Image stitching

Digital Visual Effects, Spring 2009 Yung-Yu Chuang 2009/3/26

with slides by Richard Szeliski, Steve Seitz, Matthew Brown and Vaclav Hlavac

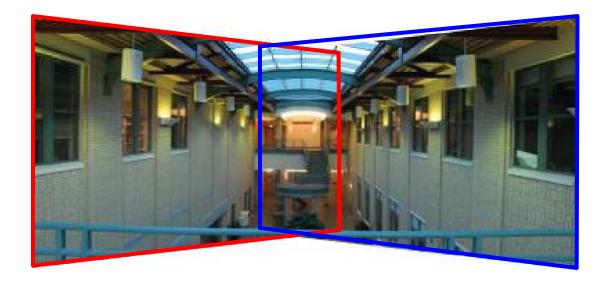




Stitching = alignment + blending
 geometrical photometric registration registration







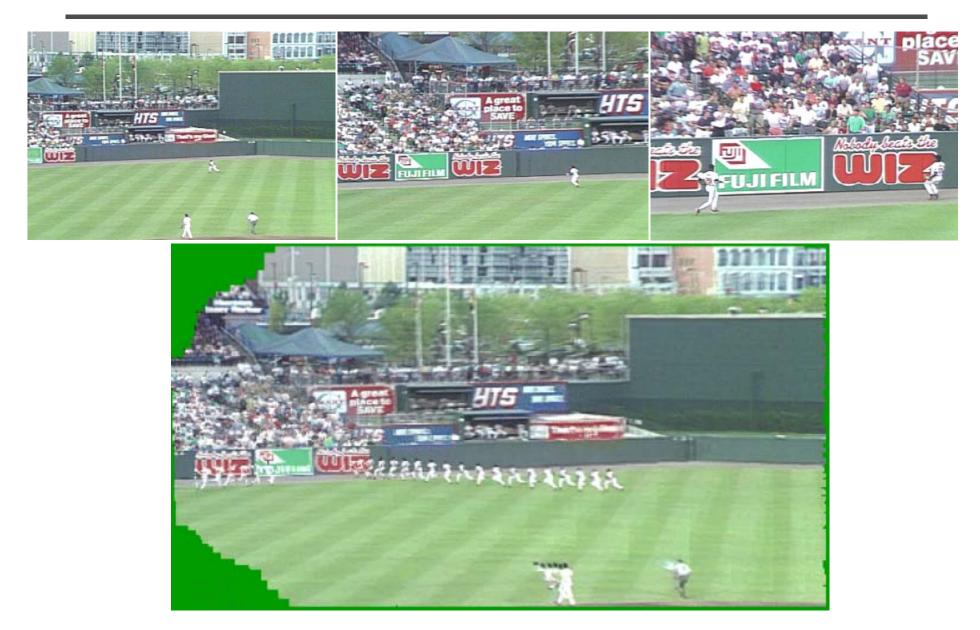


Applications of image stitching

- Video stabilization
- Video summarization
- Video compression
- Video matting
- Panorama creation

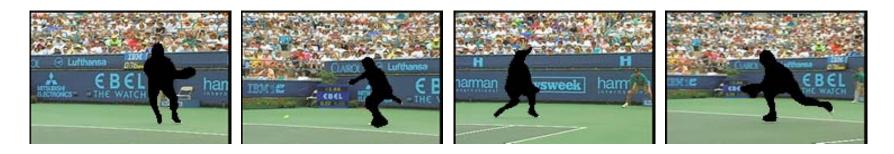


Video summarization





Video compression



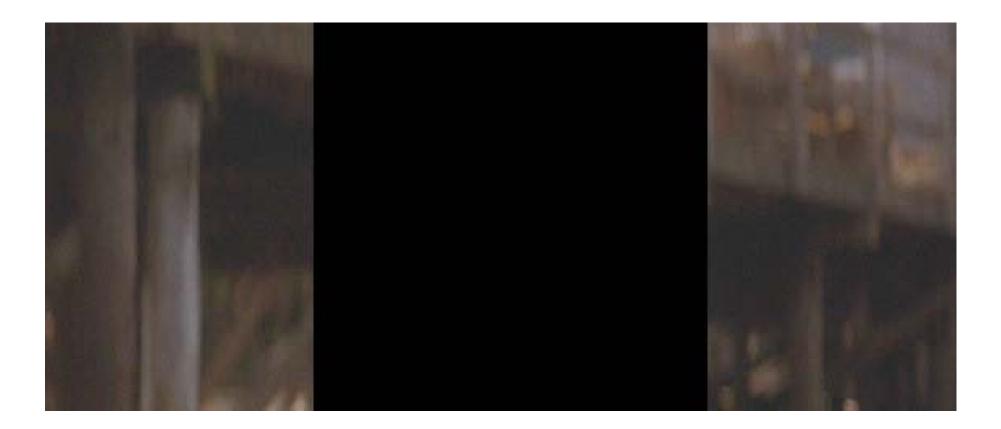






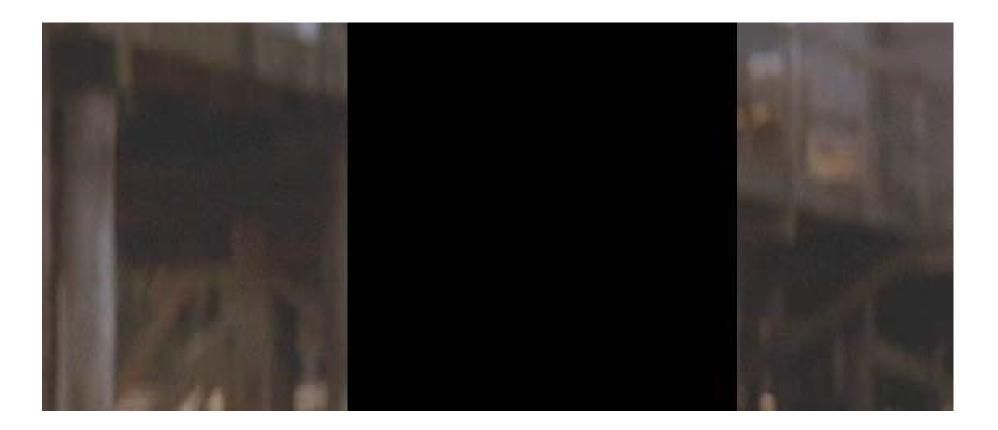
input video





remove foreground





estimate background





background estimation



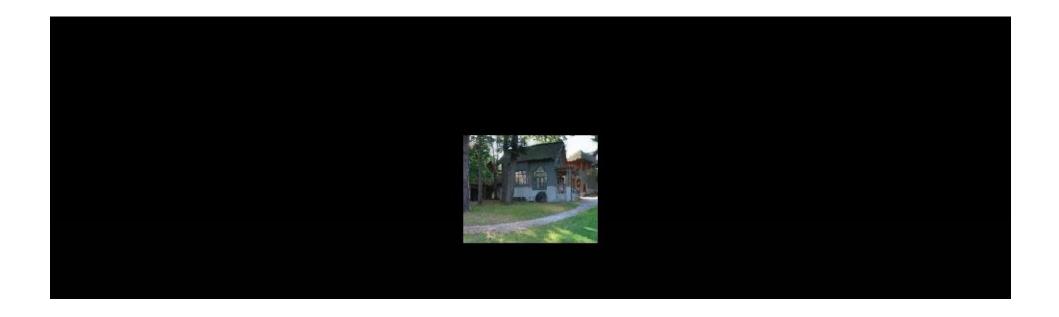
Panorama creation







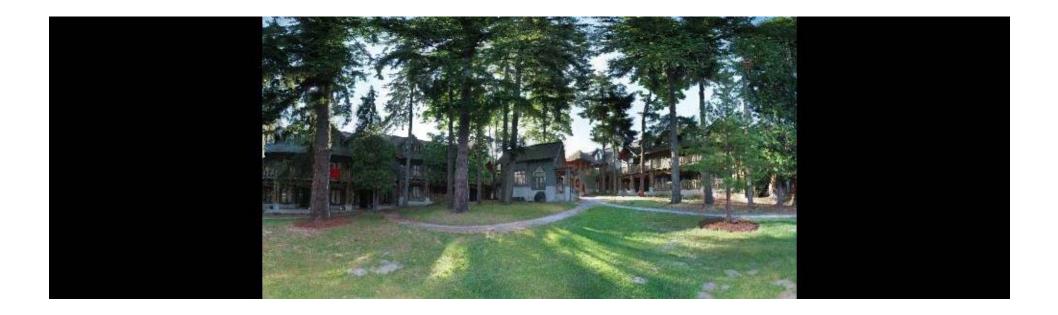
- Are you getting the whole picture?
 - Compact Camera FOV = 50 x 35°





Why panorama?

