

# Computational Photography (I)

Digital Visual Effects, Spring 2008

*Yung-Yu Chuang*

2008/5/20

*with slides by Fredo Durand, Ramesh Raskar, Sylvain Paris, Soonmin Bae, Amit Agrawal, Ramesh Raskar*

DigiVFX

## Computational photography

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wikipedia:

**Computational photography** refers broadly to computational imaging techniques that enhance or extend the capabilities of digital photography. The output of these techniques is an ordinary photograph, but one that could not have been taken by a traditional camera.

## What is computational photography

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- Convergence of image processing, computer vision, computer graphics and photography
- Digital photography:
  - Simply mimics traditional sensors and recording by digital technology
  - Involves only simple image processing
- Computational photography
  - More elaborate image manipulation, more computation
  - New types of media (panorama, 3D, etc.)
  - Camera design that take computation into account

## Computational photography

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- One of the most exciting fields.
- [Symposium on Computational Photography and Video](#), 2005
- Full-semester courses in MIT, CMU, Stanford, GaTech, University of Delaware
- A new book by Raskar and Tumblin in SIGGRAPH 2007.

## Siggraph 2006 Papers (16/86=18.6%)

Hybrid Images  
 Drag-and-Drop Pasting  
 Two-scale Tone Management for Photographic Look  
 Interactive Local Adjustment of Tonal Values  
 Image-Based Material Editing  
 Flash Matting  
 Natural Video Matting using Camera Arrays  
 Removing Camera Shake From a Single Photograph  
 Coded Exposure Photography: Motion Deblurring  
 Photo Tourism: Exploring Photo Collections in 3D  
 AutoCollage  
 Photographing Long Scenes With Multi-Viewpoint Panoramas  
 Projection Defocus Analysis for Scene Capture and Image Display  
 Multiview Radial Catadioptric Imaging for Scene Capture  
 Light Field Microscopy  
 Fast Separation of Direct and Global Components of a Scene Using High Frequency Illumination

## Siggraph 2007 Papers (23/108=21.3%)

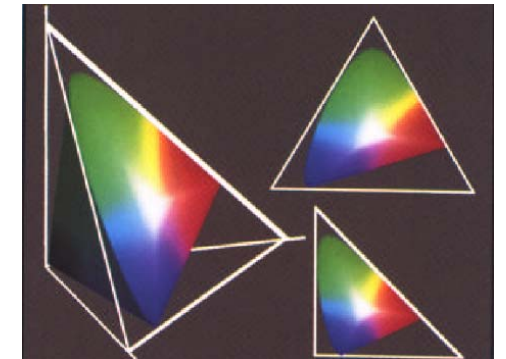
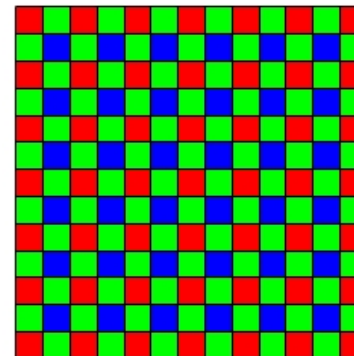
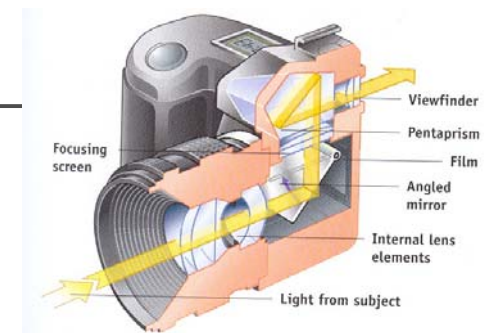
Image Deblurring with Blurred/Noisy Image Pairs  
 Photo Clip Art  
 Scene Completion Using Millions of Photographs  
 Soft Scissors: An Interactive Tool for Realtime High Quality Matting  
 Seam Carving for Content-Aware Image Resizing  
 Detail-Preserving Shape Deformation in Image Editing  
 Veiling Glare in High Dynamic Range Imaging  
 Do HDR Displays Support LDR content? A Psychophysical Evaluation  
 Ldr2hdr: On-the-fly Reverse Tone Mapping of Legacy Video and Photographs  
 Rendering for an Interactive 360-Degree Light Field Display  
 Multiscale Shape and Detail Enhancement from Multi-light Image Collections  
 Post-Production Facial Performance Relighting Using Reflectance Transfer  
 Active Refocusing of Images and Videos  
 Multi-aperture Photography  
 Dappled Photography: Mask-Enhanced Cameras for Heterodyned Light Fields and Coded Aperture Refocusing  
 Image and Depth from a Conventional Camera with a Coded Aperture  
 Capturing and Viewing Gigapixel Images  
 Efficient Gradient-Domain Compositing Using Quadrees  
 Image Upsampling via Imposed Edges Statistics  
 Joint Bilateral Upsampling  
 Factored Time-Lapse Video  
 Computational Time-Lapse Video  
 Real-Time Edge-Aware Image Processing With the Bilateral Grid

## Scope

- We can't yet set its precise definition. The following are scopes of what researchers are exploring in this field.
  - Record a richer visual experience
  - Overcome long-standing limitations of conventional cameras
  - Enable new classes of visual signal
  - Enable synthesis impossible photos

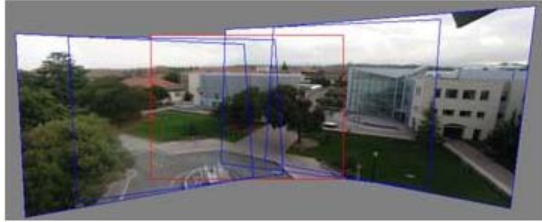
## Scope

- Image formation
- Color and color perception

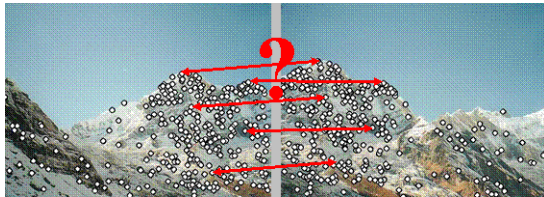


## Scope

- Panoramic imaging



- Image and video registration



- Spatial warping operations

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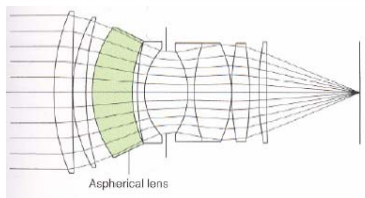
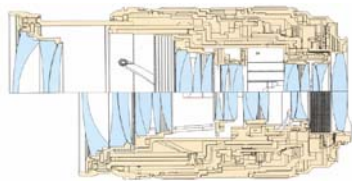
## Scope

- High Dynamic Range Imaging
- Bilateral filtering and HDR display
- Matting



## Scope

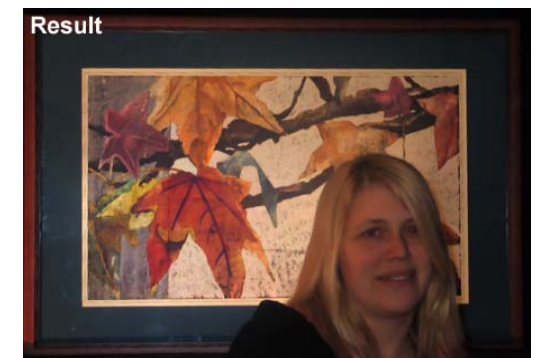
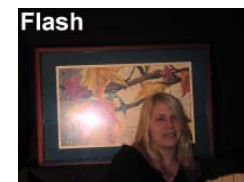
- Active flash methods
- Lens technology
- Depth and defocus



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## Removing Photography Artifacts using Gradient Projection and Flash-Exposure Sampling



## Continuous flash

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Flash = 0.0



Flash = 1.0



Flash = 0.3



Flash = 0.7



Flash = 1.4

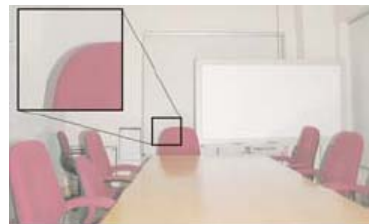
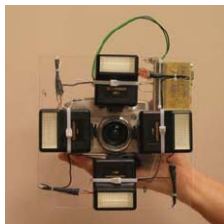
## Flash matting

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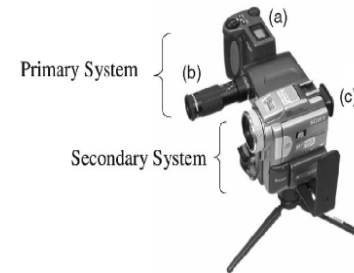
## Depth Edge Detection and Stylized Rendering Using a Multi-Flash Camera

