3D photography

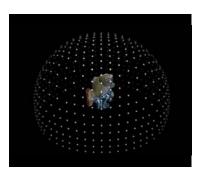
Digital Visual Effects, Spring 2009 Yung-Yu Chuang 2009/5/14

with slides by Szymon Rusinkiewicz, Richard Szeliski, Steve Seitz and Brian Curless

3D photography

Digi<mark>VFX</mark>

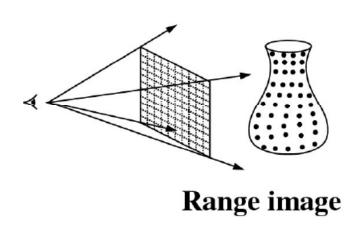
• Acquisition of geometry and material





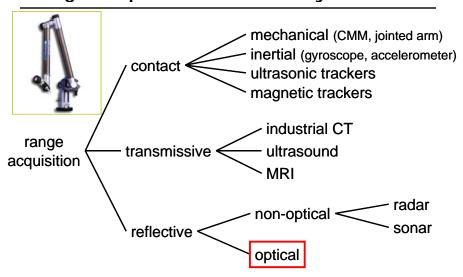
Range acquisition





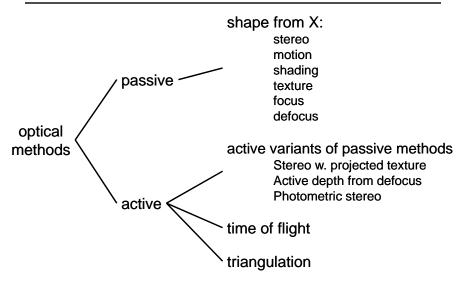
Range acquisition taxonomy





Range acquisition taxonomy









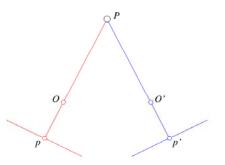
- Passive approaches
 - Stereo
 - Multiview approach
- Active approaches
 - Triangulation
 - Shadow scanning
- Active variants of passive approaches
 - Photometric stereo
 - Example-based photometric stereo

Passive approaches



Stereo

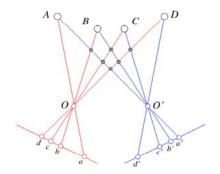
- **Digi**VFX
- One distinguishable point being observed
 - The preimage can be found at the intersection of the rays from the focal points to the image points



Stereo



- Many points being observed
 - Need some method to establish correspondences



Components of stereo vision systems



- Camera calibration
- Image rectification: simplifies the search for correspondences
- Correspondence: which item in the left image corresponds to which item in the right image
- Reconstruction: recovers 3-D information from the 2-D correspondences

Epipolar geometry



- Epipolar constraint: corresponding points must lie on conjugate epipolar lines
 - Search for correspondences becomes a 1-D problem

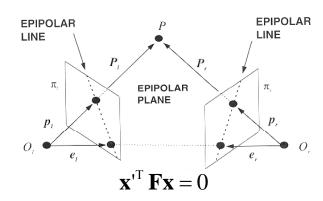
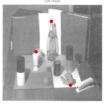
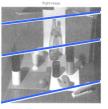


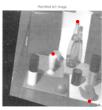
Image rectification

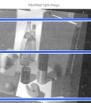


 Warp images such that conjugate epipolar lines become collinear and parallel to u axis









Disparity

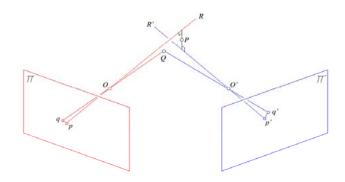


- With rectified images, disparity is just (horizontal) displacement of corresponding features in the two images
 - Disparity = 0 for distant points
 - Larger disparity for closer points
 - Depth of point proportional to 1/disparity

Reconstruction

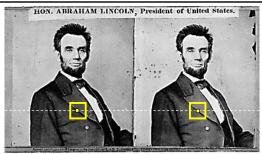


- Geometric
 - Construct the line segment perpendicular to R and R' that intersects both rays and take its mid-point



Basic stereo algorithm





For each epipolar line

For each pixel in the left image

- compare with every pixel on same epipolar line in right image
- · pick pixel with minimum match cost

Improvement: match windows

Basic stereo algorithm

DigiVFX

- For each pixel
 - For each disparity
 - For each pixel in window
 - Compute difference
 - Find disparity with minimum SSD

Reverse order of loops

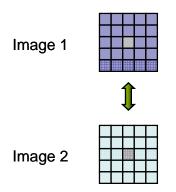


- For each disparity
 - For each pixel
 - For each pixel in window
 - Compute difference
- Find disparity with minimum SSD at each pixel

Incremental computation



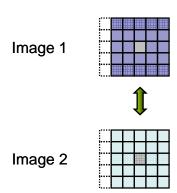
• Given SSD of a window, at some disparity



Incremental computation



Want: SSD at next location



Incremental computation



• Subtract contributions from leftmost column, add contributions from rightmost column

