Image stitching

Digital Visual Effects

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with slides by Richard Szeliski, Steve Seitz, Matthew Brown and Vaclav Hlavac

Image stitching

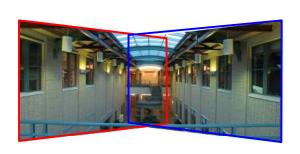


• Stitching = alignment + blending

geometrical photometric registration







Applications of image stitching



- Video stabilization
- Video summarization
- Video compression
- Video matting
- Panorama creation

Video summarization







Video compression







DigiVFX







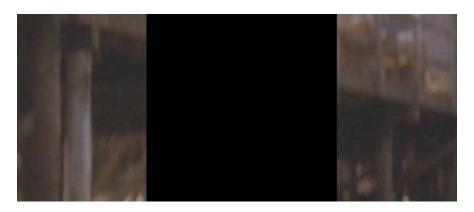




input video

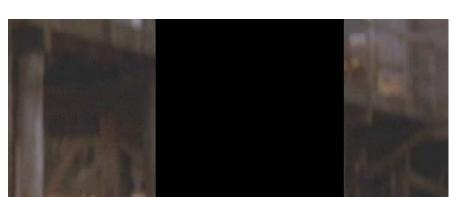
Object removal

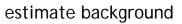




remove foreground

Object removal





Object removal





background estimation

Panorama creation







Why panorama?



- Are you getting the whole picture?
 - Compact Camera FOV = 50 x 35°



Why panorama?



- Are you getting the whole picture?
 - Compact Camera FOV = 50 x 35°
 - Human FOV = $200 \times 135^{\circ}$



Why panorama?



Are you getting the whole picture?

- Compact Camera FOV = 50 x 35°

- Human FOV = $200 \times 135^{\circ}$

- Panoramic Mosaic = 360 x 180°



Panorama examples



- Like HDR, it is a topic of computational photography, seeking ways to build a better camera mostly in software.
- Most consumer cameras have a panorama mode
- Mars:

http://www.panoramas.dk/fullscreen3/f2_mars97.html

• Earth:

http://www.panoramas.dk/new-year-2006/taipei.html
http://www.360cities.net/

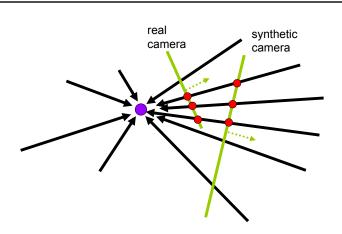
What can be globally aligned?



- In image stitching, we seek for a matrix to globally warp one image into another. Are any two images of the same scene can be aligned this way?
 - Images captured with the same center of projection
 - A planar scene or far-away scene

A pencil of rays contains all views

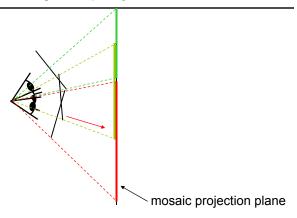




Can generate any synthetic camera view as long as it has the same center of projection!

Mosaic as an image reprojection

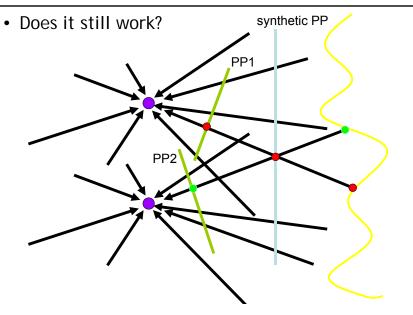




- The images are reprojected onto a common plane
- The mosaic is formed on this plane
- Mosaic is a *synthetic wide-angle camera*

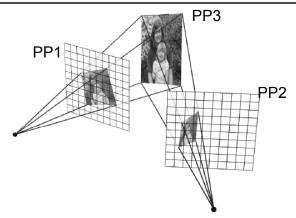
Changing camera center





Planar scene (or a faraway one)





- PP3 is a projection plane of both centers of projection, so we are OK!
- This is how big aerial photographs are made

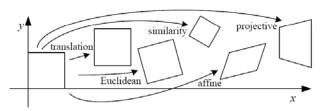
Motion models



• Parametric models as the assumptions on the relation between two images.

