

# Matting and Compositing

*Digital Visual Effects*  
Yung-Yu Chuang

## Outline

- Traditional matting and compositing
- The matting problem
- Bayesian matting and extensions
- Matting with less user inputs
- Matting with multiple observations
- Beyond the compositing equation\*
- Conclusions

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- **Traditional matting and compositing**
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## Photomontage



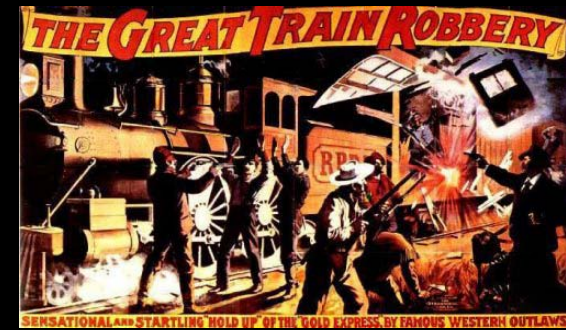
The Two Ways of Life, 1857, Oscar Gustav Rejlander  
Printed from the original 32 wet collodion negatives.

## Photographic compositions



Lang Ching-shan

## Use of mattes for compositing



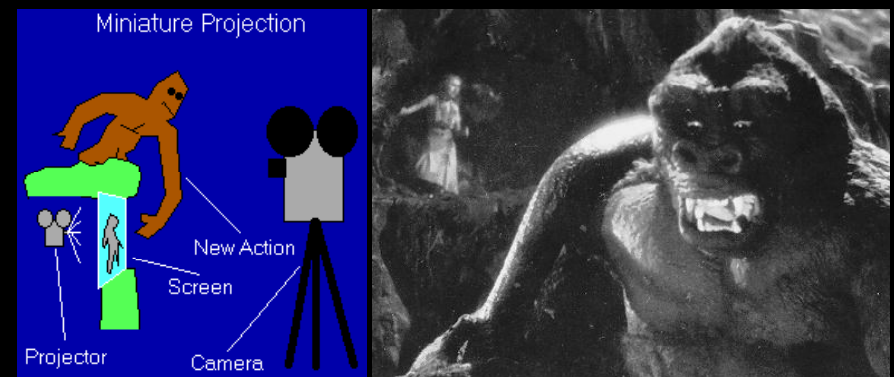
The Great Train Robbery (1903) matte shot

## Use of mattes for compositing



The Great Train Robbery (1903) matte shot

## Optical compositing



King Kong (1933) Stop-motion + optical compositing

## Digital matting and compositing

The lost world (1925)



Miniature, stop-motion

The lost world (1997)



Computer-generated images

## Digital matting and compositing

King Kong (1933)



Optical compositing

Jurassic Park III (2001)

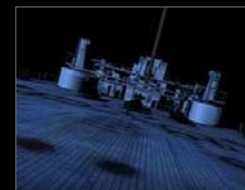


Blue-screen matting,  
digital composition,  
digital matte painting

Smith Duff Catmull Porter



Oscar award, 1996



Titanic



Matting and Compositing



background replacement



background editing



## Matting and Compositing

## Digital matting: bluescreen matting



Forrest Gump (1994)

- The most common approach for films.
- Expensive, studio setup.
- Not a simple one-step process.

## Color difference method (Ultimate)

$$C = F + \bar{\alpha}B$$

F

$\bar{\alpha}$



Blue-screen photograph



Spill suppression if  $B > G$  then  $B = G$



Matte creation  $\bar{\alpha} = B - \max(G, R)$

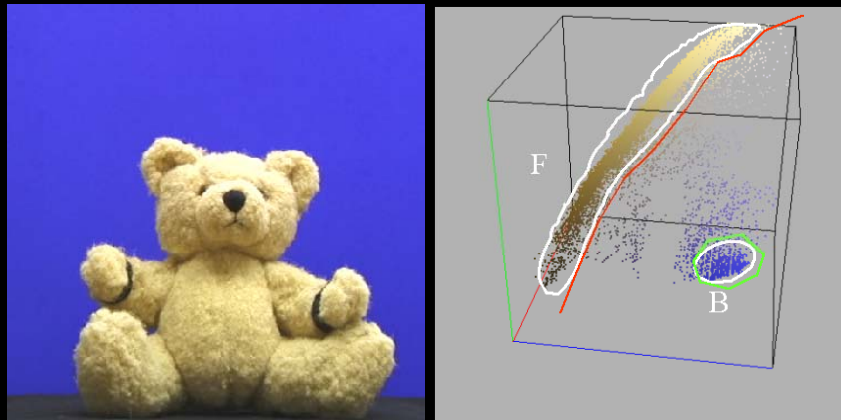
demo with Paint Shop Pro ( $B = \min(B, G)$ )

## Problems with color difference

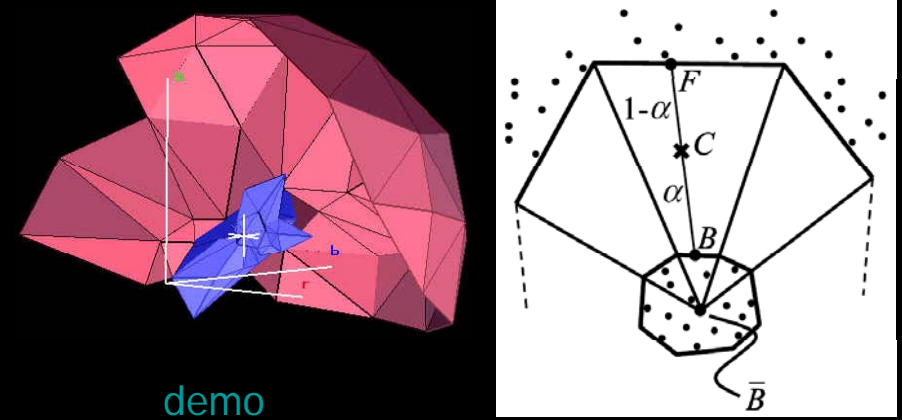


Background color is usually not perfect! (lighting, shadowing...)

## Chroma-keying (Primatte)



## Chroma-keying (Primatte)

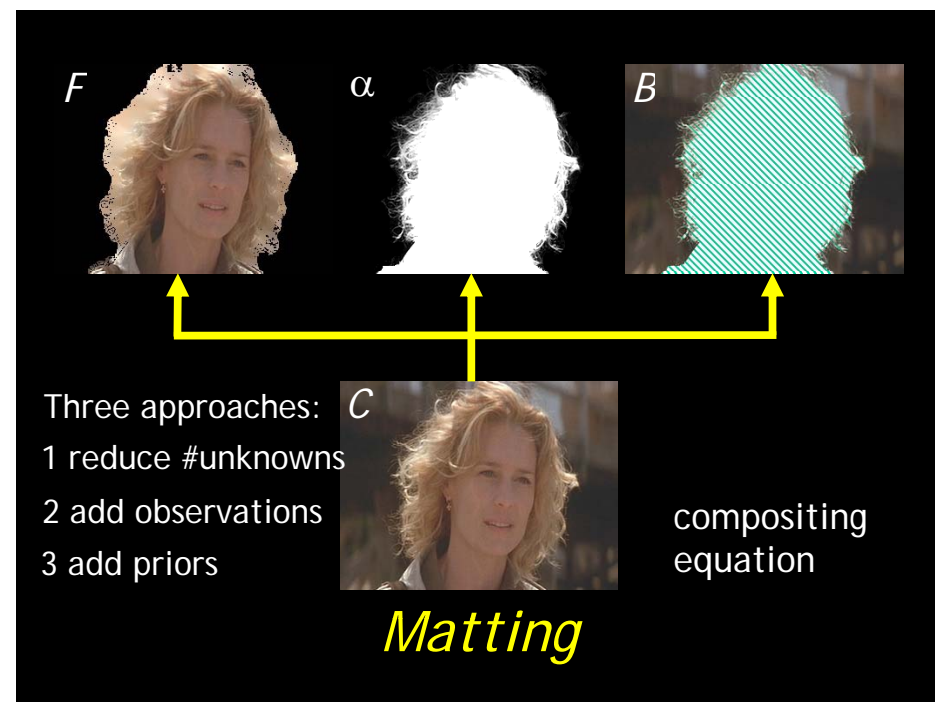
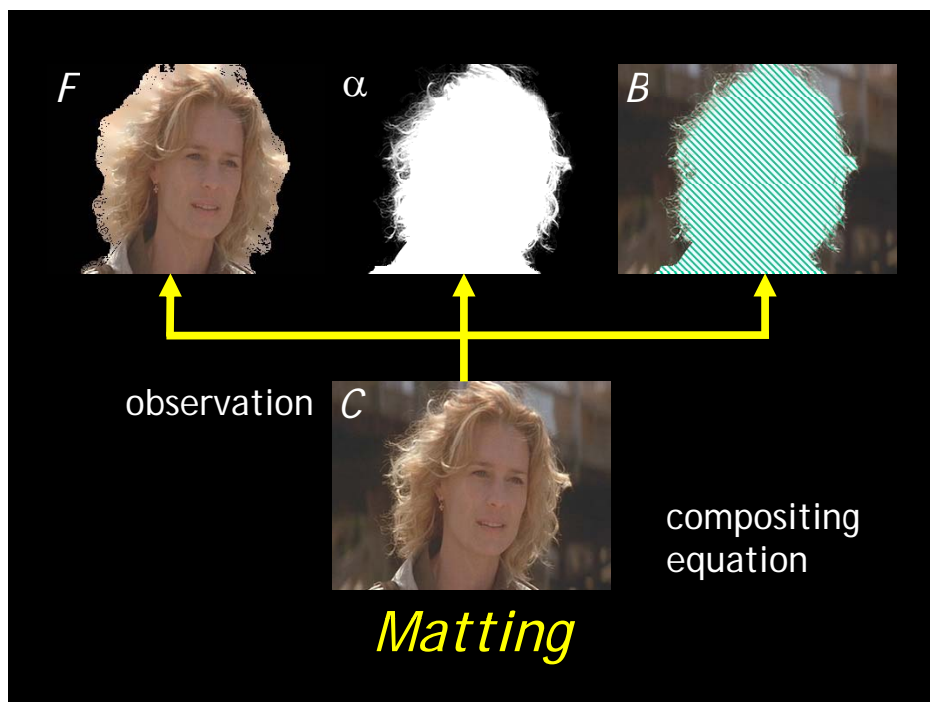
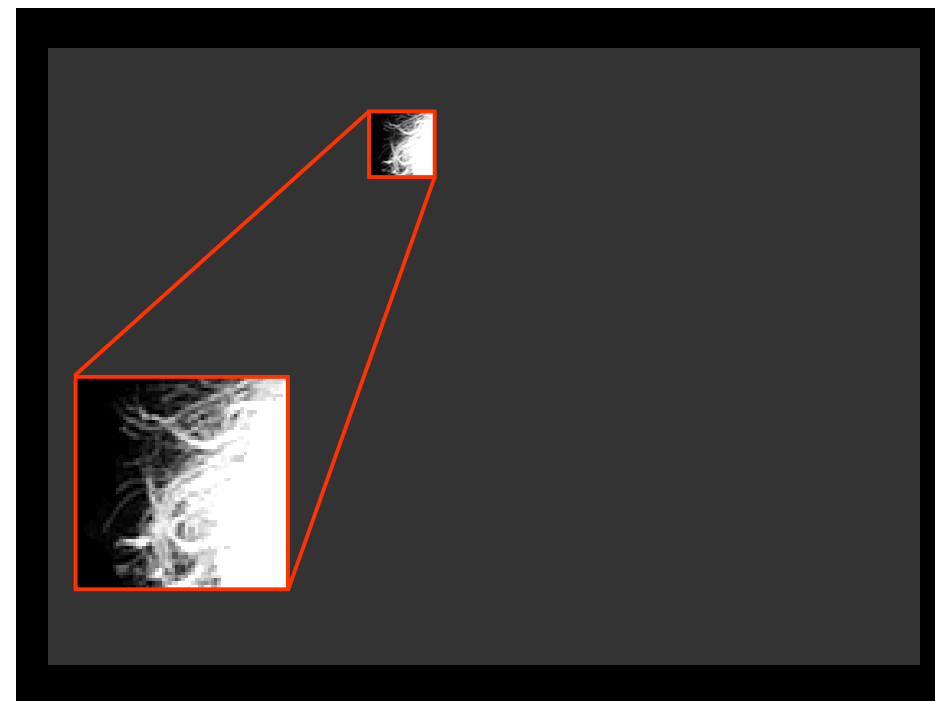
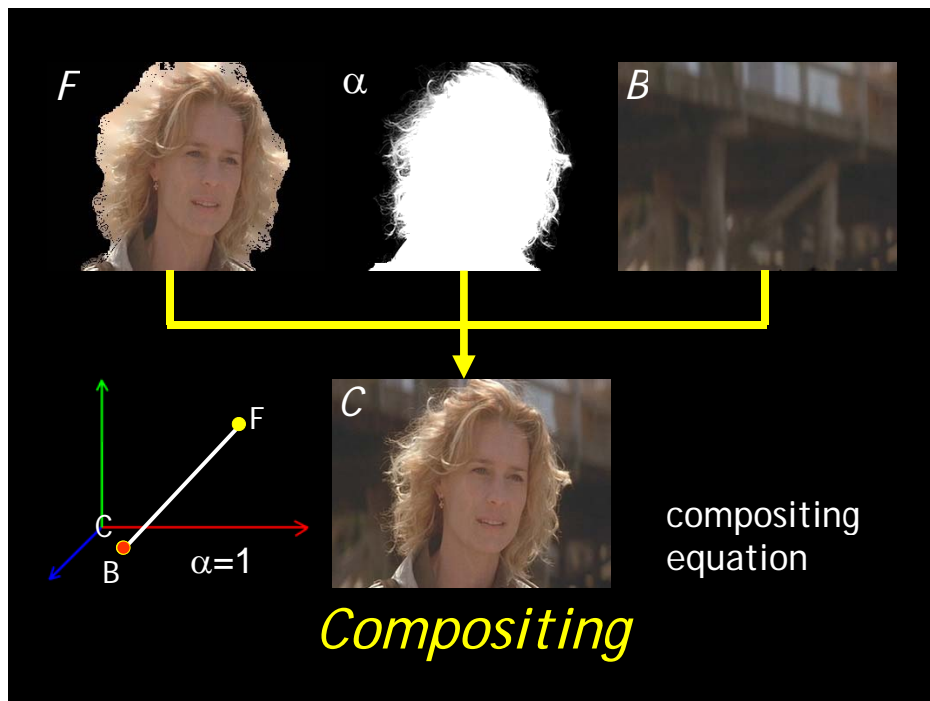


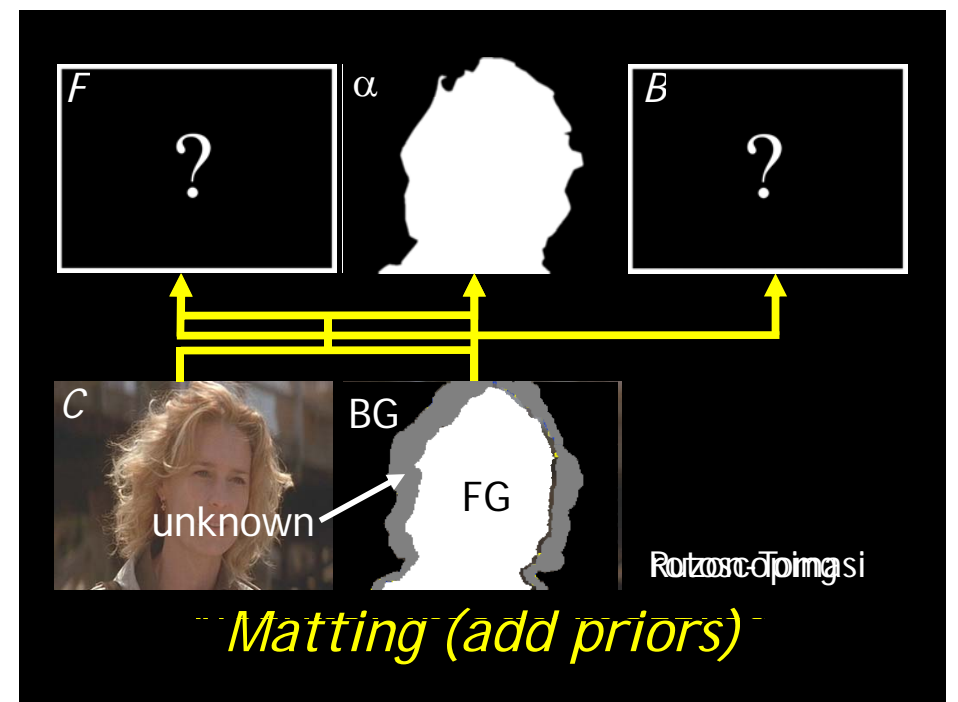
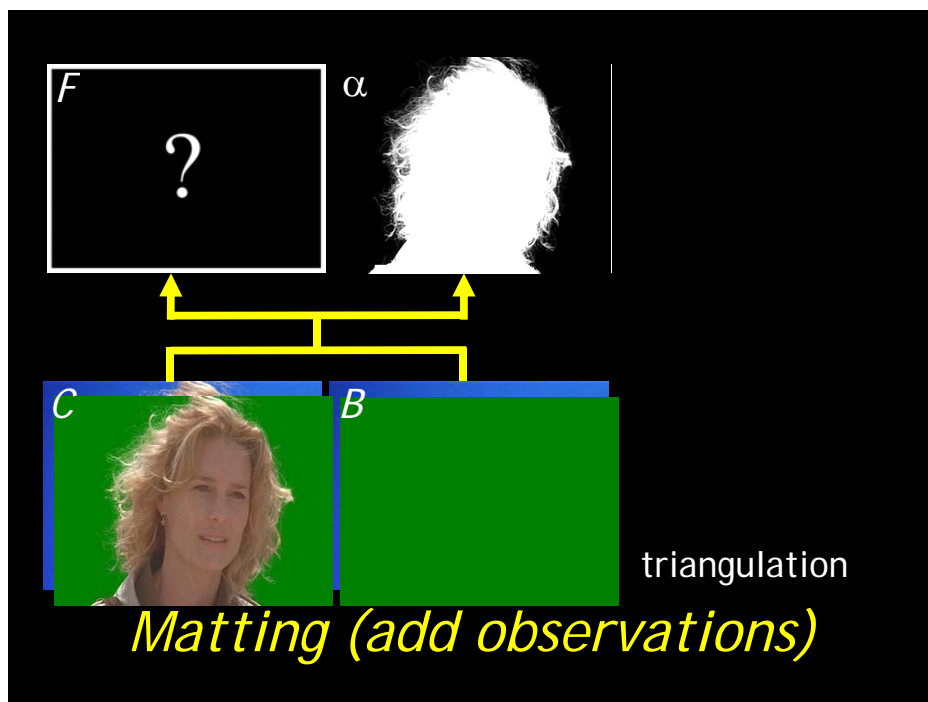
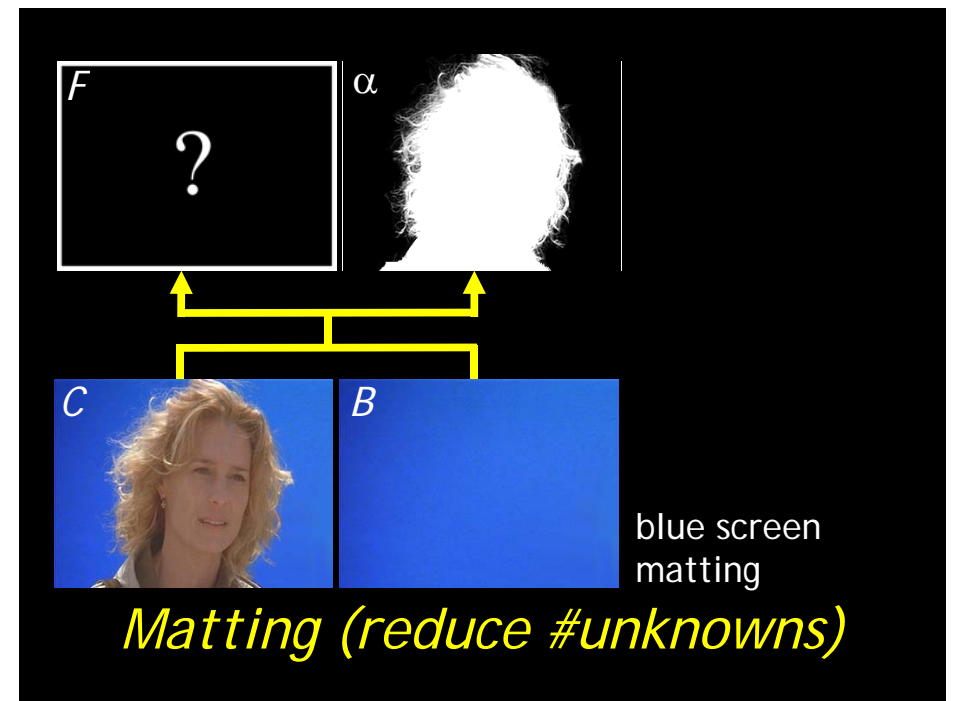
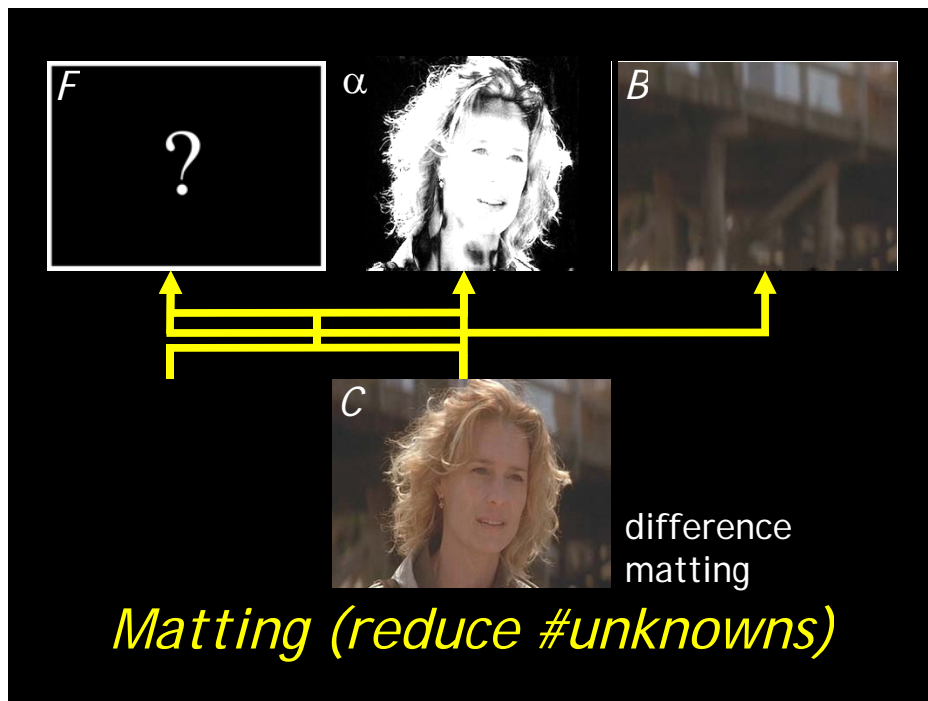
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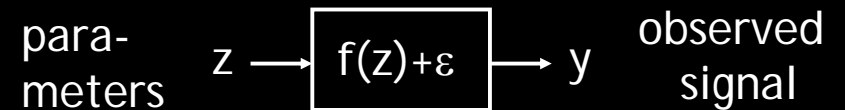
## Compositing





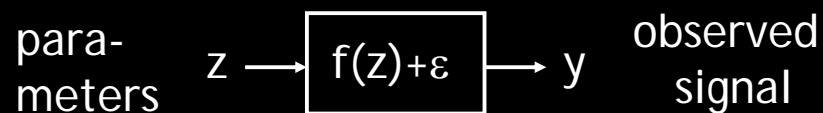
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Example:  
super-resolution  
de-blurring  
de-blocking  
...