Image 1



Image 2



Selecting window size



- Small window: more detail, but more noise
- · Large window: more robustness, less detail
- Example:

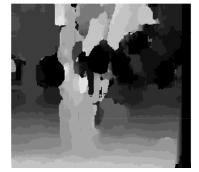




Selecting window size







3 pixel window

20 pixel window

Non-square windows



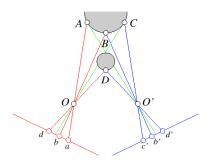
- Compromise: have a large window, but higher weight near the center
- Example: Gaussian
- Example: Shifted windows





Ordering constraint

- **Digi**VFX
- Order of matching features usually the same in both images
- But not always: occlusion



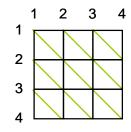
Dynamic programming

Digi<mark>VFX</mark>

• Treat feature correspondence as graph problem

Right image features

Left image features



Cost of edges = similarity of regions between image features

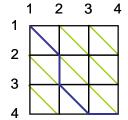
Dynamic programming



• Find min-cost path through graph

Right image features

Left image features



Energy minimization



- Another approach to improve quality of correspondences
- Assumption: disparities vary (mostly) smoothly
- Minimize energy function:

$$E_{data} + \lambda E_{smoothness}$$

- \bullet $\ensuremath{\text{E}_{\text{data}}}\xspace$ how well does disparity match data
- E_{smoothness}: how well does disparity match that of neighbors regularization

Energy minimization



- If data and energy terms are nice (continuous, smooth, etc.) can try to minimize via gradient descent, etc.
- In practice, disparities only piecewise smooth
- Design smoothness function that doesn't penalize large jumps too much
 - Example: $V(\alpha,\beta)=\min(|\alpha-\beta|, K)$



Matching Cost Formulated as Energy

Stereo as energy minimization

- "data" term penalizing bad matches

$$D(x, y, d) = |\mathbf{I}(x, y) - \mathbf{J}(x + d, y)|$$

- "neighborhood term" encouraging spatial smoothness

$$V(d_1, d_2)$$
 = cost of adjacent pixels with labels d1 and d2
= $\left| d_1 - d_2 \right|$ (or something similar)

$$E = \sum_{(x,y)} D(x, y, d_{x,y}) + \sum_{\text{neighbors } (x1,y1), (x2,y2)} V(d_{x1,y1}, d_{x2,y2})$$

Energy minimization



- Hard to find global minima of non-smooth functions
 - Many local minima
 - Provably NP-hard
- · Practical algorithms look for approximate minima (e.g., simulated annealing)

Stereo results



- Data from University of Tsukuba





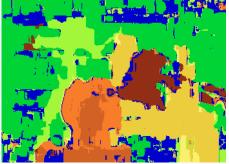
scene

ground truth

http://cat.middlebury.edu/stereo/

Results with window correlation







normalized correlation (best window size)

ground truth

Results with graph cuts







graph cuts
(Potts model *E*,
expansion move algorithm)

ground truth

Stereo evaluation





Stereo

Evaluation • Datasets • Code • Submit

Daniel Scharstein • Richard Szeliski

Welcome to the Middlebury Stereo Vision Page, formerly located at <u>www.middlebury.edu/stereo</u>. This website accompanies our taxonomy and comparison of two-frame stereo correspondence algorithms [1]. It contains:

- . An on-line evaluation of current algorithms
- Many <u>stereo datasets</u> with ground-truth disparities
- Our stereo correspondence software
- An on-line submission script that allows you to evaluate your stereo algorithm in our framework

How to cite the materials on this website:

We grant permission to use and publish all images and numerical results on this website. If you report performance results, we request that you cite our paper [1] instructions on how to cite our datasets are listed on the <u>datasets page</u>. If you want to cite this website, please use the URL "vision.middlebury.edu/stereor".

References

[1] D. Scharstein and R. Szeliski. <u>A taxonomy and evaluation of dense two-frame stereo correspondence algorithms.</u> International Journal of Computer Vision, 47(12/3):7-42, April-June 2002. <u>Microsoft Research Technical Report MSR-TR-2001-81</u>, November 2001.