2D Motion models

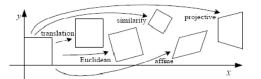




Name	Matrix	# D.O.F.	Preserves:	Icon
translation	$egin{bmatrix} I \ I \ \end{bmatrix}_{2 imes 3}$	2	orientation $+\cdots$	
rigid (Euclidean)	$egin{bmatrix} ig[m{R} m{\mid} m{t} \ ig]_{2 imes 3} \end{split}$	3	lengths $+\cdots$	\Diamond
similarity	$\begin{bmatrix} sR \mid t \end{bmatrix}_{2 \times 3}$	4	$angles + \cdots$	\Diamond
affine	$\left[egin{array}{c} oldsymbol{A} \end{array} ight]_{2 imes 3}$	6	$parallelism + \cdots$	
projective	$\left[egin{array}{c} ilde{H} \end{array} ight]_{3 imes 3}$	8	straight lines	

Motion models





Translation

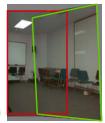
Affine

Perspective 3D rotation







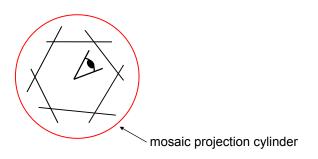


2 unknowns 6 unknowns 8 unknowns 3 unknowns

A case study: cylindrical panorama



• What if you want a 360° field of view?



Cylindrical panoramas





- Steps
 - Reproject each image onto a cylinder
 - Blend
 - Output the resulting mosaic

Cylindrical panorama

- **Digi**VFX
- 1. Take pictures on a tripod (or handheld)
- 2. Warp to cylindrical coordinate
- 3. Compute pairwise alignments
- 4. Fix up the end-to-end alignment
- 5. Blending
- 6. Crop the result and import into a viewer

It is required to do radial distortion correction for better stitching results!

Taking pictures





Kaidan panoramic tripod head

Translation model

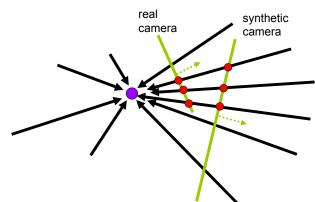






Try to align this in PaintShop Pro

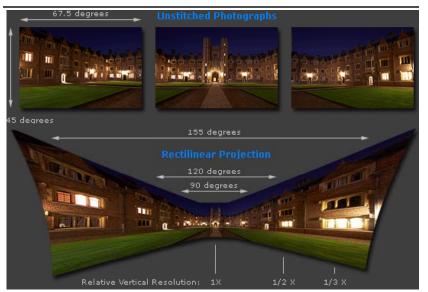
Where should the synthetic camera beigivex