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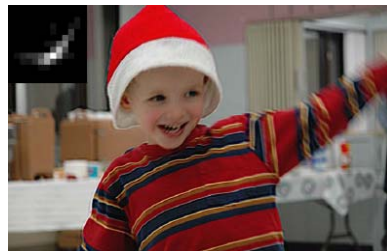
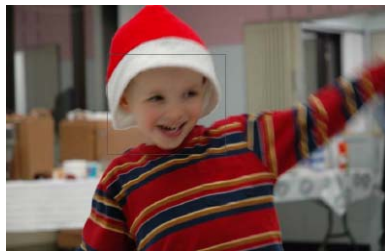
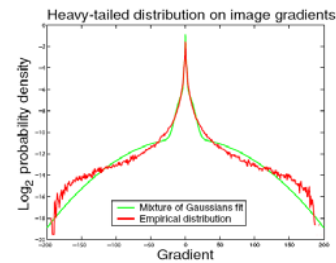


## Motion-Based Motion Deblurring

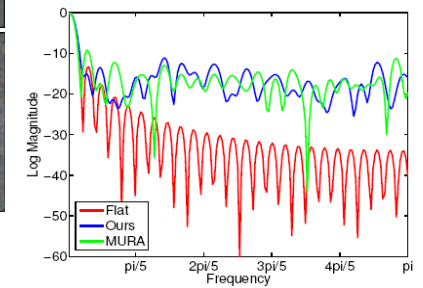
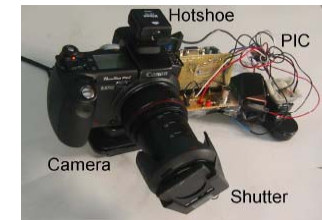
DigiVFX



# Removing Camera Shake from a Single Photograph



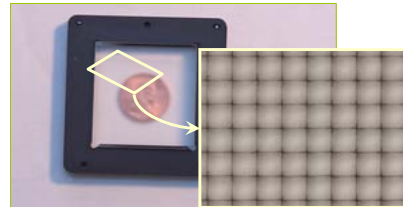
# Motion Deblurring using Fluttered Shutter



# Scope



- Future cameras
- Plenoptic function and light fields



# Scope



- Gradient image manipulation



sources/destinations



cloning



seamless cloning

# Scope

- Taking great pictures

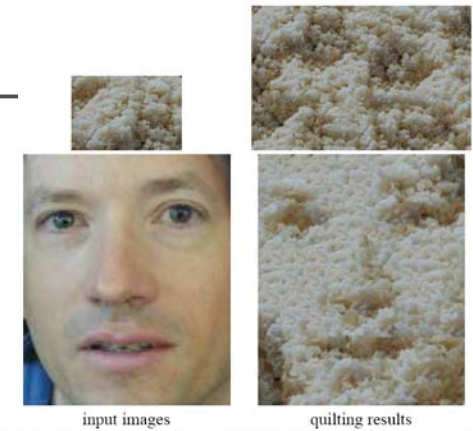


Art Wolfe

Ansel Adams

# Scope

- Non-parametric image synthesis, inpainting, analogies



input images

quilting results



A

A'

B

B'

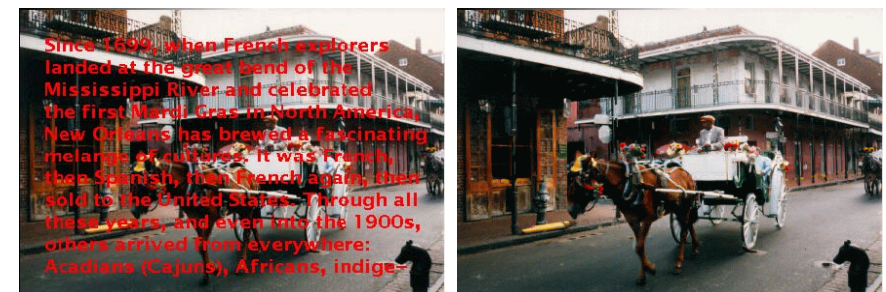
Figure 1 An image analogy. Our problem is to compute a new "analogous" image  $B'$  that relates to  $B$  in "the same way" as  $A'$  relates to  $A$ . Here,  $A$ ,  $A'$ , and  $B$  are inputs to our algorithm, and  $B'$  is the output. The full-size images are shown in Figures 10 and 11.

# Scope

- Motion analysis

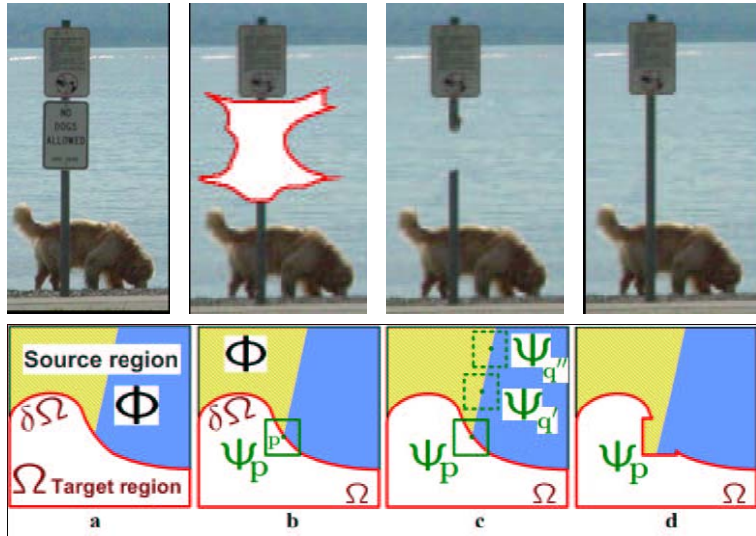


# Image Inpainting



## Object Removal by Exemplar-Based Inpainting

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## Image Completion with Structure Propagation

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## Lazy snapping

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## Grab Cut - Interactive Foreground Extraction using Iterated Graph Cuts

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# Image Tools



- Graph cuts,
  - Segmentation and mosaicing
- Gradient domain operations,
  - Tone mapping, fusion and matting
- Bilateral and Trilateral filters,
  - Denoising, image enhancement

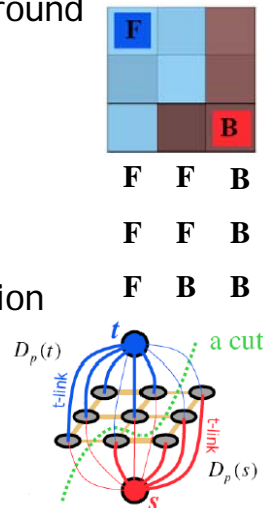
# Graph cut



# Graph cut



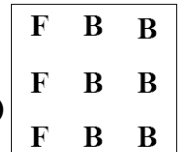
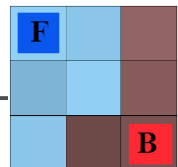
- Interactive image segmentation using graph cut
- Binary label: foreground vs. background
- User labels some pixels
  - similar to trimap, usually sparser
- Exploit
  - Statistics of known Fg & Bg
  - Smoothness of label
- Turn into discrete graph optimization
  - Graph cut (min cut / max flow)



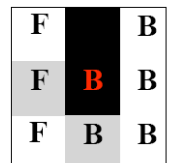
# Energy function

- Labeling: one value per pixel, F or B
- Energy(labeling) = data + smoothness
  - Very general situation
  - Will be minimized
- Data: for each pixel
  - Probability that this color belongs to F (resp. B)
  - Similar in spirit to Bayesian matting
- Smoothness (aka regularization): per neighboring pixel pair
  - Penalty for having different label
  - Penalty is downweighted if the two pixel colors are very different
  - Similar in spirit to bilateral filter

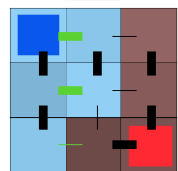
**One labeling  
(ok, not best)**



**Data**



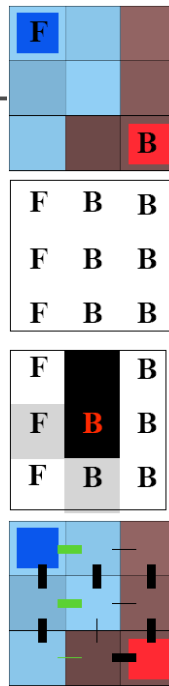
**Smoothness**





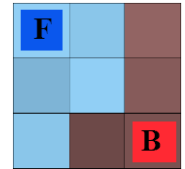
## Data term

- A.k.a regional term  
(because integrated over full region)
- $D(L) = \sum_i -\log h[L_i](C_i)$
- Where  $i$  is a pixel  
 $L_i$  is the label at  $i$  (F or B),  
 $C_i$  is the pixel value  
 $h[L_i]$  is the histogram of the observed  $F_g$   
(resp  $B_g$ )
- Note the minus sign



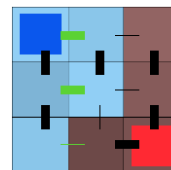
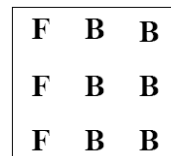
## Hard constraints

- The user has provided some labels
- The quick and dirty way to include constraints into optimization is to replace the data term by a huge penalty if not respected.
- $D(L_i) = 0$  if respected
- $D(L_i) = K$  if not respected  
– e.g.  $K = -\text{\#pixels}$



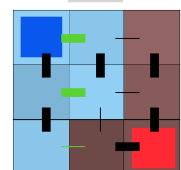
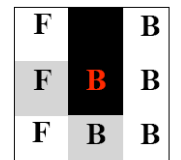
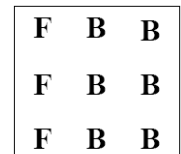
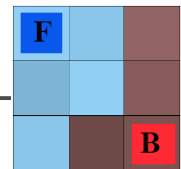
## Smoothness term