Stereo—best algorithms



Error Threshold = 1 Error Threshold			Sort by	nonocc	Sort by all						Sort by disc		
			•	7						▼			
Algorithm	Avg.	Tsukuba ground truth			Venus ground truth			Teddy ground truth			Cones ground truth		
	Rank	nonocc	all	disc	nonocc	all	disc	nonocc	all	disc	nonocc	all	disc
AdaptingBP [17]	2.8	<u>1.11</u> 8	1.37 3	5.79 7	<u>0.10</u> 1	0.21 2	1.44 1	4.22 4	7.06 2	11.8 4	<u>2.48</u> 1	7.92 ₂	7.32
DoubleBP2 [35]	2.9	0.88 1	1.29 1	4.76 1	<u>0.13</u> 3	0.45 5	1.87 5	3.53 2	8.30 3	9.63 1	<u>2.90</u> 3	8.78 8	7.79
DoubleBP [15]	4.9	0.88 2	1.29 2	4.76 2	0.14 5	0.60 13	2.00 7	<u>3.55</u> 3	8.71 5	9.70 2	<u>2.90</u> 4	9.24 11	7.80
SubPixDoubleBP [30]	5.6	<u>1.24</u> 10	1.76 13	5.98 8	<u>0.12</u> 2	0.46 6	1.74 4	<u>3.45</u> 1	8.38 4	10.0 3	<u>2.93</u> 5	8.73 7	7.91
AdaptOvrSeqBP [33]	9.9	<u>1.69</u> 22	2.04 21	5.64 6	0.14 4	0.20 1	1.47 2	<u>7.04</u> 14	11.17	16.4 11	3.60 11	8.96 10	8.84 1
SymBP+occ [7]	10.8	<u>0.97</u> 4	1.75 12	5.09 4	<u>0.16</u> 6	0.33 3	2.19 8	<u>6.47</u> 8	10.7 e	17.0 14	<u>4.79</u> 24	10.7 21	10.9
PlaneFitBP [32]	10.8	<u>0.97</u> 5	1.83 14	5.26 5	0.17 7	0.51 8	1.71 3	<u>6.65</u> 9	12.1 13	14.7 7	<u>4.17</u> 20	10.7 20	10.6
AdaptDispCalib [36]	11.8	<u>1.19</u> 8	1.42 4	6.15 9	0.23 9	0.34 4	2.50 11	<u>7.80</u> 19	13.6 21	17.3 17	<u>3.62</u> 12	9.33 12	9.72 1
Segm+visib [4]	12.2	<u>1.30</u> 15	1.57 5	6.92 18	<u>0.79</u> 21	1.06 18	6.76 22	<u>5.00</u> 5	6.54 1	12.3 5	<u>3.72</u> 13	8.62 6	10.2 1
C-SemiGlob [19]	12.3	<u>2.61</u> 29	3.29 24	9.89 27	0.25 12	0.57 10	3.24 15	<u>5.14</u> 6	11.8 8	13.0 e	<u>2.77</u> 2	8.35 4	8.20
SO+borders [29]	12.8	1.29 14	1.71 9	6.83 15	0.25 13	0.53 9	2.26 9	7.02 13	12.2 14	16.3 s	3.90 15	9.85 16	10.2 1
DistinctSM [27]	14.1	<u>1.21</u> 9	1.75 11	6.39 11	0.35 14	0.69 18	2.63 13	<u>7.45</u> 18	13.0 17	18.1 19	3.91 16	9.91 18	8.32
CostAggr+occ [39]	14.3	1.38 17	1.96 17	7.14 19	0.44 18	1.13 19	4.87 19	6.80 11	11.9 10	17.3 16	3.60 10	8.57 5	9.36 1
OverSegmBP [26]	14.5	<u>1.69</u> 23	1.97 18	8.47 24	<u>0.51</u> 18	0.68 15	4.69 18	<u>6.74</u> 10	11.9 12	15.8 8	3.19 s	8.81 9	8.89
SegmentSupport [28]	15.1	1.25 11	1.62 7	6.68 13	0.25 11	0.64 14	2.59 12	8.43 24	14.2 22	18.2 20	3.77 14	9.87 17	9.77

Volumetric multiview approaches

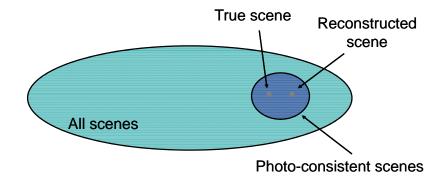


- Goal: find a model consistent with images
- "Model-centric" (vs. image-centric)
- Typically use discretized volume (voxel grid)
- For each voxel, compute occupied / free (for some algorithms, also color, etc.)

Photo consistency



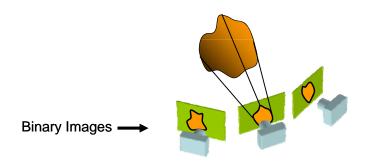
- Result: not necessarily the correct scene
- Many scenes produce the same images



Silhouette carving



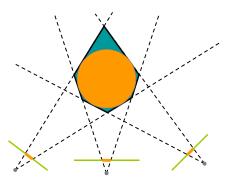
- Find silhouettes in all images
- Exact version:
 - Back-project all silhouettes, find intersection



Silhouette carving



- Find silhouettes in all images
- Exact version:
 - Back-project all silhouettes, find intersection



Silhouette carving



- Limit of silhouette carving is visual hull or line hull
- Complement of lines that don't intersect object
- In general not the same as object
 - Can't recover "pits" in object
- Not the same as convex hull

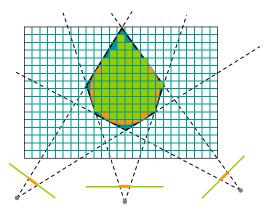
Silhouette carving



- Discrete version:
 - Loop over all voxels in some volume
 - If projection into images lies inside all silhouettes, mark as occupied
 - Else mark as free

Silhouette carving





Voxel coloring



- Seitz and Dyer, 1997
- In addition to free / occupied, store color at each voxel
- Explicitly accounts for occlusion