- The projection plan of some camera
- · Onto a cylinder

Cylindrical projection

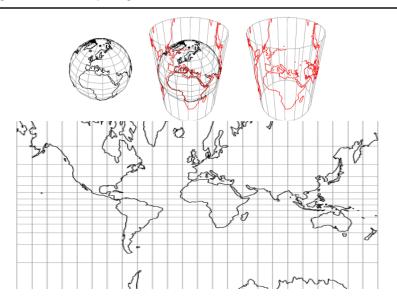




Adopted from http://www.cambridgeincolour.com/tutorials/image-projections.htm

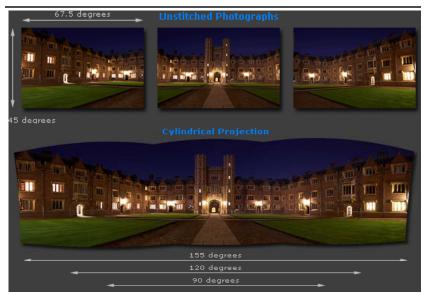
Cylindrical projection





Cylindrical projection

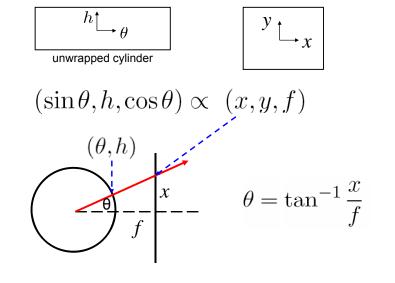




Adopted from http://www.cambridgeincolour.com/tutorials/image-projections.htm

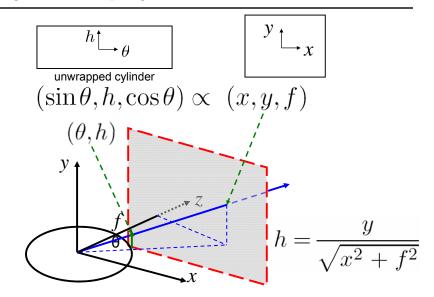
Cylindrical projection





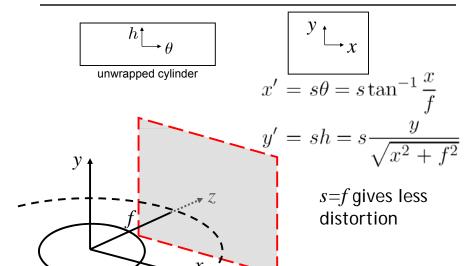
Cylindrical projection





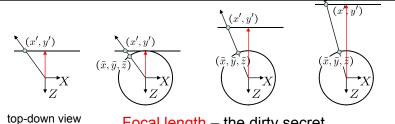
Cylindrical projection





Cylindrical reprojection





Focal length – the dirty secret...







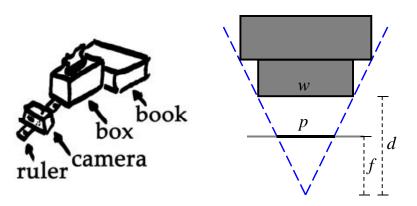


Image 384x300 f = 180 (pixels) f = 280

f = 380

A simple method for estimating f





Or, you can use other software, such as AutoStich, to help.

Input images





Cylindrical warping







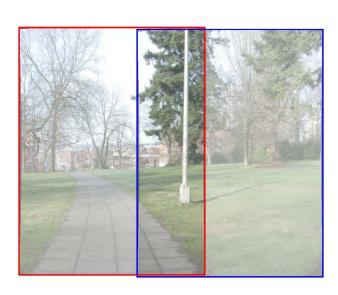
Blending



• Why blending: parallax, lens distortion, scene motion, exposure difference

Blending





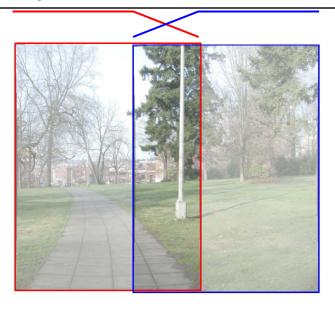
Blending



Blending



DigiVFX





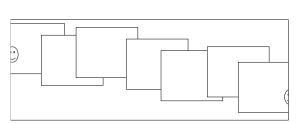
Assembling the panorama





• Stitch pairs together, blend, then crop

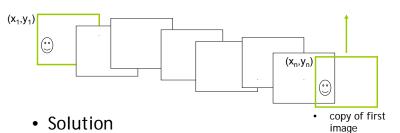
Problem: Drift



- Error accumulation
 - small errors accumulate over time

Problem: Drift





- add another copy of first image at the end
- there are a bunch of ways to solve this problem
 - add displacement of $(y_1 y_n)/(n-1)$ to each image after the first
 - compute a global warp: y' = y + ax
 - run a big optimization problem, incorporating this constraint
 - best solution, but more complicated
 - known as "bundle adjustment"

End-to-end alignment and crop







Viewer: panorama





 $example: $$ \underline{ \text{http://www.cs.washington.edu/education/courses/cse590ss/01wi/projects/project1/students/dougz/index.html} $$ $\underline{ \text{http://www.cs.washington.edu/education/courses/cse590ss/01wi/projects/project1/students/dougz/index.html} $$ $\underline{ \text{http://www.cs.washington.edu/education/courses/cse590ss/01wi/projects/project1/students/dougz/index.html} $$ $\underline{ \text{http://www.cs.washington.edu/education/cse590ss/01wi/projects/project1/students/dougz/index.html} $$ $\underline{ \text{http://www.cs.washington.edu/education/cse590ss/o1wi/project1/students/dougs/index.html} $$ \underline

Viewer: texture mapped model





example: http://www.panoramas.dk/

Cylindrical panorama



- 1. Take pictures on a tripod (or handheld)
- 2. Warp to cylindrical coordinate
- 3. Compute pairwise alignments
- 4. Fix up the end-to-end alignment
- 5. Blending
- 6. Crop the result and import into a viewer

