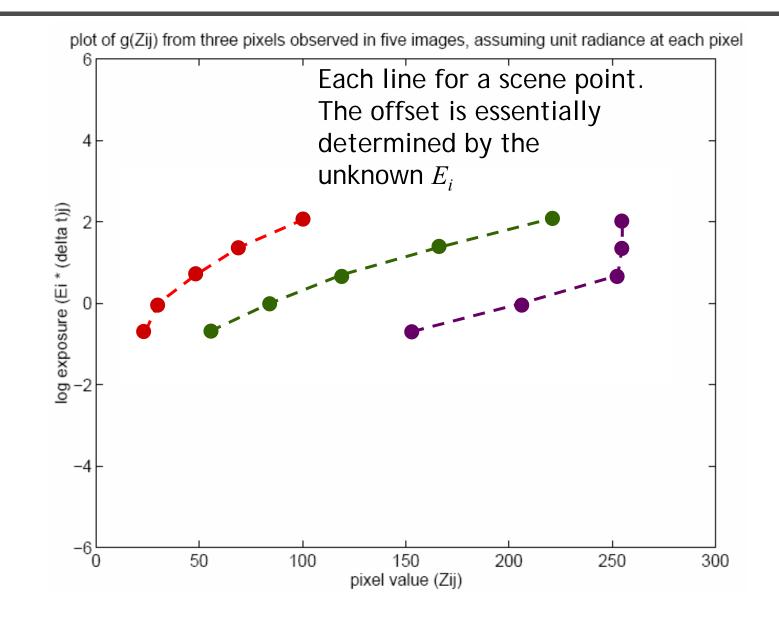




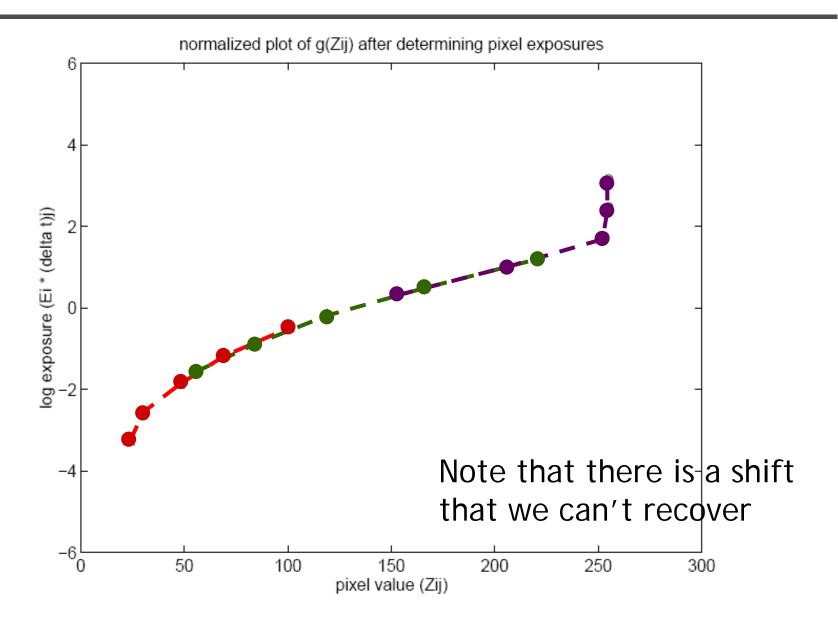




Idea behind the math









Basic idea

- Design an objective function
- Optimize it



$$Z_{ij} = f(E_i \Delta t_j)$$

f is monotonic, it is invertible

$$\ln f^{-1}(Z_{ij}) = \ln E_i + \ln \Delta t_j$$

let us define function $g = \ln f^{-1}$

$$g(Z_{ij}) = \ln E_i + \ln \Delta t_j$$

minimize the following

$$\mathcal{O} = \sum_{i=1}^{N} \sum_{j=1}^{P} \left[g(Z_{ij}) - \ln E_i - \ln \Delta t_j \right]^2 + \lambda \sum_{z=Z_{min}+1}^{Z_{max}-1} g''(z)^2$$
$$g''(z) = g(z-1) - 2g(z) + g(z+1)$$

• The solution can be only up to a scale, add a constraint

$$g(Z_{mid}) = 0$$
, where $Z_{mid} = \frac{1}{2}(Z_{min} + Z_{max})$

Add a hat weighting function

$$w(z) = \begin{cases} z - Z_{min} & \text{for } z \leq \frac{1}{2}(Z_{min} + Z_{max}) \\ Z_{max} - z & \text{for } z > \frac{1}{2}(Z_{min} + Z_{max}) \end{cases}$$
$$\mathcal{O} = \sum_{i=1}^{N} \sum_{j=1}^{P} \{w(Z_{ij}) \left[g(Z_{ij}) - \ln E_i - \ln \Delta t_j\right]\}^2 + \lambda \sum_{z=Z_{min}+1}^{Z_{max}-1} [w(z)g''(z)]^2$$



- We want $N(P-1) > (Z_{max} Z_{min})$ If P=11, N~25 (typically 50 is used)
- We prefer that selected pixels are well distributed and sampled from constant regions. They picked points by hand.
- It is an overdetermined system of linear equations and can be solved using SVD



How to optimize?

$$\mathcal{O} = \sum_{i=1}^{N} \sum_{j=1}^{P} \{w(Z_{ij}) [g(Z_{ij}) - \ln E_i - \ln \Delta t_j]\}^2 + \lambda \sum_{z=Z_{min}+1}^{Z_{max}-1} [w(z)g''(z)]^2$$

1. Set partial derivatives to zero

$$\mathcal{O} = \sum_{i=1}^{N} \sum_{j=1}^{P} \{w(Z_{ij}) [g(Z_{ij}) - \ln E_i - \ln \Delta t_j]\}^2 + \lambda \sum_{z=Z_{min}+1}^{Z_{max}-1} [w(z)g''(z)]^2$$



How to optimize?