- Are you getting the whole picture?
 - Compact Camera FOV = 50 x 35°
 - Human FOV = $200 \times 135^{\circ}$





Why panorama?

- Are you getting the whole picture?
 - Compact Camera FOV = 50 x 35°
 - Human FOV = $200 \times 135^{\circ}$
 - Panoramic Mosaic = $360 \times 180^{\circ}$





- Like HDR, it is a topic of computational photography, seeking ways to build a better camera mostly in software.
- Most consumer cameras have a panorama mode
- Mars:

http://www.panoramas.dk/fullscreen3/f2_mars97.html

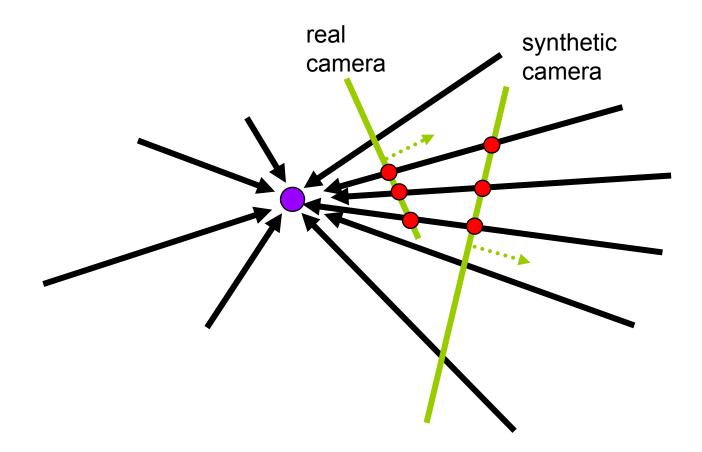
• Earth:

http://www.panoramas.dk/new-year-2006/taipei.html http://www.360cities.net/

- In image stitching, we seek for a matrix to globally warp one image into another. Are any two images of the same scene can be aligned this way?
 - Images captured with the same center of projection
 - A planar scene or far-away scene

A pencil of rays contains all views

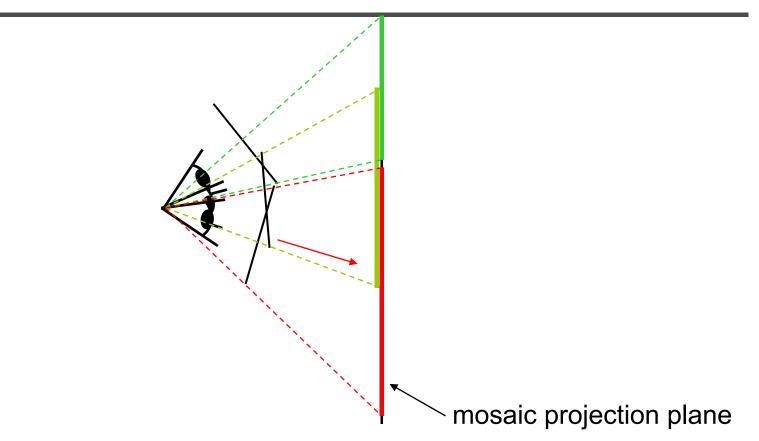




Can generate any synthetic camera view as long as it has **the same center of projection**!



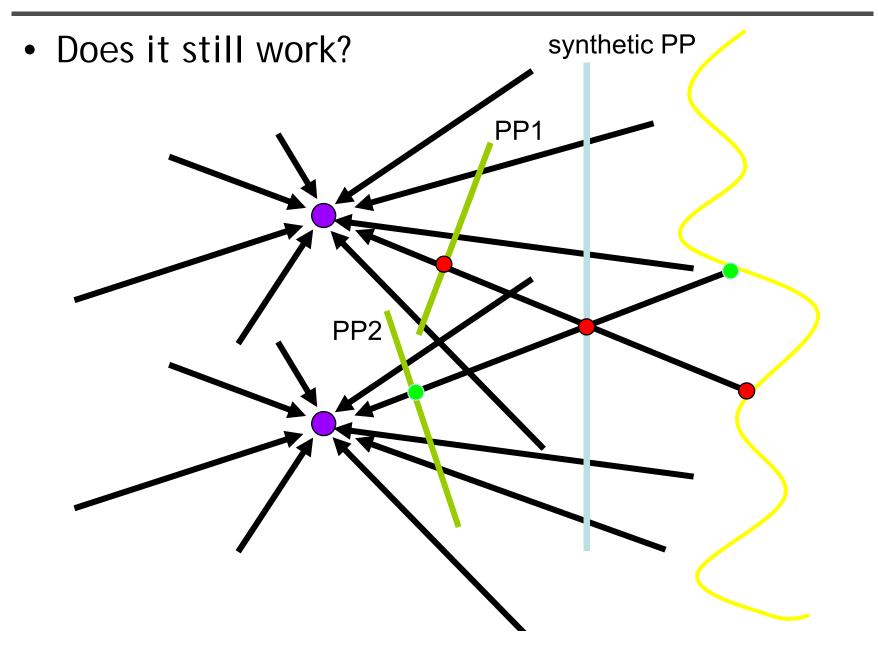
Mosaic as an image reprojection



- The images are reprojected onto a common plane
- The mosaic is formed on this plane
- Mosaic is a *synthetic wide-angle camera*

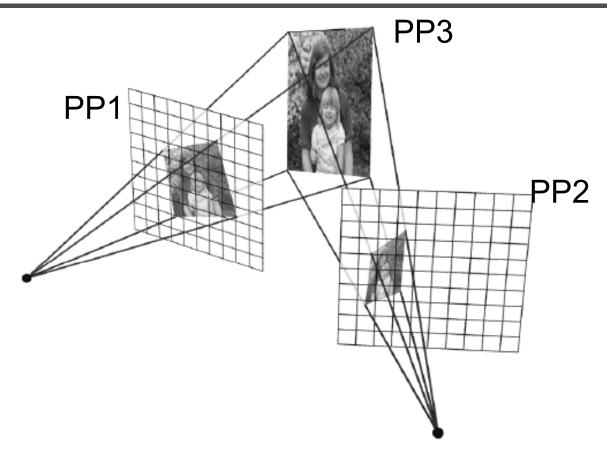
Changing camera center







Planar scene (or a faraway one)



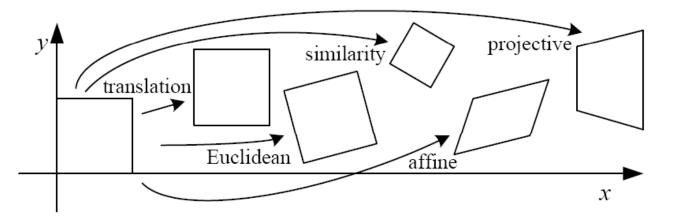
- PP3 is a projection plane of both centers of projection, so we are OK!
- This is how big aerial photographs are made



• Parametric models as the assumptions on the relation between two images.