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Determine pairwise alignment

- p'=Mp, where M is a transformation matrix, p and p' are feature matches
- It is possible to use more complicated models such as affine or perspective
- For example, assume M is a 2x2 matrix

$$\begin{pmatrix} x' \\ y' \end{pmatrix} = \begin{pmatrix} m_{11} & m_{12} \\ m_{21} & m_{22} \end{pmatrix} \begin{pmatrix} x \\ y \end{pmatrix}$$

• Find M with the least square error

$$\sum_{i=1}^{n} (Mp - p')^2$$

Determine pairwise alignment?



- Feature-based methods: only use feature points to estimate parameters
- We will study the "Recognising panorama" paper published in ICCV 2003
- Run SIFT (or other feature algorithms) for each image, find feature matches.

Determine pairwise alignment



$$\begin{pmatrix} x' \\ y' \end{pmatrix} = \begin{pmatrix} m_{11} & m_{12} \\ m_{21} & m_{22} \end{pmatrix} \begin{pmatrix} x \\ y \end{pmatrix}$$

$$x_1 m_{11} + y_1 m_{12} = x_1$$

$$x_1 m_{21} + y_1 m_{22} = y_1$$

Overdetermined system

$$\begin{pmatrix} x_1 & y_1 & 0 & 0 \\ 0 & 0 & x_1 & y_1 \\ x_2 & y_2 & 0 & 0 \\ \vdots & \vdots & \vdots & \vdots \\ x_n & y_n & 0 & 0 \\ 0 & 0 & x_n & y_n \end{pmatrix} \begin{pmatrix} m_{11} \\ m_{12} \\ m_{21} \\ m_{22} \end{pmatrix} = \begin{pmatrix} x_1 \\ y_1 \\ x_2 \\ \vdots \\ x_n \\ y_n \end{pmatrix}$$

Normal equation

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Given an overdetermined system

$$\mathbf{A}\mathbf{x} = \mathbf{b}$$

the normal equation is that which minimizes the sum of the square differences between left and right sides

$$\mathbf{A}^{\mathrm{T}}\mathbf{A}\mathbf{x} = \mathbf{A}^{\mathrm{T}}\mathbf{b}$$

Why?

Normal equation



$$E(\mathbf{x}) = (\mathbf{A}\mathbf{x} - \mathbf{b})^2$$

$$\begin{bmatrix} a_{11} & \dots & a_{1m} \\ \vdots & & \vdots \\ \vdots & & \vdots \\ a_{n1} & \dots & a_{nm} \end{bmatrix} \begin{bmatrix} x_1 \\ \vdots \\ x_m \end{bmatrix} = \begin{bmatrix} b_1 \\ \vdots \\ \vdots \\ b_n \end{bmatrix}$$

nxm, n equations, m variables

Normal equation



$$\mathbf{A}\mathbf{x} - \mathbf{b} = \begin{bmatrix} \sum_{j=1}^{m} a_{1j} x_j \\ \vdots \\ \sum_{j=1}^{m} a_{ij} x_j \\ \vdots \\ \sum_{j=1}^{m} a_{nj} x_j \end{bmatrix} - \begin{bmatrix} b_1 \\ \vdots \\ b_n \end{bmatrix} = \begin{bmatrix} \sum_{j=1}^{m} a_{1j} x_j \\ \vdots \\ \sum_{j=1}^{m} a_{nj} x_j \end{bmatrix} - b_i$$

$$\vdots \\ \begin{bmatrix} \sum_{j=1}^{m} a_{nj} x_j \\ \vdots \\ \sum_{j=1}^{m} a_{nj} x_j \end{bmatrix} - b_n$$

$$E(\mathbf{x}) = (\mathbf{A}\mathbf{x} - \mathbf{b})^2 = \sum_{j=1}^{m} \left[\sum_{j=1}^{m} a_{ij} x_j - b_i \right]^2$$