- a.k.a boundary term, a.k.a. regularization
- $S(L) = \sum_{\langle i, j \rangle \text{ in } N} B(C_i, C_j) \delta(L_i - L_j)$
- Where  $i, j$  are neighbors  
– e.g. 8-neighborhood  
(but I show 4 for simplicity)
- $\delta(L_i - L_j)$  is 0 if  $L_i = L_j$ , 1 otherwise
- $B(C_i, C_j)$  is high when  $C_i$  and  $C_j$  are similar, low if there is a discontinuity between those two pixels  
– e.g.  $\exp(-||C_i - C_j||^2 / 2\sigma^2)$   
– where  $\sigma$  can be a constant or the local variance
- Note positive sign



## Optimization

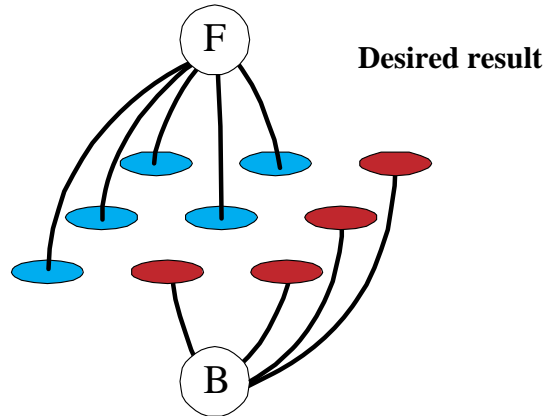
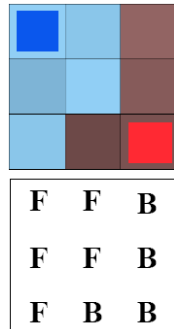
- $E(L) = D(L) + \lambda S(L)$
- $\lambda$  is a black-magic constant
- Find the labeling that minimizes  $E$
- In this case, how many possibilities?  
–  $2^9$  (512)  
– We can try them all!  
– What about megapixel images?



## Labeling as a graph problem

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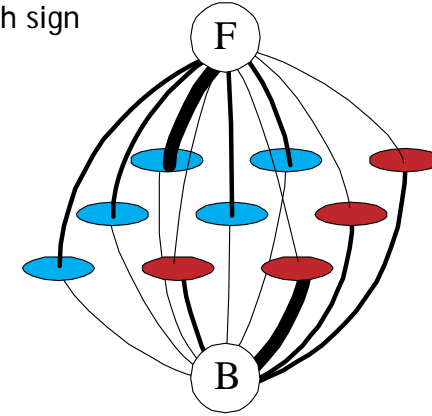
- Each pixel = node
- Add two nodes F & B
- Labeling: link each pixel to either F or B



## Data term

DigiVFX

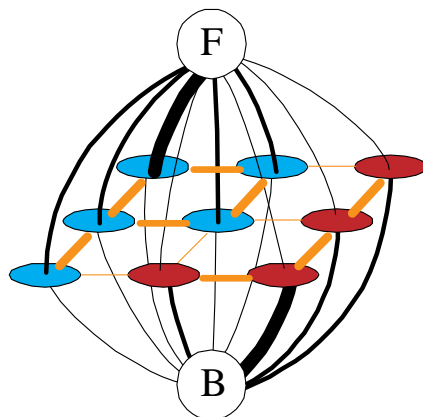
- Put one edge between each pixel and F & B
- Weight of edge = minus data term
  - Don't forget huge weight for hard constraints
  - Careful with sign



## Smoothness term

DigiVFX

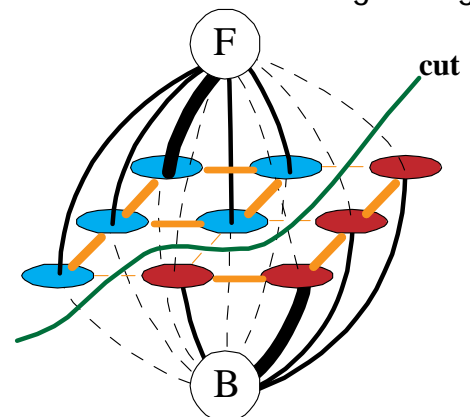
- Add an edge between each neighbor pair
- Weight = smoothness term



## Min cut

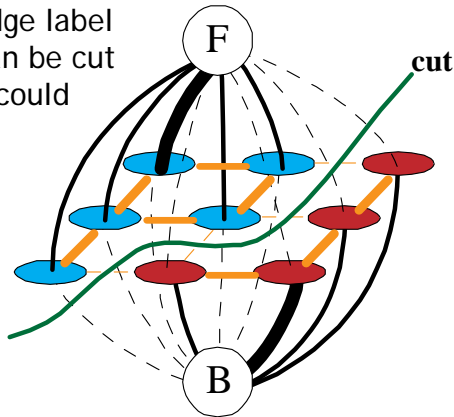
DigiVFX

- Energy optimization equivalent to min cut
- Cut: remove edges to disconnect F from B
- Minimum: minimize sum of cut edge weight



## Min cut $\Leftrightarrow$ labeling

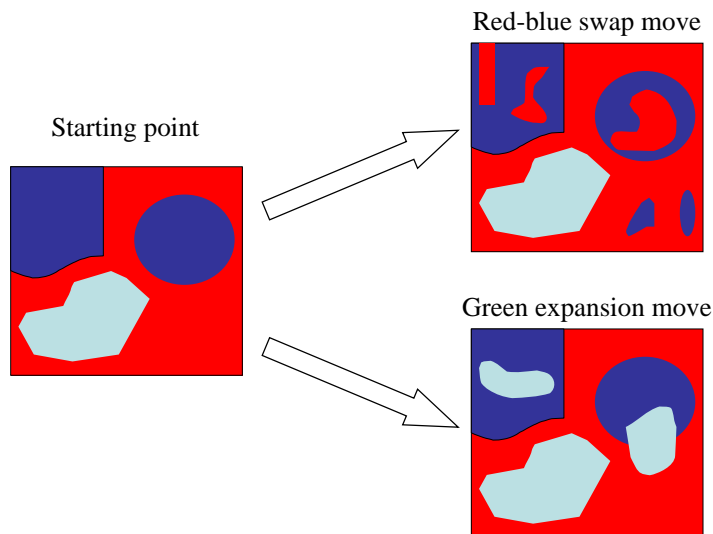
- In order to be a cut:
  - For each pixel, either the F or G edge has to be cut
- In order to be minimal
  - Only one edge label per pixel can be cut (otherwise could be added)



## Computing a multiway cut

- With 2 labels: classical min-cut problem
  - Solvable by standard flow algorithms
    - polynomial time in theory, nearly linear in practice
  - More than 2 terminals: NP-hard [Dahlhaus *et al.*, STOC '92]
- Efficient approximation algorithms exist
  - Within a factor of 2 of optimal
  - Computes local minimum in a strong sense
    - even very large moves will not improve the energy
  - Yuri Boykov, Olga Veksler and Ramin Zabih, [Fast Approximate Energy Minimization via Graph Cuts](#), International Conference on Computer Vision, September 1999.

## Move examples



## GrabCut Interactive Foreground Extraction using Iterated Graph Cuts



Carsten Rother  
Vladimir Kolmogorov  
Andrew Blake



Microsoft Research Cambridge-UK

## Demo

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- [video](#)

## Interactive Digital Photomontage DigiVFX

- Combining multiple photos
- Find seams using graph cuts
- Combine gradients and integrate

Aseem Agarwala, Mira Dontcheva, Maneesh Agrawala, Steven Drucker, Alex Colburn, Brian Curless, David Salesin, Michael Cohen, "Interactive Digital Photomontage", SIGGRAPH 2004