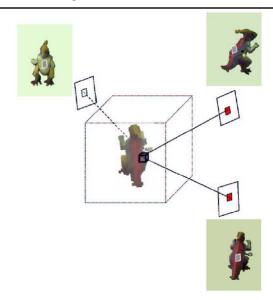
Voxel coloring



- · Basic idea: sweep through a voxel grid
 - Project each voxel into each image in which it is visible
 - If colors in images agree, mark voxel with color
 - Else, mark voxel as empty
- Agreement of colors based on comparing standard deviation of colors to threshold

Voxel coloring and occlusion





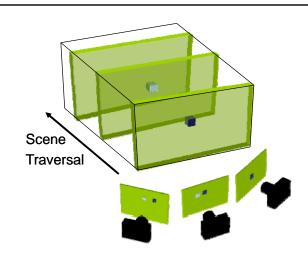
Voxel coloring and occlusion



- Problem: which voxels are visible?
- Solution: constrain camera views
 - When a voxel is considered, necessary occlusion information must be available
 - Sweep occluders before occludees
 - Constrain camera positions to allow this sweep

Voxel coloring sweep order



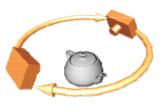


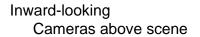
Voxel coloring camera positions





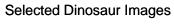








Outward-looking
Cameras inside scene



Selected Flower Images





•Calibrated Turntable

•360° rotation (21 images)

Seitz

Voxel coloring results



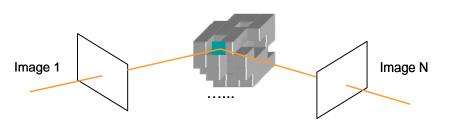


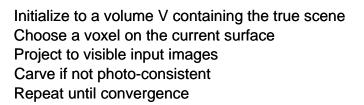
Dinosaur Reconstruction 72 K voxels colored 7.6 M voxels tested 7 min. to compute on a 250MHz SGI



Flower Reconstruction 70 K voxels colored 7.6 M voxels tested 7 min. to compute on a 250MHz SGI

Space carving







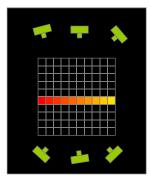
Multi-pass plane sweep

DigiVFX

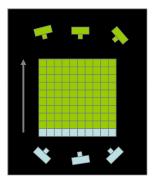
Multi-pass plane sweep

Digi<mark>VFX</mark>

- Faster alternative:
 - Sweep plane in each of 6 principal directions
 - Consider cameras on only one side of plane
 - Repeat until convergence







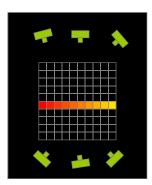
Reconstruction

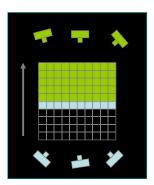
Multi-pass plane sweep

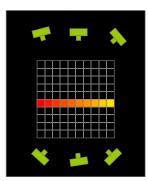


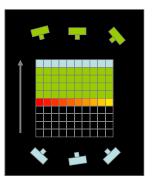




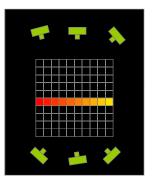


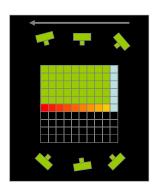


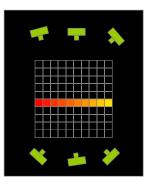


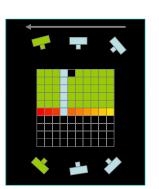








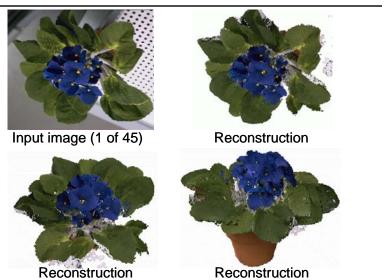




Space carving results: African violet

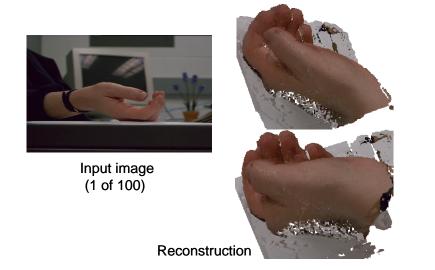


DigiVFX



Space carving results: hand





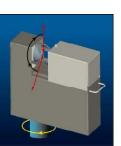
Time of flight



 Basic idea: send out pulse of light (usually laser), time how long it takes to return

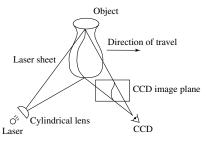
$$r = \frac{1}{2}c\Delta t$$





Laser scanning (triangulation)







Digital Michelangelo Project http://graphics.stanford.edu/projects/mich/

- Optical triangulation
 - Project a single stripe of laser light
 - Scan it across the surface of the object
 - This is a very precise version of structured light scanning