Normal equation

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$$E(\mathbf{x}) = (\mathbf{A}\mathbf{x} - \mathbf{b})^{2} = \sum_{i=1}^{n} \left[\left(\sum_{j=1}^{m} a_{ij} x_{j} \right) - b_{i} \right]^{2}$$

$$0 = \frac{\partial E}{\partial x_{1}} = \sum_{i=1}^{n} 2 \left[\left(\sum_{j=1}^{m} a_{ij} x_{j} \right) - b_{i} \right] a_{i1}$$

$$= 2 \sum_{i=1}^{n} a_{i1} \sum_{j=1}^{m} a_{ij} x_{j} - 2 \sum_{i=1}^{n} a_{i1} b_{i}$$

$$0 = \frac{\partial E}{\partial \mathbf{x}} = 2(\mathbf{A}^{T} \mathbf{A} \mathbf{x} - \mathbf{A}^{T} \mathbf{b}) \longrightarrow \mathbf{A}^{T} \mathbf{A} \mathbf{x} = \mathbf{A}^{T} \mathbf{b}$$

Normal equation



$$(\mathbf{A}\mathbf{x} - \mathbf{b})^{2}$$

$$= (\mathbf{A}\mathbf{x} - \mathbf{b})^{T} (\mathbf{A}\mathbf{x} - \mathbf{b})$$

$$= ((\mathbf{A}\mathbf{x})^{T} - \mathbf{b}^{T}) (\mathbf{A}\mathbf{x} - \mathbf{b})$$

$$= (\mathbf{x}^{T} \mathbf{A}^{T} - \mathbf{b}^{T}) (\mathbf{A}\mathbf{x} - \mathbf{b})$$

$$= \mathbf{x}^{T} \mathbf{A}^{T} \mathbf{A}\mathbf{x} - \mathbf{b}^{T} \mathbf{A}\mathbf{x} - \mathbf{x}^{T} \mathbf{A}^{T} \mathbf{b} + \mathbf{b}^{T} \mathbf{b}$$

$$= \mathbf{x}^{T} \mathbf{A}^{T} \mathbf{A}\mathbf{x} - (\mathbf{A}^{T} \mathbf{b})^{T} \mathbf{x} - (\mathbf{A}^{T} \mathbf{b})^{T} \mathbf{x} + \mathbf{b}^{T} \mathbf{b}$$

$$\frac{\partial E}{\partial \mathbf{x}} = 2\mathbf{A}^{T} \mathbf{A}\mathbf{x} - 2\mathbf{A}^{T} \mathbf{b}$$

Determine pairwise alignment



- p'=Mp, where M is a transformation matrix, p and p' are feature matches
- For translation model, it is easier.

$$E = \sum_{i=1}^{n} \left[\left(m_1 + x_i - x_i \right)^2 + \left(m_2 + y_i - y_i \right)^2 \right]$$

$$0 = \frac{\partial E}{\partial m_1}$$

 What if the match is false? Avoid impact of outliers.

RANSAC



- RANSAC = Random Sample Consensus
- An algorithm for robust fitting of models in the presence of many data outliers
- Compare to robust statistics
- Given N data points x_i , assume that mjority of them are generated from a model with parameters Θ , try to recover Θ .

RANSAC algorithm



Run k times: \longrightarrow How many times?

- (1) draw(n samples) randomly How big?
 Smaller is better
- (2) fit parameters Θ with these n samples
- (3) for each of other N-n points, calculate its distance to the fitted model, count the number of inlier points c

Output Θ with the largest c

How to define? Depends on the problem.

How to determine k

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p: probability of real inliers