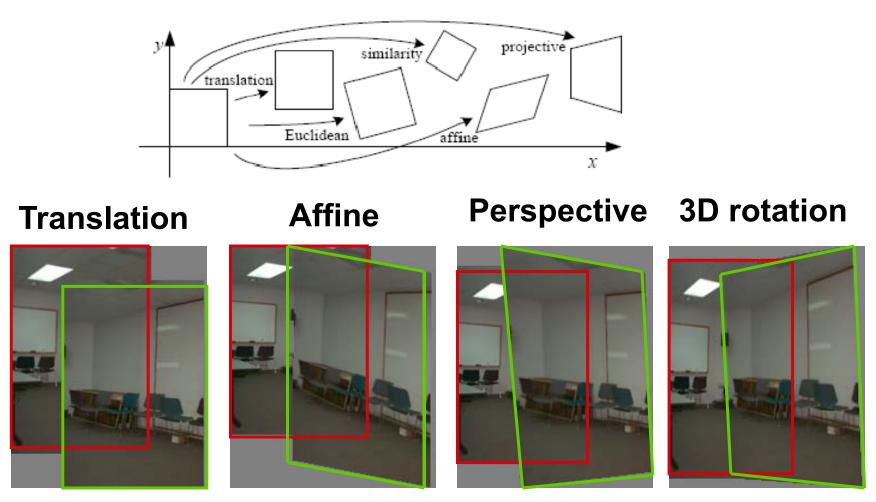


2D Motion models



Name	Matrix	# D.O.F.	Preserves:	Icon
translation	$igg[egin{array}{c c c c c c c c c c c c c c c c c c c $	2	orientation $+\cdots$	
rigid (Euclidean)	$\left[egin{array}{c c c c c c c c c c c c c c c c c c c $	3	lengths $+\cdots$	\bigcirc
similarity	$\left[\left. s oldsymbol{R} \right oldsymbol{t} ight]_{2 imes 3}$	4	angles $+ \cdots$	\bigcirc
affine	$\left[egin{array}{c} m{A} \end{array} ight]_{2 imes 3}$	6	parallelism $+\cdots$	
projective	$\left[egin{array}{c} ilde{H} \end{array} ight]_{3 imes 3}$	8	straight lines	



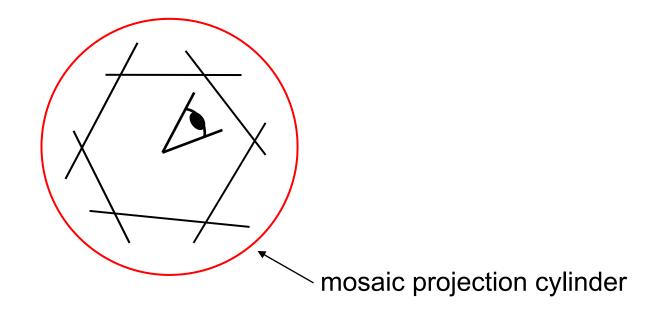


2 unknowns 6 unknowns 8 unknowns 3 unknowns

A case study: cylindrical panorama

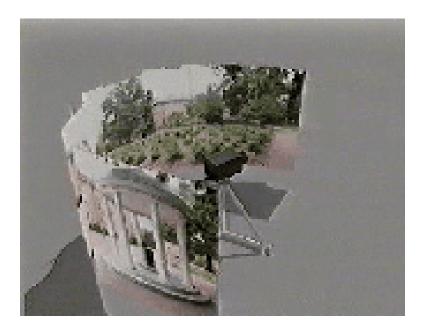


• What if you want a 360° field of view?





Cylindrical panoramas



- Steps
 - Reproject each image onto a cylinder
 - Blend
 - Output the resulting mosaic



- 1. Take pictures on a tripod (or handheld)
- 2. Warp to cylindrical coordinate
- 3. Compute pairwise alignments
- 4. Fix up the end-to-end alignment
- 5. Blending
- 6. Crop the result and import into a viewer

It is required to do radial distortion correction for better stitching results!



Taking pictures





Kaidan panoramic tripod head

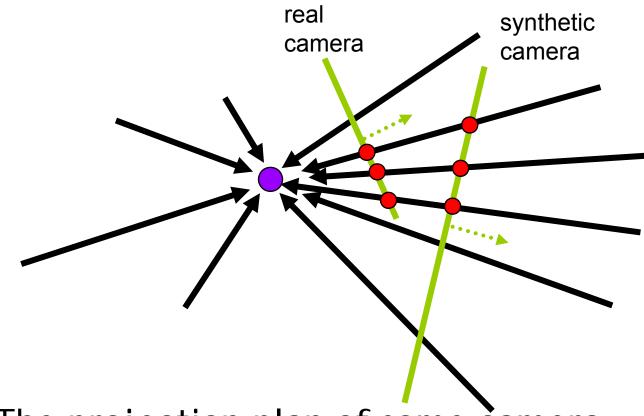


Translation model



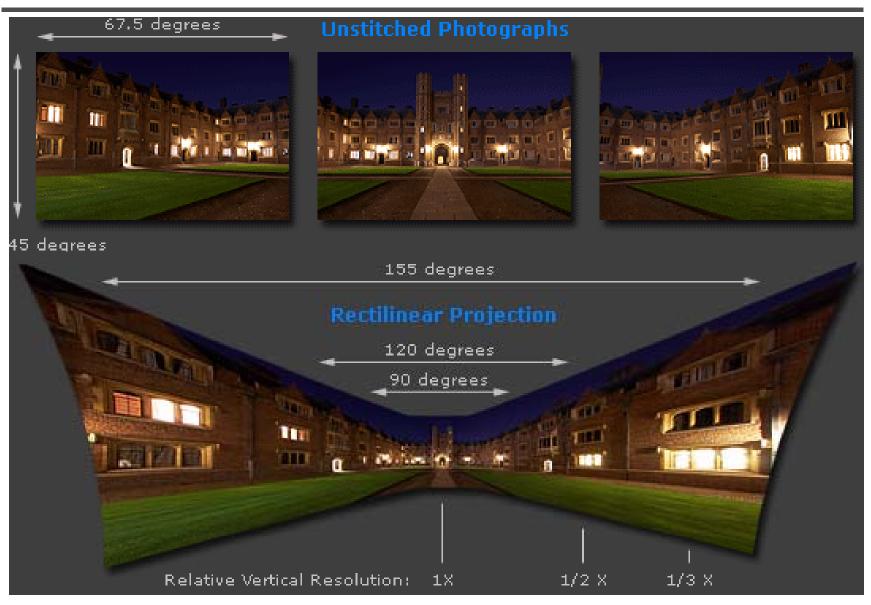
Try to align this in PaintShop Pro

Where should the synthetic camera be



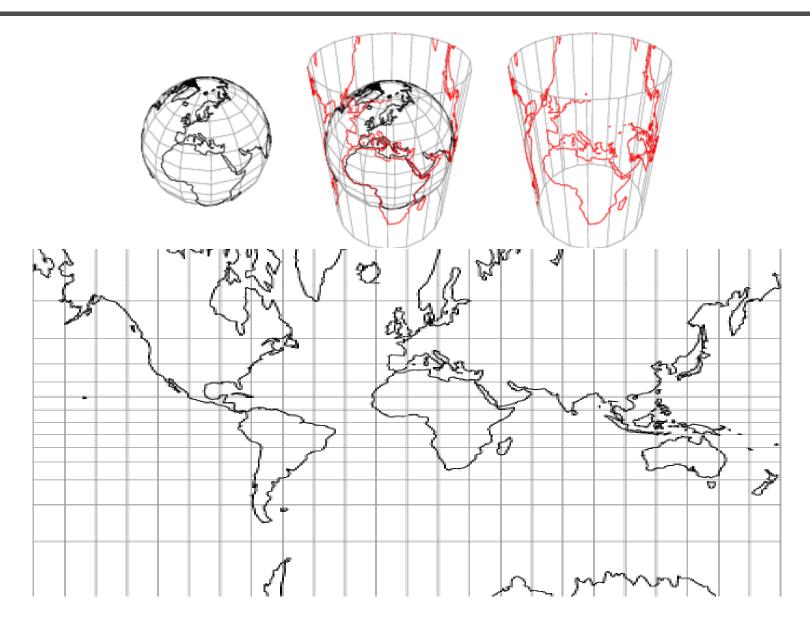
- The projection plan of some camera
- Onto a cylinder