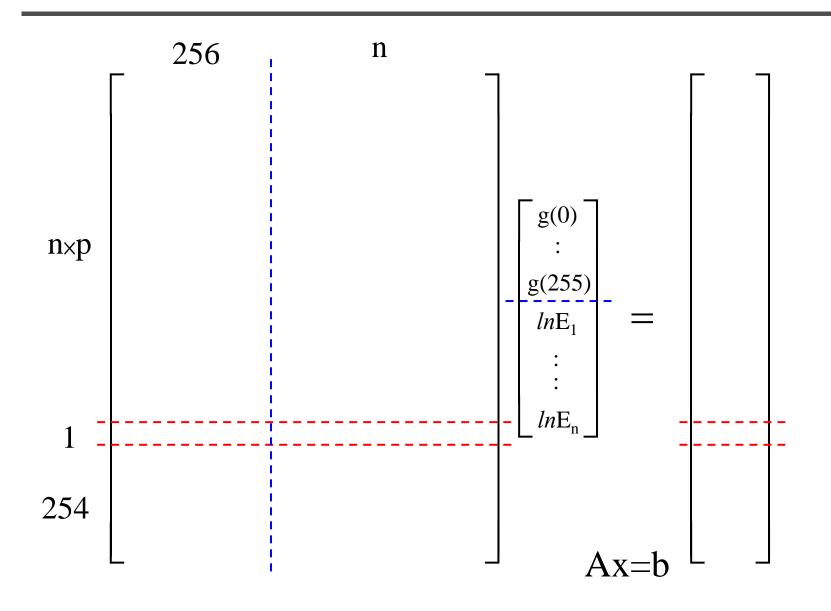
$$\mathcal{O} = \sum_{i=1}^{N} \sum_{j=1}^{P} \{w(Z_{ij}) [g(Z_{ij}) - \ln E_i - \ln \Delta t_j]\}^2 + \lambda \sum_{z=Z_{min}+1}^{Z_{max}-1} [w(z)g''(z)]^2$$

Set partial derivatives to zero
 2.

2.

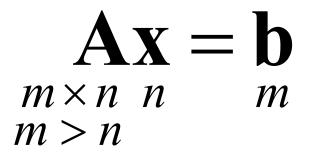
$$\min \sum_{i=1}^{N} (\mathbf{a}_i \mathbf{x} - \mathbf{b}_i)^2 \rightarrow \text{least-square solution of} \begin{bmatrix} \mathbf{a}_1 \\ \mathbf{a}_2 \\ \vdots \\ \mathbf{a}_N \end{bmatrix} \mathbf{x} = \begin{bmatrix} \mathbf{b}_1 \\ \mathbf{b}_2 \\ \vdots \\ \mathbf{b}_N \end{bmatrix}$$





- Will g(127)=0 always be satisfied? Why or why not?
- How to find the least-square solution for an over-determined system?

Least-square solution for a linear system



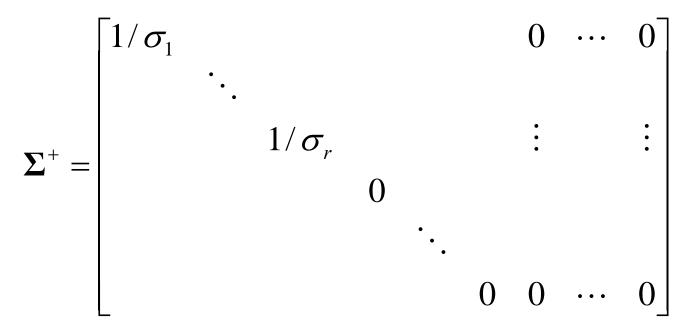
They are often mutually incompatible. We instead find \mathbf{x} to minimize the norm $\|\mathbf{A}\mathbf{x} - \mathbf{b}\|$ of the residual vector $\mathbf{A}\mathbf{x} - \mathbf{b}$. If there are multiple solutions, we prefer the one with the minimal length $\|\mathbf{x}\|$.