*Bayesian framework*



data  
evidence

*a-priori*  
knowledge

*Bayesian framework*

posterior probability

likelihood

priors

$$\arg \max_{F, B, \alpha} P(F, B, \alpha | C)$$
$$= \arg \max_{F, B, \alpha} P(C | F, B, \alpha) P(F) P(B) P(\alpha) / P(C)$$

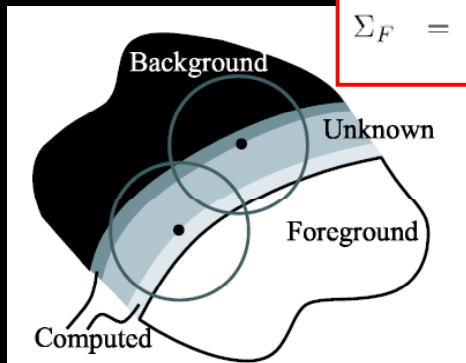
$$L(C | F, B, \alpha) = -\|C - \alpha F - (1 - \alpha)B\|^2 / 2\sigma_C^2$$

*Bayesian framework*



$$\bar{F} = \frac{1}{W} \sum_{i \in N} w_i F_i$$

$$\Sigma_F = \frac{1}{W} \sum_{i \in N} w_i (F_i - \bar{F})(F_i - \bar{F})^T$$



$$L(F) = -(F - \bar{F})^T \Sigma_F^{-1} (F - \bar{F}) / 2$$

*Priors*

$$\arg \max_{F, B, \alpha} L(C | F, B, \alpha) + L(F) + L(B)$$

$$\arg \max_{F, B, \alpha} -\|C - \alpha F - (1 - \alpha)B\|^2 / 2\sigma_C^2$$

$$-(F - \bar{F})^T \Sigma_F^{-1} (F - \bar{F}) / 2$$

$$-(B - \bar{B})^T \Sigma_B^{-1} (B - \bar{B}) / 2$$

*Bayesian matting*

repeat

1. fix alpha

$$\begin{bmatrix} \Sigma_F^{-1} + I\alpha^2/\sigma_C^2 & I\alpha(1 - \alpha)/\sigma_C^2 \\ I\alpha(1 - \alpha)/\sigma_C^2 & \Sigma_B^{-1} + I(1 - \alpha)^2/\sigma_C^2 \end{bmatrix} \begin{bmatrix} F \\ B \end{bmatrix}$$

$$= \begin{bmatrix} \Sigma_F^{-1}\bar{F} + C\alpha/\sigma_C^2 \\ \Sigma_B^{-1}\bar{B} + C(1 - \alpha)/\sigma_C^2 \end{bmatrix}$$

2. fix F and B

$$\alpha = \frac{(C - B) \cdot (F - B)}{\|F - B\|^2}$$

until converge

*Optimization*



**Bayesian image matting**



**Bayesian image matting**



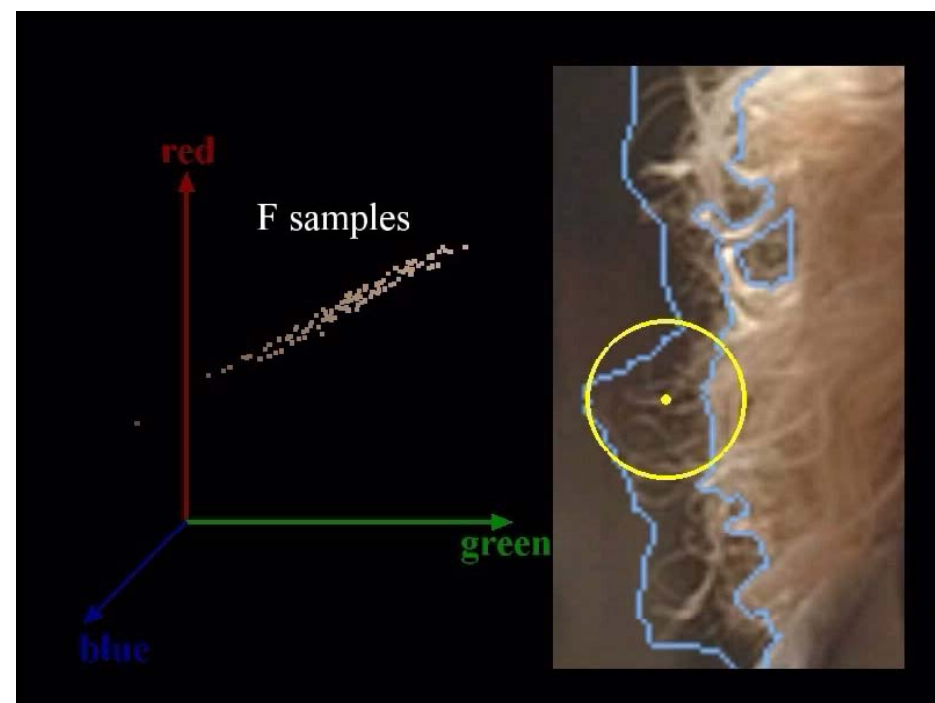
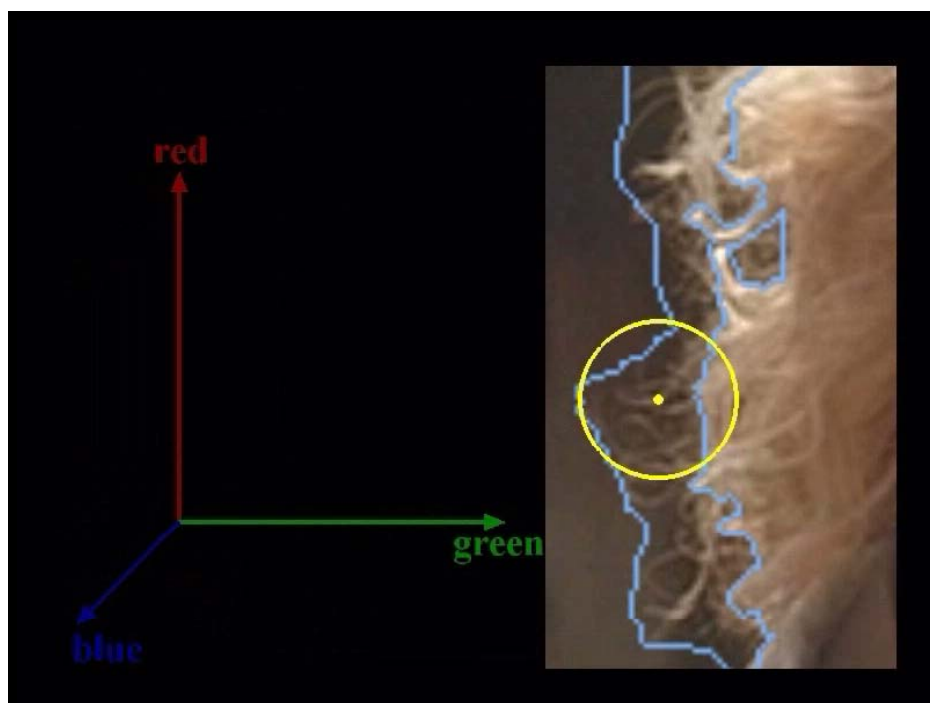
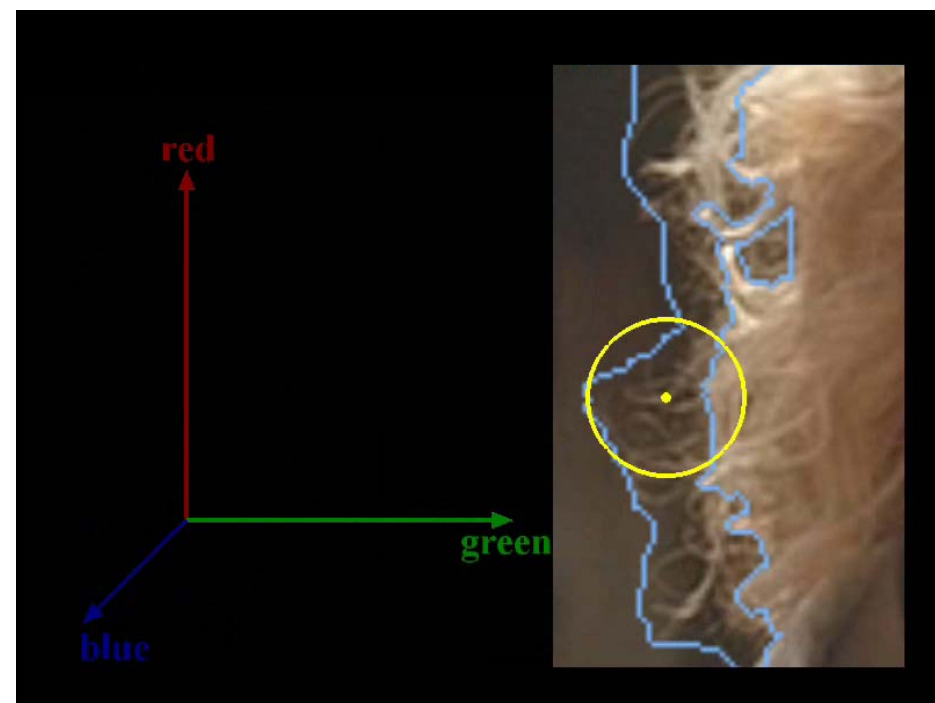
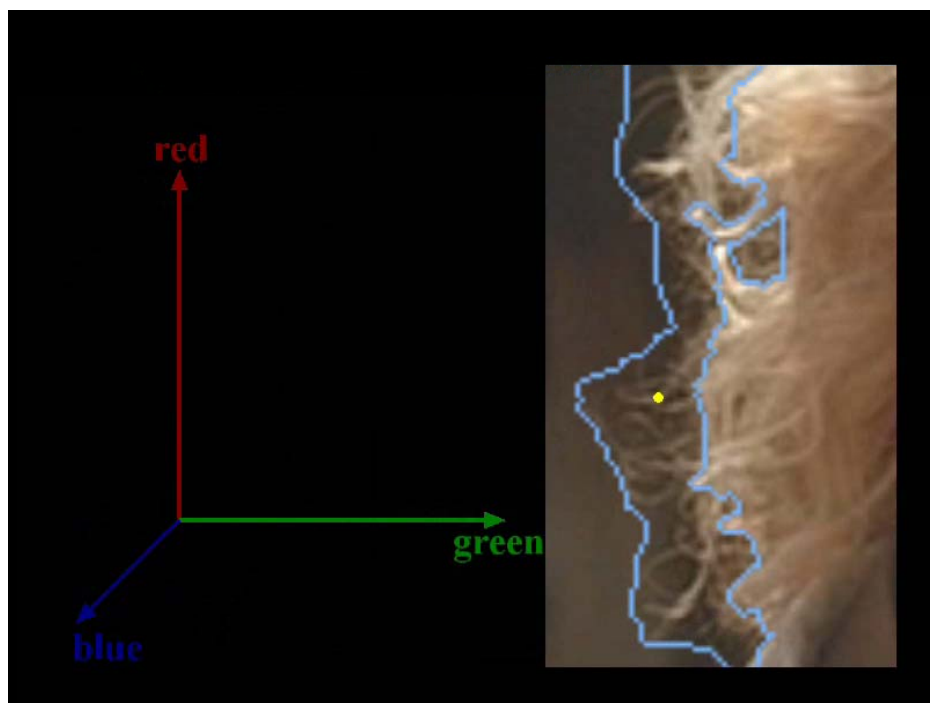
**Bayesian image matting**

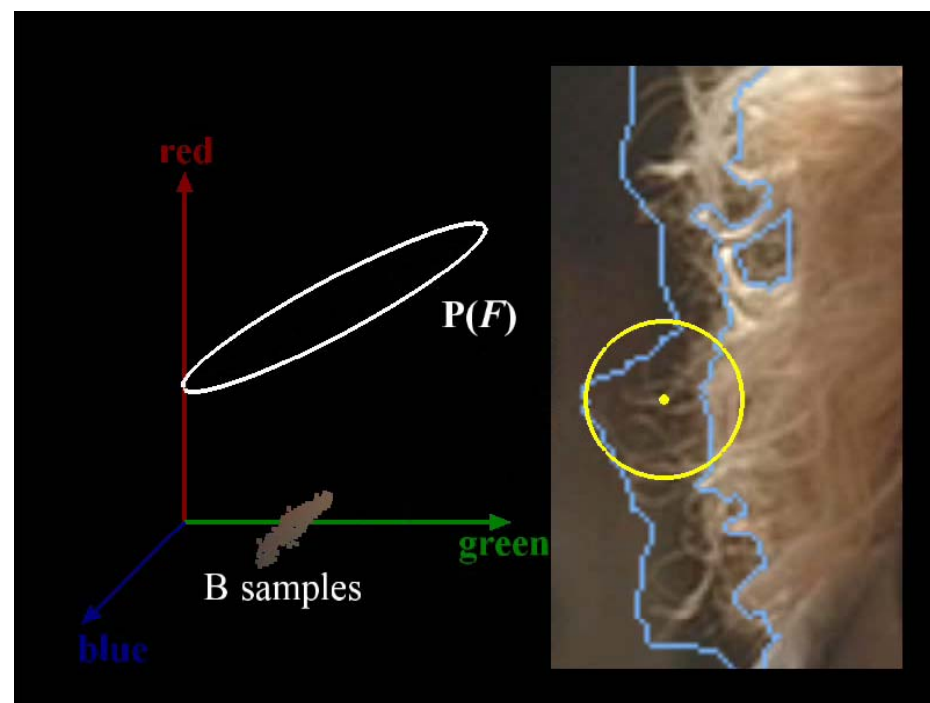
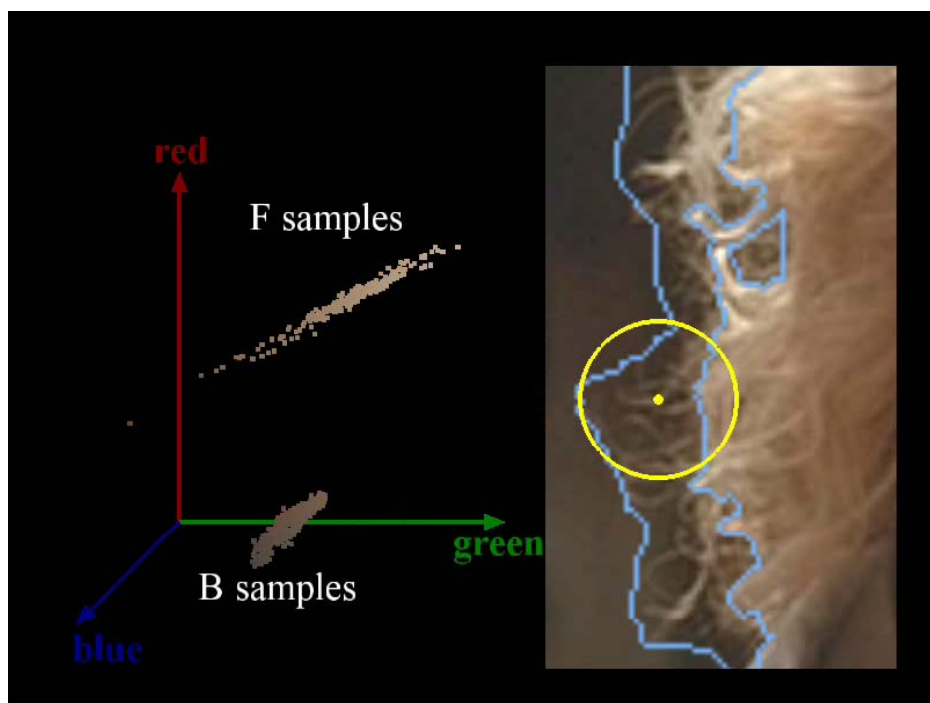
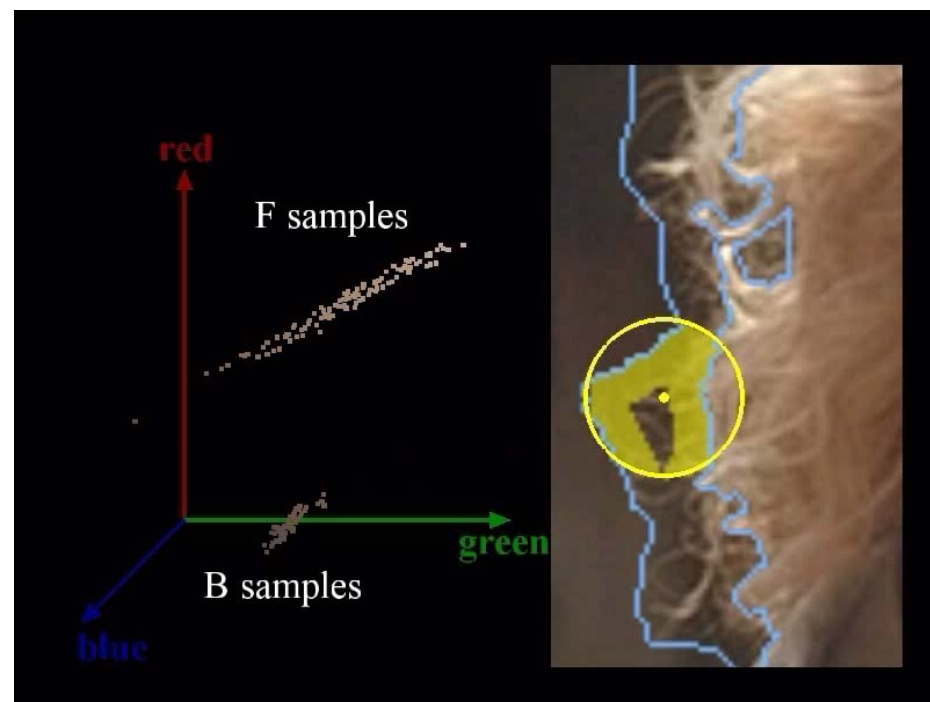
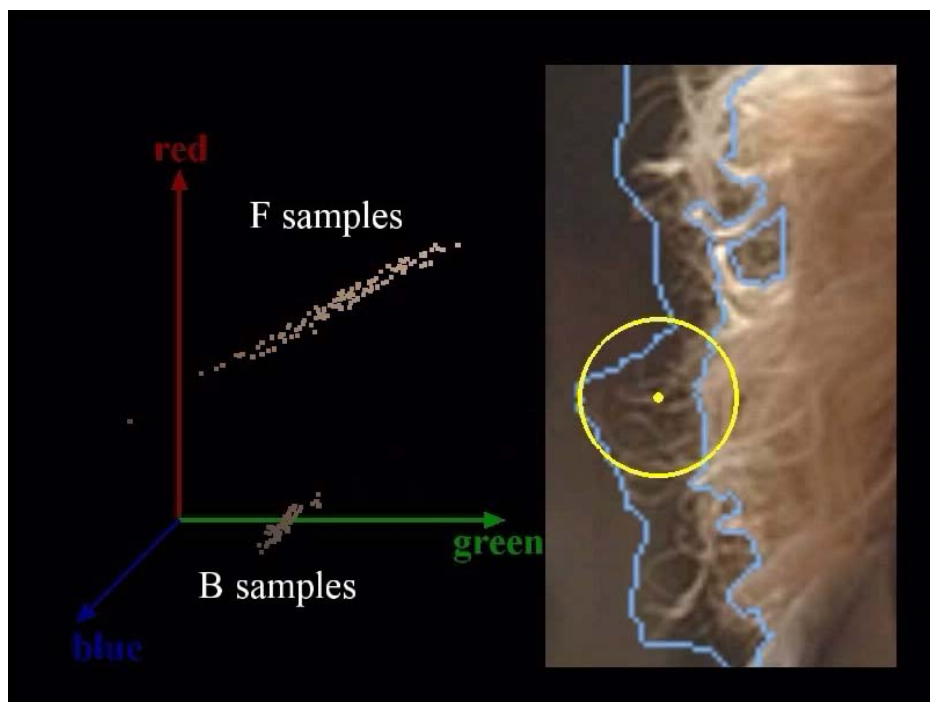


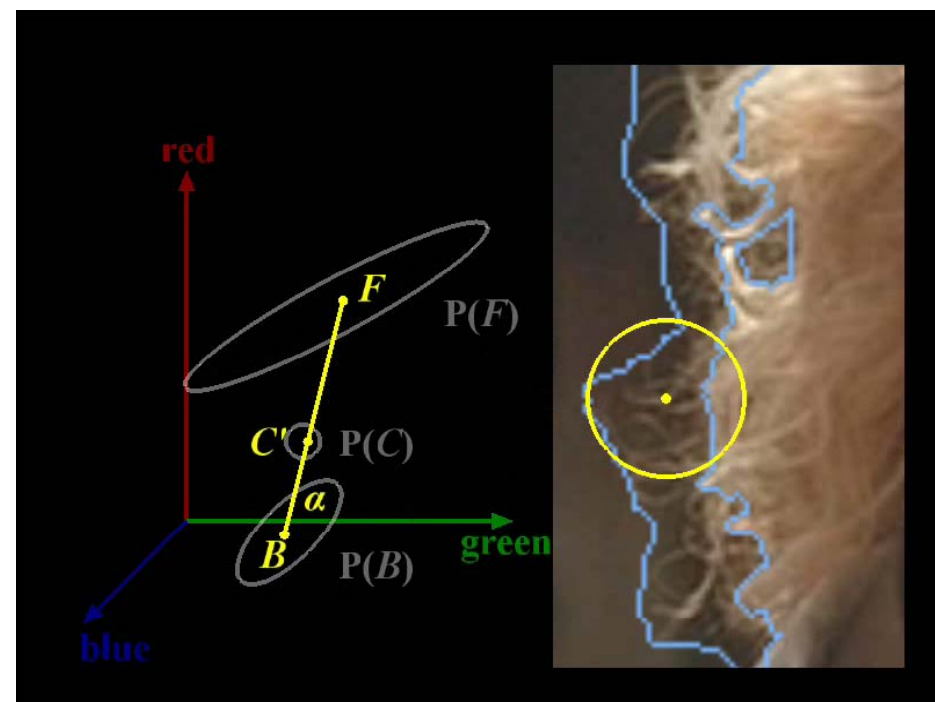
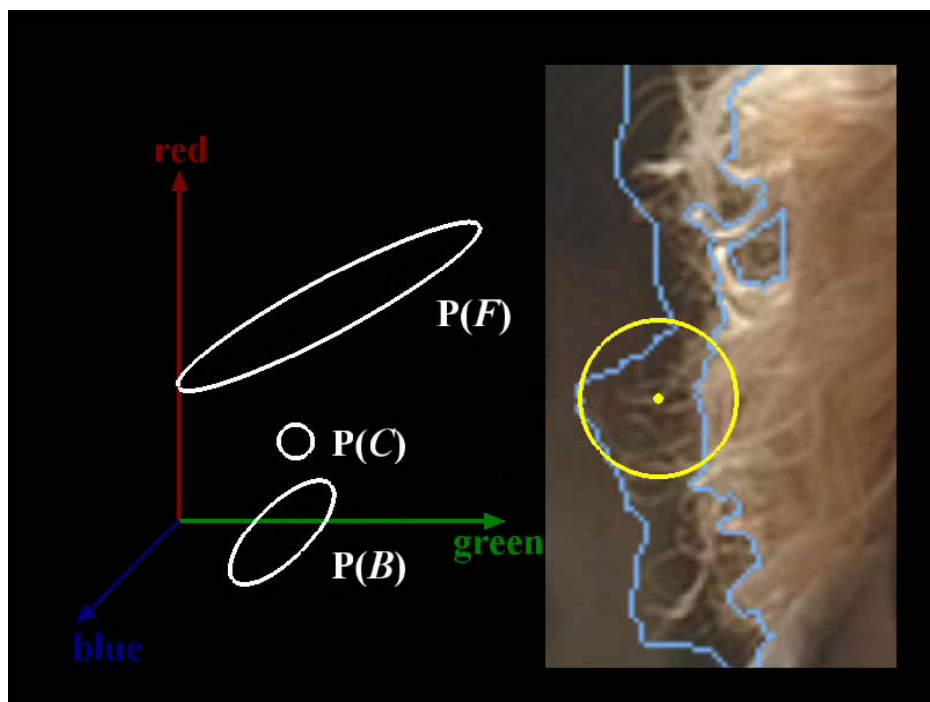
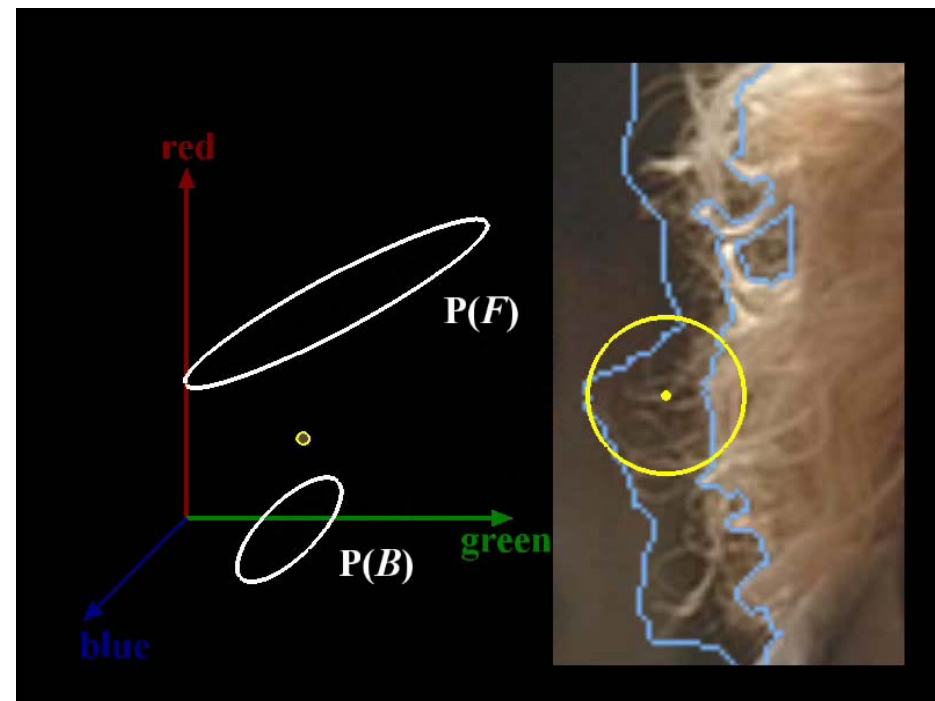
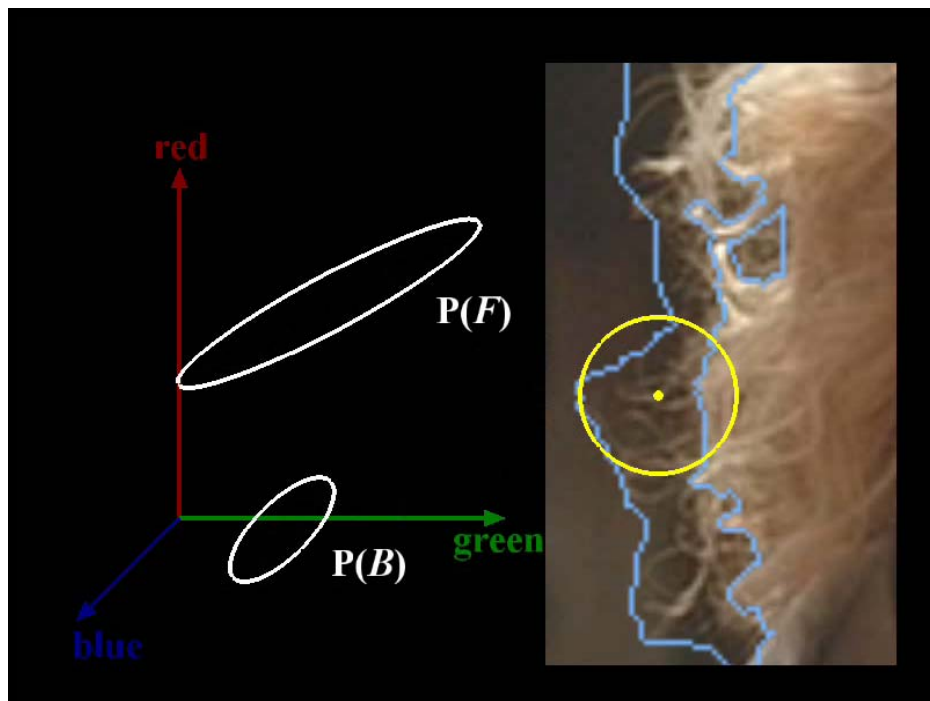
**Bayesian image matting**