Active approaches

• Other patterns are possible

Cyberware



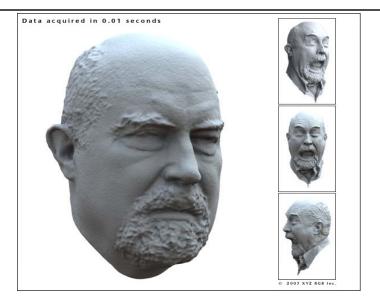
face and hand

full body



XYZRGB





XYZRGB

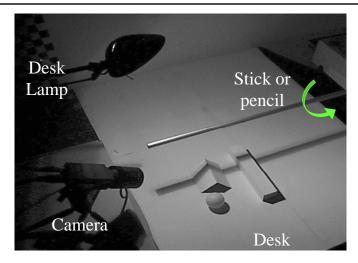


DigiVFX



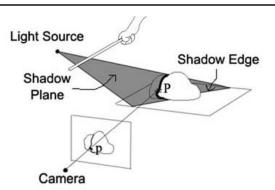
Shadow scanning





http://www.vision.caltech.edu/bouguetj/ICCV98/

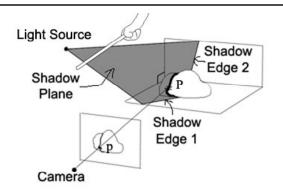
Basic idea



- Calibration issues:
 - where's the camera wrt. ground plane?
 - where's the shadow plane?
 - depends on light source position, shadow edge

Two Plane Version

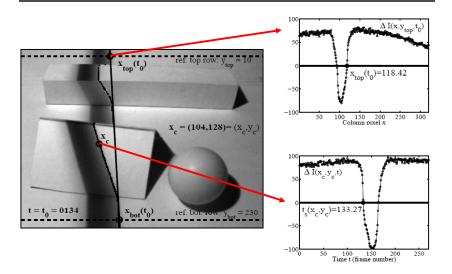




- Advantages
 - don't need to pre-calibrate the light source
 - shadow plane determined from two shadow edges

Estimating shadow lines





Shadow scanning in action





Results





accuracy: 0.1mm over 10cm - ~ 0.1% error

Textured objects



Scanning with the sun











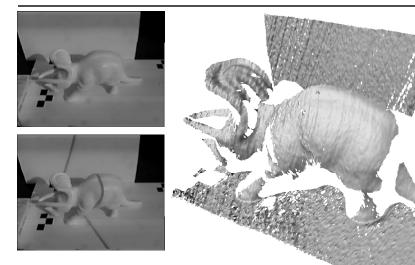










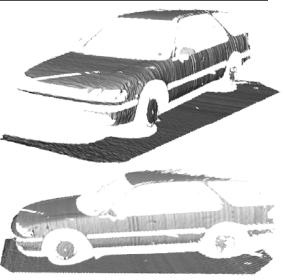


accuracy: 1mm over 50cm ~ 0.5% error

Scanning with the sun





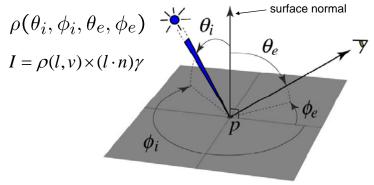


Active variants of passive approaches

The BRDF

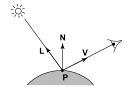


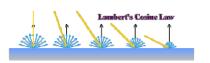
- · The Bidirectional Reflection Distribution Function
 - Given an incoming ray (θ_i, ϕ_i) and outgoing ray (θ_e, ϕ_e) what proportion of the incoming light is reflected along outgoing ray?



Diffuse reflection (Lambertian)





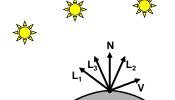


$$ho(l,v)=k_d$$
 albedo
$$I=k_d\mathbf{N}\cdot\mathbf{L}$$

Assuming that light strength is 1.

Photometric stereo







$$I_1 = k_d \mathbf{N} \cdot \mathbf{L}_1$$

$$I_2 = k_d \mathbf{N} \cdot \mathbf{L}_2$$

$$I_3 = k_d \mathbf{N} \cdot \mathbf{L}_3$$

• Can write this as a matrix equation:

$$\begin{bmatrix} I_1 \\ I_2 \\ I_3 \end{bmatrix} = k_d \begin{bmatrix} \mathbf{L_1}^T \\ \mathbf{L_2}^T \\ \mathbf{L_3}^T \end{bmatrix} \mathbf{N}$$

Solving the equations



$$\begin{bmatrix} I_1 \\ I_2 \\ I_3 \end{bmatrix} = \begin{bmatrix} \mathbf{L_1}^T \\ \mathbf{L_2}^T \\ \mathbf{L_3}^T \end{bmatrix} k_d \mathbf{N}$$

$$\mathbf{I} \quad \mathbf{L} \quad \mathbf{G}$$

$$\mathbf{3} \times \mathbf{1} \quad \mathbf{G}$$

$$\mathbf{3} \times \mathbf{3} \quad \mathbf{3} \times \mathbf{1}$$

$$\mathbf{G} = \mathbf{L}^{-1}\mathbf{I}$$
$$k_d = \|\mathbf{G}\|$$

$$\mathbf{N} = \frac{1}{k_d}\mathbf{G}$$

More than three lights



• Get better results by using more lights

$$\begin{bmatrix} I_1 \\ \vdots \\ I_n \end{bmatrix} = \begin{bmatrix} \mathbf{L_1} \\ \vdots \\ \mathbf{L_n} \end{bmatrix} k_d \mathbf{N}$$