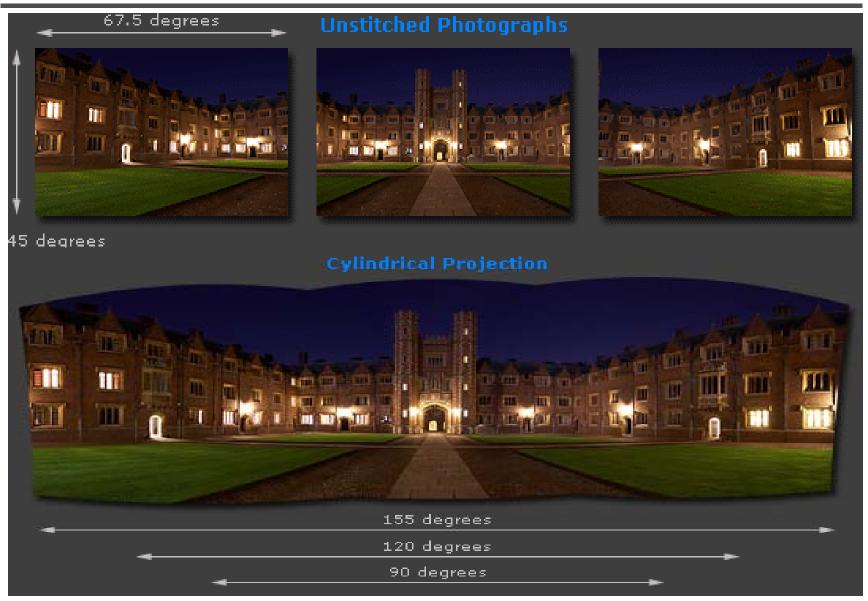


Adopted from http://www.cambridgeincolour.com/tutorials/image-projections.htm



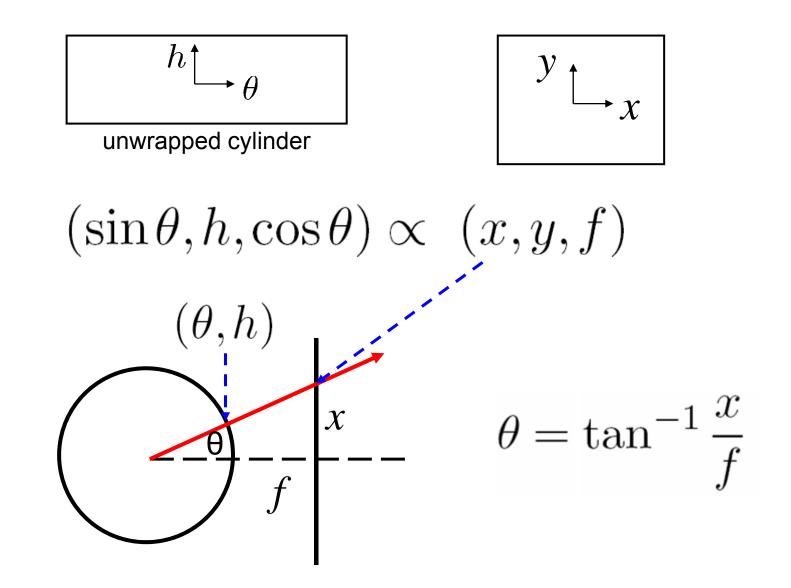




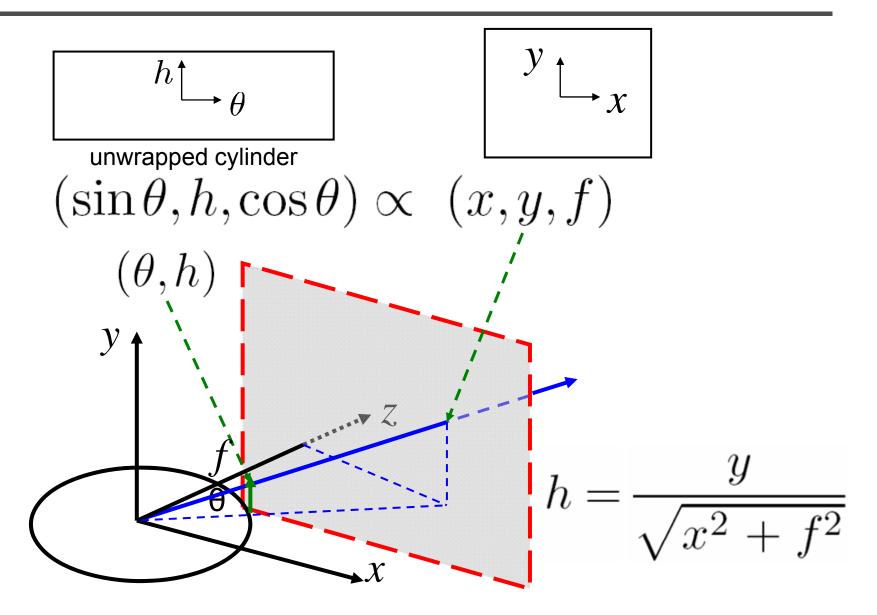


Adopted from http://www.cambridgeincolour.com/tutorials/image-projections.htm

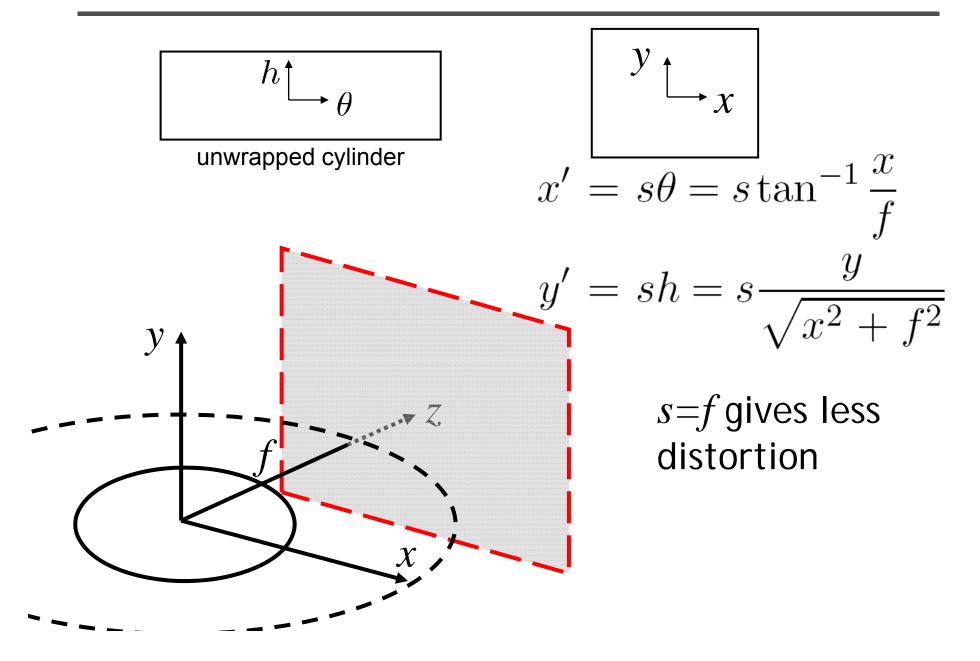














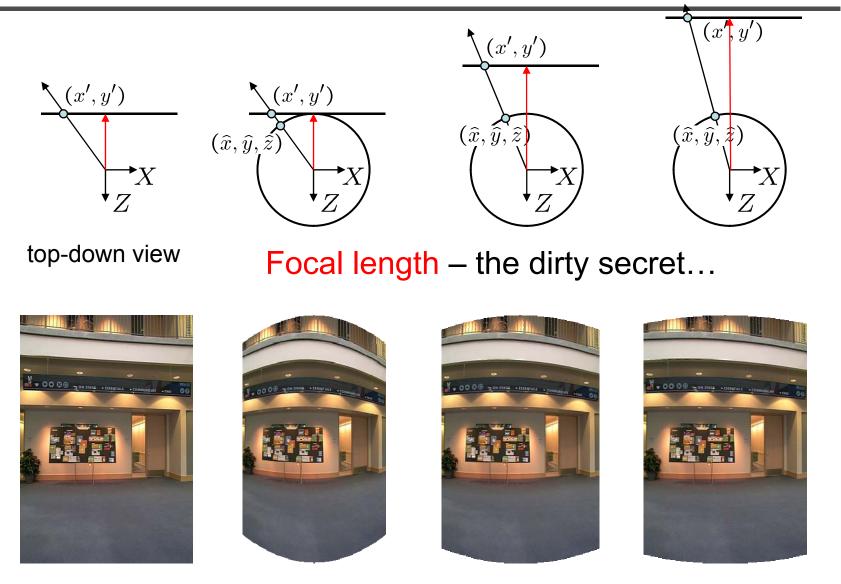


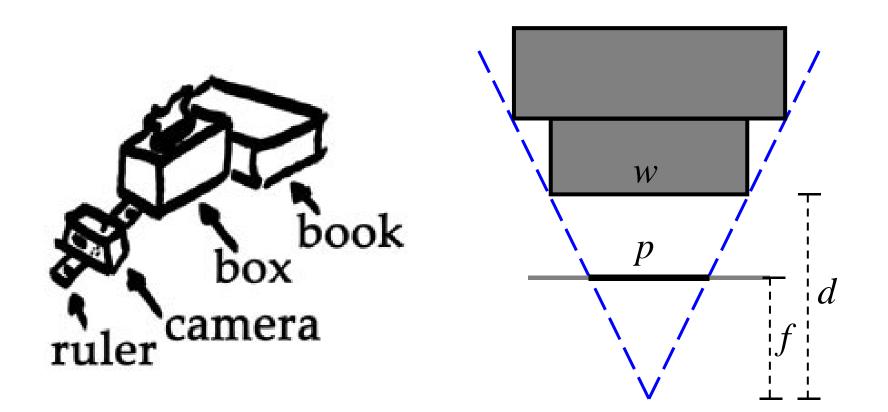
Image 384x300

f = 180 (pixels)

f = 280

f = 380





Or, you can use other software, such as AutoStich, to help.



Input images





Cylindrical warping

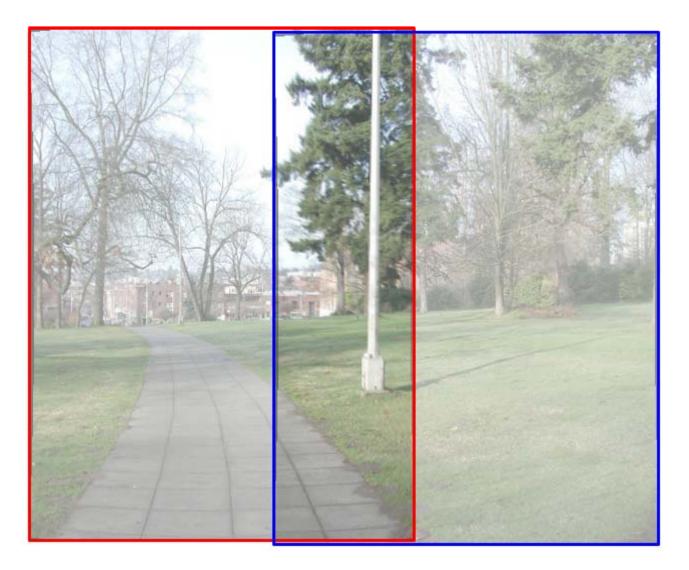




• Why blending: parallax, lens distortion, scene motion, exposure difference



Blending







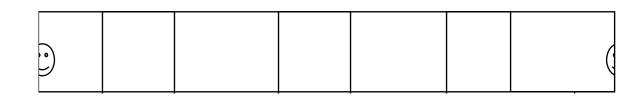


Blending



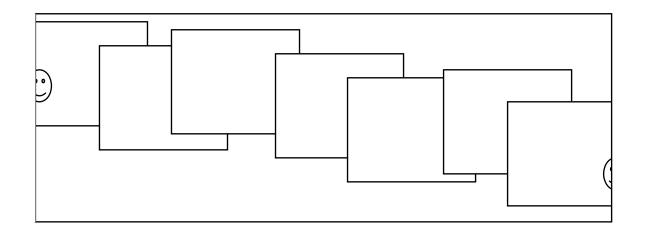
Assembling the panorama





• Stitch pairs together, blend, then crop

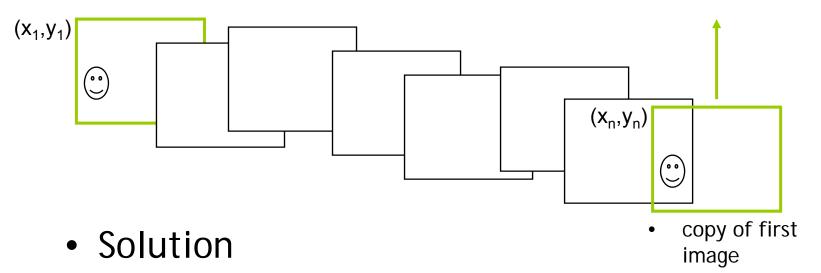




- Error accumulation
 - small errors accumulate over time



Problem: Drift



- add another copy of first image at the end