**Bayesian image matting**









*Demo*

alpha



*Results*

input

composite



*Results*

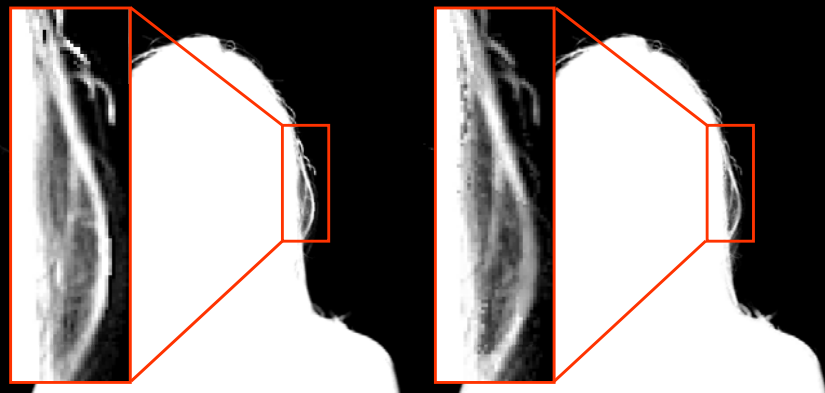
trimap



*Comparisons*

Bayesian

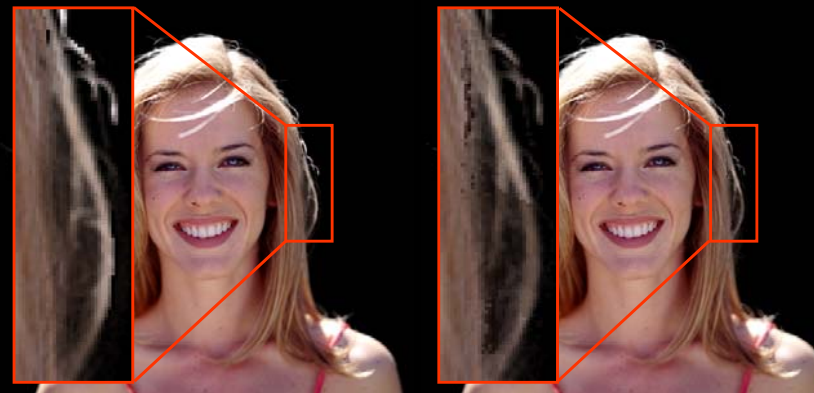
Ruzon-Tomasi



*Comparisons*

Bayesian

Ruzon-Tomasi



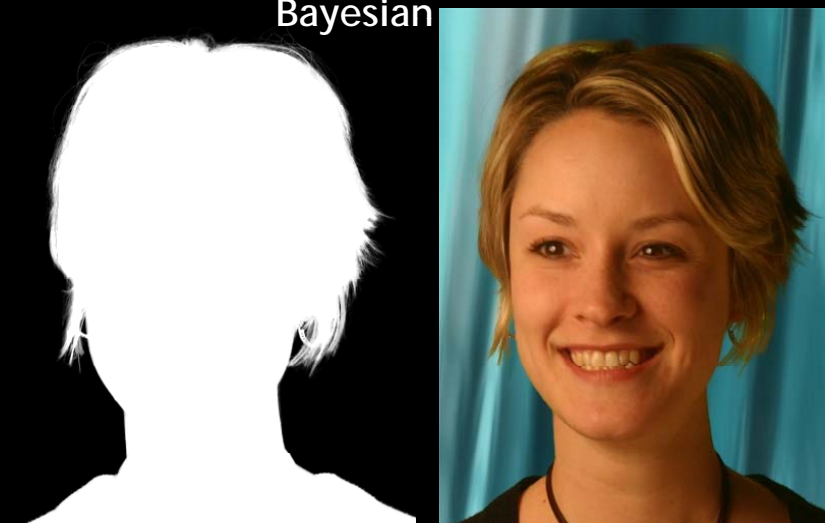
*Comparisons*

Mishima



*Comparisons*

Bayesian



*Comparisons*

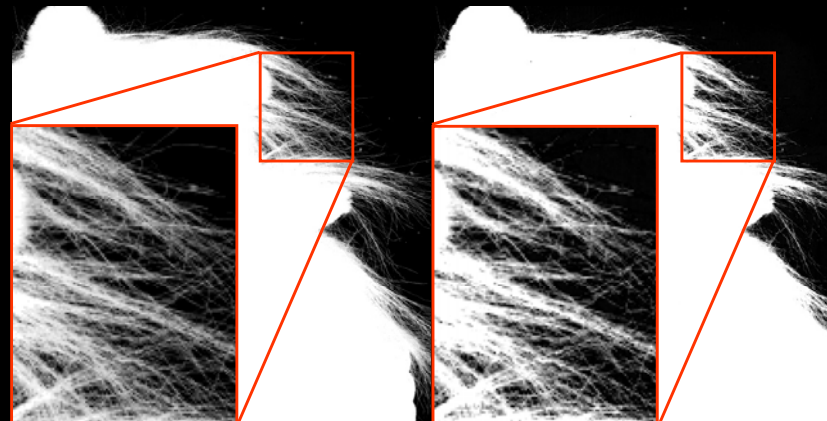
input image



*Comparisons*

Bayesian

Mishima



*Comparisons*

Bayesian

Mishima



*Comparisons*

input  
video



*Video matting*



input  
video



input  
key  
trimaps



*Video matting*

input  
video



interpo-  
lated  
trimaps

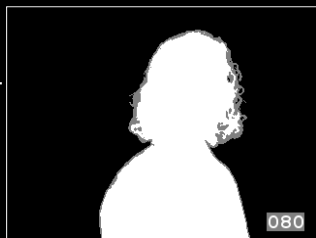


*Video matting*

input  
video



interpo-  
lated  
trimaps



output  
alpha

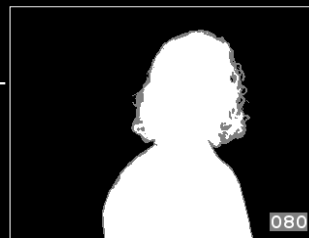


*Video matting*

input  
video



interpo-  
lated  
trimaps



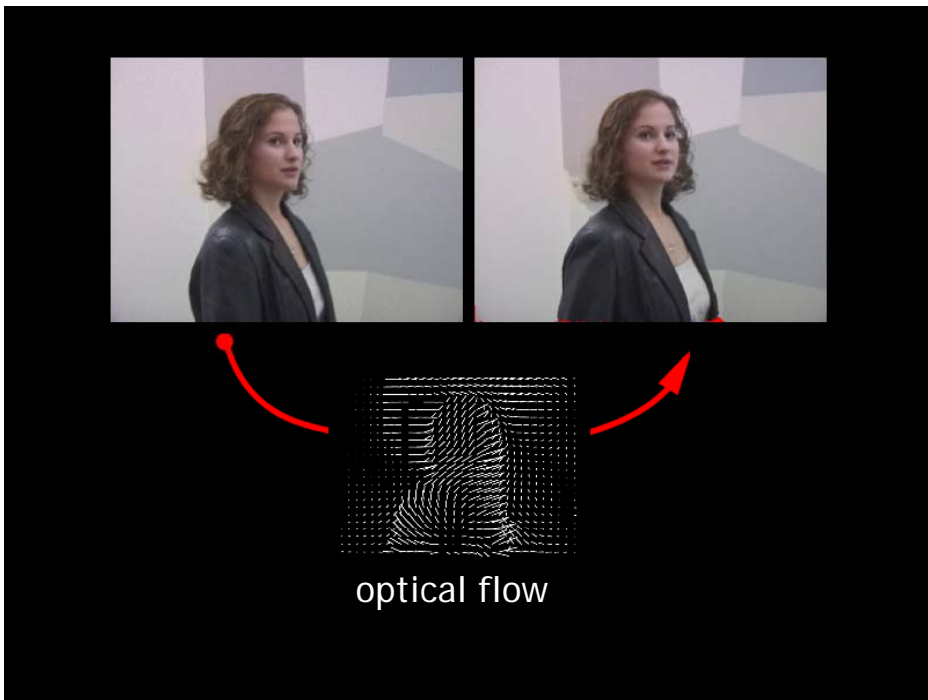
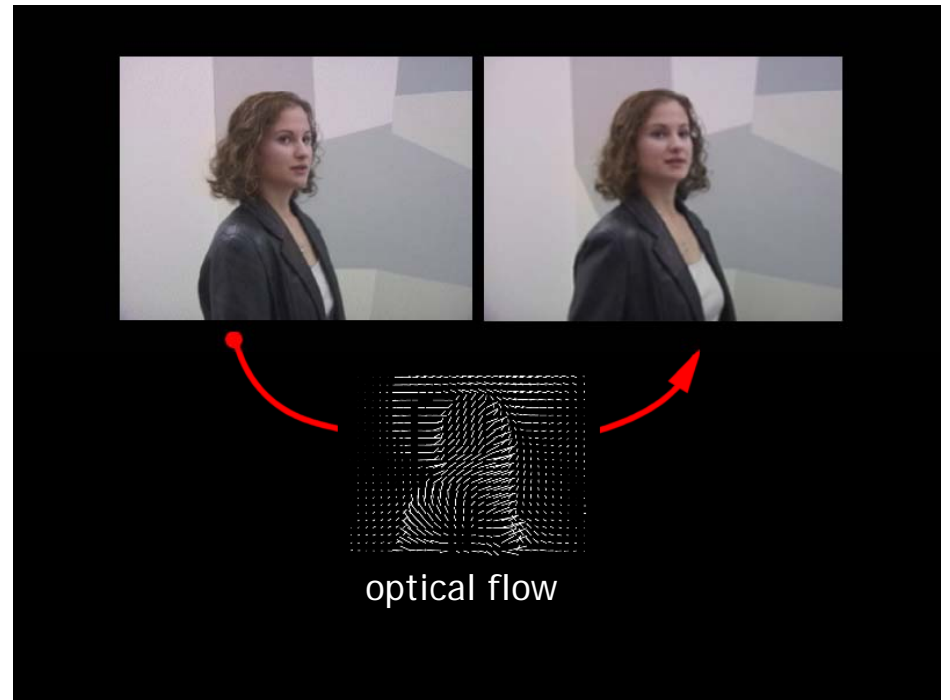
Compo-  
site



output  
alpha



*Video matting*









*Garbage mattes*



*Garbage mattes*



*Background estimation*



*Background estimation*



*Alpha matte*



*without  
background*

*with  
background*

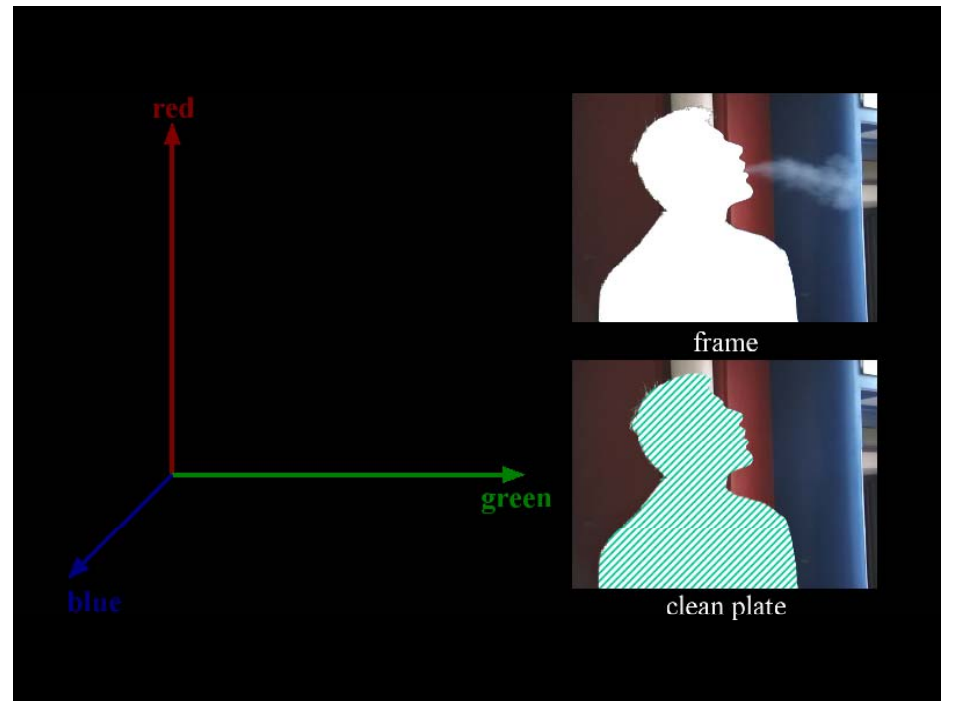
*Comparison*

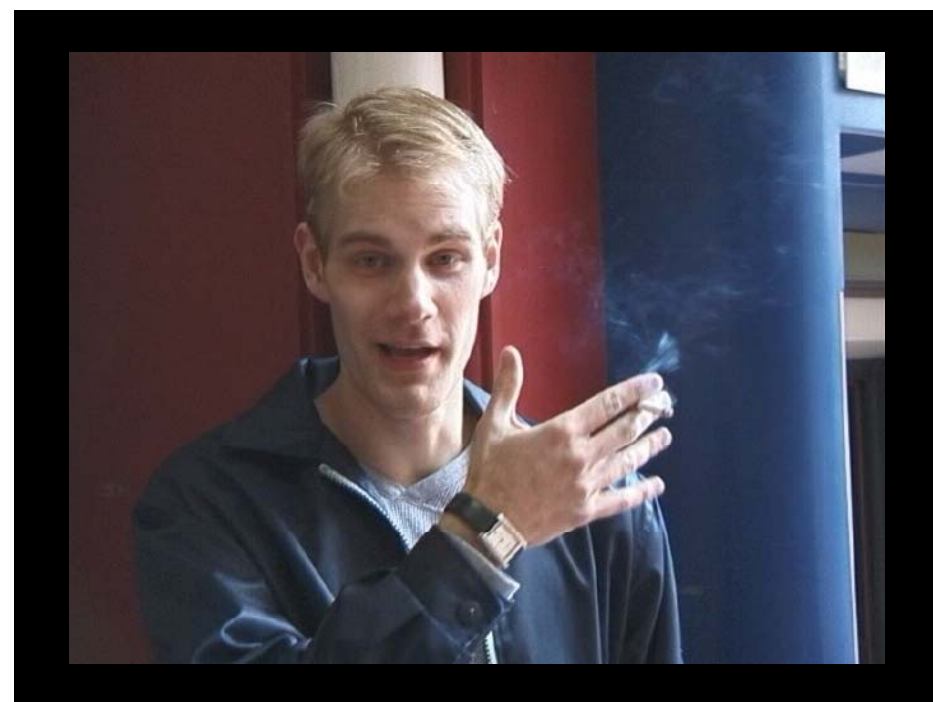
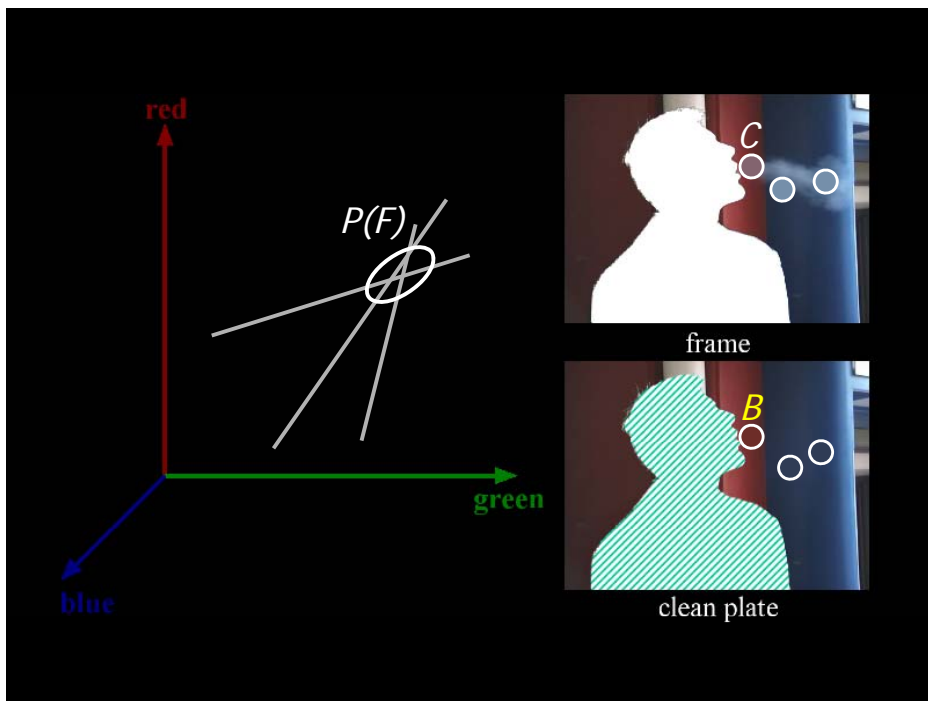
**input**



**composite**









## *Problems with Bayesian matting*

- It requires fine trimaps for good results
- It is tedious to generate fine trimaps
- Its performance rapidly degrades when foreground and background patterns become complex
- There is no direct and local control to the resulting mattes

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## *Scribble-based input*



trimap

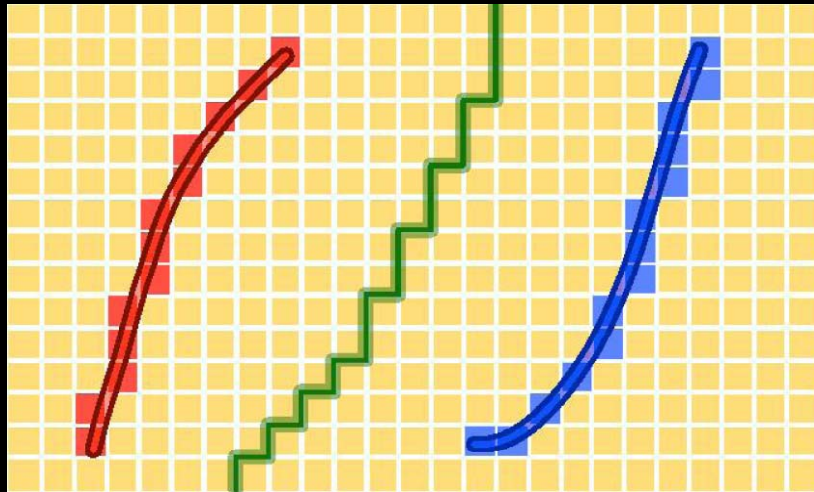


scribble

## *Motivation*



## LazySnapping



$$E(X) = \sum_{i \in \mathcal{V}} E_1(x_i) + \lambda \sum_{(i,j) \in \mathcal{E}} E_2(x_i, x_j)$$

$$E_1(x_i = 1) = 0 \quad E_1(x_i = 0) = \infty \quad \forall i \in \mathcal{F}$$

$$E_1(x_i = 1) = \infty \quad E_1(x_i = 0) = 0 \quad \forall i \in \mathcal{B}$$

$$E_1(x_i = 1) = \frac{d_i^{\mathcal{F}}}{d_i^{\mathcal{F}} + d_i^{\mathcal{B}}} \quad E_1(x_i = 0) = \frac{d_i^{\mathcal{B}}}{d_i^{\mathcal{F}} + d_i^{\mathcal{B}}} \quad \forall i \in \mathcal{U}$$

$$d_i^{\mathcal{F}} = \min_n \|C(i) - K_n^{\mathcal{F}}\|$$

n-th mean foreground color

## LazySnapping

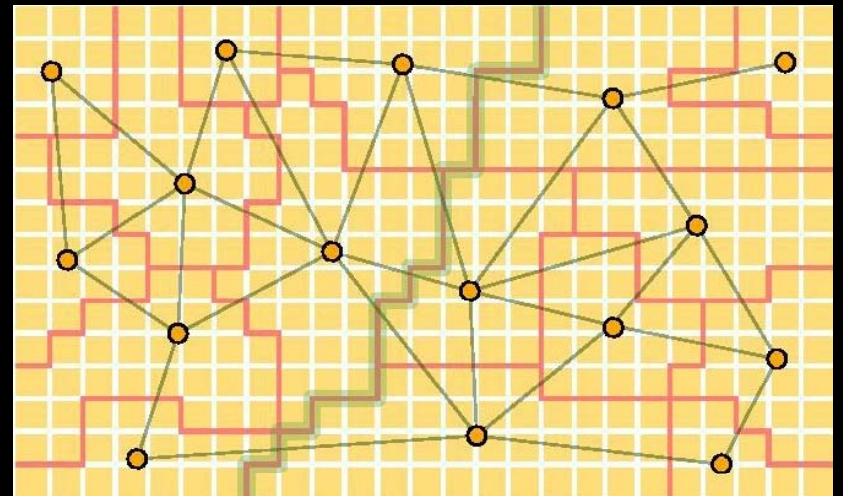
$$E(X) = \sum_{i \in \mathcal{V}} E_1(x_i) + \lambda \sum_{(i,j) \in \mathcal{E}} E_2(x_i, x_j)$$

$$E_2(x_i, x_j) = |x_i - x_j| \cdot g(C_{ij})$$

$$C_{ij} = \|C(i) - C(j)\|^2$$

$$g(\epsilon) = \frac{1}{\epsilon + 1}$$

## LazySnapping



## LazySnapping

## Matting approaches

- Sampling approaches: solve for each alpha separately by utilizing local fg/bg samples, e.g. Ruzon/Tomasi, Knockout and Bayesian matting.
- Propagation approaches: solve the whole matte together by optimizing, e.g. Poisson, BP, random walker, closed-form and robust matting.

## Poisson matting

$$I = \alpha F + (1 - \alpha)B$$

$$\nabla I = (F - B)\nabla\alpha + \alpha\nabla F + (1 - \alpha)\nabla B$$

$$\nabla\alpha \approx \frac{1}{F - B}\nabla I$$

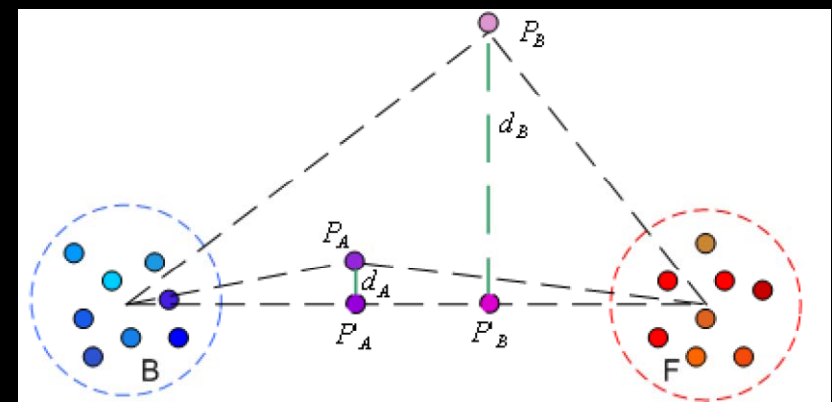
$$\alpha^* = \arg \min_{\alpha} \int \int_{p \in \Omega} \left\| \nabla\alpha_p - \frac{1}{F_p - B_p} \nabla I_p \right\|^2 dp$$

## Poisson matting



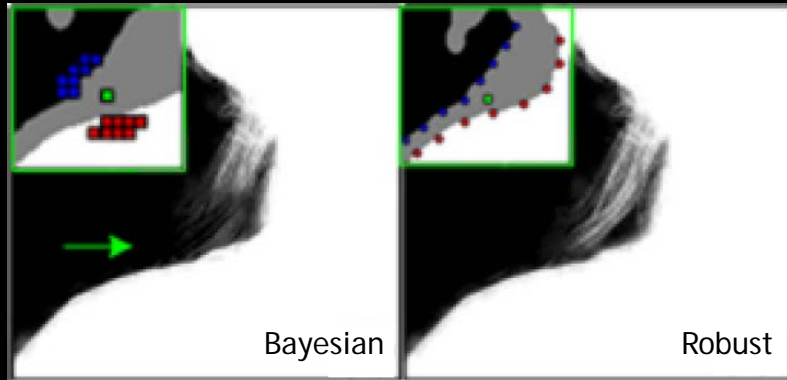
## Robust matting

- Jue Wang and Michael Cohen, CVPR 2007



## Robust matting

- Instead of fitting models, a non-parametric approach is used



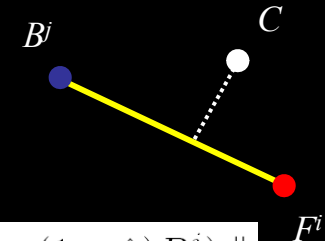
## Robust matting

- We must evaluate hypothesized foreground/background pairs

$$\hat{\alpha} = \frac{(C - B^j)(F^i - B^j)}{\|F^i - B^j\|^2}$$

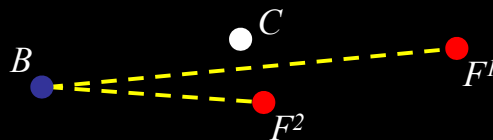
distance ratio

$$R_d(F^i, B^j) = \frac{\|C - (\hat{\alpha}F^i + (1 - \hat{\alpha})B^j)\|}{\|F^i - B^j\|}$$



## Robust matting

- To encourage pure fg/bg pixels, add weights



$$w(F^i) = \exp\left\{-\|F^i - C\|^2 / D_F^2\right\}$$

$$\min_i(\|F^i - C\|)$$

$$w(B^j) = \exp\left\{-\|B^j - C\|^2 / D_B^2\right\}$$

$$\min_j(\|B^j - C\|)$$

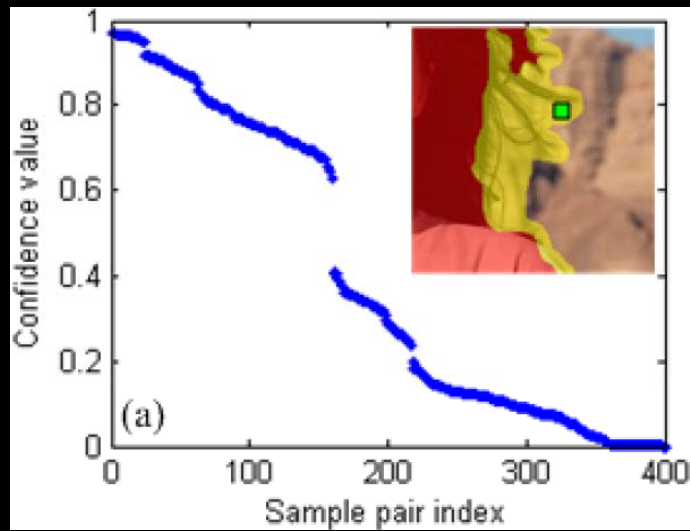
## Robust matting

- Combine them together. Pick up the best 3 pairs and average them

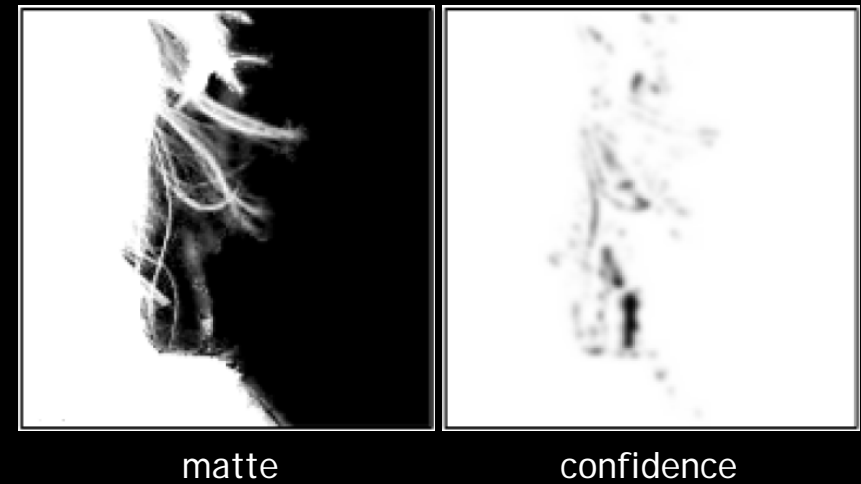
confidence

$$f(F^i, B^j) = \exp\left\{-\frac{R_d(F^i, B^j)^2 \cdot w(F^i) \cdot w(B^j)}{\sigma^2}\right\}$$