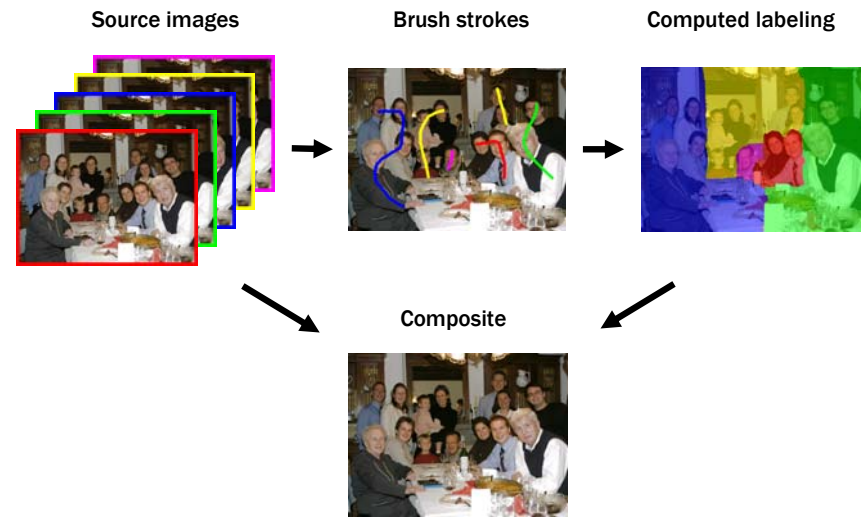






set of originals

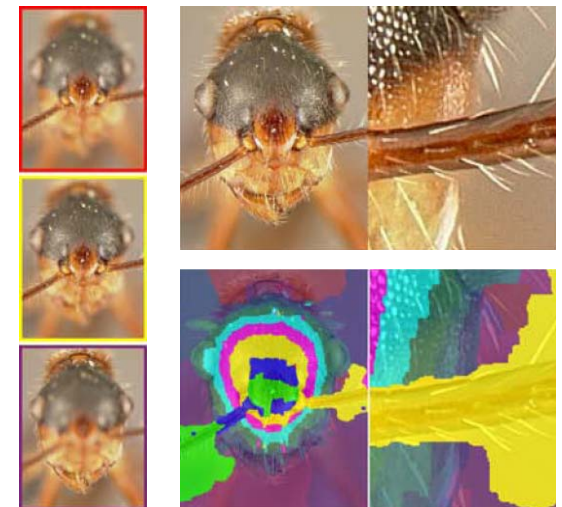
photomontage



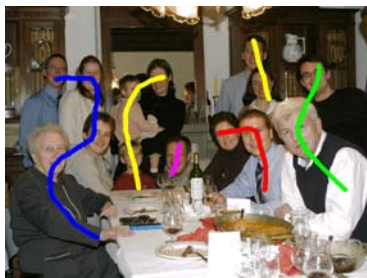
## Interactive Digital Photomontage



- Extended depth of field



Brush strokes

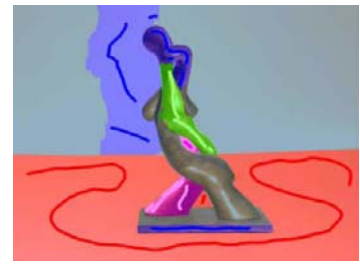


Computed labeling



# Interactive Digital Photomontage DigiVFX

- Relighting

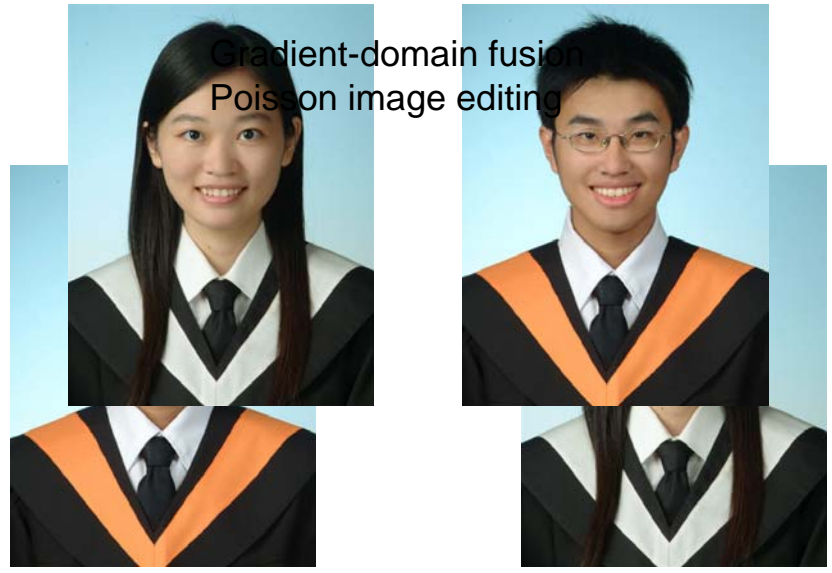


# Interactive Digital Photomontage DigiVFX



# Interactive Digital Photomontage DigiVFX

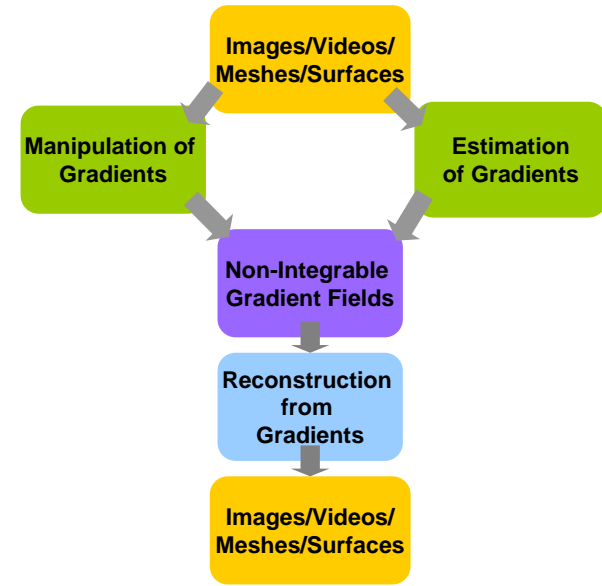
Gradient-domain fusion  
Poisson image editing



# Demo DigiVFX

- [video](#)

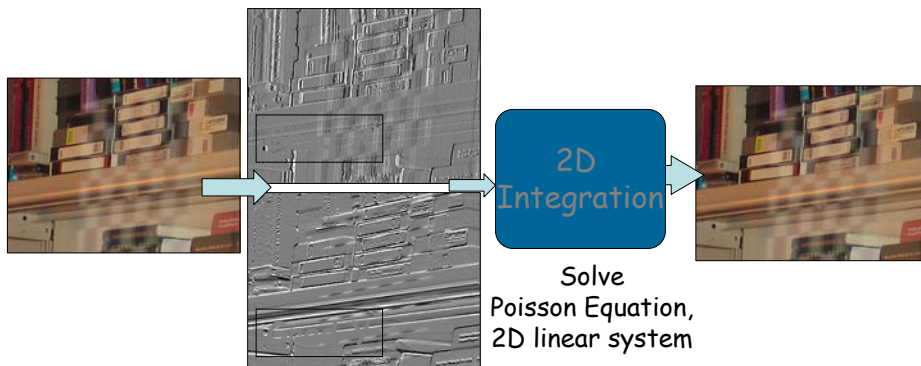
# Gradient Domain Manipulations



## Gradient domain operators

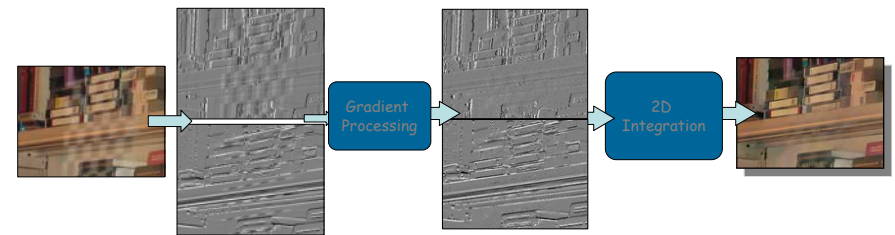


## Image Intensity Gradients in 2D



## Intensity Gradient Manipulation

### A Common Pipeline



1. Gradient manipulation
2. Reconstruction from gradients

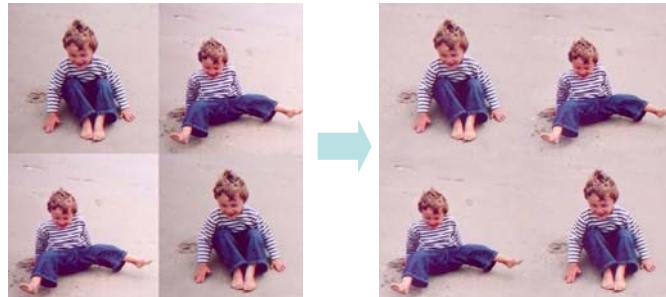


# Example Applications

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Removing Glass Reflections



Seamless Image Stitching

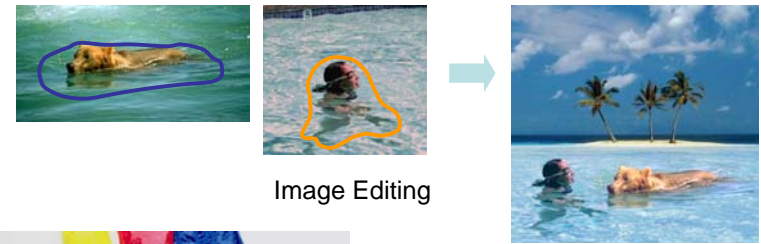
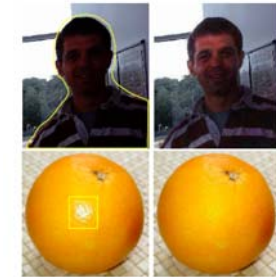


Image Editing



Changing Local Illumination



Original

PhotoshopGrey

Color2Gray

Color to Gray Conversion



High Dynamic Range Compression



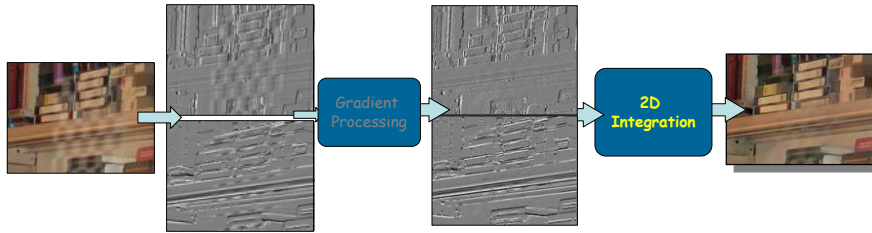
Edge Suppression under Significant Illumination Variations