- there are a bunch of ways to solve this problem
 - add displacement of (y₁ y_n)/(n -1) to each image after the first
 - compute a global warp: y' = y + ax
 - run a big optimization problem, incorporating this constraint
 - best solution, but more complicated
 - known as "bundle adjustment"

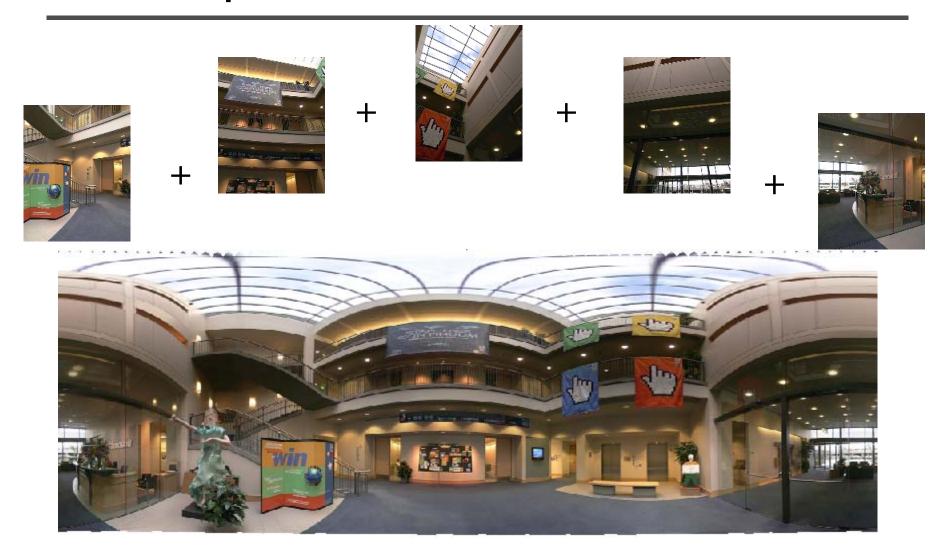








Viewer: panorama



example: http://www.cs.washington.edu/education/courses/cse590ss/01wi/projects/project1/students/dougz/index.html

Viewer: texture mapped model





example: http://www.panoramas.dk/

Cylindrical panorama



- 1. Take pictures on a tripod (or handheld)
- 2. Warp to cylindrical coordinate
- 3. Compute pairwise alignments
- 4. Fix up the end-to-end alignment
- 5. Blending
- 6. Crop the result and import into a viewer

Determine pairwise alignment?

- Feature-based methods: only use feature points to estimate parameters
- We will study the "Recognising panorama" paper published in ICCV 2003
- Run SIFT (or other feature algorithms) for each image, find feature matches.