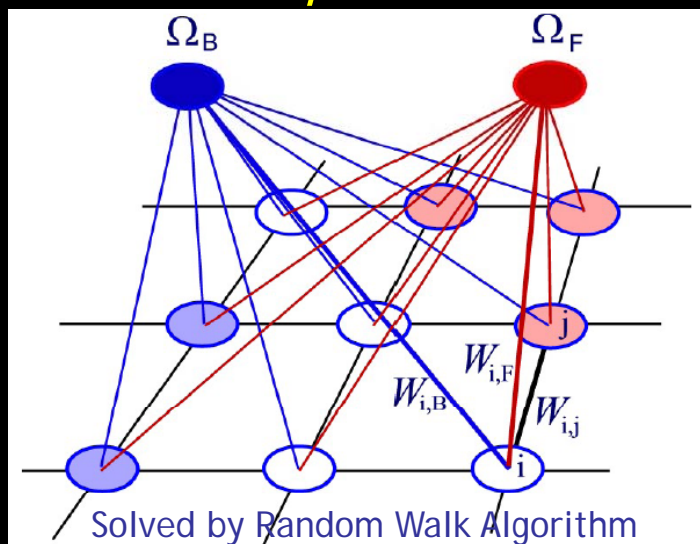
## Robust matting



## Robust matting



## Matte optimization



## Matte optimization

data constraints

$$W(i, F) = \gamma \cdot [f_i \hat{\alpha}_i + (1 - f_i) \delta(\hat{\alpha}_i > 0.5)]$$

$$W(i, B) = \gamma \cdot [f_i (1 - \hat{\alpha}_i) + (1 - f_i) \delta(\hat{\alpha}_i < 0.5)]$$

neighborhood constraints

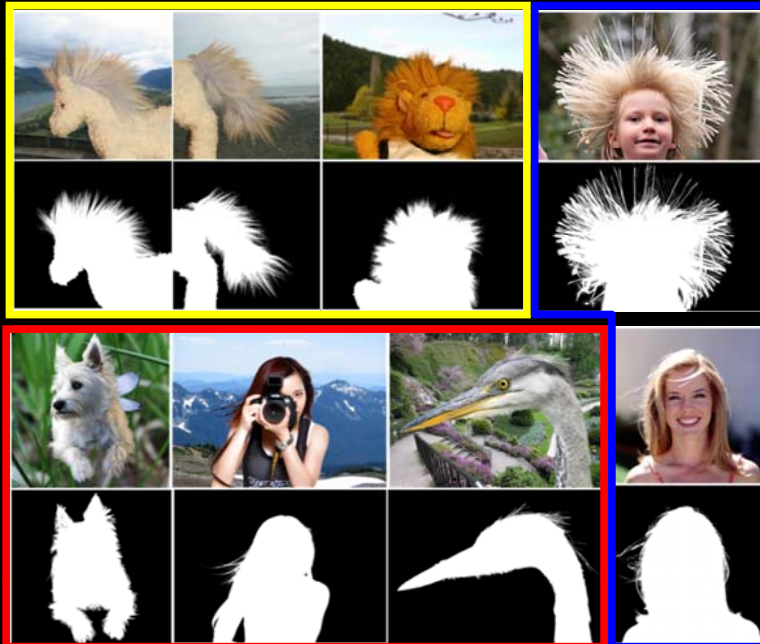
$$W_{ij} = \sum_k^{(i,j) \in w_k} \frac{1}{9} (1 + (C_i - \mu_k)(\Sigma_k + \frac{\epsilon}{9}I)^{-1}(C_j - \mu_k))$$

## Demo (EZ Mask)



## Evaluation

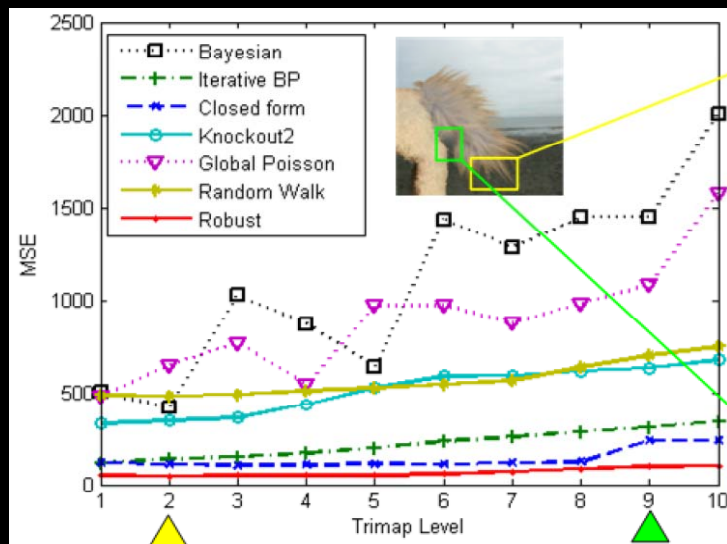
- 8 images collected in 3 different ways
- Each has a “ground truth” matte



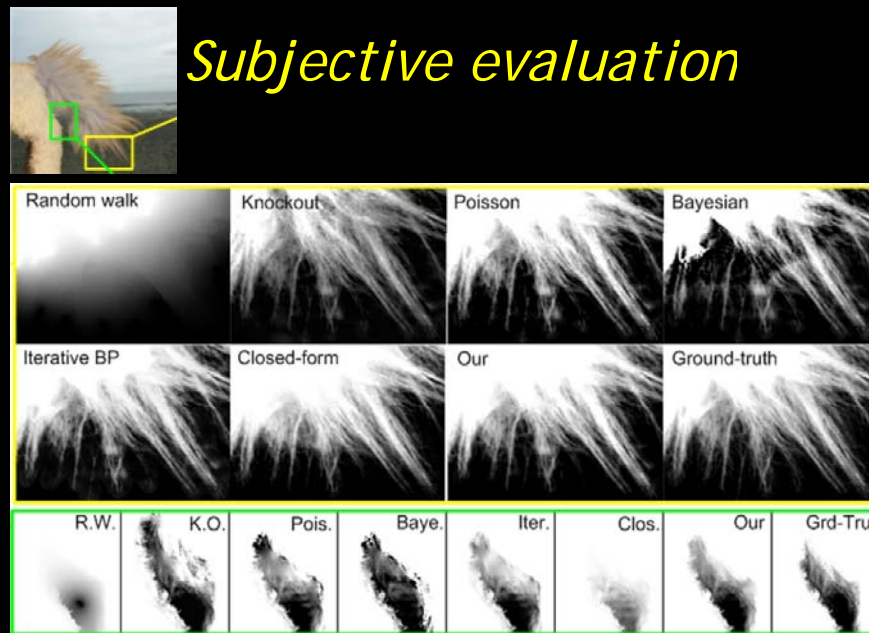
## Evaluation

- Mean square error is used as the accuracy metric
- Try 8 trimaps with different accuracy for testing robustness
- 7 methods are tested: Bayesian, Belief propagation, Poisson, Random Walk, KnockOut2, Closed-Form and Robust matting

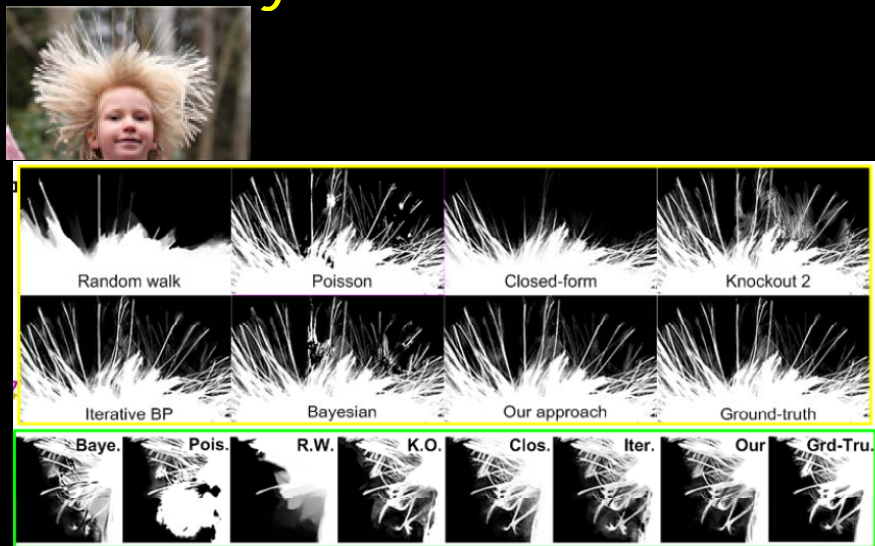
## Quantitative evaluation



## Subjective evaluation



## Subjective evaluation



## Ranks of these algorithms

	accuracy	robustness
Poisson	6.9	6.8
Random walk	6.0	4.4
<b>Knockout2</b>	<b>4.5</b>	<b>4.5</b>
<b>Bayesian</b>	<b>3.9</b>	<b>6.0</b>
Belief Propagation	3.3	3.1
Close-form	2.6	2.0
<b>Robust matting</b>	<b>1.0</b>	<b>1.3</b>

## Summary

- Propagation-based methods are more robust
- Sampling-based methods often generate more accurate mattes than propagation-based ones with fine trimaps
- Robust matting combines strengths of both

## New evaluation (CVPR 2009)

- <http://www.alphamatting.com/>

Method	SAD	MSE	Grad.	Conn.
Closed-form [13]	<b>1.3</b>	<b>1.4</b>	<b>1.5</b>	2.0
Robust matting [23]	1.9	1.8	1.7	3.4
Random walk [8]	3.3	3.2	3.5	<b>1.3</b>
Easy matting [9]	4.0	4.4	4.2	3.7
Bayesian matting [6]	4.5	4.3	4.3	5.0
Poisson matting [20]	5.9	5.9	6.0	5.6

## Soft scissor

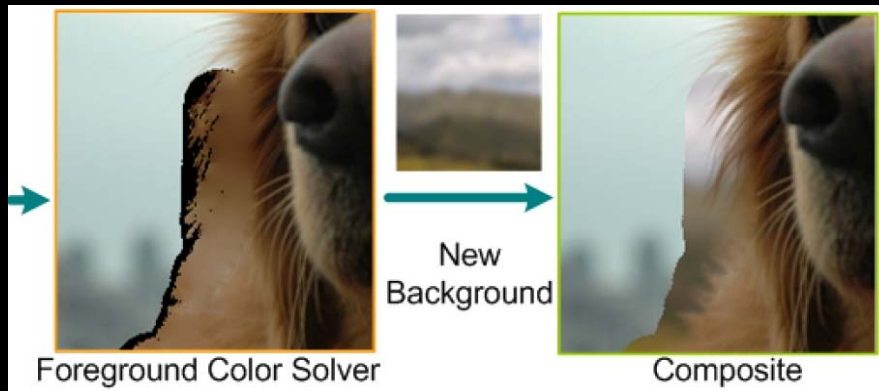
- Jue Wang et. al., SIGGRAPH 2007
- Users interact in a similar way to intelligent scissors

## Flowchart

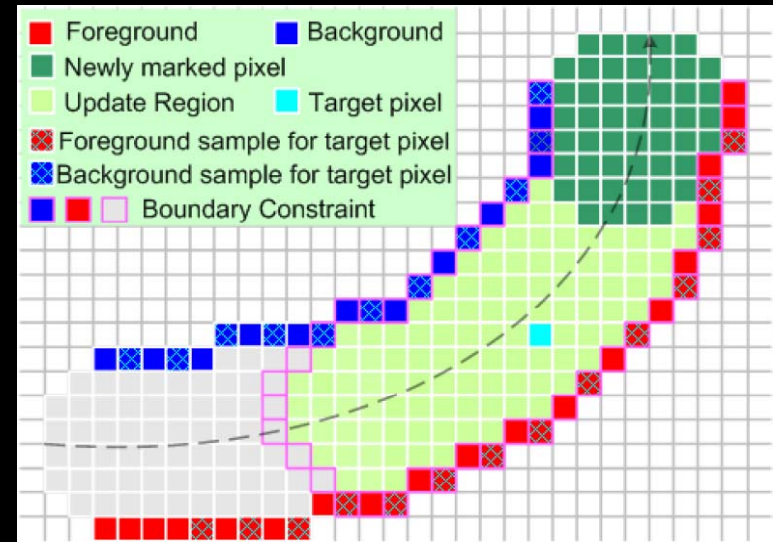




## Flowchart



## Soft scissor



## Demo (Power Mask)



## Outline

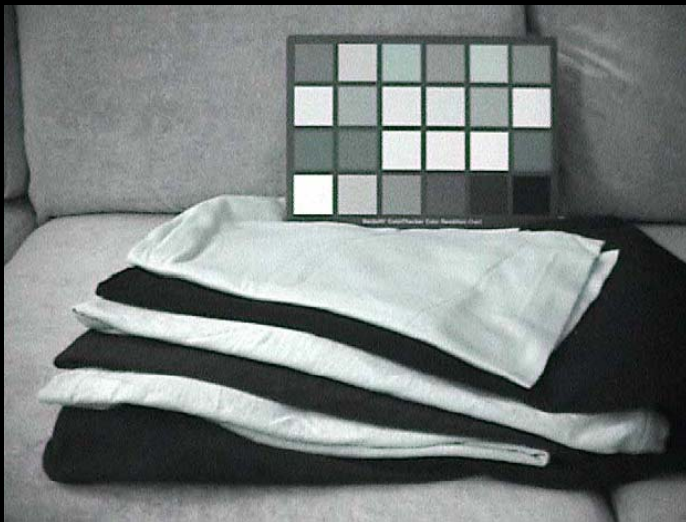
- Traditional matting and compositing
- The matting problem
- Bayesian matting and extensions
- Matting with less user inputs
- **Matting with multiple observations**
- Beyond the compositing equation\*
- Conclusions

## *Matting with multiple observations*

- Invisible lights
  - Polarized lights
  - Infrared
- Thermo-key
- Depth Keying (ZCam)
- Flash matting



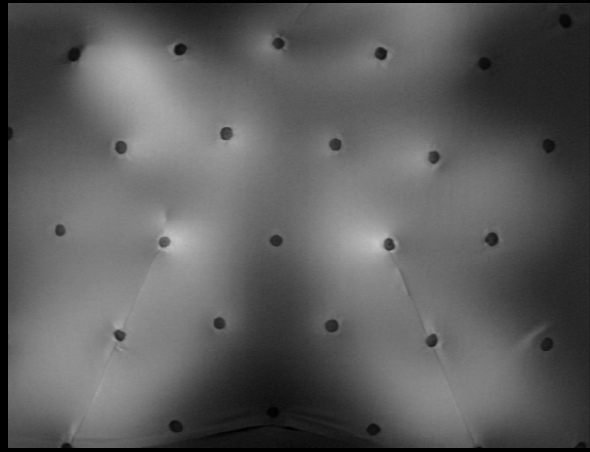
*Invisible lights (Infared)*



*Invisible lights (Infared)*



*Invisible lights (Infared)*



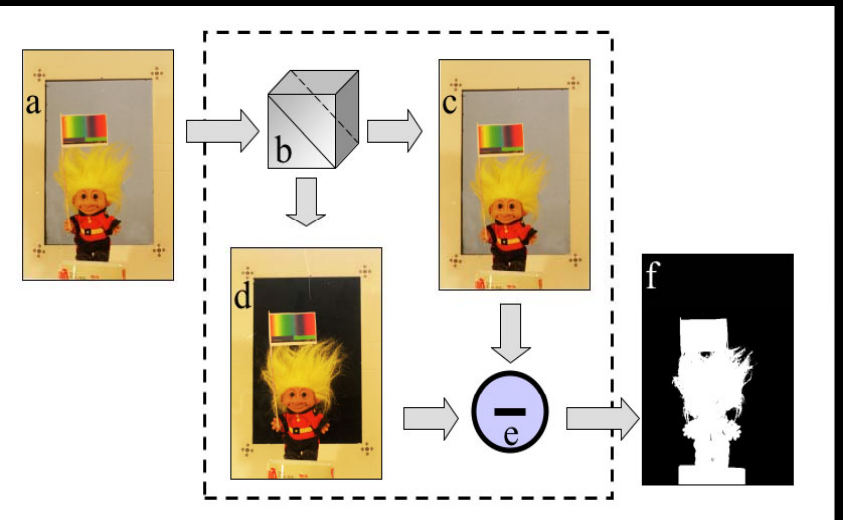
*Invisible lights (Infared)*



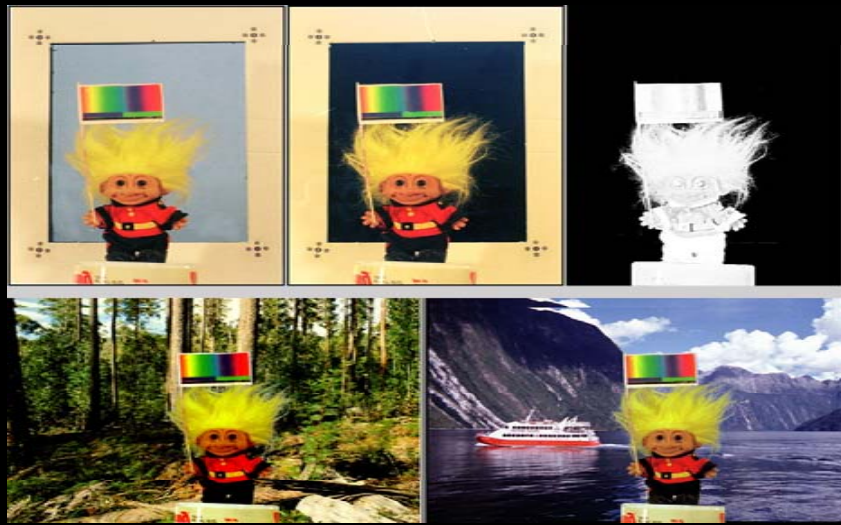
*Invisible lights (Infared)*



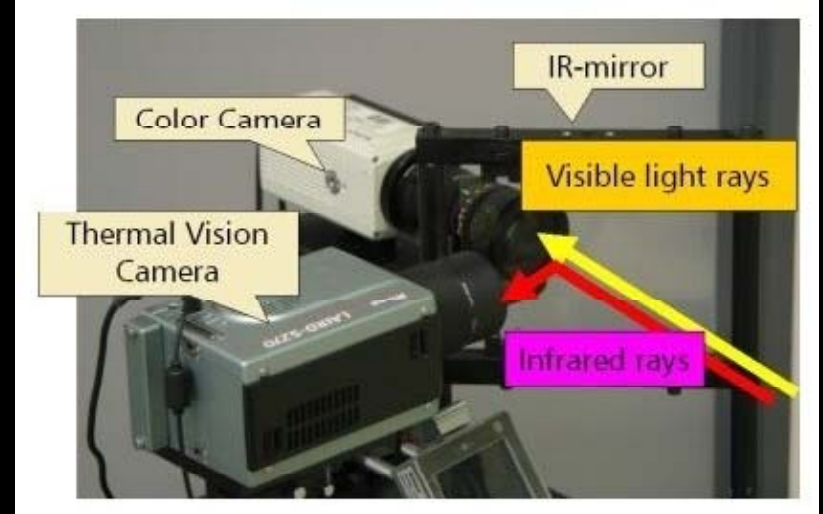
*Invisible lights (Infared)*



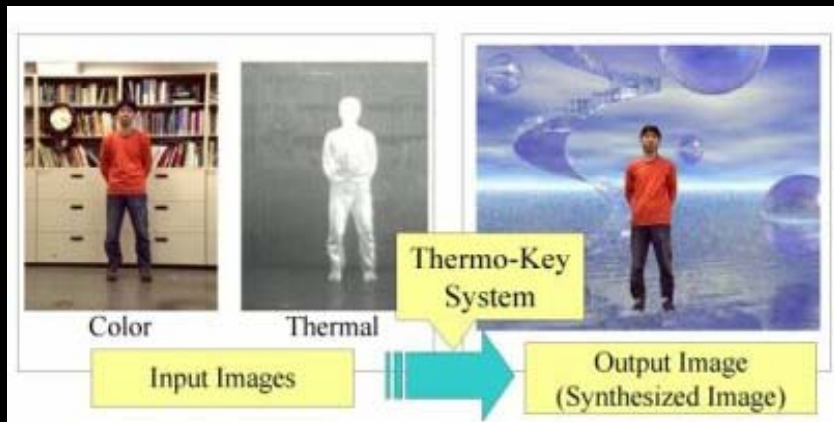
*Invisible lights (Polarized)*



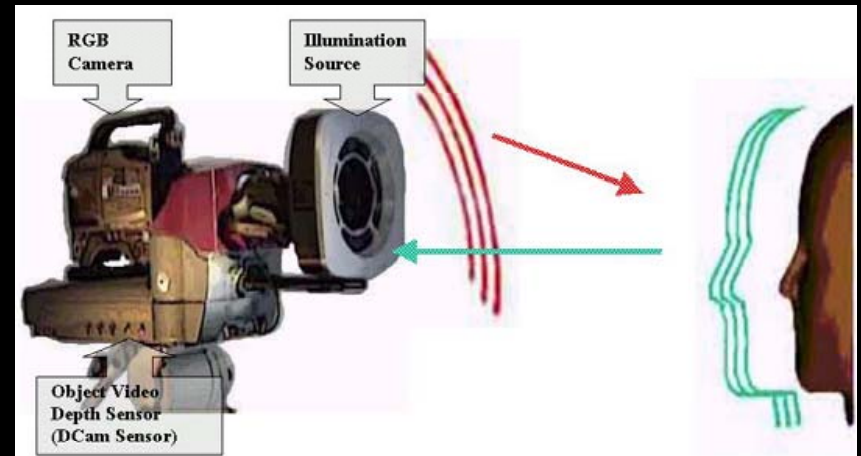
*Invisible lights (Polarized)*



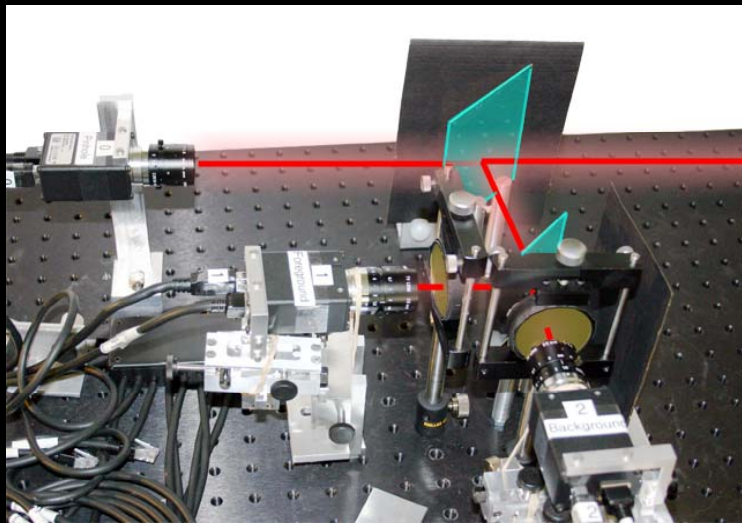
*Thermo-Key*



*Thermo-Key*



*ZCam*



*Defocus matting*



[video](#)



[video](#)

*Matting with camera arrays*



*Flash matting*

$$I = \alpha F + (1 - \alpha)B,$$

$$I^f = \alpha F^f + (1 - \alpha)B^f,$$

Background is much further than foreground and receives almost no flash light

$$B^f \approx B$$

$$I^f = \alpha F^f + (1 - \alpha)B$$

*Flash matting*

Foreground flash matting equation

$$I' = I^f - I = \alpha(F^f - F) = \alpha F'$$

Generate a trimap and directly apply Bayesian matting.

$$\arg \max_{\alpha, F'} L(\alpha, F' | I')$$

$$= \arg \max_{\alpha, F'} \{L(I' | \alpha, F') + L(F') + L(\alpha)\}$$

$$L(I' | \alpha, F') = -\|I' - \alpha F'\| / \sigma_{I'}^2$$

$$L(F') = -(F' - \overline{F'})^T \Sigma_{F'}^{-1} (F' - \overline{F'})$$

*Flash matting*



*Foreground flash matting*

$$I = \alpha F + (1 - \alpha)B$$

$$I' = \alpha F'$$

$$\arg \max_{\alpha, F, B, F'} L(\alpha, F, B, F' | I, I')$$

$$= \arg \max_{\alpha, F, B, F'} \{L(I | \alpha, F, B) + L(I' | \alpha, F') +$$

$$L(F) + L(B) + L(F') + L(\alpha)\}$$

*Joint Bayesian flash matting*

$$\alpha = \frac{\sigma_{I'}^2 (F - B)^T (I - B) + \sigma_I^2 F'^T I'}{\sigma_{I'}^2 (F - B)^T (F - B) + \sigma_I^2 F'^T F'}$$

$$\begin{bmatrix} \Sigma_F^{-1} + \mathbf{I}\alpha^2/\sigma_I^2 & \mathbf{I}\alpha(1-\alpha)\sigma_I^2 & \mathbf{0} \\ \mathbf{I}\alpha(1-\alpha)\sigma_I^2 & \Sigma_B^{-1} + \mathbf{I}\alpha^2/\sigma_I^2 & \mathbf{0} \\ \mathbf{0} & \mathbf{0} & \Sigma_{F'}^{-1} + \mathbf{I}\alpha^2/\sigma_I^2 \end{bmatrix} \begin{bmatrix} F \\ B \\ F' \end{bmatrix}$$

$$= \begin{bmatrix} \Sigma_F^{-1} \bar{F} + \mathbf{I}\alpha/\sigma_I^2 \\ \Sigma_B^{-1} \bar{B} + \mathbf{I}(1-\alpha)/\sigma_I^2 \\ \Sigma_{F'}^{-1} \bar{F}' + \mathbf{I}'\alpha/\sigma_I^2 \end{bmatrix},$$

*Joint Bayesian flash matting*

flash

no flash



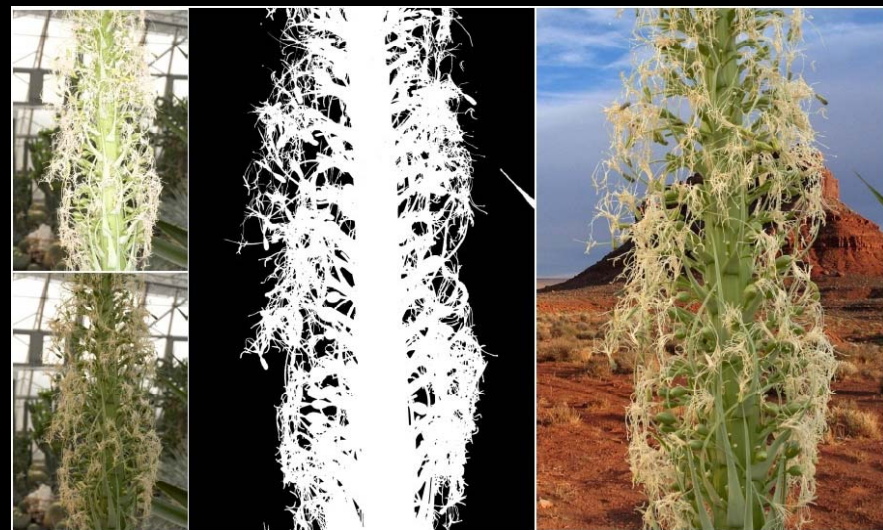
*Comparison*

foreground  
flash matting

joint Bayesian  
flash matting



*Comparison*



*Flash matting*

## *Outline*

- Traditional matting and compositing
- The matting problem
- Bayesian matting and extensions
- Matting with less user inputs
- Matting with multiple observations
- Beyond the compositing equation\*
- **Conclusions**