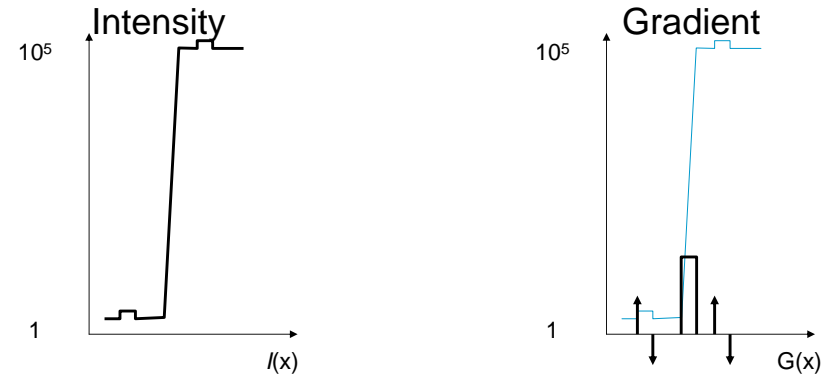
Fusion of day and night images

# Intensity Gradient Manipulation

A Common Pipeline



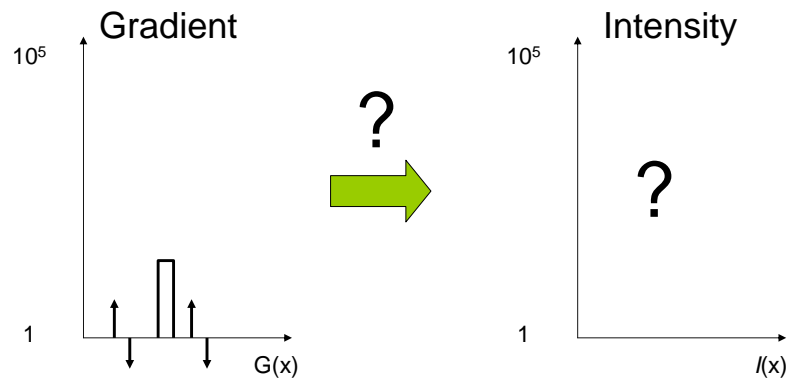
# Intensity Gradient in 1D



Gradient at x,  

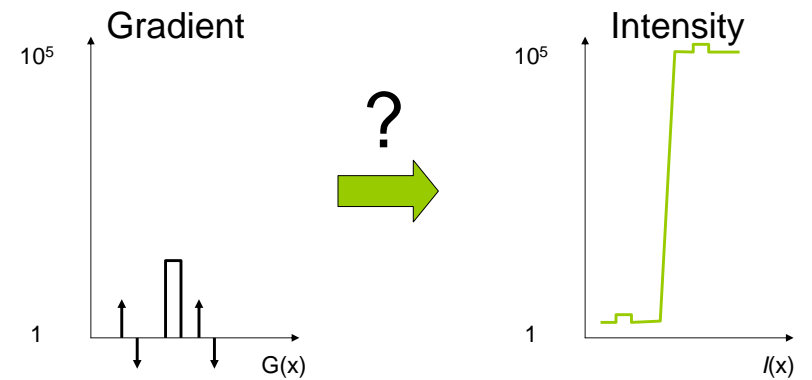
$$G(x) = I(x+1) - I(x)$$
 Forward Difference

# Reconstruction from Gradients



For  $n$  intensity values, about  $n$  gradients

# Reconstruction from Gradients

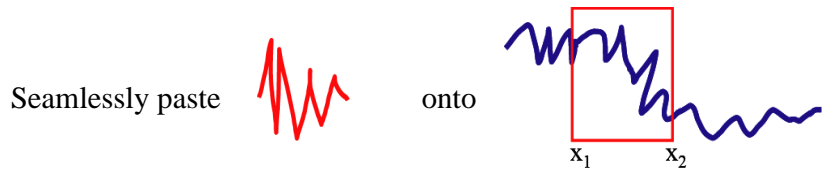


1D Integration

$$I(x) = I(x-1) + G(x)$$

Cumulative sum

# 1D case with constraints

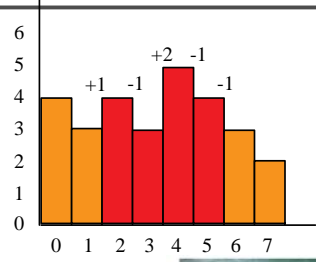


Just add a linear function so that the boundary condition is respected

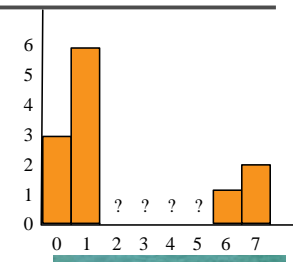


# Discrete 1D example: minimization

• Copy



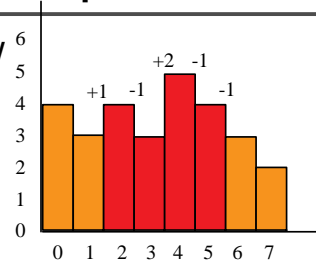
to



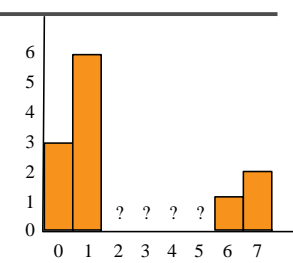
- $\text{Min} ((f_2-f_1)-1)^2$
  - $\text{Min} ((f_3-f_2)-(-1))^2$
  - $\text{Min} ((f_4-f_3)-2)^2$
  - $\text{Min} ((f_5-f_4)-(-1))^2$
  - $\text{Min} ((f_6-f_5)-(-1))^2$
- With  $f_1=6$   
 $f_6=1$

# 1D example: minimization

• Copy



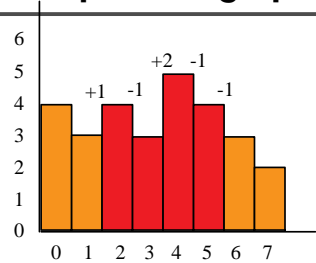
to



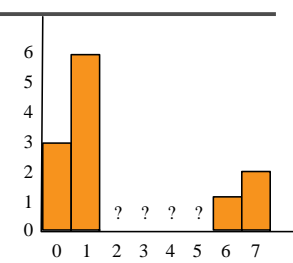
- $\text{Min} ((f_2-6)-1)^2 \implies f_2^2+49-14f_2$
- $\text{Min} ((f_3-f_2)-(-1))^2 \implies f_3^2+f_2^2+1-2f_3f_2+2f_3-2f_2$
- $\text{Min} ((f_4-f_3)-2)^2 \implies f_4^2+f_3^2+4-2f_3f_4-4f_4+4f_3$
- $\text{Min} ((f_5-f_4)-(-1))^2 \implies f_5^2+f_4^2+1-2f_5f_4+2f_5-2f_4$
- $\text{Min} ((1-f_5)-(-1))^2 \implies f_5^2+4-4f_5$

# 1D example: big quadratic

• Copy

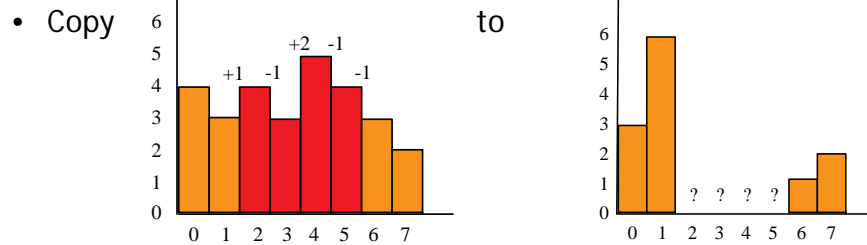


to



- $\text{Min} (f_2^2+49-14f_2 + f_3^2+f_2^2+1-2f_3f_2+2f_3-2f_2 + f_4^2+f_3^2+4-2f_3f_4-4f_4+4f_3 + f_5^2+f_4^2+1-2f_5f_4+2f_5-2f_4 + f_5^2+4-4f_5)$   
Denote it Q

# 1D example: derivatives



Min  $(f_2^2 + 49 - 14f_2$   
 $+ f_3^2 + f_2^2 + 1 - 2f_3f_2 + 2f_3 - 2f_2$   
 $+ f_4^2 + f_3^2 + 4 - 2f_3f_4 - 4f_4 + 4f_3$   
 $+ f_5^2 + f_4^2 + 1 - 2f_5f_4 + 2f_5 - 2f_4$   
 $+ f_5^2 + 4 - 4f_5)$