Least-square solution for a linear system

If we perform SVD on A and rewrite it as

$$\mathbf{A} = \mathbf{U} \mathbf{\Sigma} V^{\mathrm{T}}$$

then $\hat{\mathbf{x}} = \mathbf{V} \boldsymbol{\Sigma}^{+} \mathbf{U}^{T} \mathbf{b}$ is the least-square solution. pseudo inverse





Proof

$$find \propto t \notin ||A \times -b|| \frac{1}{100} ||$$

$$||A \times -b|| = || \cup (\sum \sqrt{x} - \bigcup Tb) || \quad (\pounds \text{ votation} \\ = || \cup (\sum \sqrt{x} - \bigcup Tb) || \quad (\pounds \text{ votation} \\ \forall \exists b \notin a \notin a \notin b \notin b \end{pmatrix} ||$$

$$(\underbrace{ \sum \sqrt{x} - \bigcup Tb}_{k} || \sum \sqrt{x} - \bigcup Tb \\ \Re || \# \Re \exists f \notin x \neq T \notin || \sum \sqrt{x} - C || \Re ||$$

$$(\underbrace{ \sum \sqrt{x} - \bigcup Tb}_{k} || \sum \sqrt{x} - C || \Re || = C || =$$



Proof

 $\Rightarrow Y_i = \frac{C_i}{\sigma_i} \quad i = 1 \dots \gamma \qquad Y_i = 0 \quad i = r + 1 \dots \gamma$ $\Rightarrow \tilde{Y} = \left(\begin{array}{c} \tilde{y} \\ \tilde{y}$

 $= \sum_{x=1}^{T} \sum$

 $\Rightarrow \widetilde{\chi} = \sqrt{\Sigma^{\dagger} U^{\dagger} b}$



Libraries for SVD

- Matlab
- GSL
- Boost
- LAPACK
- ATLAS

Matlab code



```
%
% gsolve.m - Solve for imaging system response function
%
% Given a set of pixel values observed for several pixels in several
% images with different exposure times, this function returns the
% imaging system's response function q as well as the log film irradiance
% values for the observed pixels.
%
% Assumes:
%
% Zmin = 0
% Zmax = 255
%
% Arguments:
%
% Z(i, j) is the pixel values of pixel location number i in image j
% B(j) is the log delta t, or log shutter speed, for image j
          is lamdba, the constant that determines the amount of smoothness
%
   1
%
 w(z)
          is the weighting function value for pixel value z
%
% Returns:
%
% g(z)
         is the log exposure corresponding to pixel value z
%
  lE(i) is the log film irradiance at pixel location i
%
```

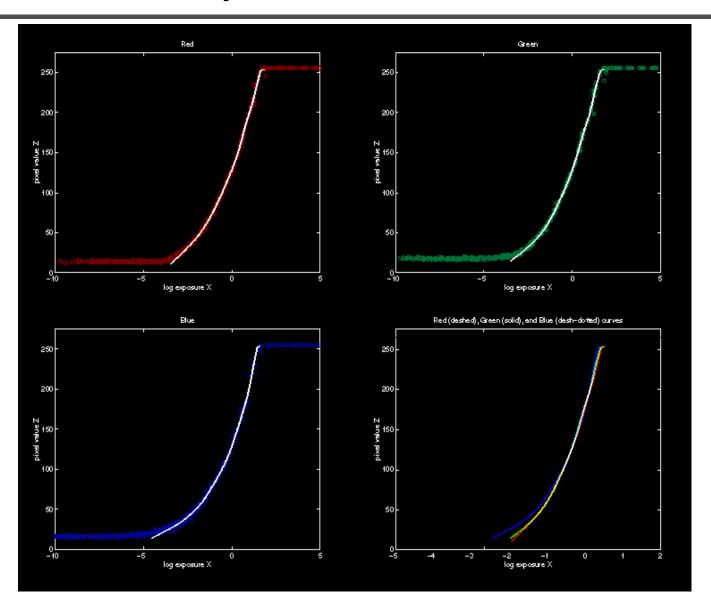
Digi<mark>VFX</mark>

Matlab code

```
function [g,lE]=gsolve(Z,B,l,w)
n = 256;
A = zeros(size(Z,1)*size(Z,2)+n+1,n+size(Z,1));
b = zeros(size(A,1),1);
k = 1; %% Include the data-fitting equations
for i=1:size(Z,1)
  for j=1:size(Z,2)
    wij = w(Z(i,j)+1);
    A(k,Z(i,j)+1) = wij; A(k,n+i) = -wij; b(k,1) = wij * B(j);
   k=k+1;
  end
end
A(k,129) = 1; %% Fix the curve by setting its middle value to 0
k=k+1;
for i=1:n-2 %% Include the smoothness equations
  A(k,i)=1*w(i+1); A(k,i+1)=-2*1*w(i+1); A(k,i+2)=1*w(i+1);
  k=k+1;
end
\mathbf{x} = \mathbf{A} \setminus \mathbf{b};
                  %% Solve the system using SVD
g = x(1:n);
lE = x(n+1:size(x,1));
```



Recovered response function





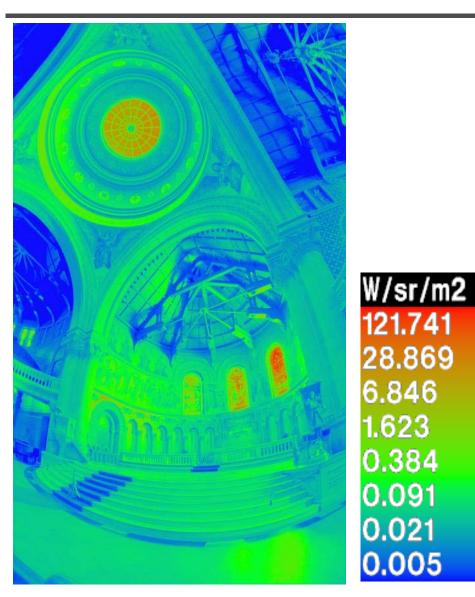
$$\ln E_i = g(Z_{ij}) - \ln \Delta t_j$$

combine pixels to reduce noise and obtain a more reliable estimation

$$\ln E_{i} = \frac{\sum_{j=1}^{P} w(Z_{ij})(g(Z_{ij}) - \ln \Delta t_{j})}{\sum_{j=1}^{P} w(Z_{ij})}$$