Determine pairwise alignment

- p'=Mp, where M is a transformation matrix, p and p' are feature matches
- It is possible to use more complicated models such as affine or perspective
- For example, assume M is a 2x2 matrix

$$\begin{pmatrix} x' \\ y' \end{pmatrix} = \begin{pmatrix} m_{11} & m_{12} \\ m_{21} & m_{22} \end{pmatrix} \begin{pmatrix} x \\ y \end{pmatrix}$$

• Find M with the least square error

$$\sum_{i=1}^n (Mp - p')^2$$



Determine pairwise alignment

$$\begin{pmatrix} x' \\ y' \end{pmatrix} = \begin{pmatrix} m_{11} & m_{12} \\ m_{21} & m_{22} \end{pmatrix} \begin{pmatrix} x \\ y \end{pmatrix}$$

$$x_1 m_{11} + y_1 m_{12} = x_1$$

$$x_1 m_{21} + y_1 m_{22} = y_1$$

• Overdetermined system

$$\begin{pmatrix} x_1 & y_1 & 0 & 0 \\ 0 & 0 & x_1 & y_1 \\ x_2 & y_2 & 0 & 0 \\ \vdots & \vdots & \vdots & \vdots \\ x_n & y_n & 0 & 0 \\ 0 & 0 & x_n & y_n \end{pmatrix} \begin{pmatrix} m_{11} \\ m_{12} \\ m_{21} \\ m_{22} \end{pmatrix} = \begin{pmatrix} x_1 \\ y_1 \\ x_2 \\ \vdots \\ m_{21} \\ m_{22} \end{pmatrix}$$



Given an overdetermined system

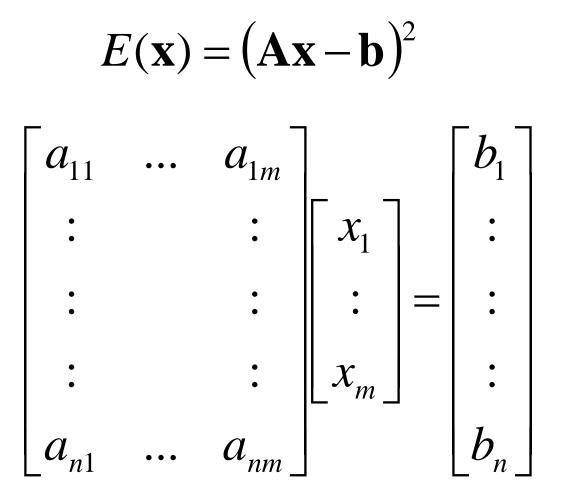
$\mathbf{A}\mathbf{x} = \mathbf{b}$

the normal equation is that which minimizes the sum of the square differences between left and right sides

$\mathbf{A}^{\mathrm{T}}\mathbf{A}\mathbf{x} = \mathbf{A}^{\mathrm{T}}\mathbf{b}$

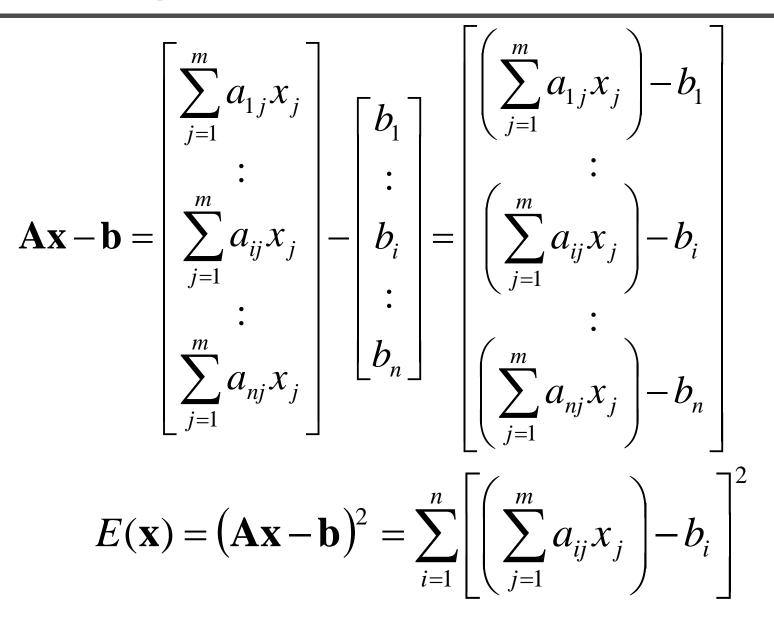
Why?





*n*X*m*, *n* equations, *m* variables







$$E(\mathbf{x}) = (\mathbf{A}\mathbf{x} - \mathbf{b})^2 = \sum_{i=1}^n \left[\left(\sum_{j=1}^m a_{ij} x_j \right) - b_i \right]^2$$
$$0 = \frac{\partial E}{\partial x_1} = \sum_{i=1}^n 2 \left[\left(\sum_{j=1}^m a_{ij} x_j \right) - b_i \right] a_{i1}$$
$$= 2 \sum_{i=1}^n a_{i1} \sum_{j=1}^m a_{ij} x_j - 2 \sum_{i=1}^n a_{i1} b_i$$

$$0 = \frac{\partial E}{\partial \mathbf{x}} = 2(\mathbf{A}^{\mathsf{T}}\mathbf{A}\mathbf{x} - \mathbf{A}^{\mathsf{T}}\mathbf{b}) \rightarrow \mathbf{A}^{\mathsf{T}}\mathbf{A}\mathbf{x} = \mathbf{A}^{\mathsf{T}}\mathbf{b}$$



$$(\mathbf{A}\mathbf{x} - \mathbf{b})^{2}$$

= $(\mathbf{A}\mathbf{x} - \mathbf{b})^{T} (\mathbf{A}\mathbf{x} - \mathbf{b})$
= $((\mathbf{A}\mathbf{x})^{T} - \mathbf{b}^{T})(\mathbf{A}\mathbf{x} - \mathbf{b})$
= $(\mathbf{x}^{T}\mathbf{A}^{T} - \mathbf{b}^{T})(\mathbf{A}\mathbf{x} - \mathbf{b})$
= $\mathbf{x}^{T}\mathbf{A}^{T}\mathbf{A}\mathbf{x} - \mathbf{b}^{T}\mathbf{A}\mathbf{x} - \mathbf{x}^{T}\mathbf{A}^{T}\mathbf{b} + \mathbf{b}^{T}\mathbf{b}$
= $\mathbf{x}^{T}\mathbf{A}^{T}\mathbf{A}\mathbf{x} - (\mathbf{A}^{T}\mathbf{b})^{T}\mathbf{x} - (\mathbf{A}^{T}\mathbf{b})^{T}\mathbf{x} + \mathbf{b}^{T}\mathbf{b}$
 $\frac{\partial E}{\partial \mathbf{x}} = 2\mathbf{A}^{T}\mathbf{A}\mathbf{x} - 2\mathbf{A}^{T}\mathbf{b}$



Determine pairwise alignment

- p'=Mp, where M is a transformation matrix, p and p' are feature matches
- For translation model, it is easier.

$$E = \sum_{i=1}^{n} \left[\left(m_1 + x_i - x_i^{'} \right)^2 + \left(m_2 + y_i - y_i^{'} \right)^2 \right]$$

$$0 = \frac{\partial E}{\partial m_1}$$

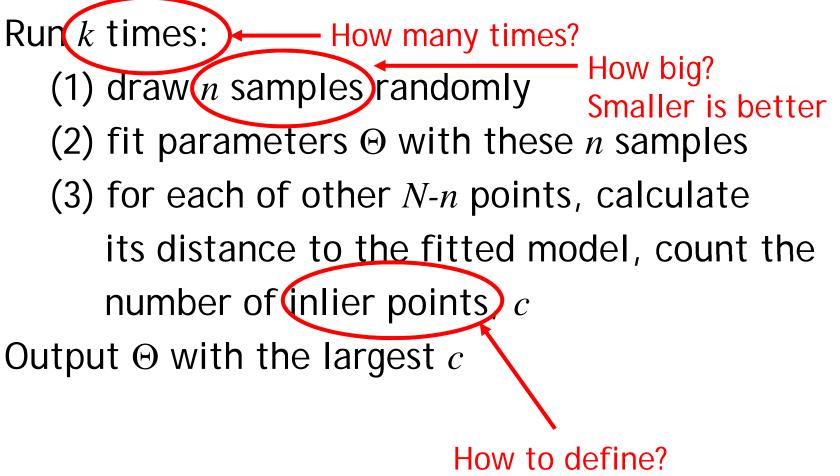
• What if the match is false? Avoid impact of outliers.