## *Conclusions*

- Matting algorithms improves a lot in these 10 years
- In production, it is still always preferable to shoot against uniform backgrounds
- Algorithms for more complex backgrounds
- Devices or algorithms for automatic matting

*Thanks for your attention!*

*Shadow matting  
and compositing*



source scene



target background



blue screen image



target background



blue screen composite



target background



blue screen composite

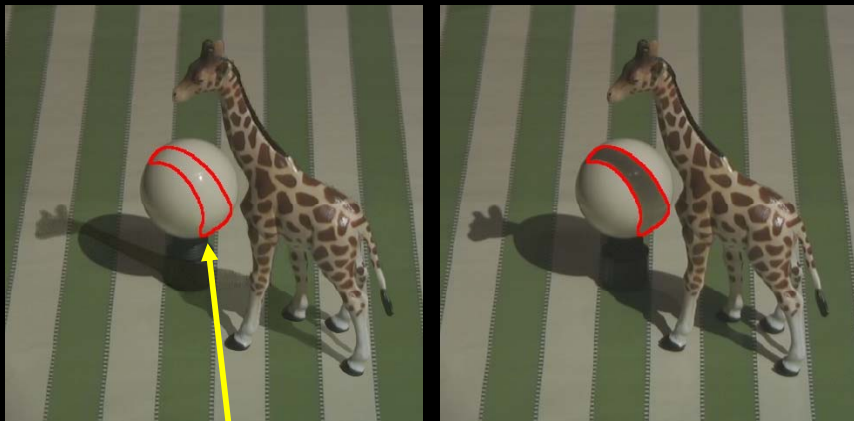


photograph



blue screen composite

photograph



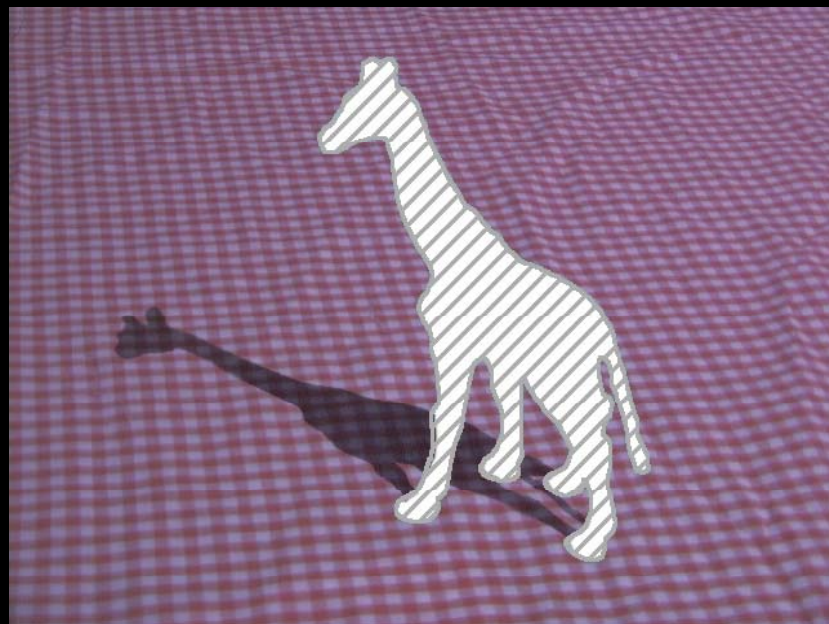
*Geometric errors*

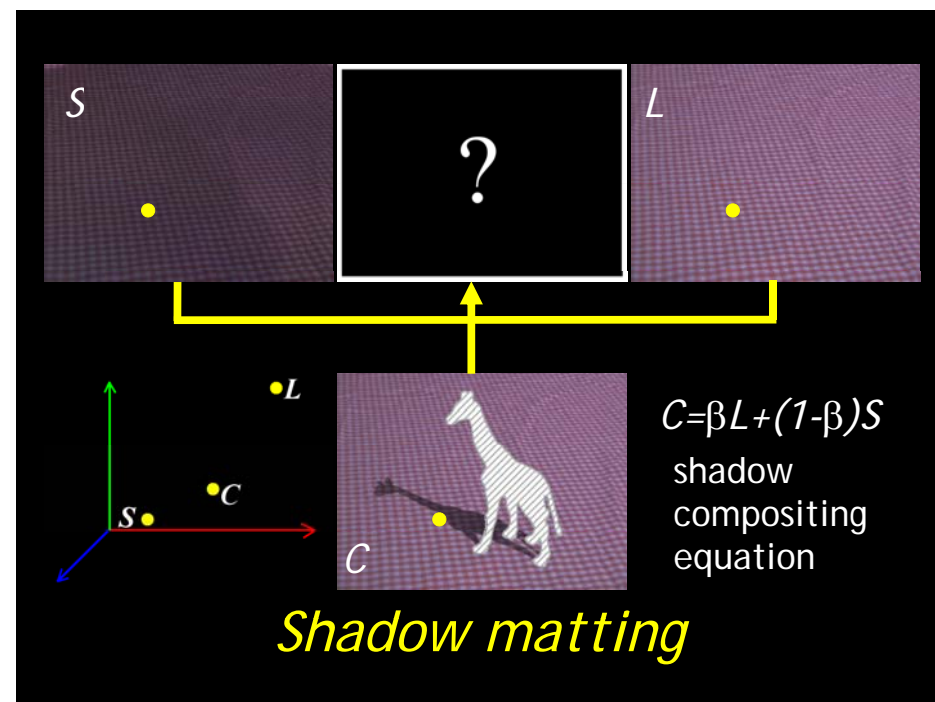
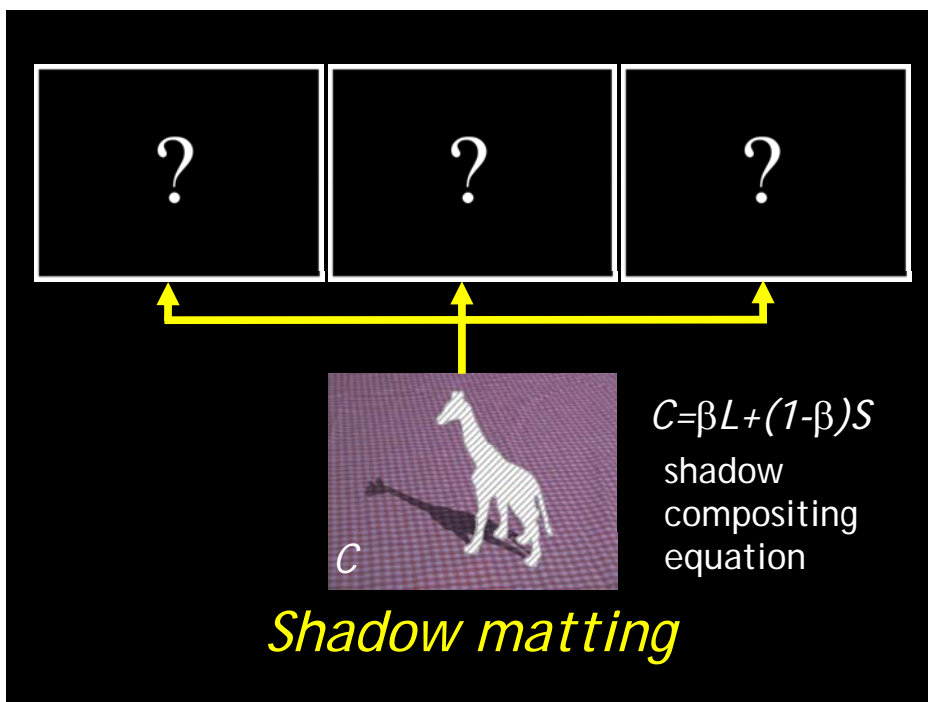
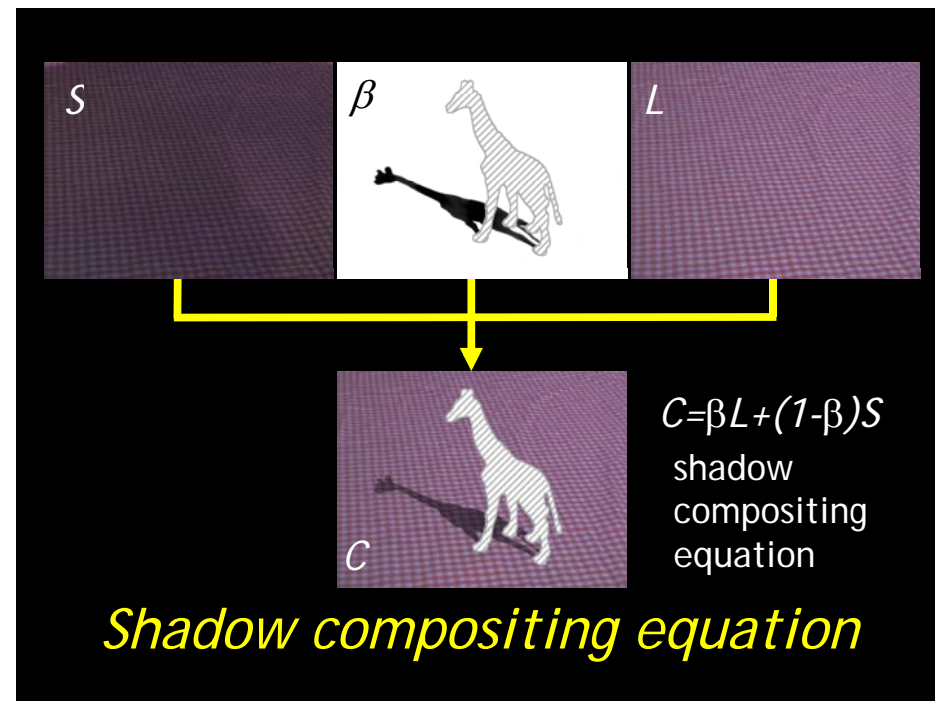
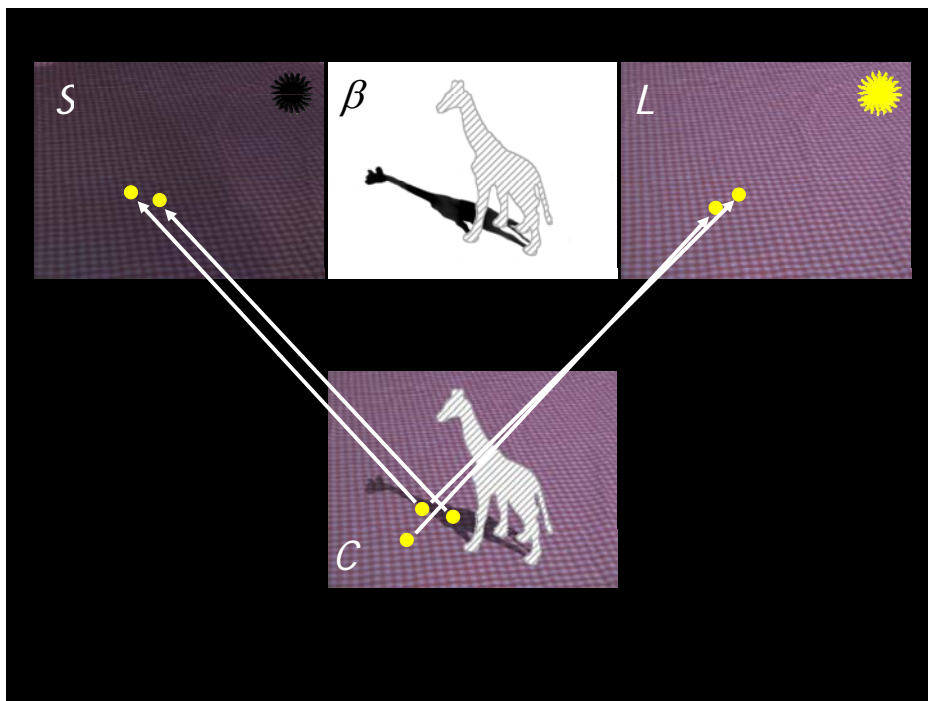
blue screen composite

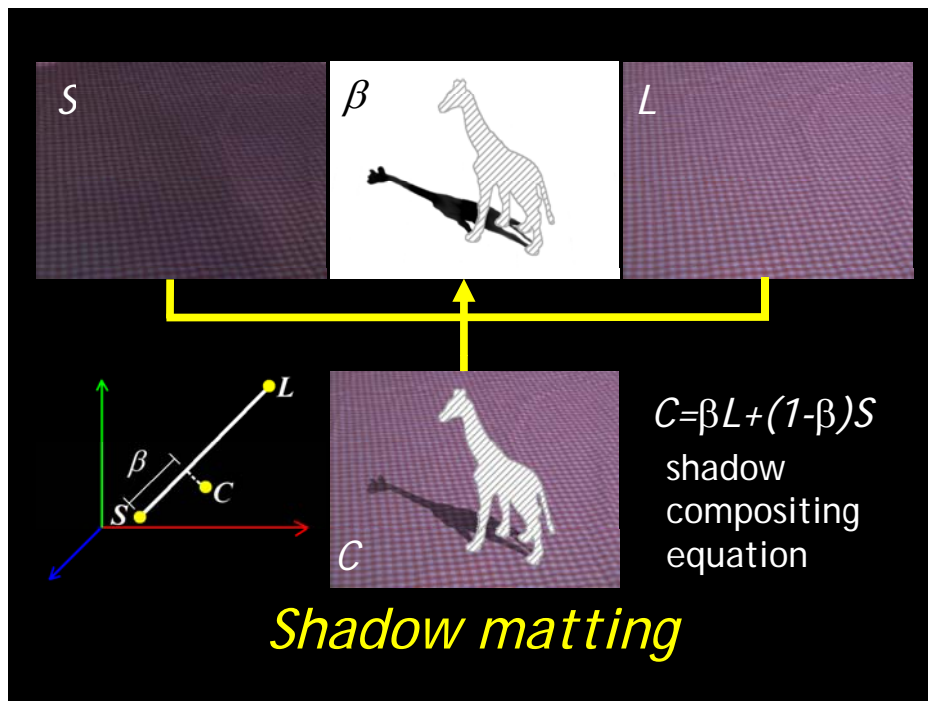
photograph



*Photometric errors*

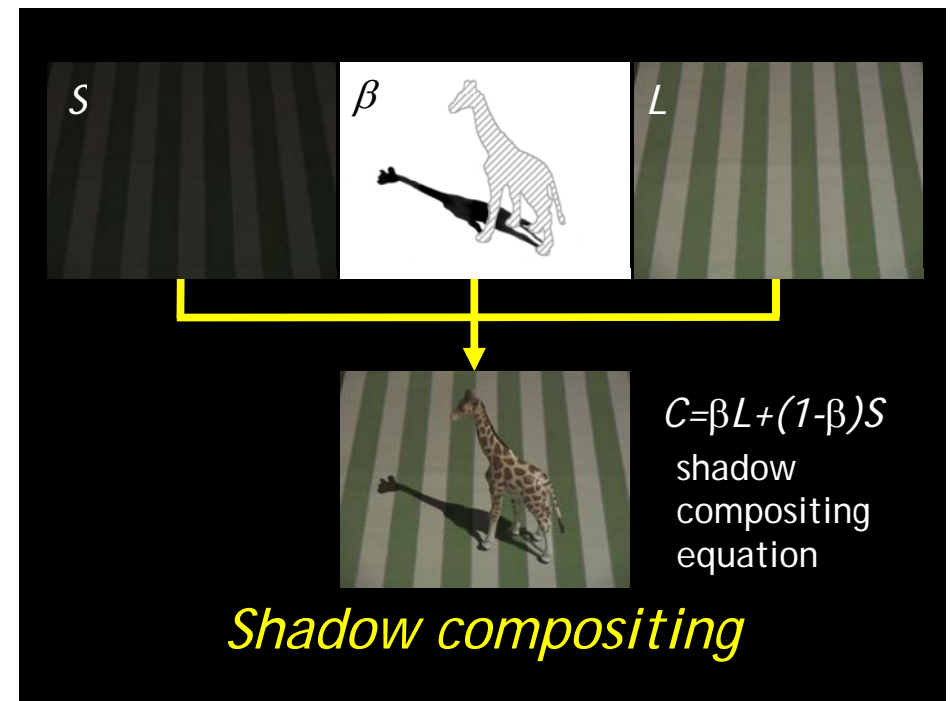






The diagram illustrates the shadow matting process. At the top, three panels are shown:  $S$  (a purple textured background),  $\beta$  (a giraffe silhouette with a shadow), and  $L$  (a purple textured background). A yellow bracket connects these three panels to a central diagram. The central diagram shows a 2D vector space with axes  $S$  (red),  $L$  (green), and  $C$  (blue). A vector  $C$  is shown as a linear combination of  $S$  and  $L$ , with the coefficient  $\beta$  indicated. Below this diagram is a composite image of the giraffe on the purple background, labeled  $C$ . To the right of the composite image is the equation  $C = \beta L + (1 - \beta)S$  and the text "shadow compositing equation".

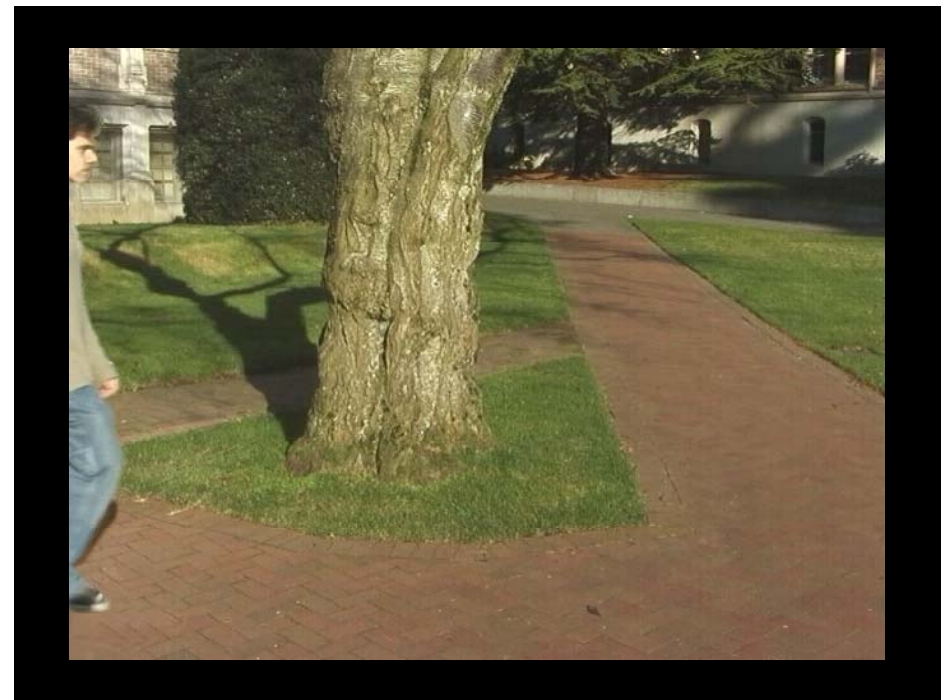
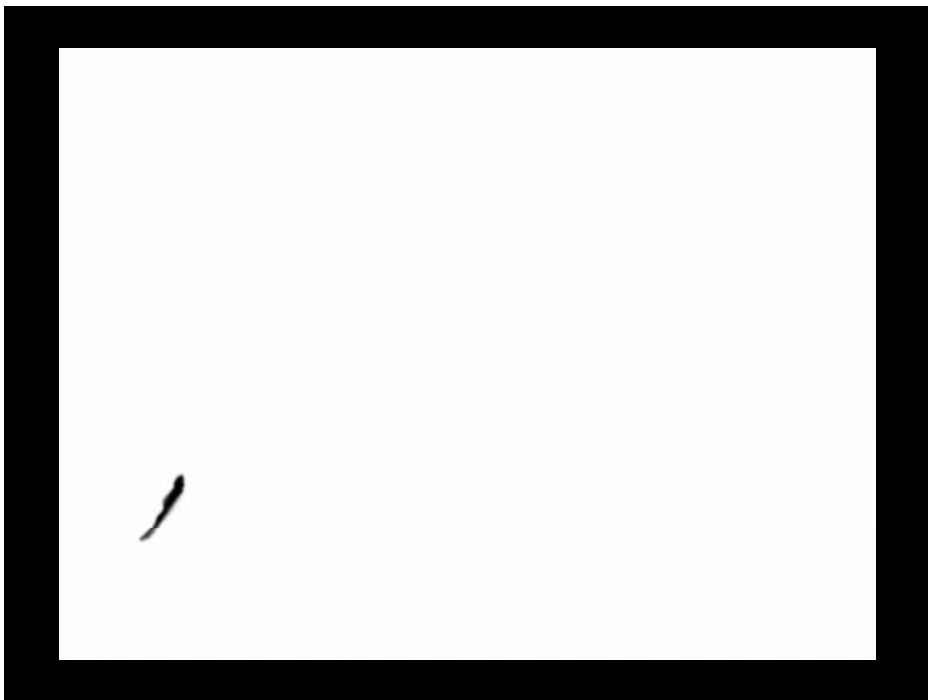
*Shadow matting*

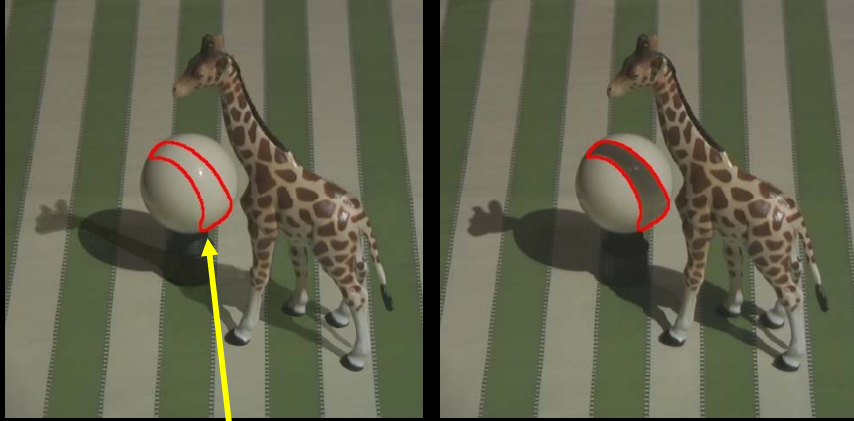


The diagram illustrates the shadow compositing process. At the top, three panels are shown:  $S$  (a dark background with vertical stripes),  $\beta$  (a giraffe silhouette with a shadow), and  $L$  (a background with vertical stripes). A yellow bracket connects these three panels to a central diagram. The central diagram shows the composite image of the giraffe on the striped background, labeled  $C$ . To the right of the composite image is the equation  $C = \beta L + (1 - \beta)S$  and the text "shadow compositing equation".