• Least squares solution:

$$I = LG$$

$$L^{T}I = L^{T}LG$$

$$G = (L^{T}L)^{-1}(L^{T}I)$$

Solve for N, k_d as before

Trick for handling shadows



• Weight each equation by the pixel brightness:

$$I_i(I_i) = I_i[k_d \mathbf{N} \cdot \mathbf{L_i}]$$

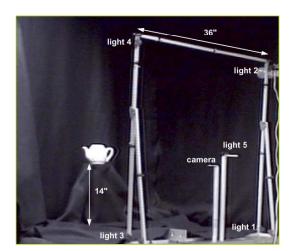
• Gives weighted least-squares matrix equation:

$$\begin{bmatrix} I_1^2 \\ \vdots \\ I_n^2 \end{bmatrix} = \begin{bmatrix} I_1 \mathbf{L}_1^T \\ \vdots \\ I_n \mathbf{L}_n^T \end{bmatrix} k_d \mathbf{N}$$

• Solve for N, k_d as before

Photometric Stereo Setup





Procedure

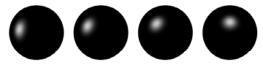


- Calibrate camera
- Calibrate light directions/intensities
- Photographing objects (HDR recommended)
- Estimate normals
- · Estimate depth

Estimating light directions

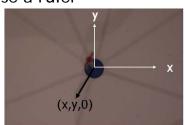
DigiVFX

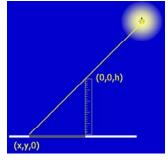
• Trick: place a chrome sphere in the scene



- the location of the highlight tells you where the light source is

Use a ruler





Photographing objects









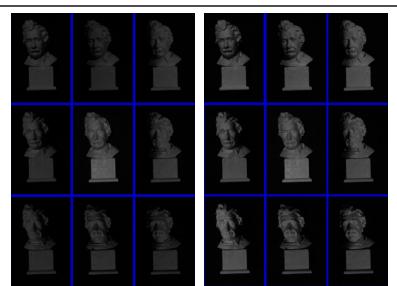






Normalize light intensities





Estimate normals





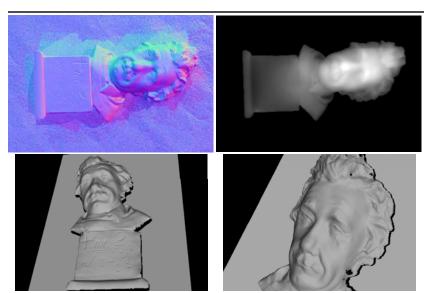
Depth from normals



$$\begin{aligned} &(n_x, n_y, n_z) = (\frac{\partial z}{\partial x}, \frac{\partial z}{\partial y}, -1) = (p, q, -1) \\ &E = E_{data} + E_{smooth} + E_{cons} \\ &= \sum_{i,j} w_{data} * \left[\left(\frac{\partial z(i,j)}{\partial x} - p_{ij} \right)^2 + \left(\frac{\partial z(i,j)}{\partial y} - q_{ij} \right)^2 \right] \\ &+ \sum_{i,j} w_{smooth} * \left[\left(\frac{\partial^2 z(i,j)}{\partial x^2} \right)^2 + 2 \left(\frac{\partial^2 z(i,j)}{\partial x \partial y} \right)^2 + \left(\frac{\partial^2 z(i,j)}{\partial y^2} \right)^2 \right] \\ &+ \sum_{(i,j) \in Cons} w_{cons} * \left(z(i,j) - c_{ij} \right)^2 \\ &E = \frac{1}{2} z^T A z - b^T z + c \quad \equiv \quad Az = b \end{aligned}$$

Results





Limitations

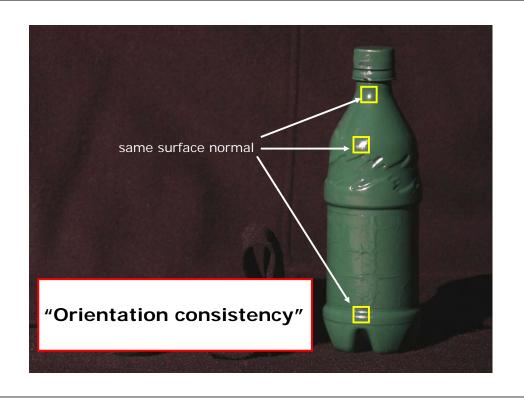


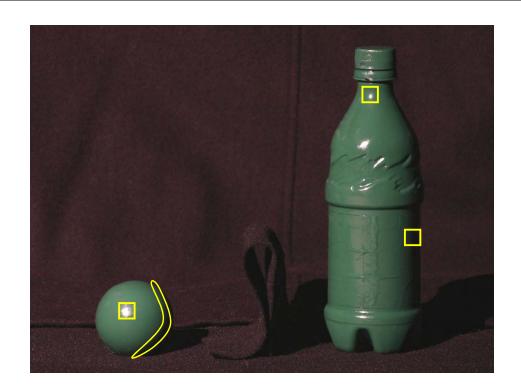
- Big problems
 - doesn't work for shiny things, semi-translucent things
 - shadows, inter-reflections
- Smaller problems
 - calibration requirements
 - measure light source directions, intensities
 - · camera response function