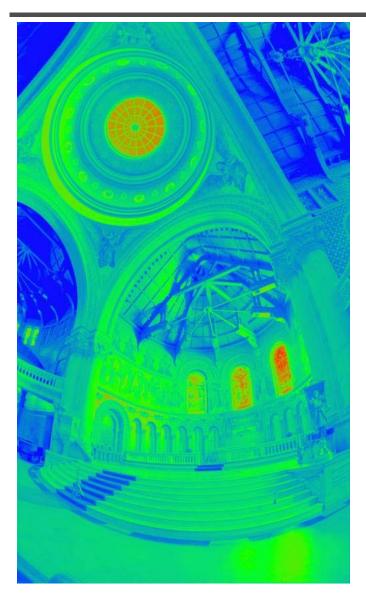
Reconstructed radiance map





What is this for?





- Human perception
- Vision/graphics applications



Automatic ghost removal





before

after



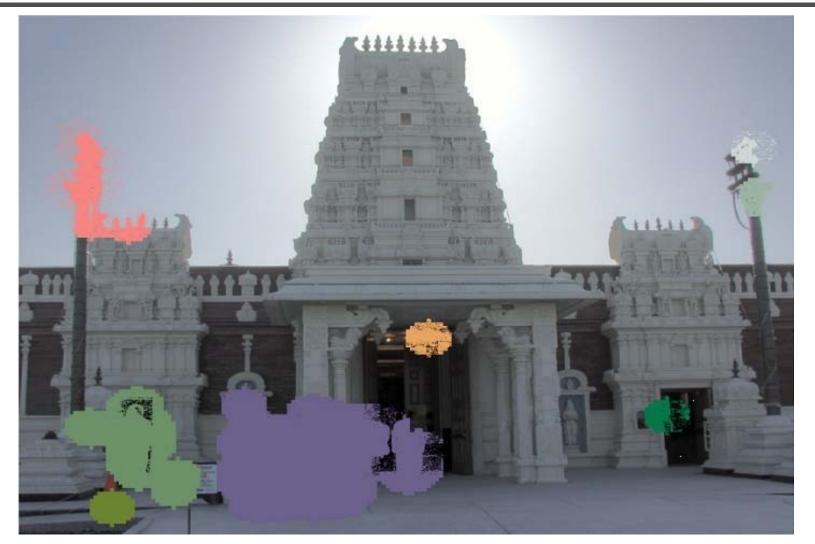
Weighted variance



Moving objects and high-contrast edges render high variance.



Region masking



Thresholding; dilation; identify regions;