*Shadow compositing*







*Geometric errors*

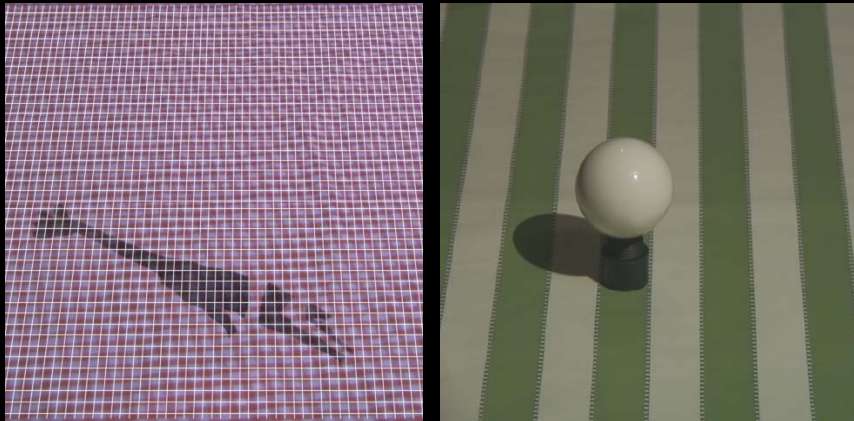
source scene

target background



source scene

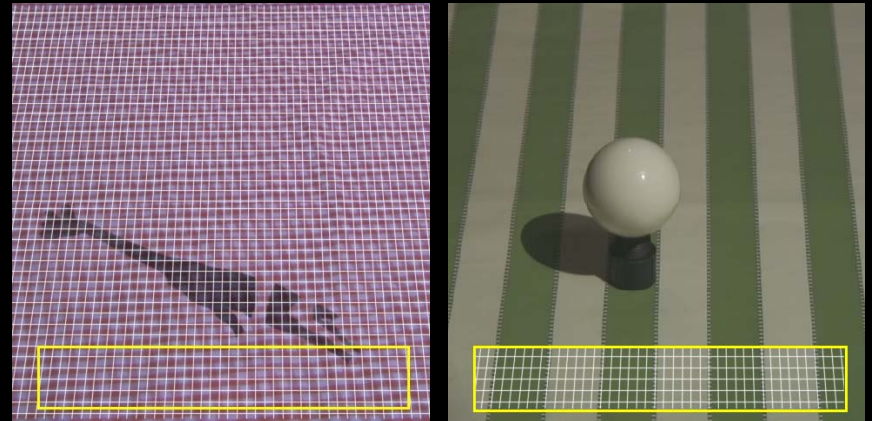
target background



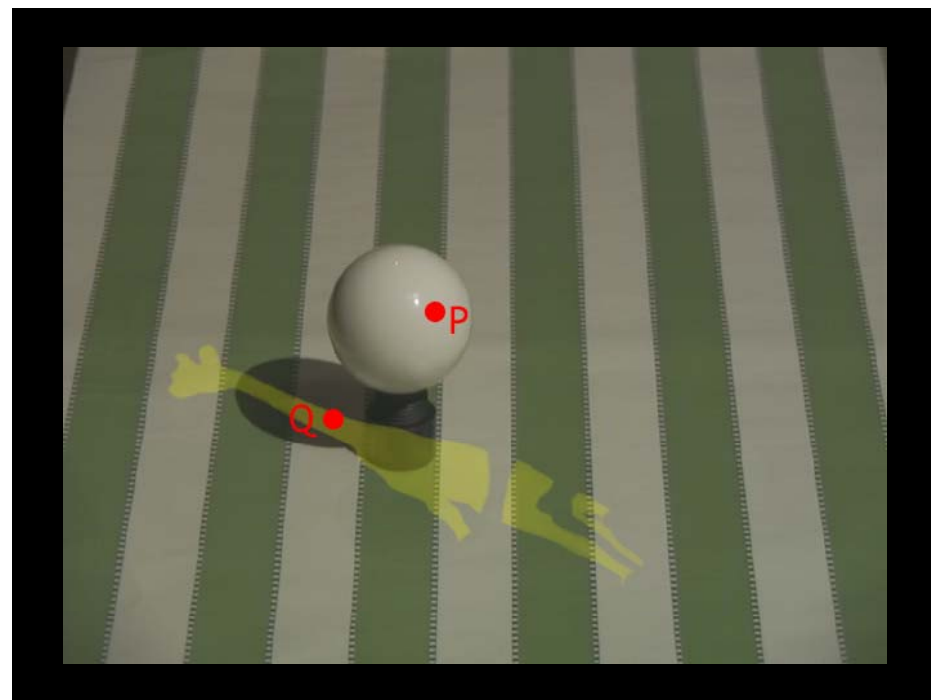
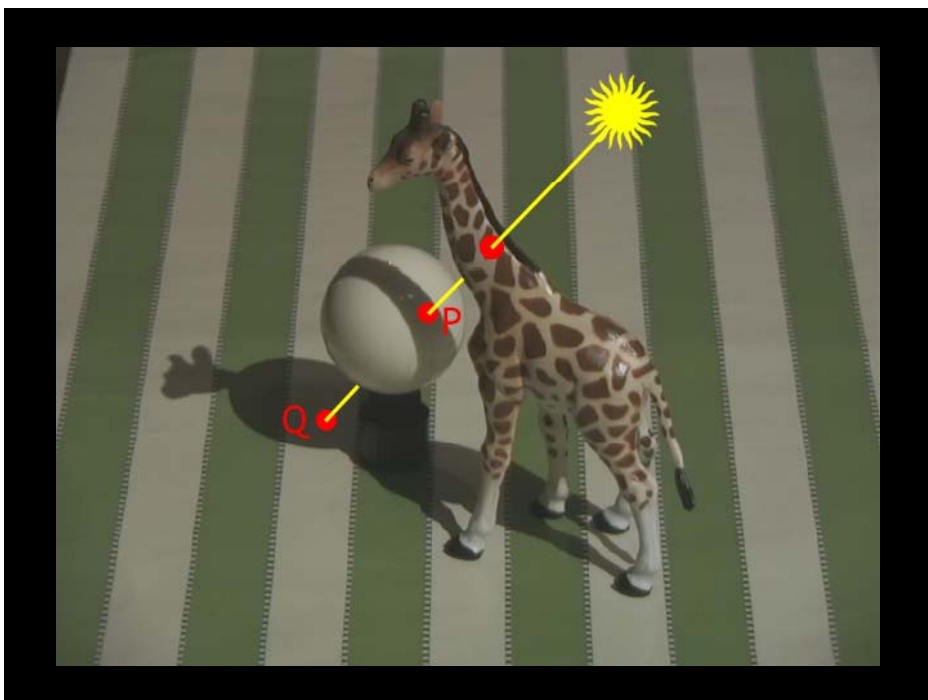
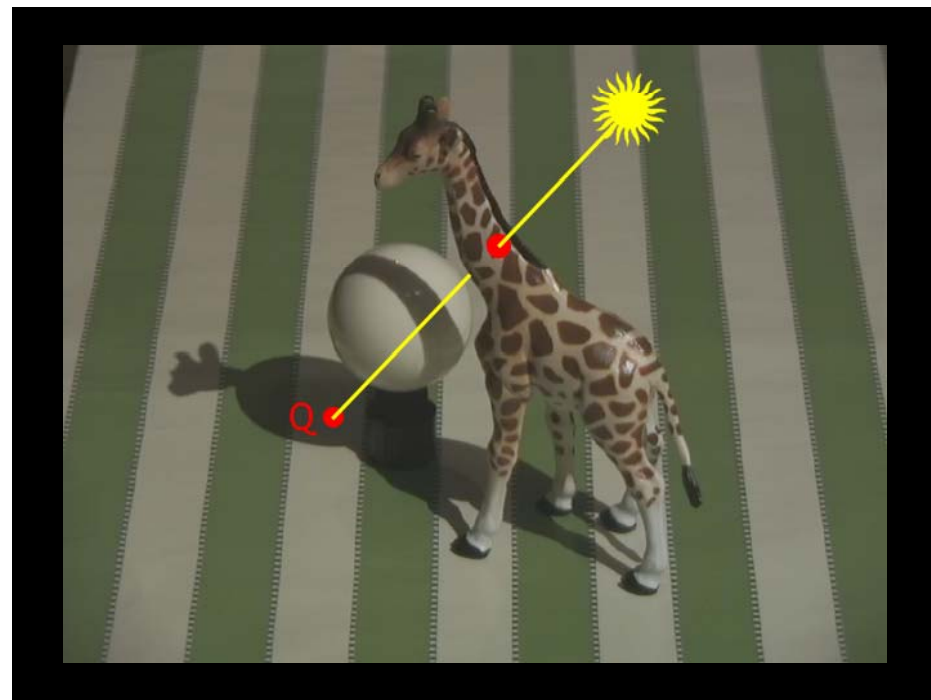
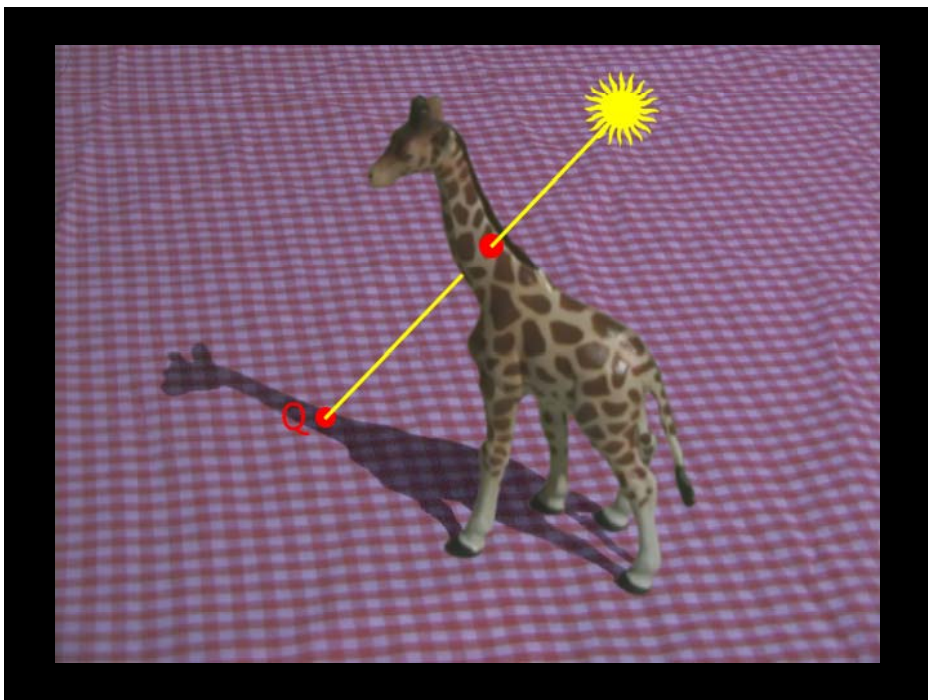
*Requirement #1*

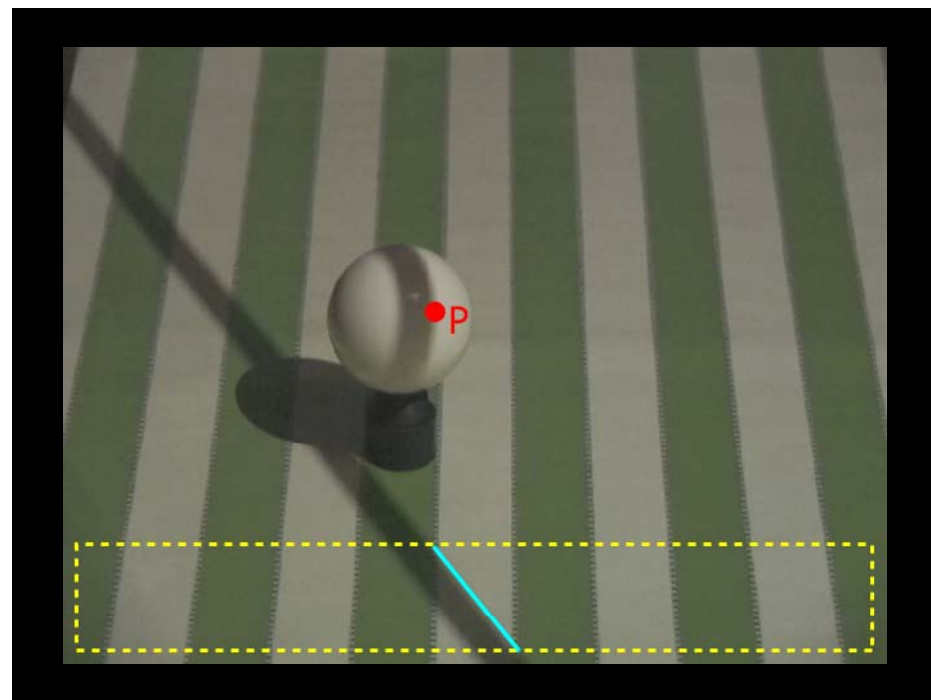
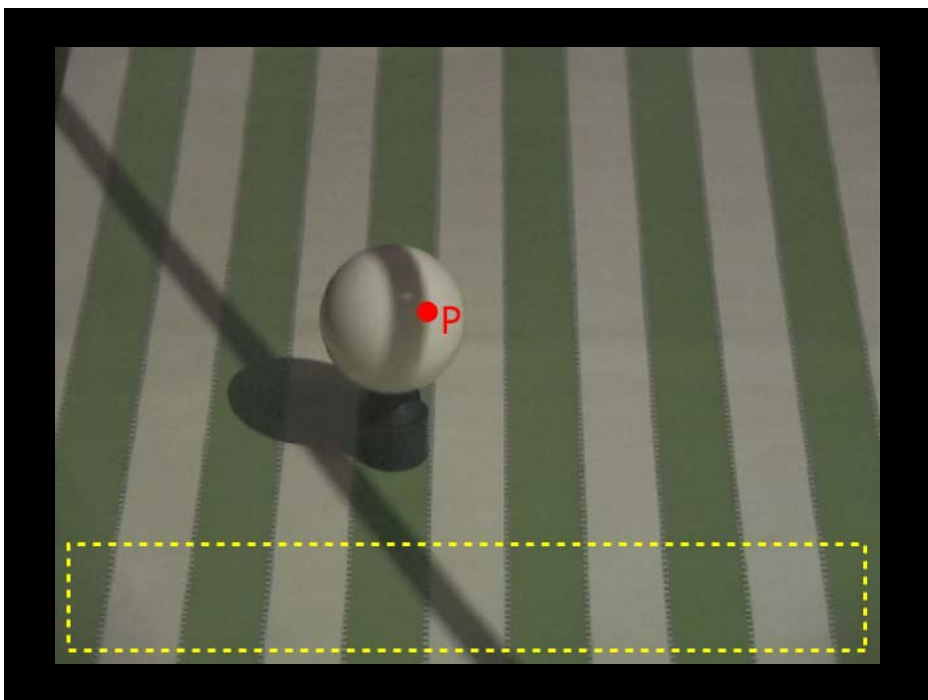
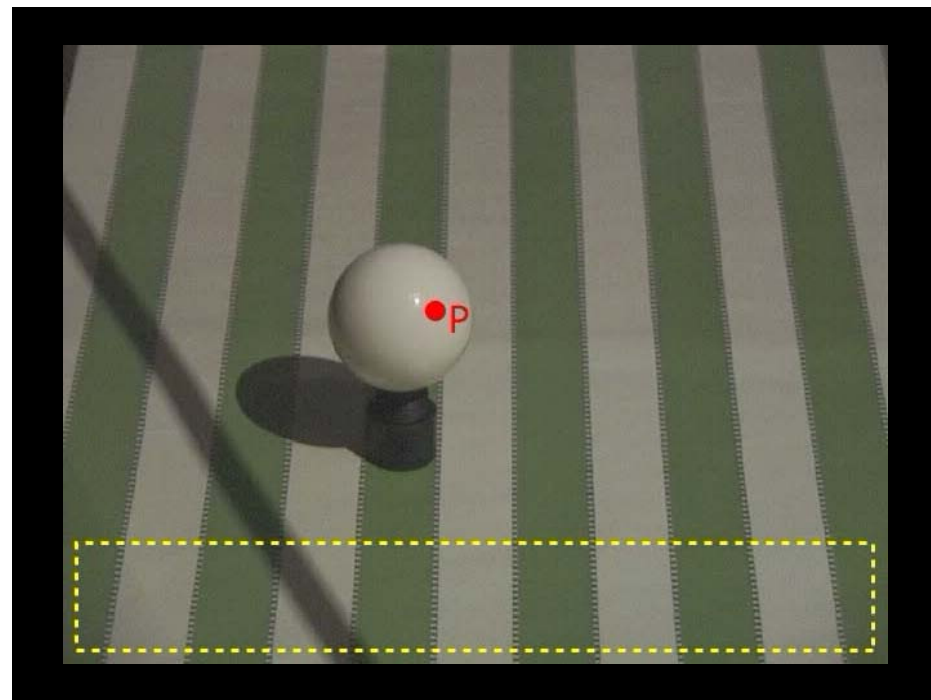
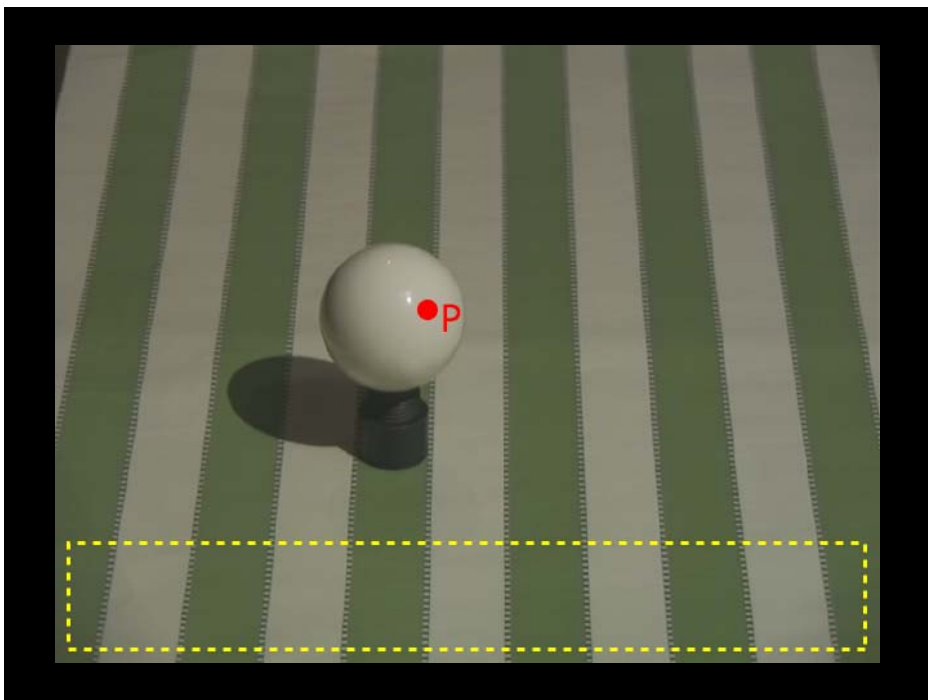
source scene

target background

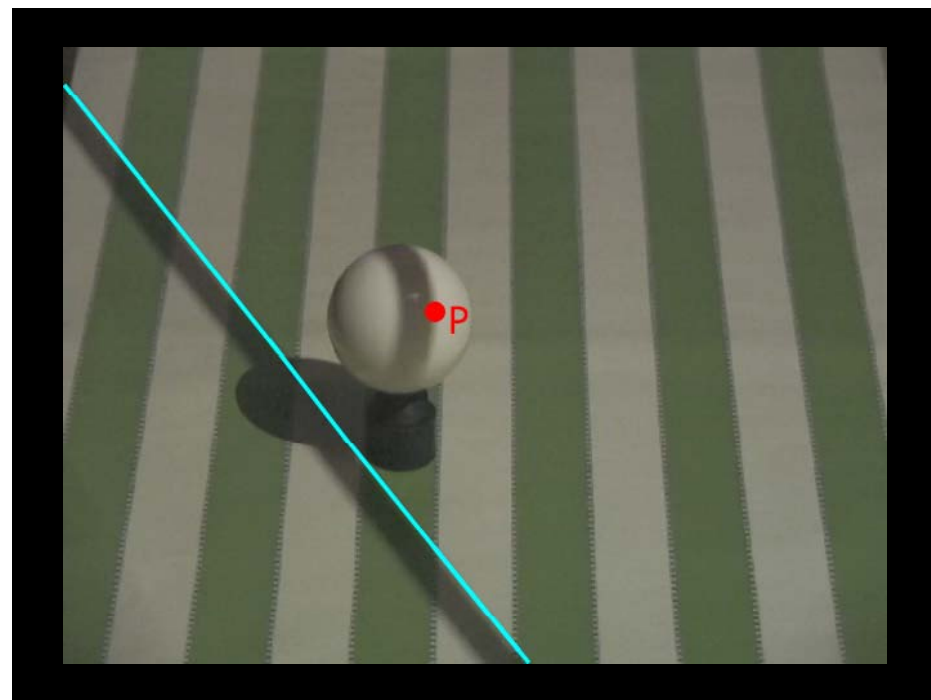
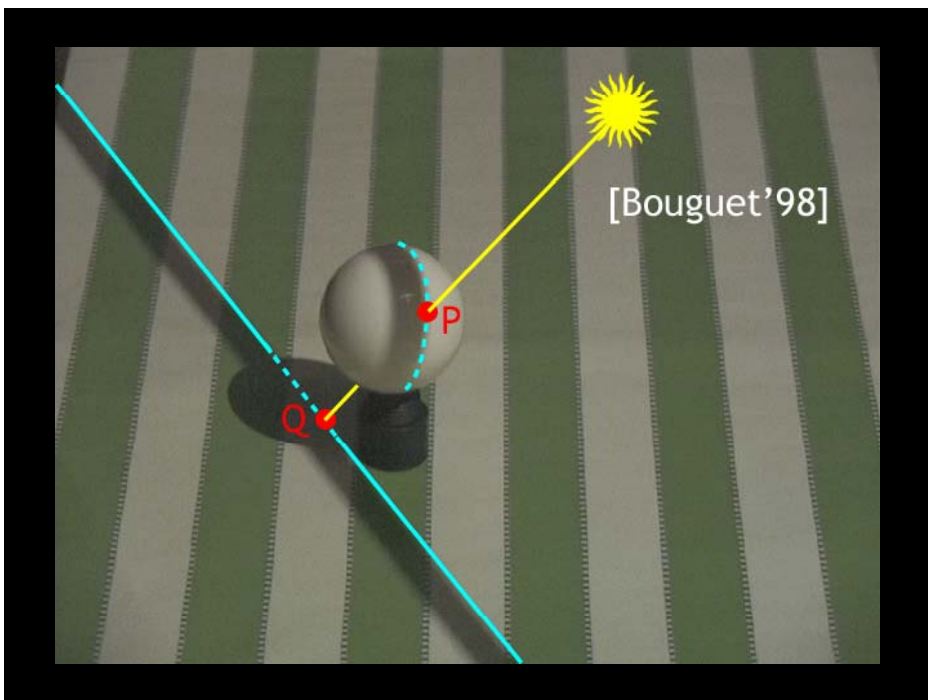
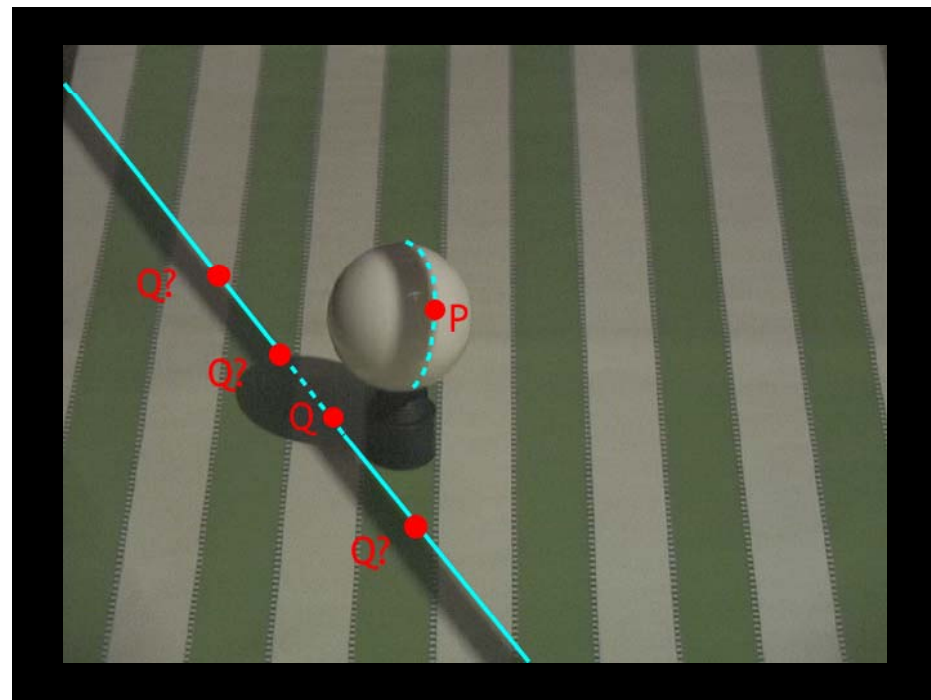
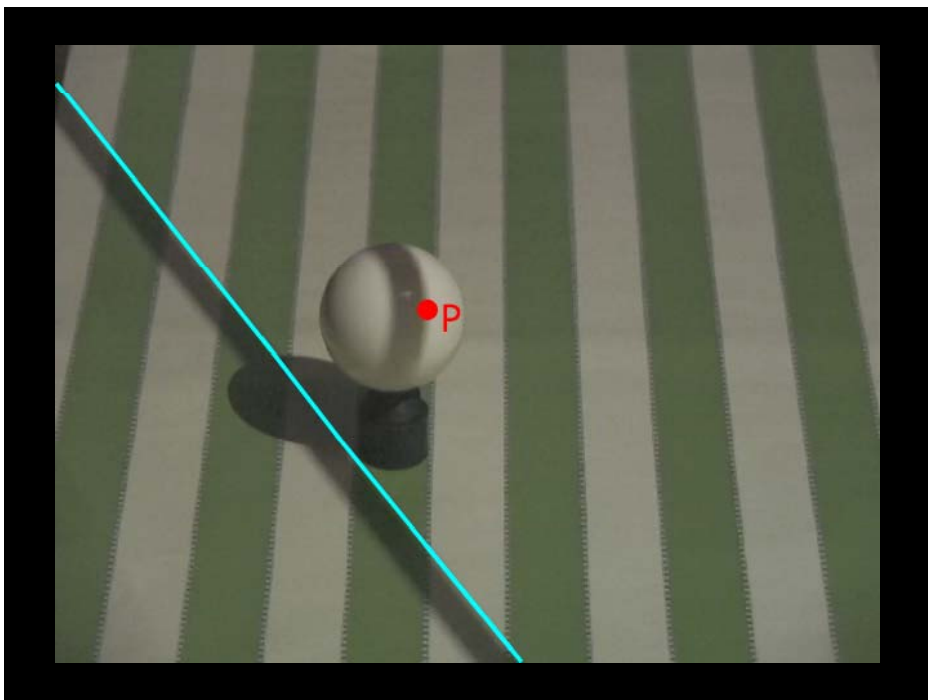


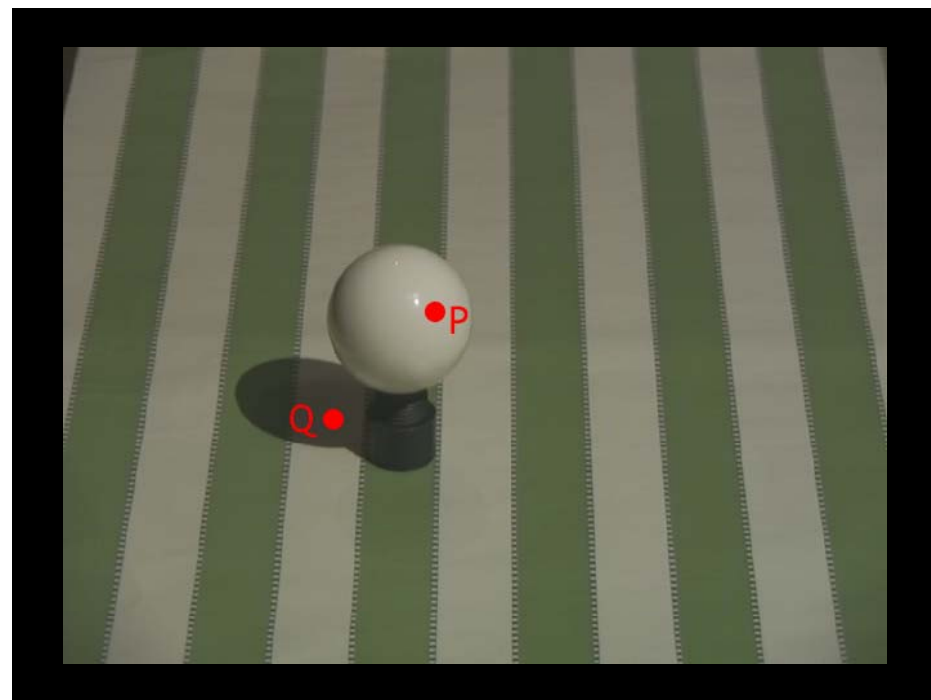
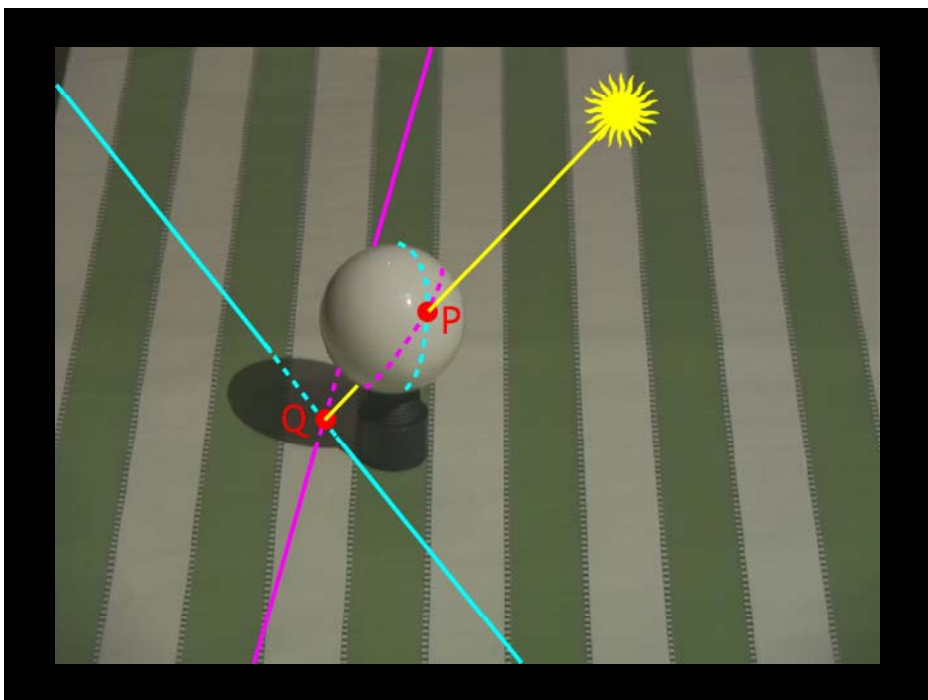
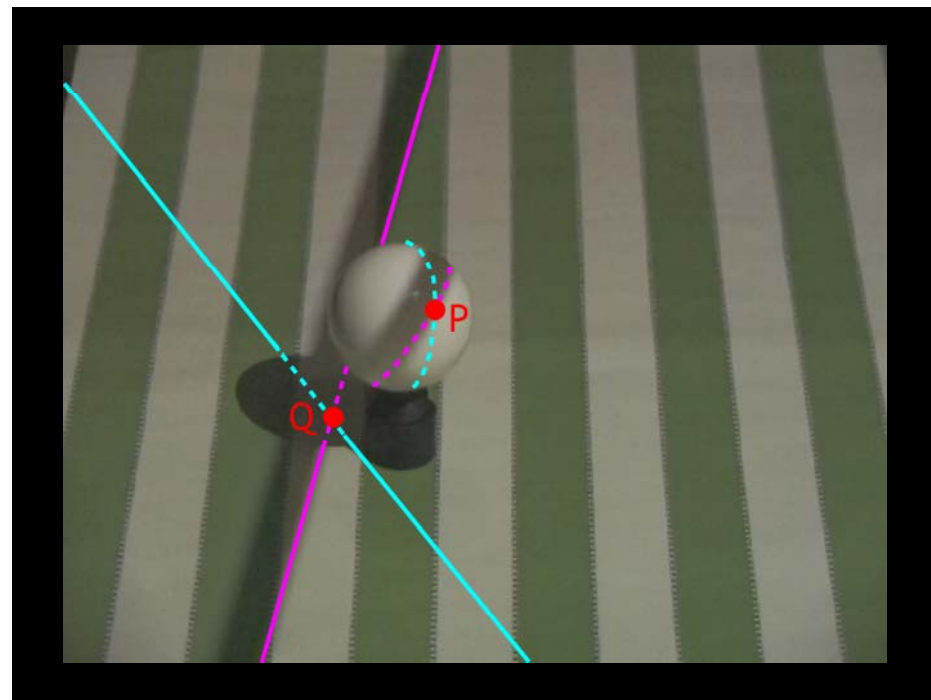
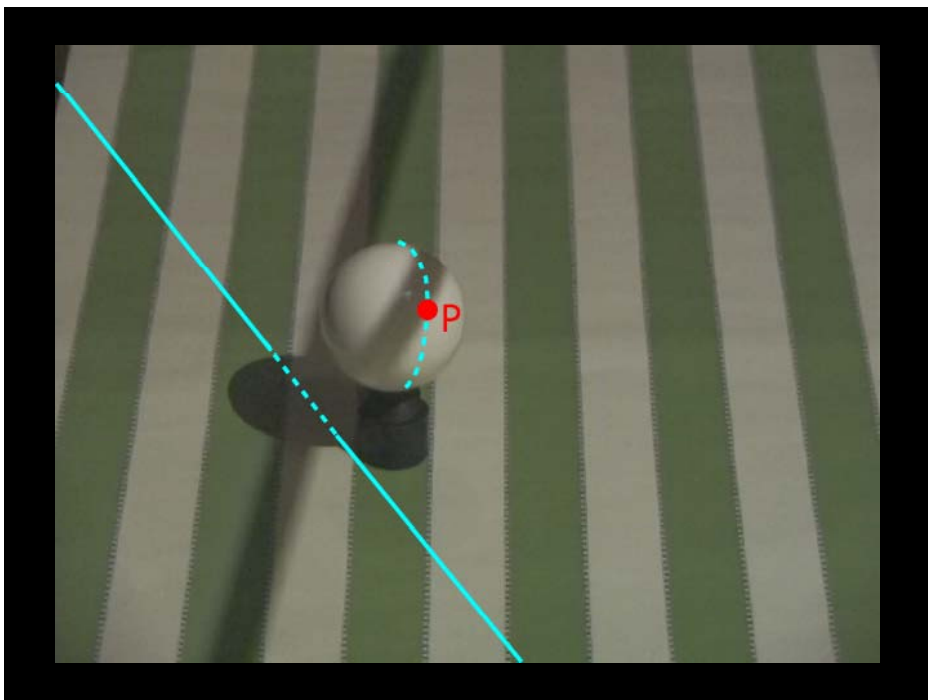
*Requirement #2*