- RANSAC = Random Sample Consensus
- An algorithm for robust fitting of models in the presence of many data outliers
- Compare to robust statistics
- Given N data points x_i, assume that mjority of them are generated from a model with parameters Θ, try to recover Θ.



RANSAC algorithm



Depends on the problem.



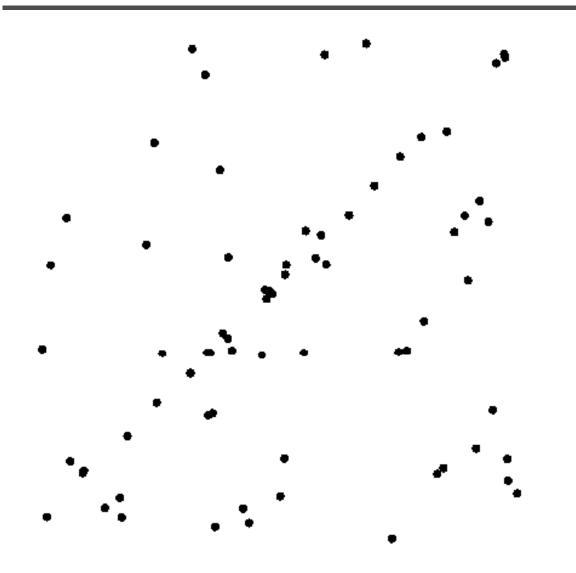
p: probability of real inliers

P: probability of success after k trials

$$P = 1 - (1 - p^{n})^{k}$$
n samples are all inliers
a failure
failure after k trials
$$k = \frac{\log(1 - P)}{\log(1 - p^{n})}$$
 for $P = 0.99$
$$\frac{n}{6} \frac{p}{0.5} \frac{k}{293}$$