Best exposure in each region







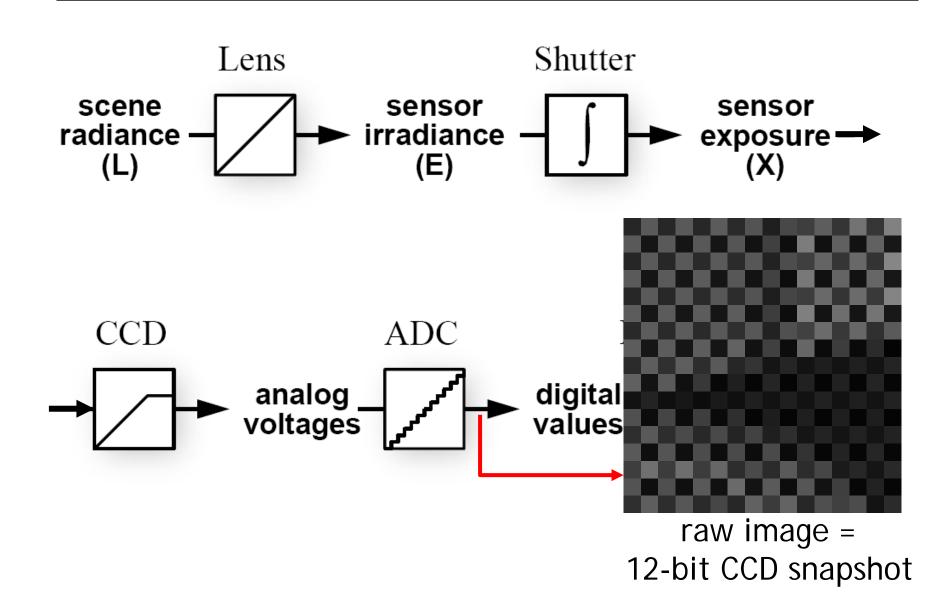
Lens flare removal



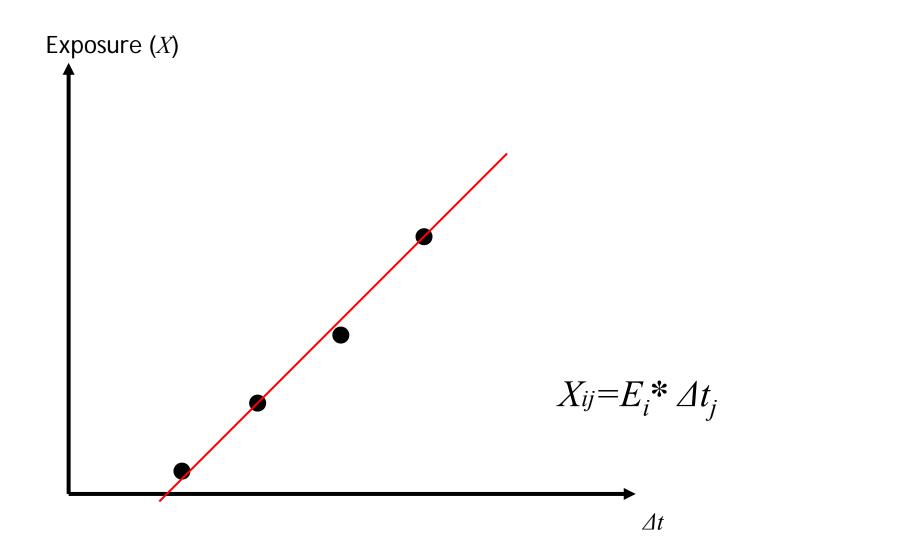
before

after





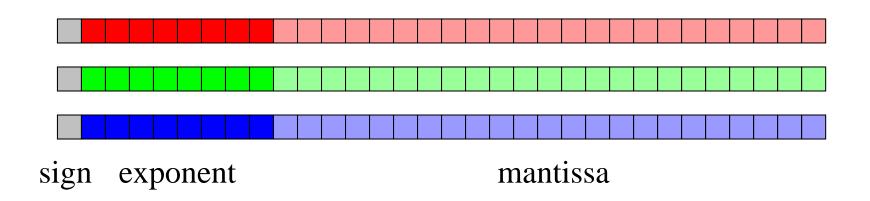




Portable floatMap (.pfm)



• 12 bytes per pixel, 4 for each channel

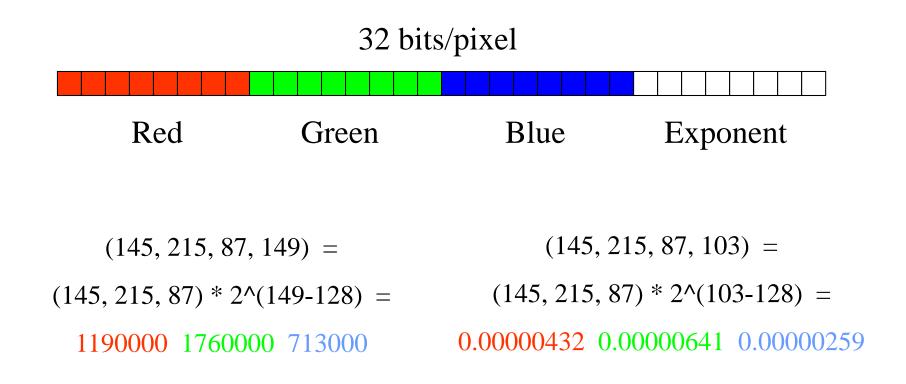


Text header similar to Jeff Poskanzer's .ppm image format:

PF 768 512 1 <binary image data>

Floating Point TIFF similar



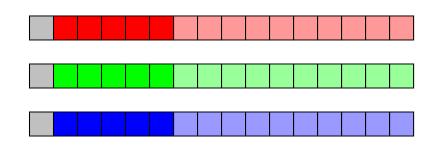


Ward, Greg. "Real Pixels," in Graphics Gems IV, edited by James Arvo, Academic Press, 1994

ILM's OpenEXR (.exr)



• 6 bytes per pixel, 2 for each channel, compressed



sign exponent mantissa

- Several lossless compression options, 2:1 typical
- Compatible with the "half" datatype in NVidia's Cg
- Supported natively on GeForce FX and Quadro FX
- Available at http://www.openexr.net/

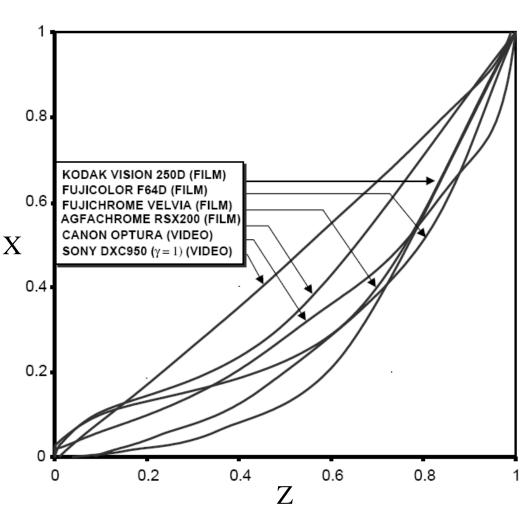


Radiometric self calibration

 Assume that any response function can be modeled as a high-order polynomial

$$X = g(Z) = \sum_{m=0}^{M} c_m Z^m$$

 No need to know exposure time in advance. Useful for cheap cameras





• To find the coefficients c_m to minimize the following

$$\mathcal{E} = \sum_{i=1}^{N} \sum_{j=1}^{P} \left[\sum_{m=0}^{M} c_m Z_{ij}^m - R_{j,j+1} \sum_{m=0}^{M} c_m Z_{i,j+1}^m \right]^2$$
A guess for the ratio of
$$\frac{X_{ij}}{X_{i,j+1}} = \frac{E_i \Delta t_j}{E_i \Delta t_{j+1}} = \frac{\Delta t_j}{\Delta t_{j+1}}$$