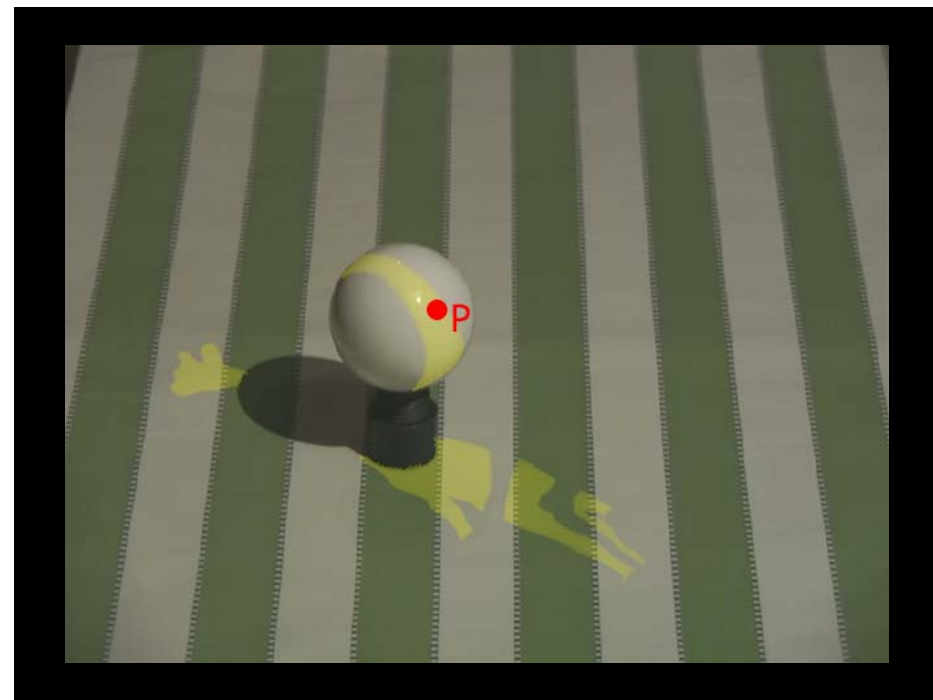
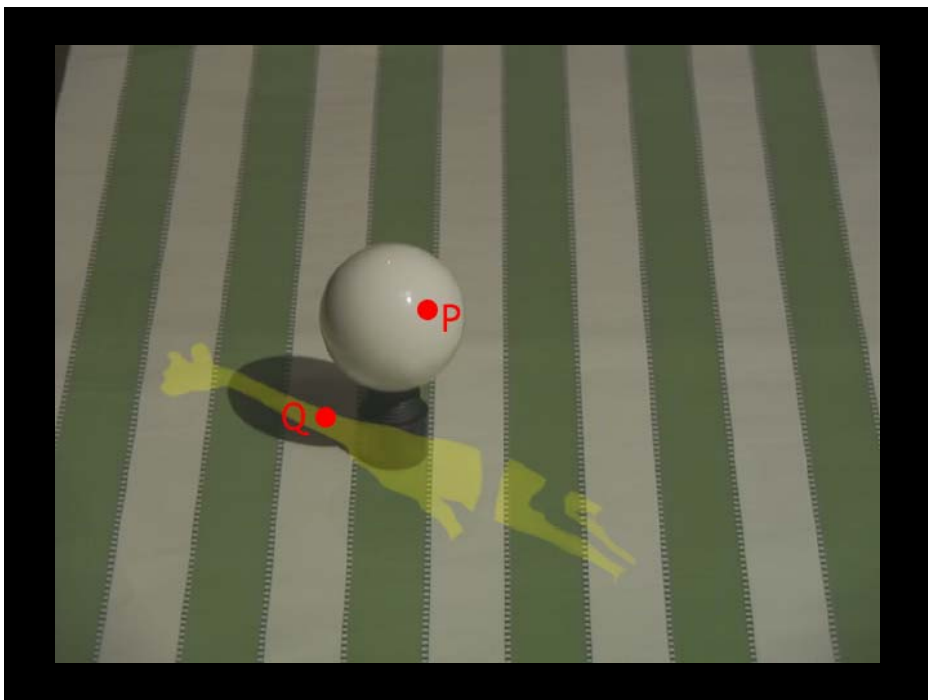


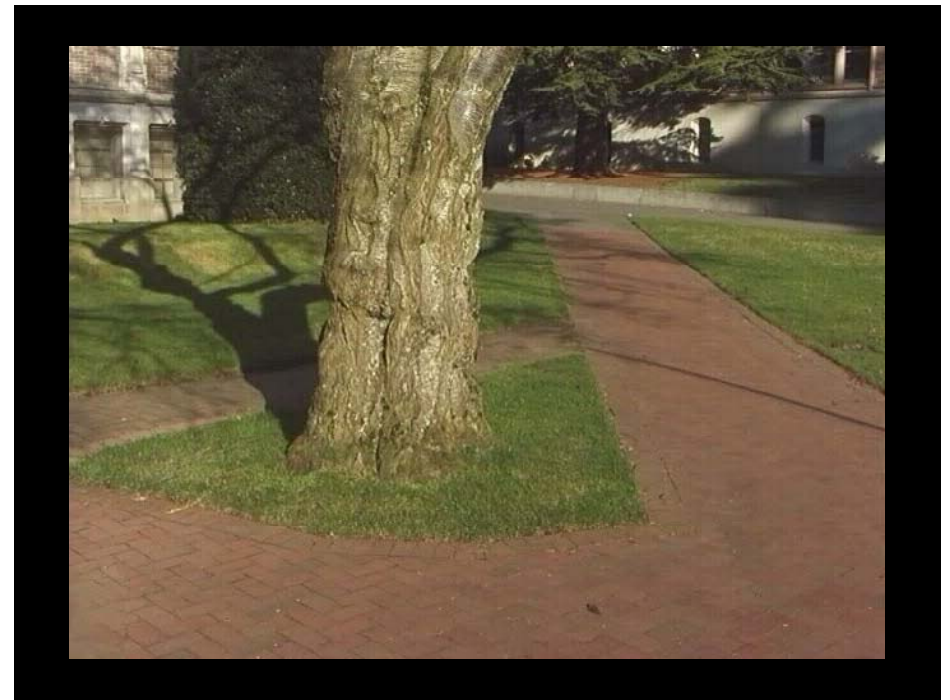


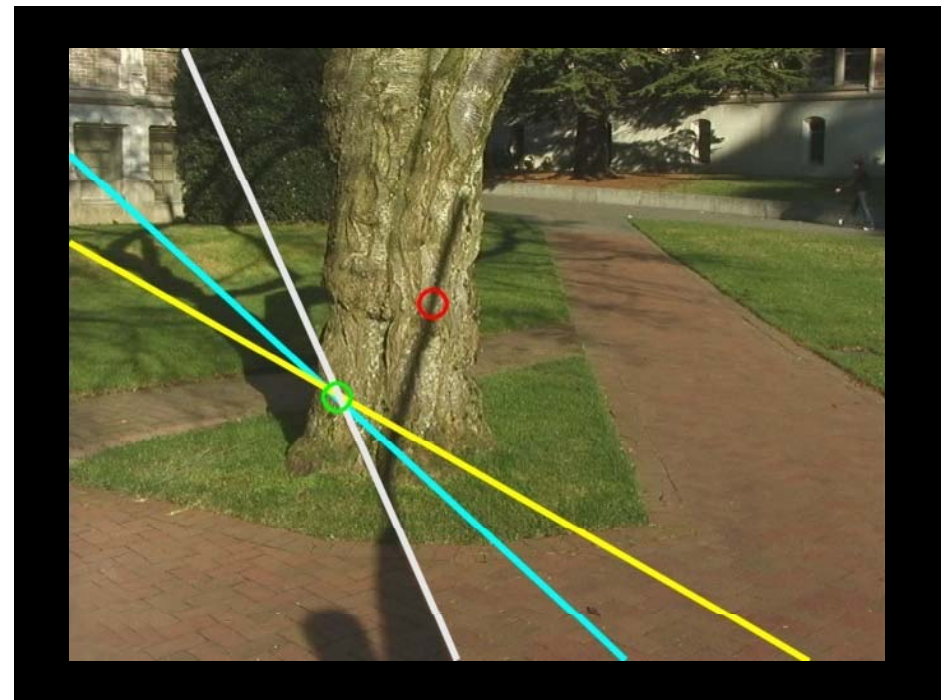
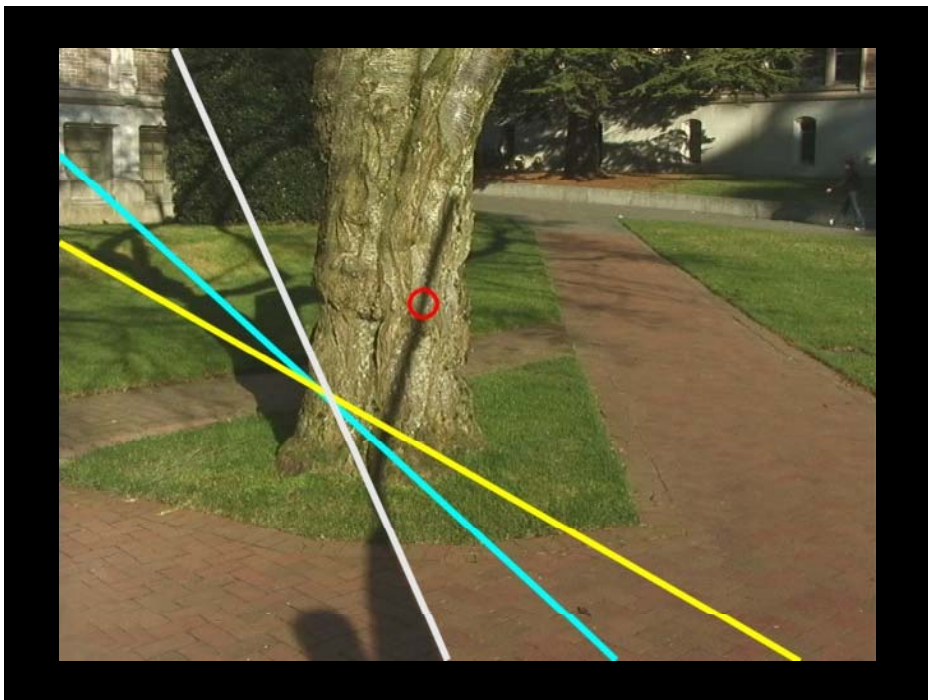


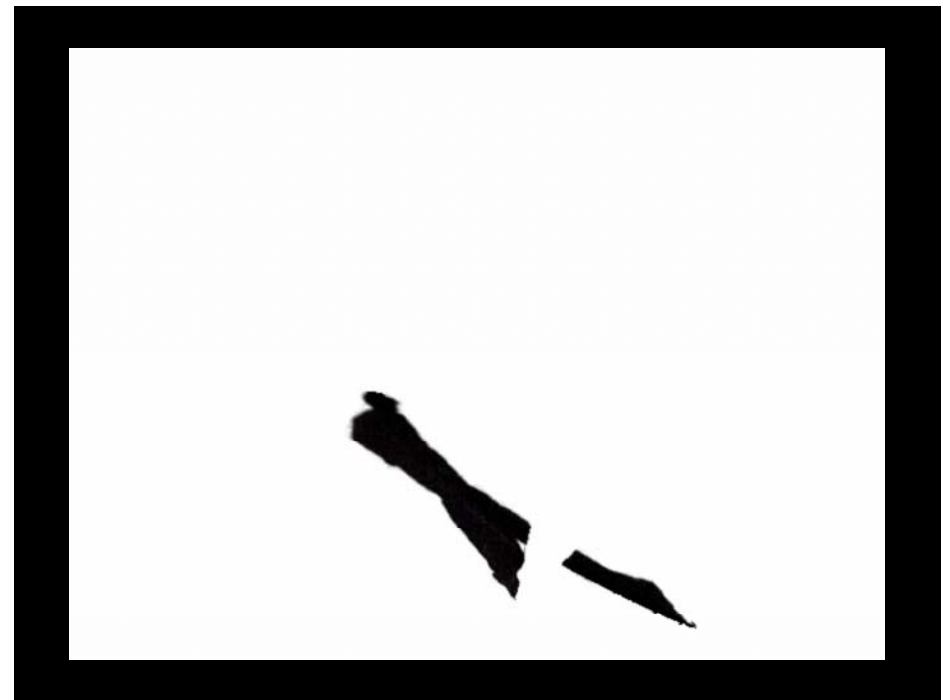
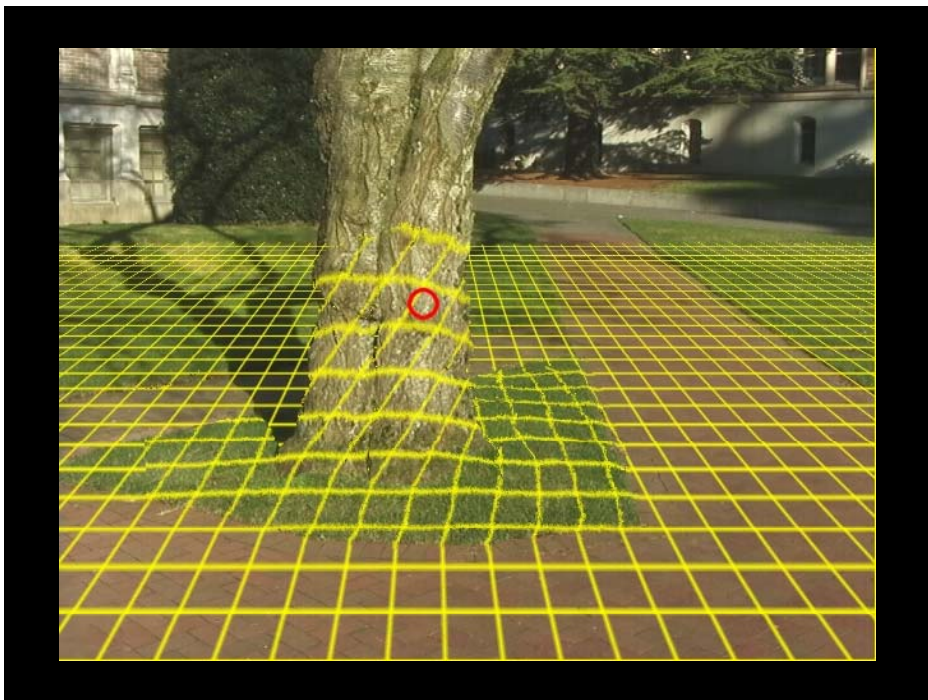
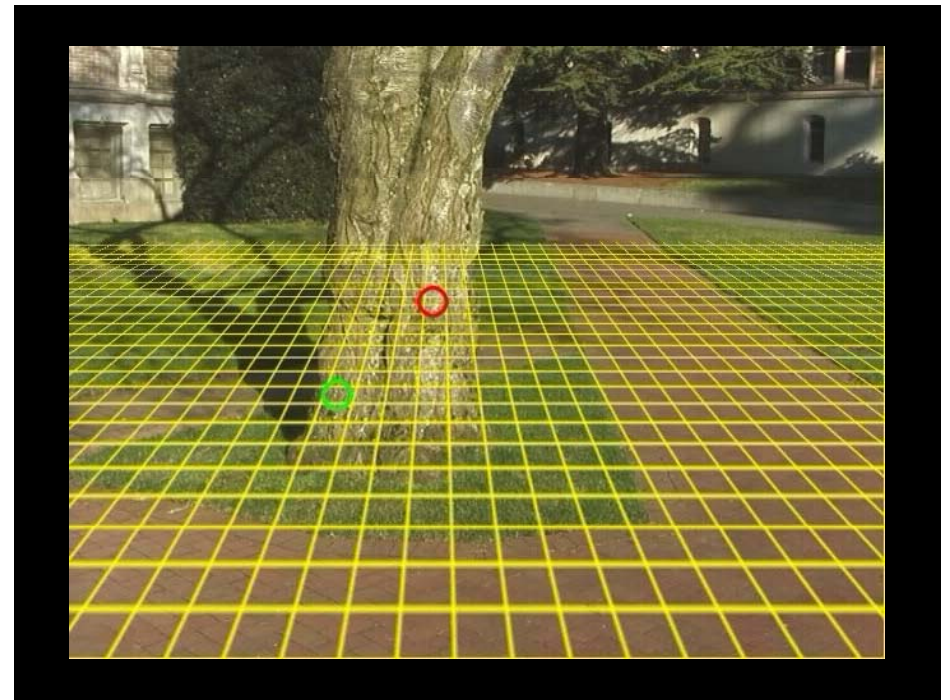
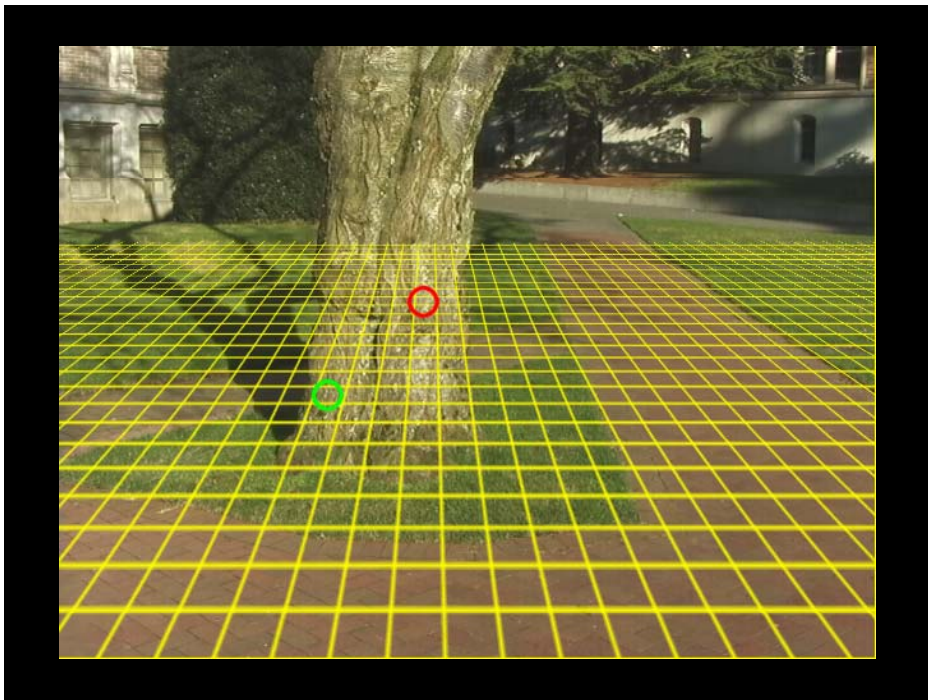


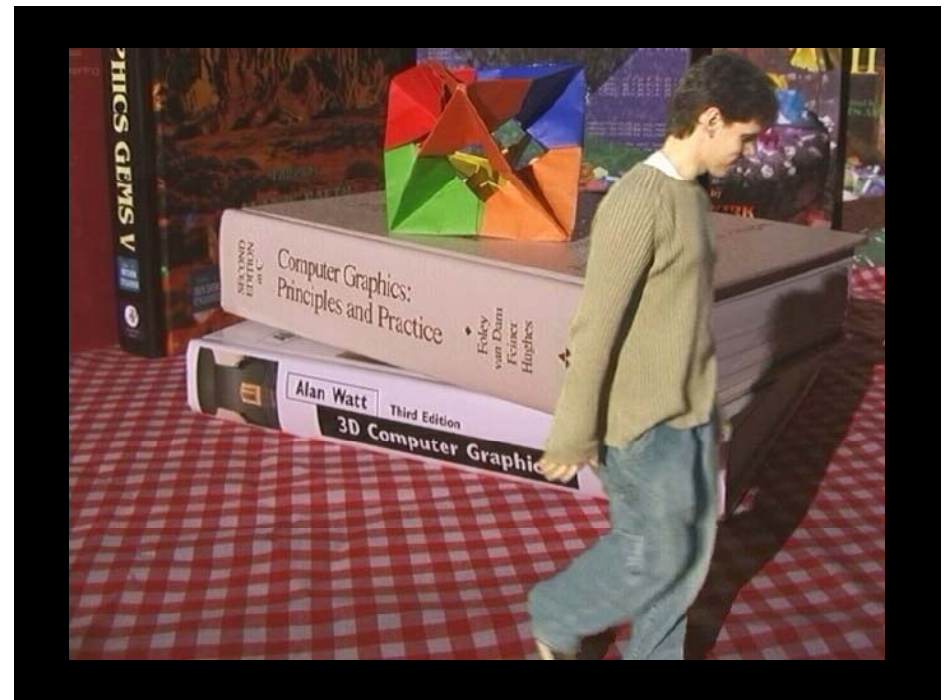
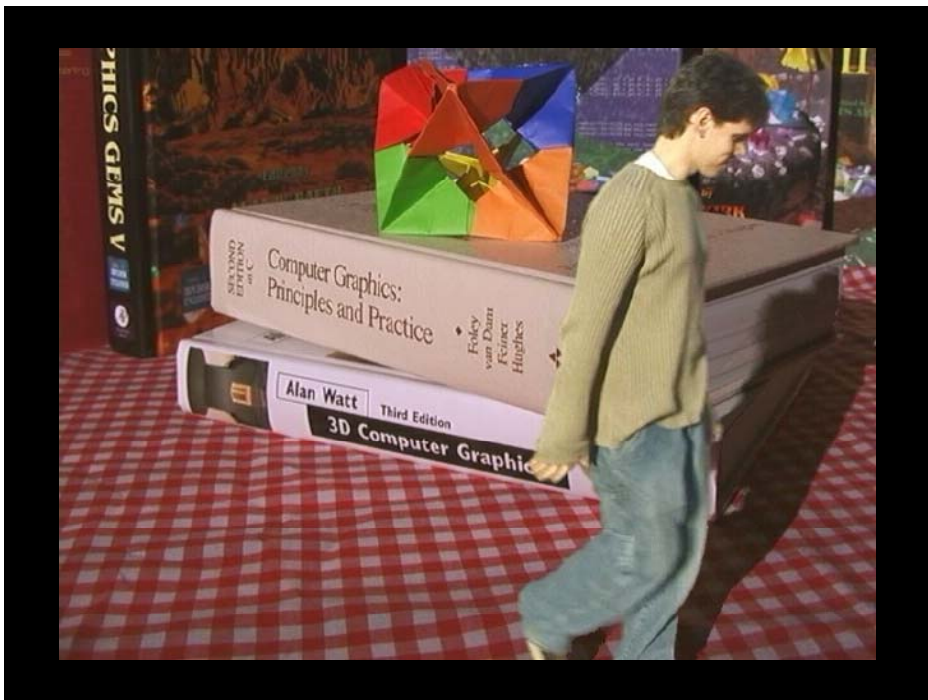