Denote it Q

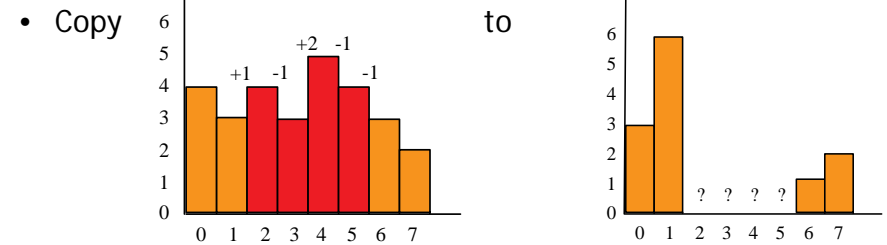
$$\frac{dQ}{df_2} = 2f_2 + 2f_2 - 2f_3 - 16$$

$$\frac{dQ}{df_3} = 2f_3 - 2f_2 + 2 + 2f_3 - 2f_4 + 4$$

$$\frac{dQ}{df_4} = 2f_4 - 2f_3 - 4 + 2f_4 - 2f_5 - 2$$

$$\frac{dQ}{df_5} = 2f_5 - 2f_4 + 2 + 2f_5 - 4$$

# 1D example: set derivatives to zero



$$\frac{dQ}{df_2} = 2f_2 + 2f_2 - 2f_3 - 16$$

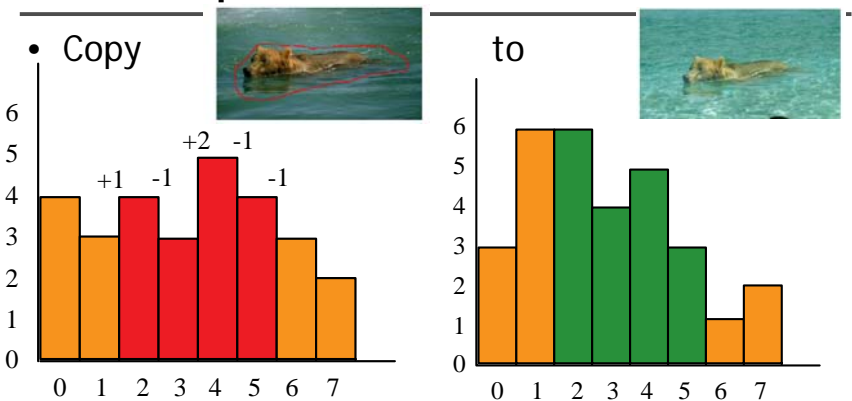
$$\frac{dQ}{df_3} = 2f_3 - 2f_2 + 2 + 2f_3 - 2f_4 + 4$$

$$\frac{dQ}{df_4} = 2f_4 - 2f_3 - 4 + 2f_4 - 2f_5 - 2$$

$$\frac{dQ}{df_5} = 2f_5 - 2f_4 + 2 + 2f_5 - 4$$

$$\implies \begin{pmatrix} 4 & -2 & 0 & 0 \\ -2 & 4 & -2 & 0 \\ 0 & -2 & 4 & -2 \\ 0 & 0 & -2 & 4 \end{pmatrix} \begin{pmatrix} f_2 \\ f_3 \\ f_4 \\ f_5 \end{pmatrix} = \begin{pmatrix} 16 \\ -6 \\ 6 \\ 2 \end{pmatrix}$$

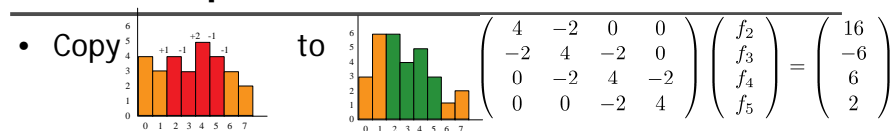
# 1D example



$$\begin{pmatrix} 4 & -2 & 0 & 0 \\ -2 & 4 & -2 & 0 \\ 0 & -2 & 4 & -2 \\ 0 & 0 & -2 & 4 \end{pmatrix} \begin{pmatrix} f_2 \\ f_3 \\ f_4 \\ f_5 \end{pmatrix} = \begin{pmatrix} 16 \\ -6 \\ 6 \\ 2 \end{pmatrix}$$

$$\begin{pmatrix} f_2 \\ f_3 \\ f_4 \\ f_5 \end{pmatrix} = \begin{pmatrix} 6 \\ 4 \\ 5 \\ 3 \end{pmatrix}$$

# 1D example: remarks

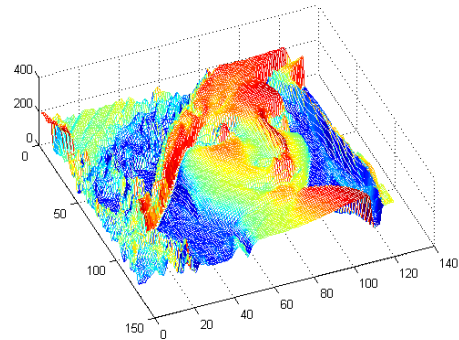
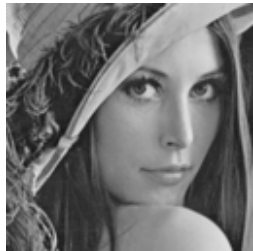


- Matrix is sparse
- Matrix is symmetric
- Everything is a multiple of 2
  - because square and derivative of square
- Matrix is a convolution (kernel -2 4 -2)
- Matrix is independent of gradient field. Only RHS is
- Matrix is a second derivative

# Basics

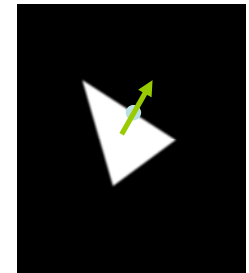
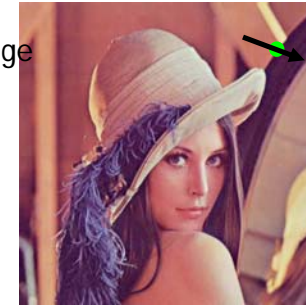
- Images as scalar fields

–  $\mathbb{R}^2 \rightarrow \mathbb{R}$



# Gradients

- Vector field (gradient field)
  - Derivative of a scalar field
- Direction
  - Maximum rate of change of scalar field
- Magnitude
  - Rate of change



# Gradient Field

- Components of gradient
  - Partial derivatives of scalar field

$$I(x, y)$$

$$\nabla I = \left\{ \frac{\partial I}{\partial x}, \frac{\partial I}{\partial y} \right\}$$

$$I(x, y, t)$$

$$\nabla I = \left\{ \frac{\partial I}{\partial x}, \frac{\partial I}{\partial y}, \frac{\partial I}{\partial t} \right\}$$

# Example

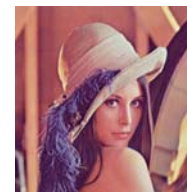


Image  
 $I(x,y)$



$I_x$



$I_y$

Gradient at  $x,y$  as Forward Differences

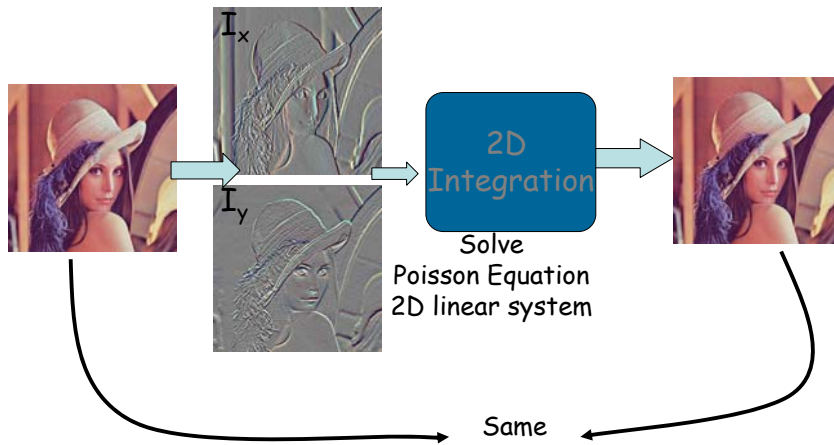
$$G_x(x,y) = I(x+1, y) - I(x,y)$$

$$G_y(x,y) = I(x, y+1) - I(x,y)$$

$$G(x,y) = (G_x, G_y)$$

# Reconstruction from Gradients

Sanity Check:  
Recovering Original Image

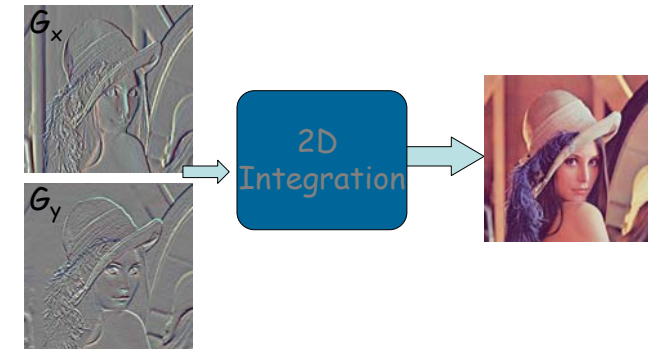


# Reconstruction from Gradients

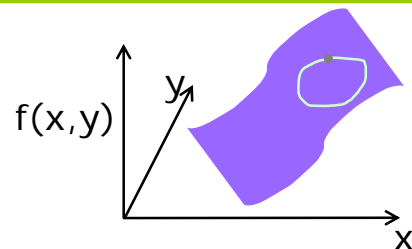
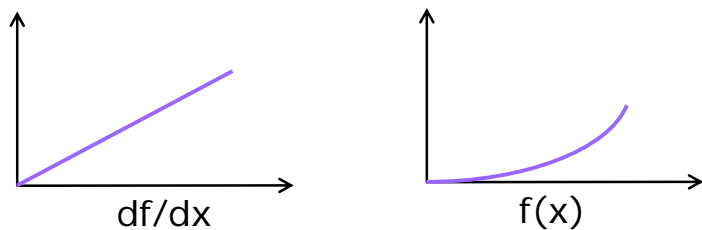
Given  $G(x,y) = (G_x, G_y)$

How to compute  $I(x,y)$  for the image ?