P: probability of success after k trials

$$P=1-(1-p^n)^k$$

n samples are all inliers

a failure

failure after k trials

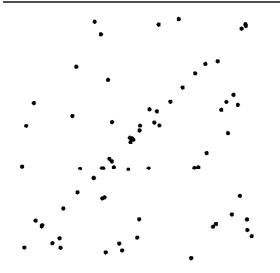
$$k = \frac{\log(1-P)}{\log(1-p^n)}$$

n	p	k
3	0.5	35
6	0.6	97
6	0.5	293

n=2

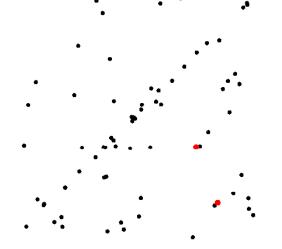
Example: line fitting





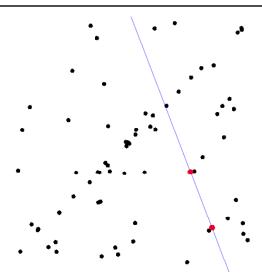
Example: line fitting

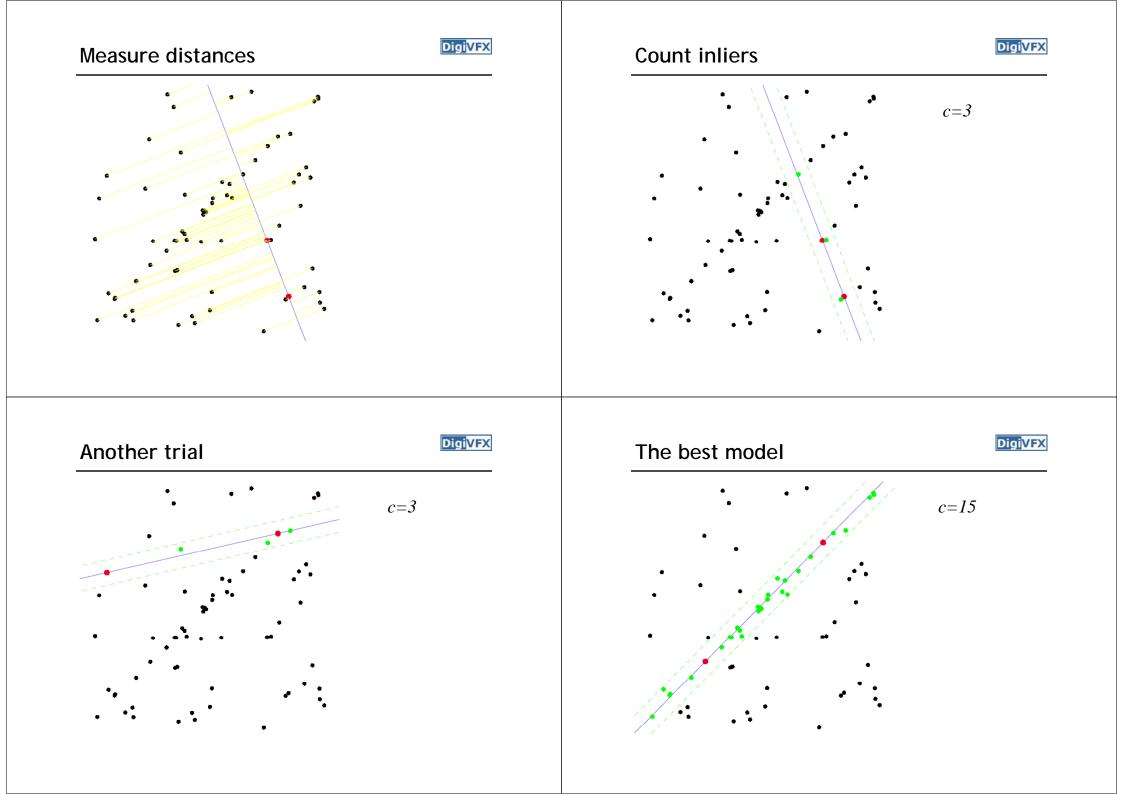




Model fitting

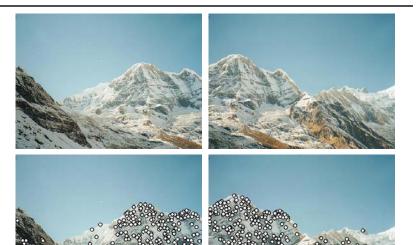






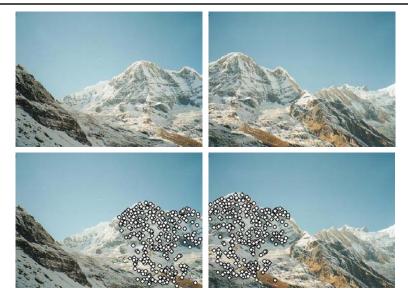
RANSAC for Homography





RANSAC for Homography





RANSAC for Homography









Applications of panorama in VFX



- Background plates
- Image-based lighting

Troy (image-based lighting)





http://www.cgnetworks.com/story_custom.php?story_id=2195&page=4

Spiderman 2 (background plate)