- Again, we can only solve up to a scale. Thus, add a constraint f(1)=1. It reduces to M-1 variables.
- How to solve it?



• We solve the above iteratively and update the exposure ratio accordingly

$$R_{j,j+1}^{(k)} = \frac{1}{N} \sum_{i=1}^{N} \frac{\sum_{m=0}^{M} c_m^{(k)} Z_{ij}^m}{\sum_{m=0}^{M} c_m^{(k)} Z_{i,j+1}^m}$$

 How to determine M? Solve up to M=10 and pick up the one with the minimal error. Notice that you prefer to have the same order for all channels. Use the combined error.



$$Z_{ij} = f(E_i \Delta t_j)$$
$$g(Z_{ij}) = f^{-1}(Z_{ij}) = E_i \Delta t_j$$

Given Z_{ij} and Δt_{ji} the goal is to find both E_i and $g(Z_{ij})$

Maximum likelihood

$$\Pr(E_i, g \mid Z_{ij}, \Delta t_j) \propto \exp\left(-\frac{1}{2} \sum_{ij} w(Z_{ij}) \left(g(Z_{ij}) - E_i \Delta t_j\right)^2\right)$$
$$\hat{g}, \hat{E}_i = \arg\min_{g, E_i} \sum_{ij} w(Z_{ij}) \left(g(Z_{ij}) - E_i \Delta t_j\right)^2$$



$$\hat{g}, \hat{E}_i = \arg\min_{g, E_i} \sum_{ij} w(Z_{ij}) \Big(g(Z_{ij}) - E_i \Delta t_j\Big)^2$$

assuming $g(Z_{ij})$ is known, optimize for E_i assuming E_i is known, optimize for $g(Z_{ij})$ until converge



$$\hat{g}, \hat{E}_i = \arg\min_{g, E_i} \sum_{ij} w(Z_{ij}) \Big(g(Z_{ij}) - E_i \Delta t_j\Big)^2$$

assuming $g(Z_{ij})$ is known, optimize for E_i assuming E_i is known, optimize for $g(Z_{ij})$ until converge



$$\hat{g}, \hat{E}_i = \arg\min_{g, E_i} \sum_{ij} w(Z_{ij}) \Big(g(Z_{ij}) - E_i \Delta t_j\Big)^2$$

assuming $g(Z_{ij})$ is known, optimize for E_i assuming E_i is known, optimize for $g(Z_{ij})$ until converge

$$E_{i} = \frac{\sum_{j} w(Z_{ij})g(Z_{ij})\Delta t_{j}}{\sum_{j} w(Z_{ij})\Delta t_{j}^{2}}$$



$$\hat{g}, \hat{E}_i = \arg\min_{g, E_i} \sum_{ij} w(Z_{ij}) \Big(g(Z_{ij}) - E_i \Delta t_j\Big)^2$$

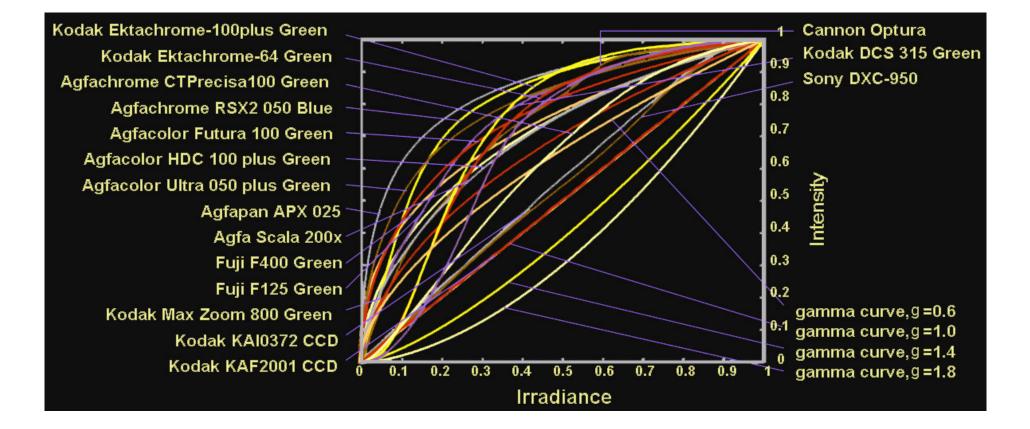
assuming $g(Z_{ij})$ is known, optimize for E_i assuming E_i is known, optimize for $g(Z_{ij})$ until converge