For  $n^2$  image pixels,  $2 n^2$  gradients !



# 2D Integration is non-trivial



Reconstruction depends on chosen path

# Reconstruction from Gradient Field $G$

- Look for image  $I$  with gradient closest to  $G$  in the least squares sense.
- $I$  minimizes the integral:  $\iint F(\nabla I, G) dx dy$

$$F(\nabla I, G) = \|\nabla I - G\|^2 = \left(\frac{\partial I}{\partial x} - G_x\right)^2 + \left(\frac{\partial I}{\partial y} - G_y\right)^2$$

# Poisson Equation

$$\nabla^2 I = \text{div}(G_x, G_y) = \frac{\partial G_x}{\partial x} + \frac{\partial G_y}{\partial y}$$

Second order PDE

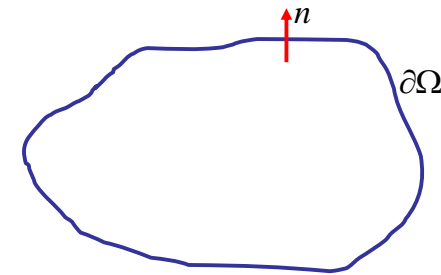
# Boundary Conditions

- Dirichlet: Function values at boundary are known

$$I(x, y) = I_0(x, y) \forall (x, y) \in \partial\Omega$$

- Neumann: Derivative normal to boundary = 0

$$\nabla I(x, y) \cdot n(x, y) = 0, \forall (x, y) \in \partial\Omega$$



# Numerical Solution

- Discretize Laplacian

$$\nabla^2 \rightarrow \begin{bmatrix} 0 & 1 & 0 \\ 1 & -4 & 1 \\ 0 & 1 & 0 \end{bmatrix}$$

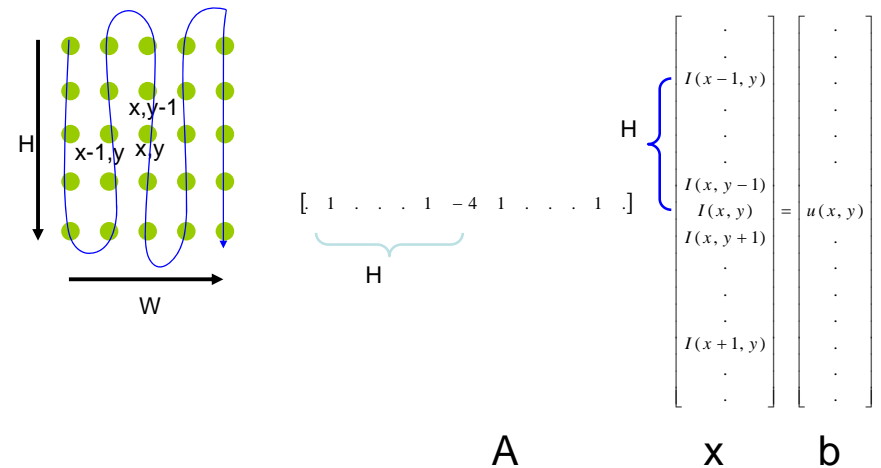
$$\nabla^2 I = \text{div}(G_x, G_y) = u(x, y)$$

$$-4I(x, y) + I(x, y+1) + I(x, y-1) + I(x+1, y) + I(x-1, y) = h^2 u(x, y)$$

h = grid size

# Linear System

$$-4I(x, y) + I(x, y+1) + I(x, y-1) + I(x+1, y) + I(x-1, y) = u(x, y)$$









## The key insight

Desired  
solution  $x$



—

Initial  
Solution  $x_0$

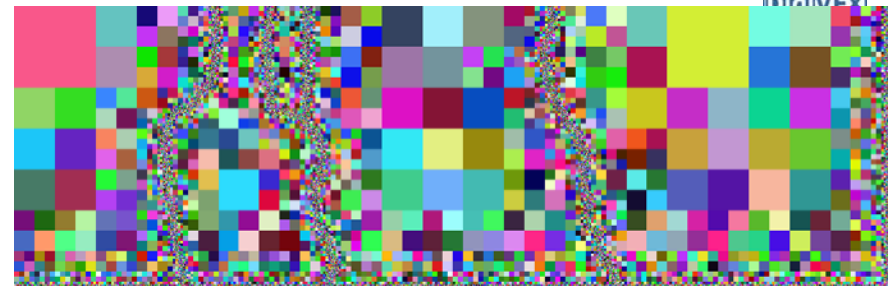
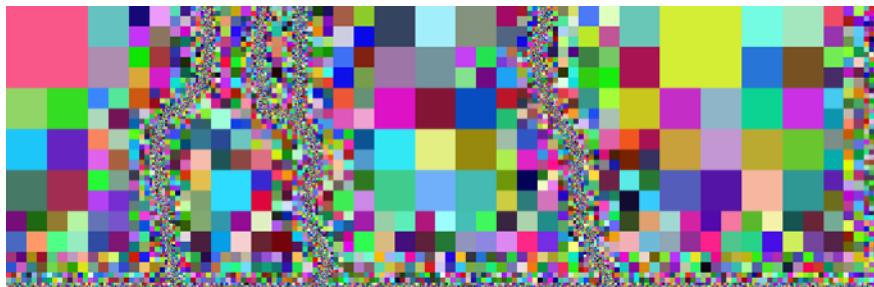


=

Difference  
 $x_\delta$



## Quadtree decomposition



- Maximally subdivide quadtree along seams
- Variables placed at node corners
- Restricted quadtree
- Bi-linear interpolation reconstructs full solution
- Square nodes