Example-based photometric stereo



- Estimate 3D shape by varying illumination, fixed camera
- Operating conditions
 - any opaque material
 - distant camera, lighting
 - reference object available
 - no shadows, interreflections, transparency











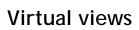


















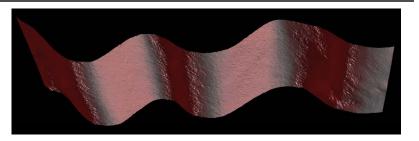


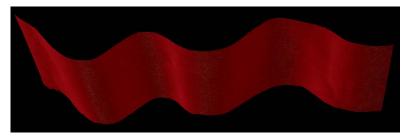


Virtual Views









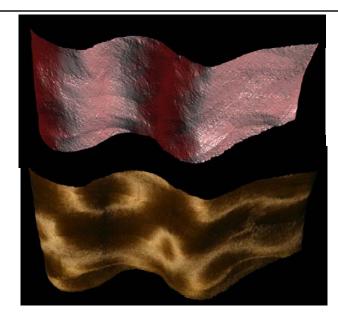
Brushed Fur



Virtual Views









Quality Control Phone & Fax Addresses E-mail Directory Methods of Payment

Salem Specialty Ball supplies industrial grade balls that are used in bearings, pumps, valves and other commercial applications. We can supply balls in just about any size that is machineable. We have produced precision balls from .002" all the way up to 12.0" and beyond. We can also produce these balls in any material. Almost without exception, if the material exists, we can make it into a ball. Not only do we specialize in hard to find materials, we also carry standard materials such as choose-steel and the steels. We stock an extensive impending or eady to ship balls. Most orders are shipped the same day. And if is isn't in stock, we can make it for you in matter of days. In addition, you will find that our prices are very commeditive.



Located in the beautiful northwest corner of Connecticut, Canton has been our company's home for the last three years and we have been in complete operation for over ten years. Proud of our reputation, Salem Specialty Ball Company has over fifty years of combined experience allowing us to provide topnotch quality technical support and expert engineering consultation



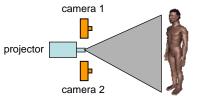
Active stereo with structured light

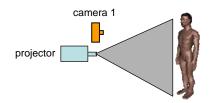






Li Zhang's one-shot stereo





- Project "structured" light patterns onto the object
 - simplifies the correspondence problem

Spacetime Stereo







http://grail.cs.washington.edu/projects/stfaces/

3D Model Acquisition Pipeline





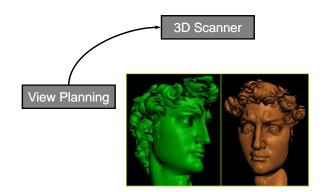


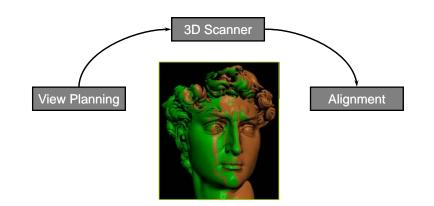
3D Model Acquisition Pipeline



3D Model Acquisition Pipeline

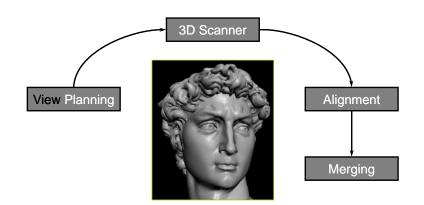






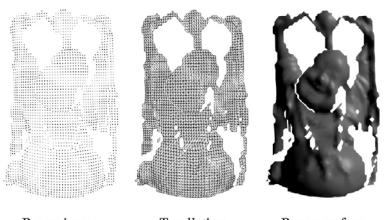
3D Model Acquisition Pipeline





Volumetric reconstruction





Range image

Tesellation

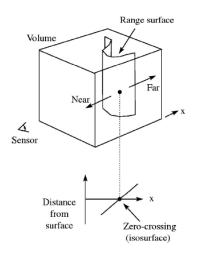
Range surface

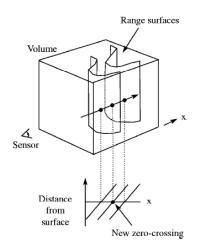
Signed distance function

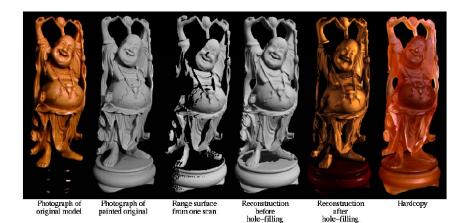












The Digital Michelangelo Project



- Goal: scan 10 sculptures by Michelangelo
- High-resolution ("quarter-millimeter") geometry
- Stanford University, led by Marc Levoy