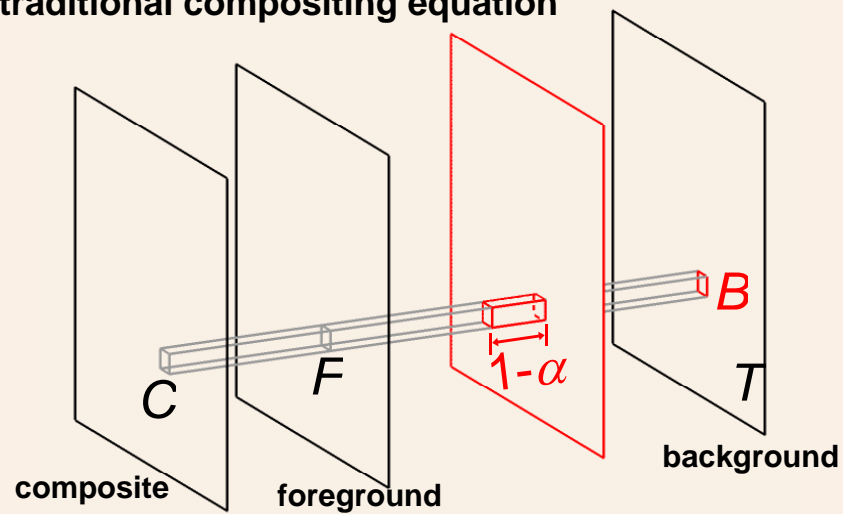
# Environment matting

blue screen matting

photograph

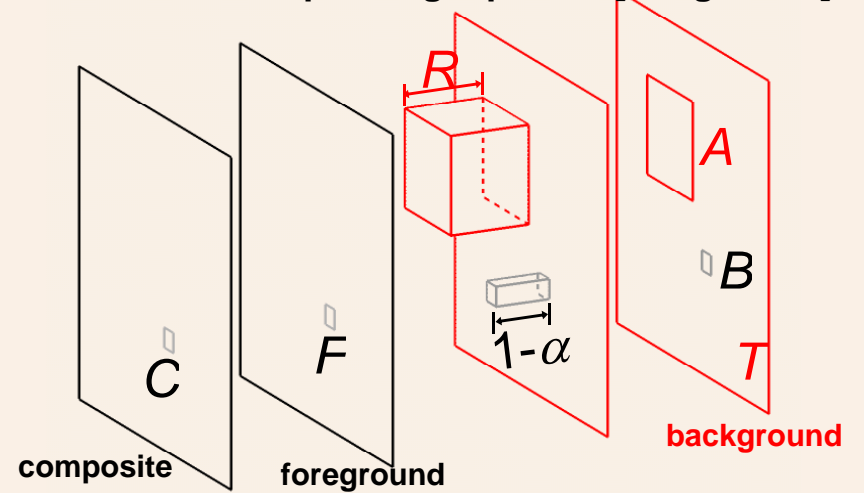


traditional compositing equation



$$C = F + (1 - \alpha)B$$

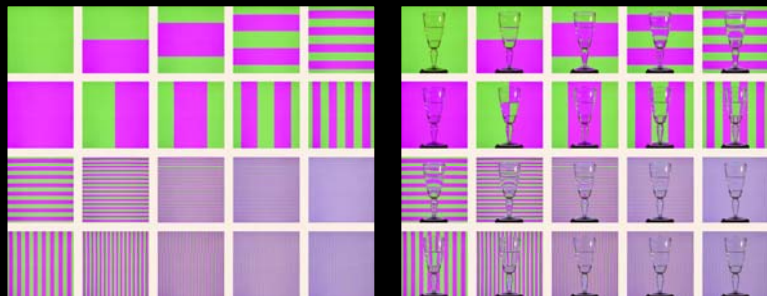
environment compositing equation [Zongker'99]



$$C = F + (1 - \alpha)B + RM(T, A)$$



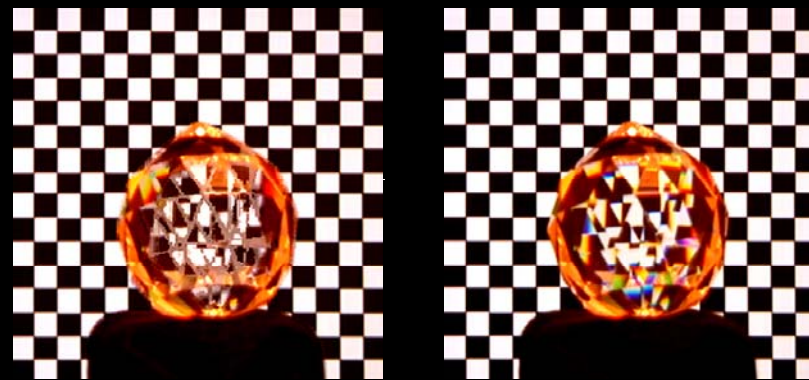
O(k) images



*Environment matting [Zongker'99]*

Zongker et al.

photograph



*Problem: color dispersion*

Zongker et al.

photograph



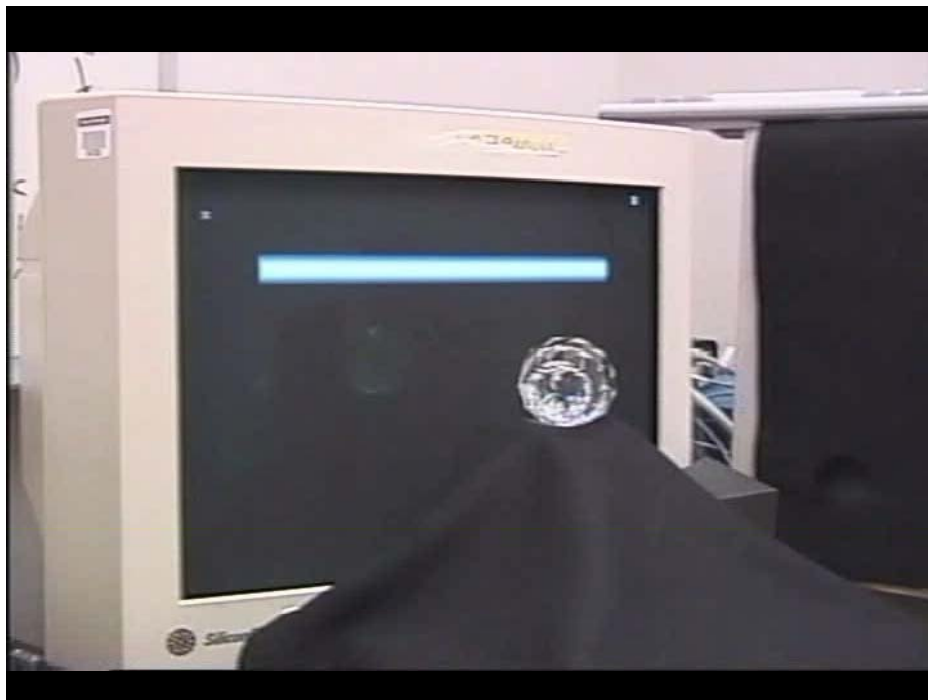
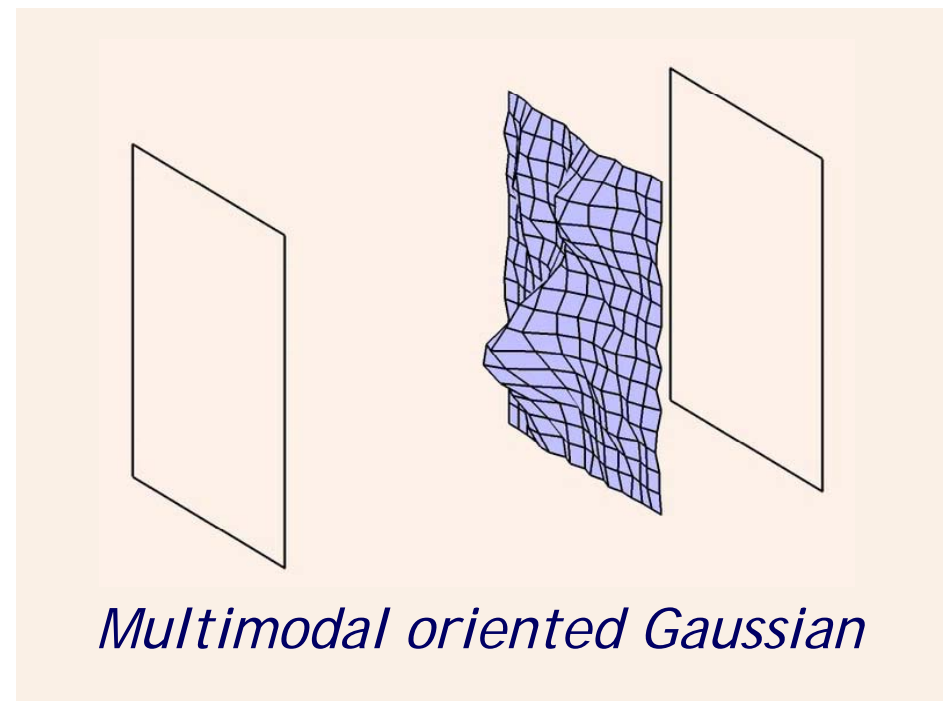
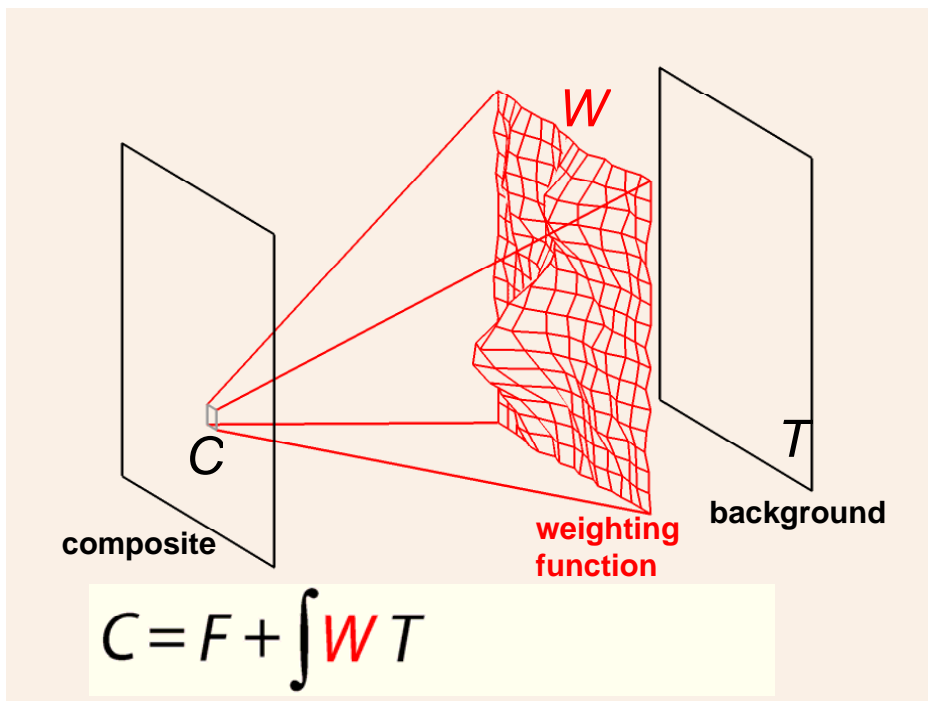
*Problem: glossy surface*

Zongker et al.

photograph

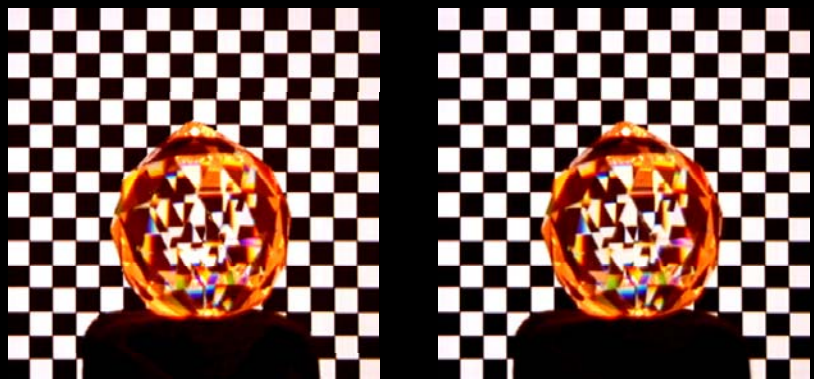


*Problem: multiple mappings*



high accuracy  
algorithm

photograph



*Problem: color dispersion*

high accuracy  
algorithm

photograph



*Glossy surface*

with  
orientation

photograph



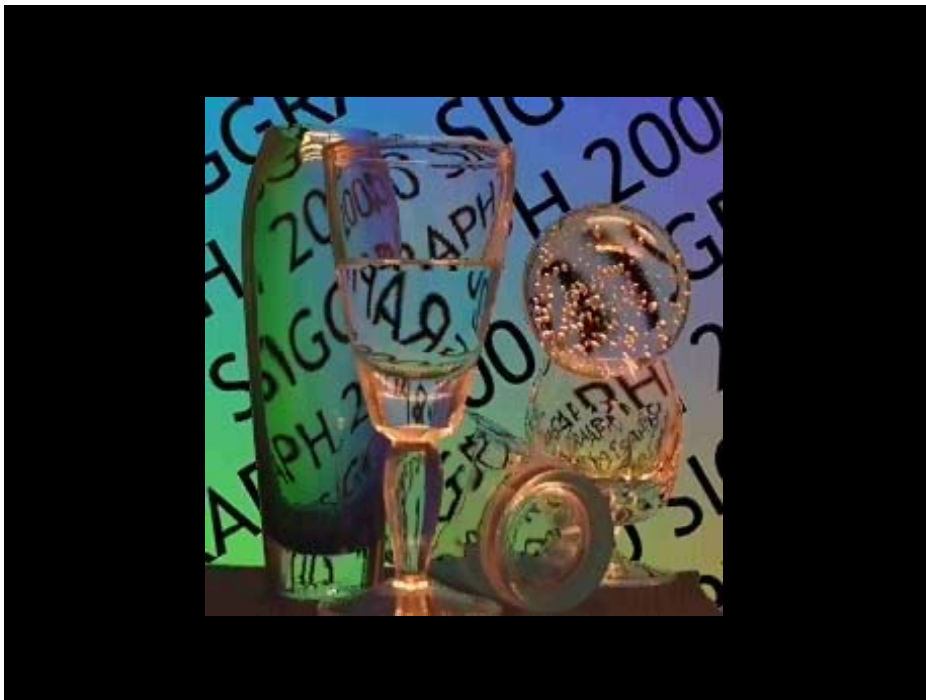
*Oriented Gaussian*

high accuracy  
algorithm

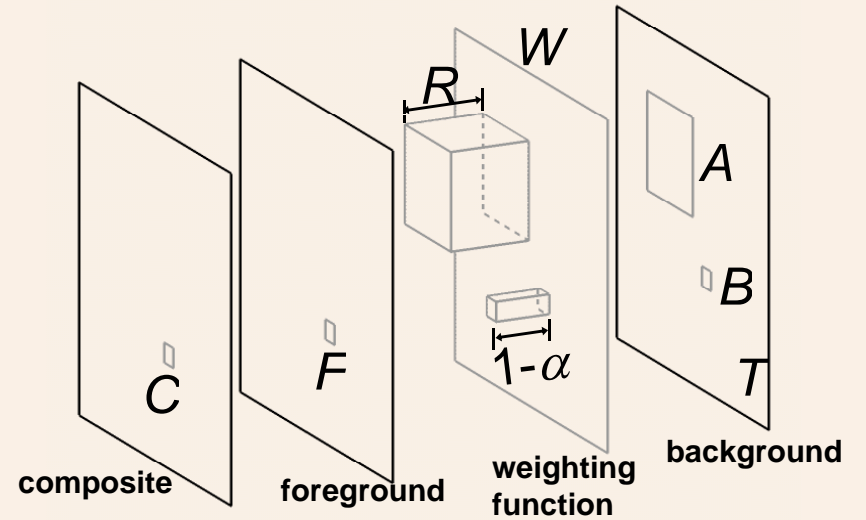
photograph



*Problem: multiple mappings*



$$C = F + (1 - \alpha)B + R\mathcal{M}(T, A)$$



$$C = F + (1 - \alpha)B + R\mathcal{M}(T, A)$$

3    3    1    3    4

3 observations  
11 variables

- $A, R$
- $\alpha$
- $F$

$$C = R\mathcal{M}(T, A)$$

3    3    4

3 observations  
7 variables

- $A, R$
- $\alpha$
- $F$

$$C = \rho \mathcal{M}(T, A)$$

3      1      4

3 observations  
5 variables

- $A, R \longrightarrow A, \rho$
- $\alpha$                       colorless
- $F$

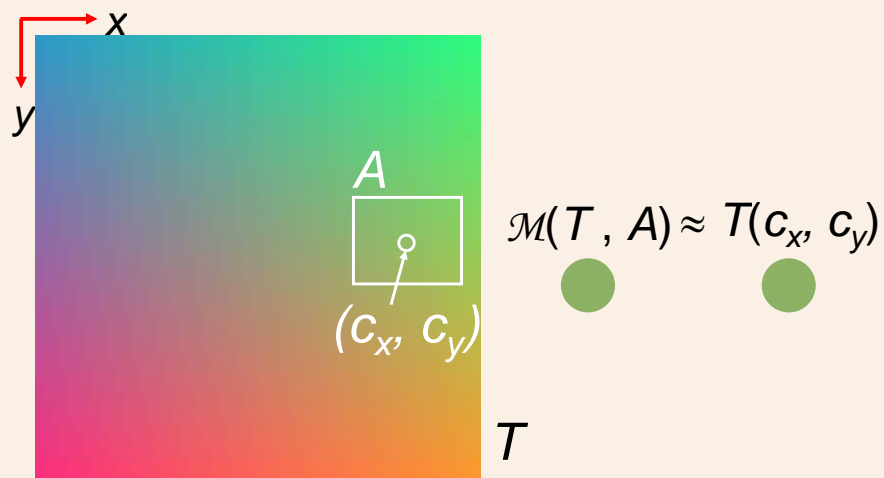
$$C = \rho T(c_x, c_y)$$

3      1      1      1

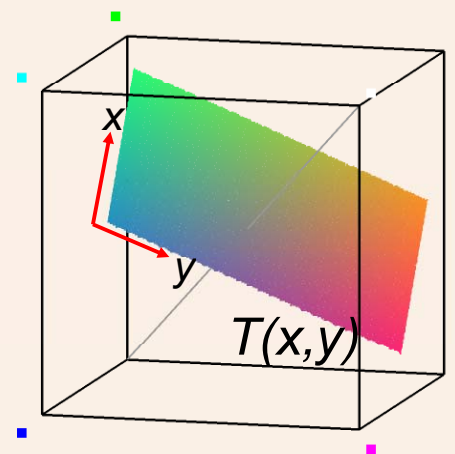
3 observations  
3 variables

- $A, R \longrightarrow A, \rho \longrightarrow c_x, c_y, \rho$
- $\alpha$                       colorless                      specularly
- $F$     refractive

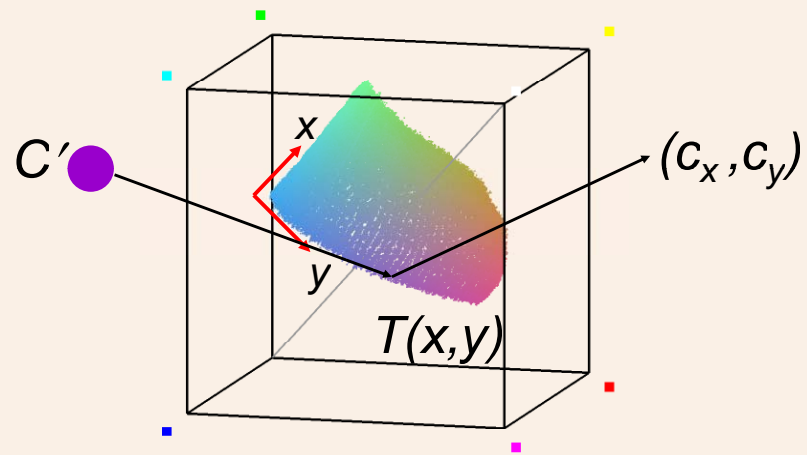
### Stimulus function



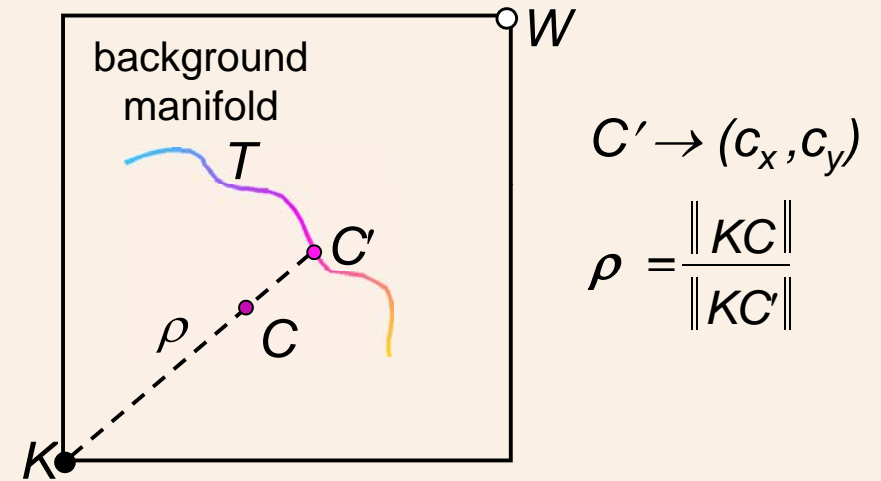
### Ideal plane in RGB cube



## Calibrated manifold in RGB cube



## Estimate $c_x, c_y$ and $\rho$



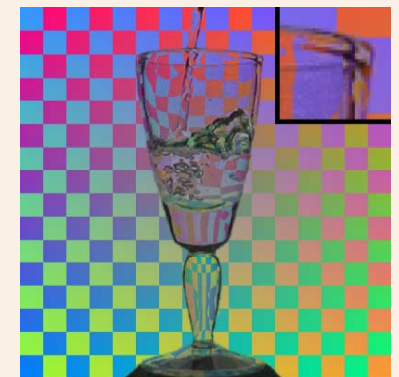
## Problem: noisy matte



## Edge-preserving filtering



without filtering

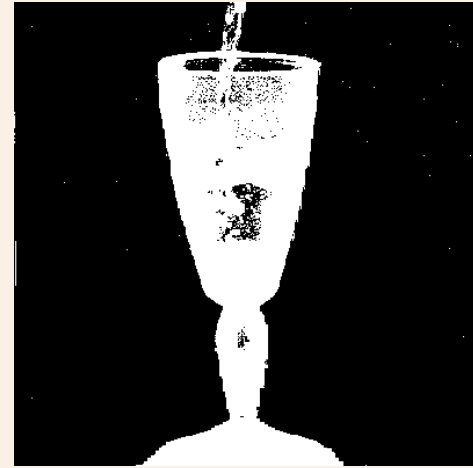


with filtering

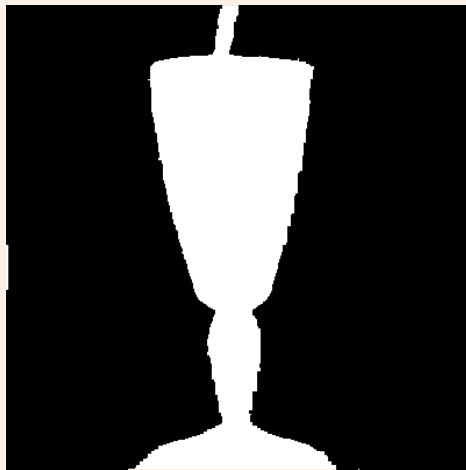
*Input image*



*Difference thresholding*



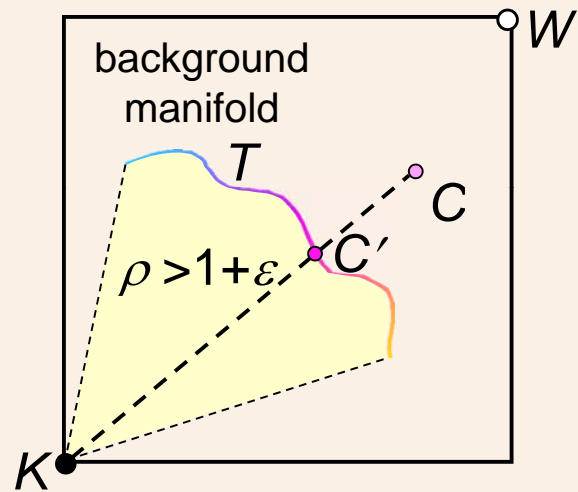
*Morphological operation*



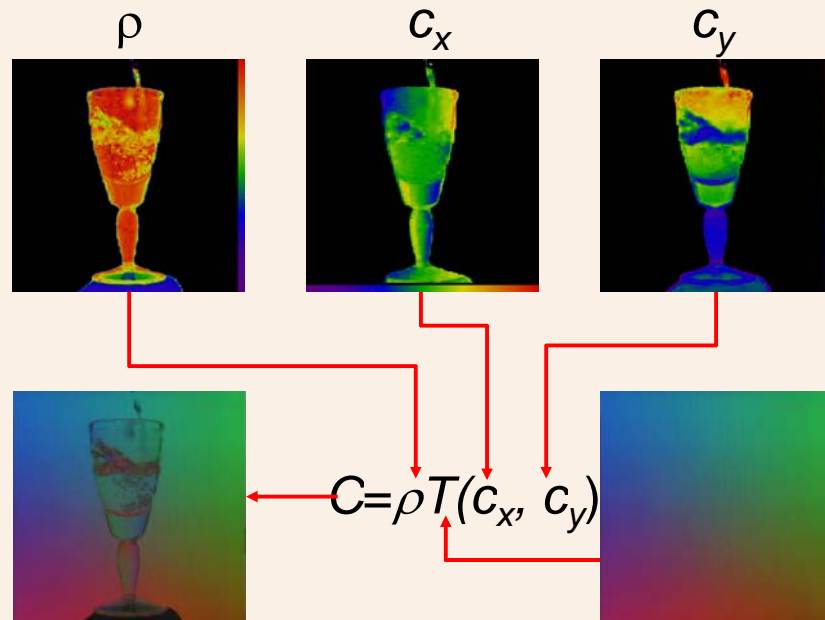
*Feathering*



## Heuristics for specular highlights



## Heuristics for specular highlights

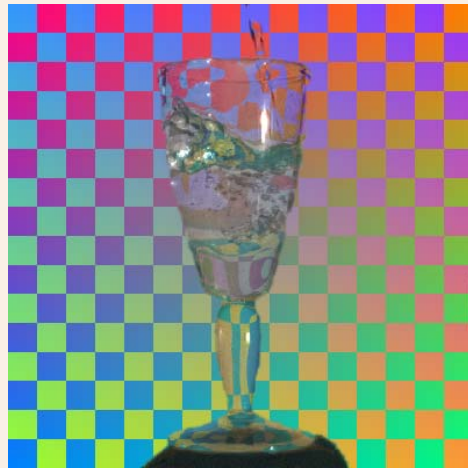


## Heuristics for specular highlights





## *Composite with highlights*



	compositing model	matting method
color blending		blue-screen Bayesian
shadow		Shadow matting
refraction reflection		High-accuracy env. matting