$$g(m) = \frac{1}{|E_m|} \sum_{ij \in E_m} E_i \Delta t_j$$

normalize so that g(128) = 1

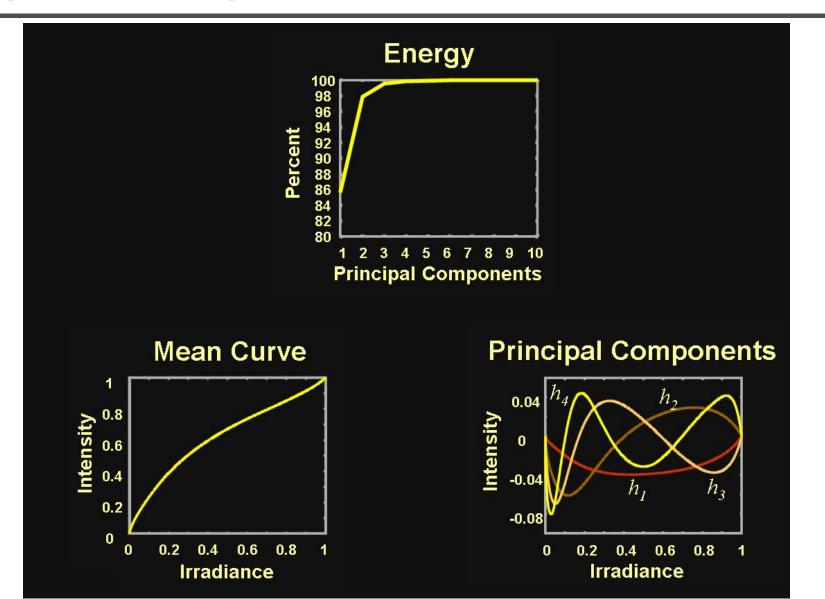
Space of response curves





Space of response curves







Patch-Based HDR



Input LDR sources

Reconstructed LDR images

Final tonemapped HDR result



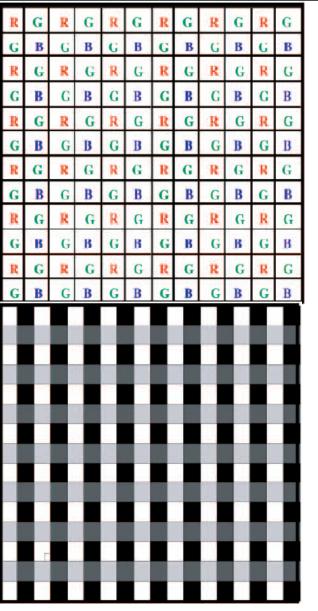
HDR Video

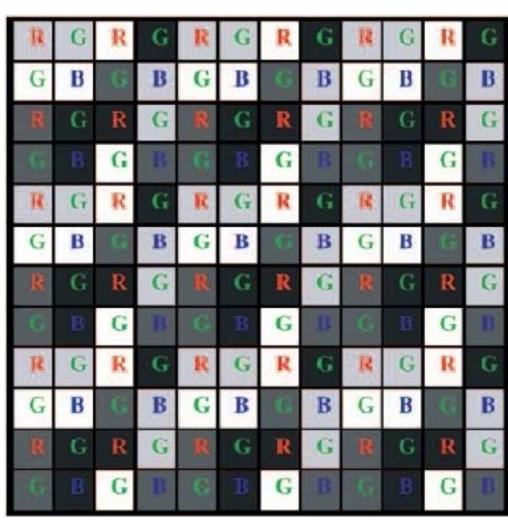
 High Dynamic Range Video Sing Bing Kang, Matthew Uyttendaele, Simon Winder, Richard Szeliski
 SIGGRAPH 2003