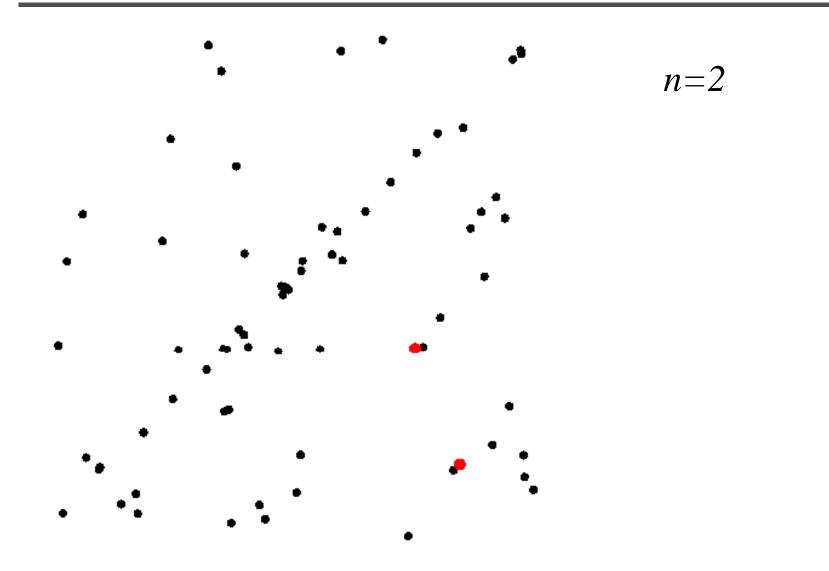


Example: line fitting



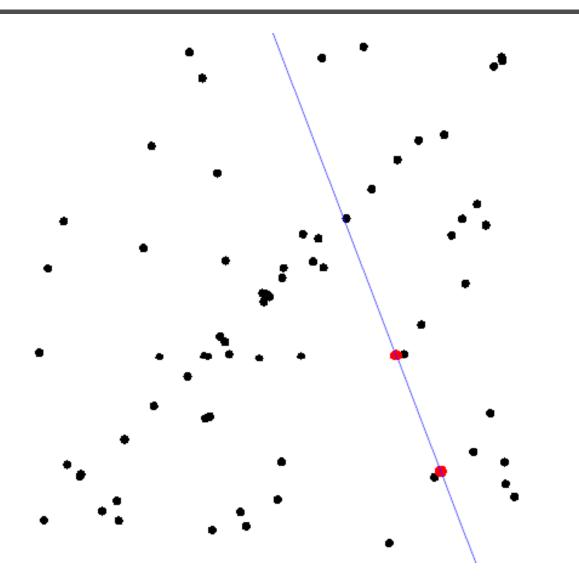
Example: line fitting





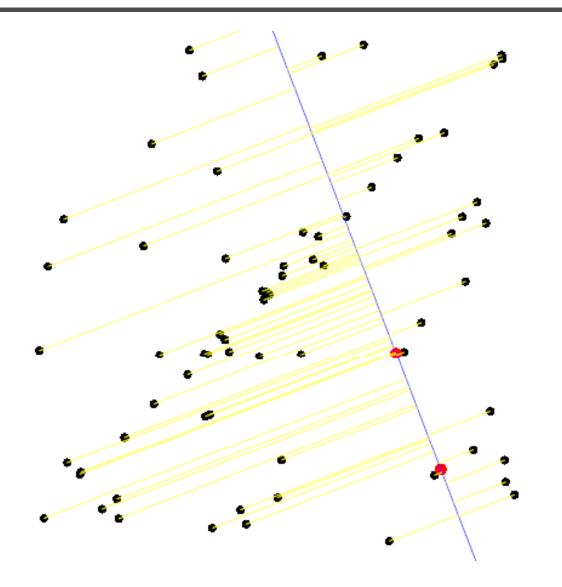


Model fitting



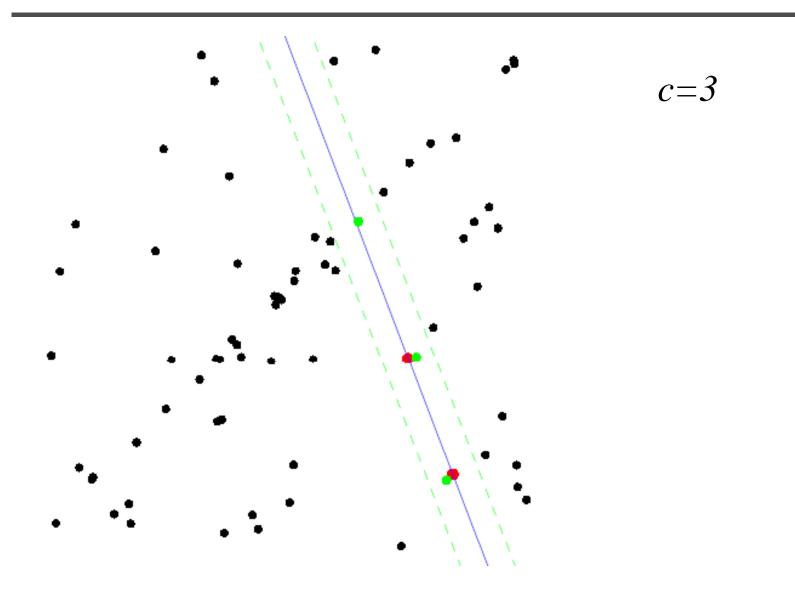


Measure distances



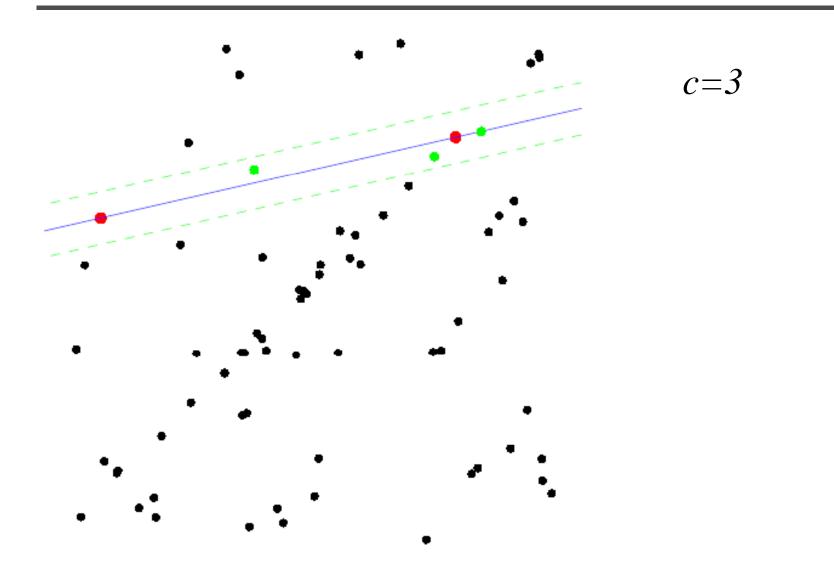


Count inliers



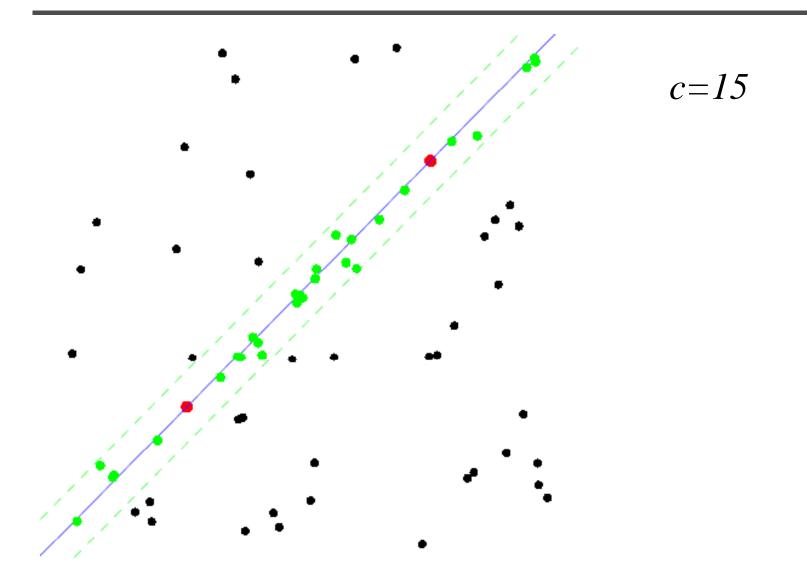


Another trial



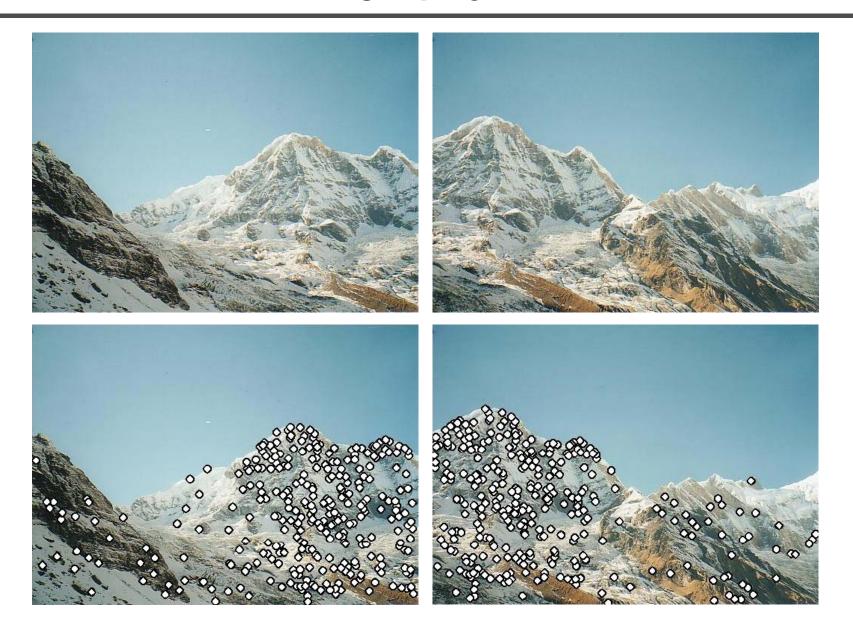


The best model



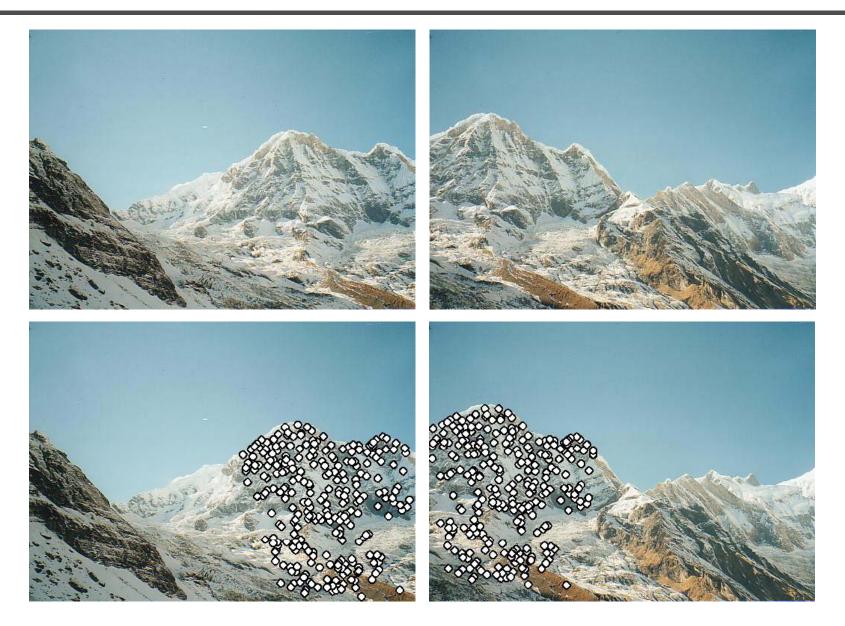
RANSAC for Homography





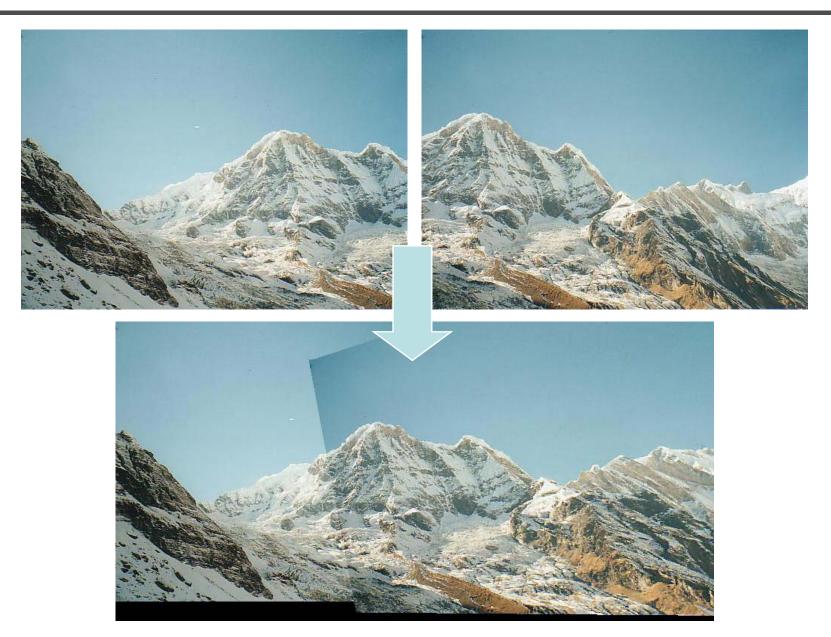
RANSAC for Homography





RANSAC for Homography







Applications of panorama in VFX

- Background plates
- Image-based lighting







http://www.cgnetworks.com/story_custom.php?story_id=2195&page=4



Spiderman 2 (background plate)