Systems, projects and applications

Scanning the David







DigiVFX





height of gantry: 7.5 meters weight of gantry:

- steps
 - 1. manual initial alignment
 - 2. ICP to one existing scan
 - 3. automatic ICP of all overlapping pairs
 - 4. global relaxation to spread out error
 - 5. merging using volumetric method



Statistics about the scan





- 480 individually aimed scans
- 2 billion polygons
- 7,000 color images
- 32 gigabytes
- 30 nights of scanning
- 22 people

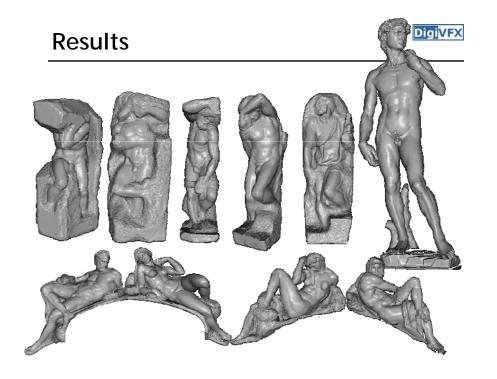
Comparison

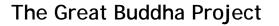






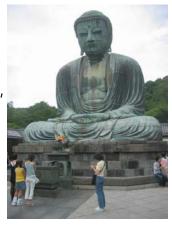
1.0 mm computer model







- Great Buddha of Kamakura
- Original made of wood, completed 1243
- Covered in bronze and gold leaf, 1267
- Approx. 15 m tall
- Goal: preservation of cultural heritage
- Institute of Industrial Science, University of Tokyo, led by Katsushi Ikeuchi



Scanner



Laser pulse time-of-flight

• Accuracy: 4 mm

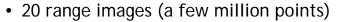
• Range: 100 m



DigiVFX



Processing



- · Simultaneous all-to-all ICP
- Variant of volumetric merging (parallelized)









Results







DigiVFX



- Hybrid camera for IMAX
- View interpolation



3D scanning





XYZRGB Inc.

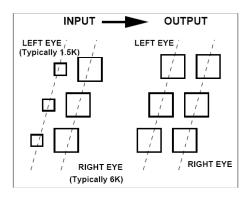
IMAX 3D



- For CG, it typically takes 6 hours for a frame
- 45-minute IMAX 3D CG film requires a 100-CPU rendering farm full-time for about a year just for rendering
- For live-action, camera is bulky (like a refrigerator)

Hybrid stereo camera

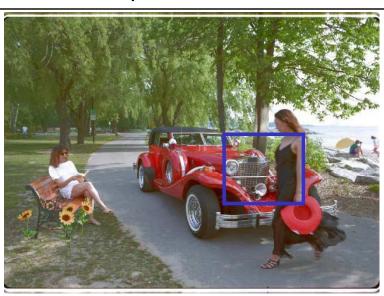




Live-action sequence



Digi<mark>VFX</mark>



Hybrid input

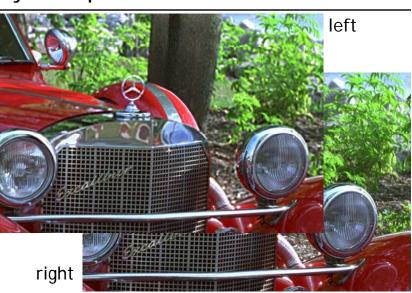




left

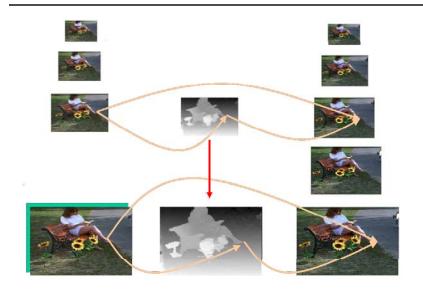


Hybrid input



Combine multiple hires to lores





Results





View interpolation





Bullet time video

View interpolation





High-quality video view interpolation

Final project

Final project



• Assigned: 5/14

• Due: ?

• Proposal by 5/27

Final project

- Research (1-2 people)
- System (1-3 people)
- Film (3-4 people)



Research



- Define a problem and try to solve it
- You don't need to solve it all, but have to make a reasonable progress, for example, solve a simplified version.
- Find inspirations from SIGGRAPH/CVPR/ICCV papers

System



 Implement existing algorithm into a useful system such as implementing recent SIGGRAPH or CVPR/ICCV papers

Film



- It must be an "effect" film.
- You can use any tools as you want. But, I assume that you have to write some on your own.
- Find inspirations from

Gatech's vfx course

 $\underline{\text{http://www.cc.gatech.edu/classes/AY2004/cs4480_spring/}}$

independent film makers

http://www.peerlessproductions.com/

ADs/films/YouTube

• Submit two videos, final and making-of.