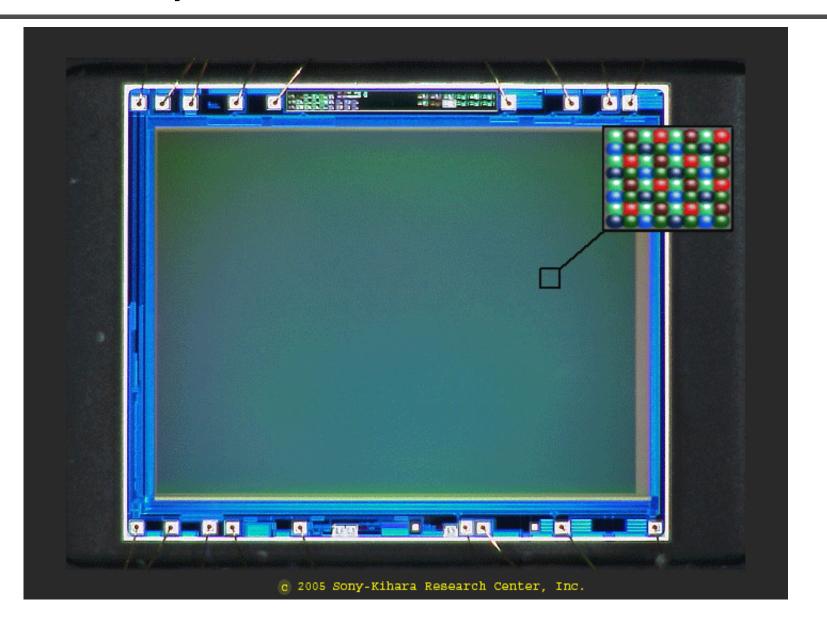
Assorted pixel







Assorted pixel





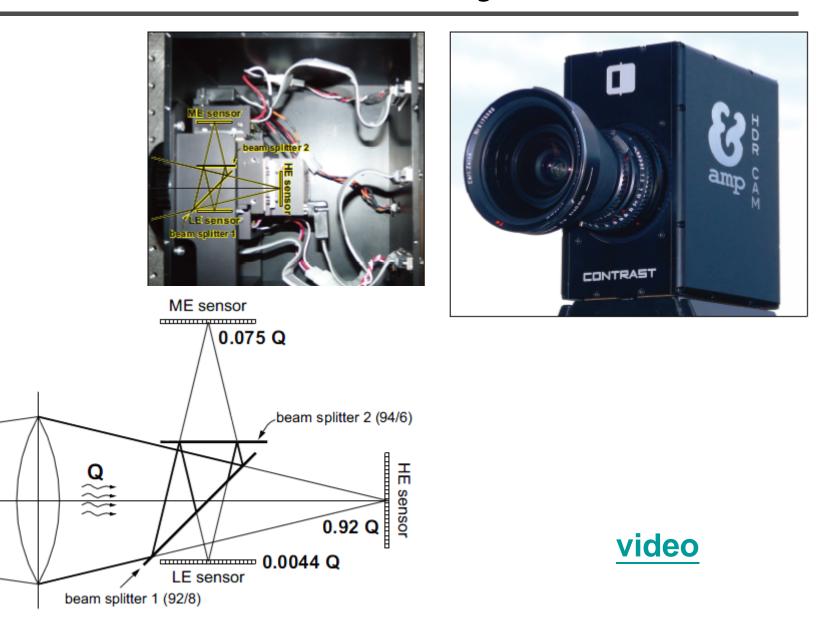
Assorted pixel



c 2005 Sony-Kihara Research Center, Inc.

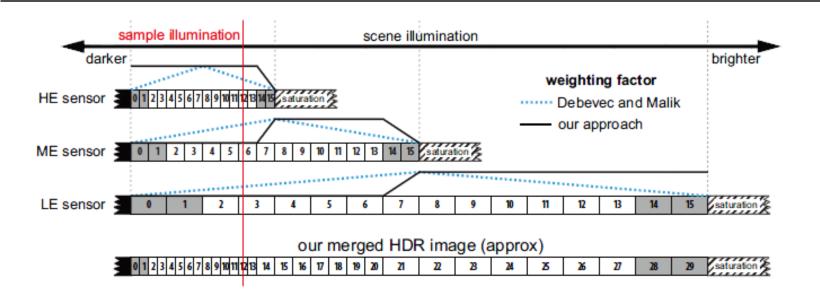


A Versatile HDR Video System



DigiVFX

A Versatile HDR Video System





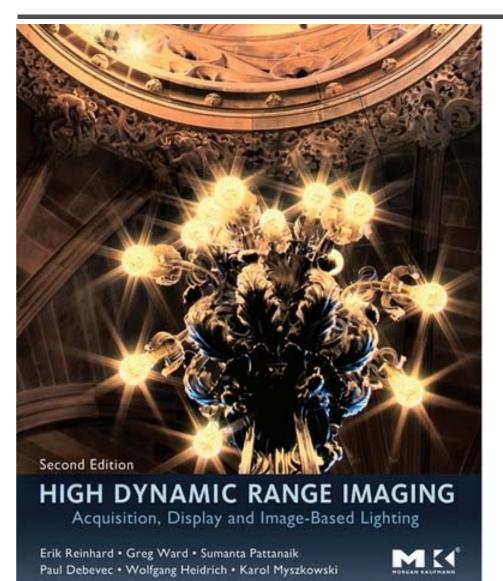
HDR becomes common practice



- Many cameras has bracket exposure modes
- iPhone 4 has HDR option, but it is more exposure blending rather than true HDR.



References



References

- Paul E. Debevec, Jitendra Malik, <u>Recovering High Dynamic Range</u> <u>Radiance Maps from Photographs</u>, SIGGRAPH 1997.
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- Mark Robertson, Sean Borman, Robert Stevenson, <u>Estimation-</u> <u>Theoretic Approach to Dynamic Range Enhancement using Multiple</u> <u>Exposures</u>, Journal of Electronic Imaging 2003.
- Michael Grossberg, Shree Nayar, <u>Determining the Camera Response</u> from Images: What Is Knowable, PAMI 2003.
- Michael Grossberg, Shree Nayar, <u>Modeling the Space of Camera</u> <u>Response Functions</u>, PAMI 2004.
- Srinivasa Narasimhan, Shree Nayar, <u>Enhancing Resolution Along</u> <u>Multiple Imaging Dimensions Using Assorted Pixels</u>, PAMI 2005.
- G. Krawczyk, M. Goesele, H.-P. Seidel, <u>Photometric Calibration of</u> <u>High Dynamic Range Cameras</u>, MPI Research Report 2005.
- G. Ward, <u>Fast Robust Image Registration for Compositing High</u> <u>Dynamic Range Photographs from Hand-held Exposures</u>, jgt 2003.