# Reduced space



$x$   
 $n$  variables



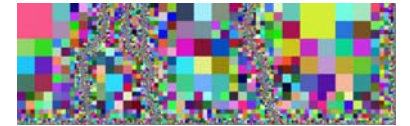
$y$   
 $m$  variables

$$m \ll n$$

# Reduced space

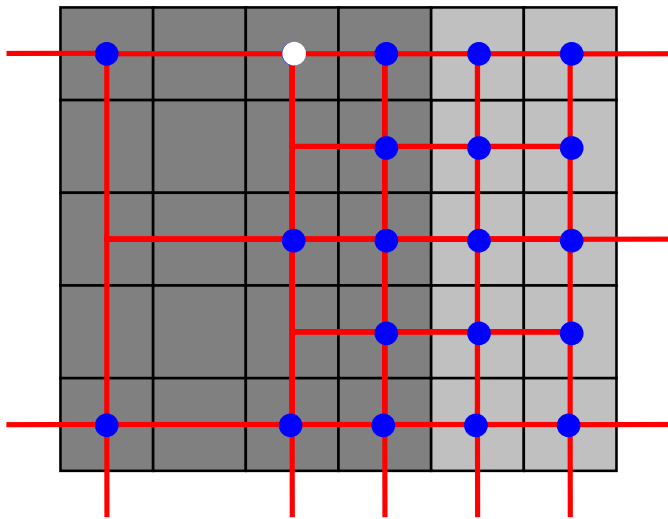


$x$   
 $n$  variables

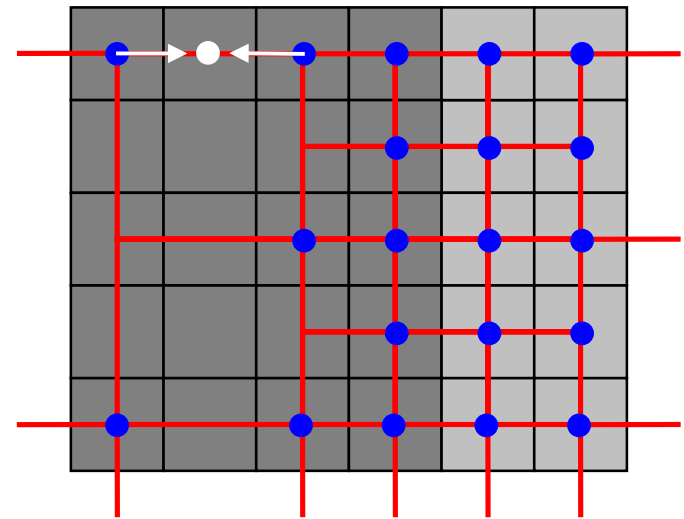


$y$   
 $m$  variables

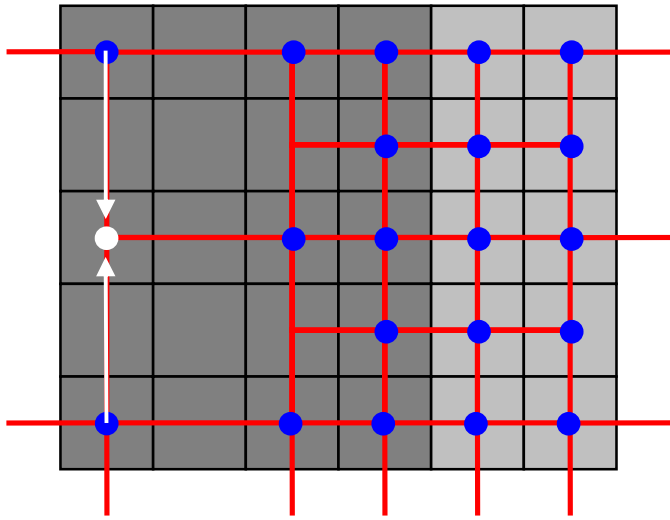
$$x = Sy$$



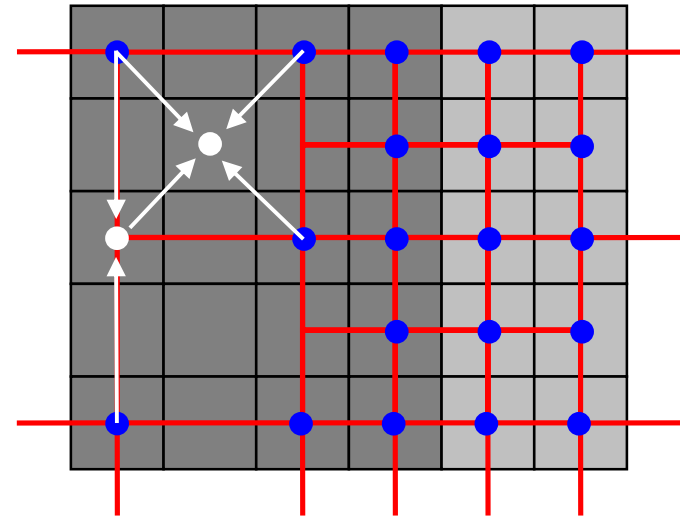
$$x = Sy$$



$$x = Sy$$



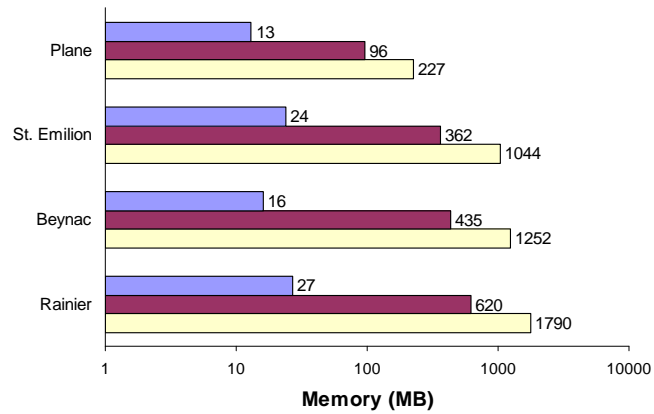
$$x = Sy$$



$$x = Sy$$

## Performance

DigiVFX



- Quadtree [Agarwala 07]
- Hierarchical basis preconditioning [Szeliski 90]
- Locally-adapted hierarchical basis preconditioning [Szeliski 06]

## Cut-and-paste

DigiVFX

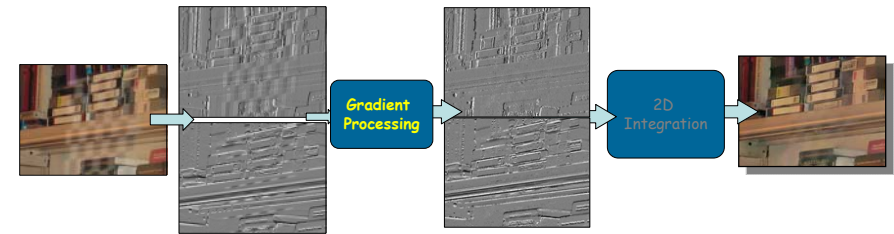


## Cut-and-paste



## Intensity Gradient Manipulation

### A Common Pipeline



## Gradient Domain Manipulations: Overview

- (A) Per pixel
- (B) Corresponding gradients in two images
- (C) Corresponding gradients in multiple images
- (D) Combining gradients along seams

## Gradient Domain Manipulations: Overview

- (A) Per pixel
  - Non-linear operations (HDR compression, local illumination change)
  - Set to zero (shadow removal, intrinsic images, texture de-emphasis)
  - Poisson Matting
- (B) Corresponding gradients in two images
  - Vector operations (gradient projection)
    - Combining flash/no-flash images, Reflection removal
  - Projection Tensors
    - Reflection removal, Shadow removal
  - Max operator
    - Day/Night fusion, Visible/IR fusion, Extending DoF
  - Binary, choose from first or second, copying
    - Image editing, seamless cloning

# Gradient Domain Manipulations

## (C) Corresponding gradients in multiple images

- Median operator
  - Specularity reduction
  - Intrinsic images

- Max operation
  - Extended DOF

## (D) Combining gradients along seams

- Weighted averaging
- Optimal seam using graph cut
  - Image stitching, Mosaics, Panoramas, Image fusion
  - A usual pipeline: Graph cut to find seams + gradient domain fusion

# A. Per Pixel Manipulations

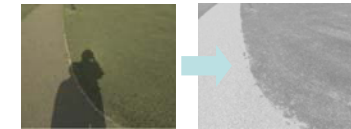
## • Non-linear operations

- HDR compression, local illumination change



## • Set to zero

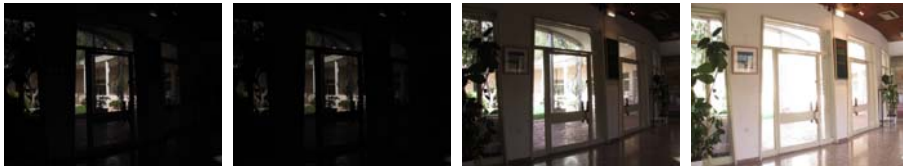
- Shadow removal, intrinsic images, texture de-emphasis



## • Poisson Matting

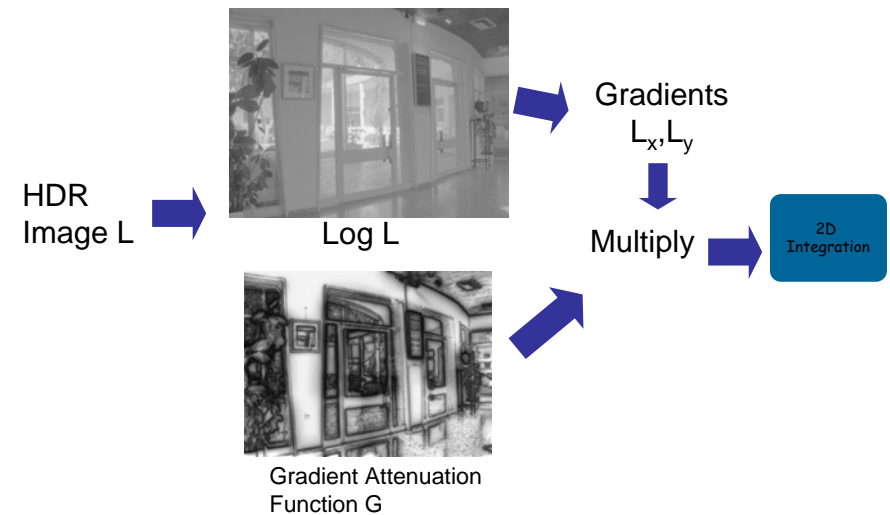


# High Dynamic Range Imaging



Images from Raanan Fattal

# Gradient Domain Compression



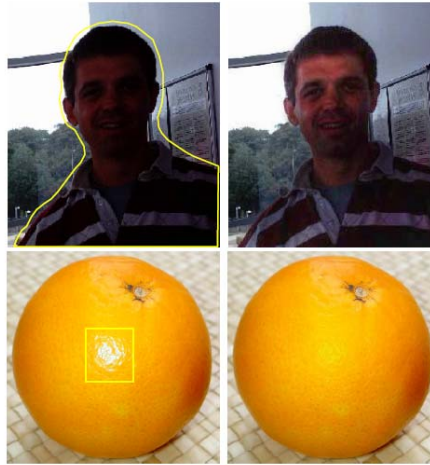
# Local Illumination Change

Original Image:  $f$

$$v = \alpha^\beta |\nabla f^*|^{-\beta} \nabla f^*$$

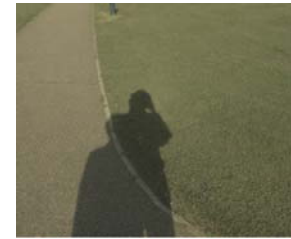
Original gradient field:  $\nabla f^*$

Modified gradient field:  $v$



Perez et al. Poisson Image editing, SIGGRAPH 2003

# Illumination Invariant Image



Original Image



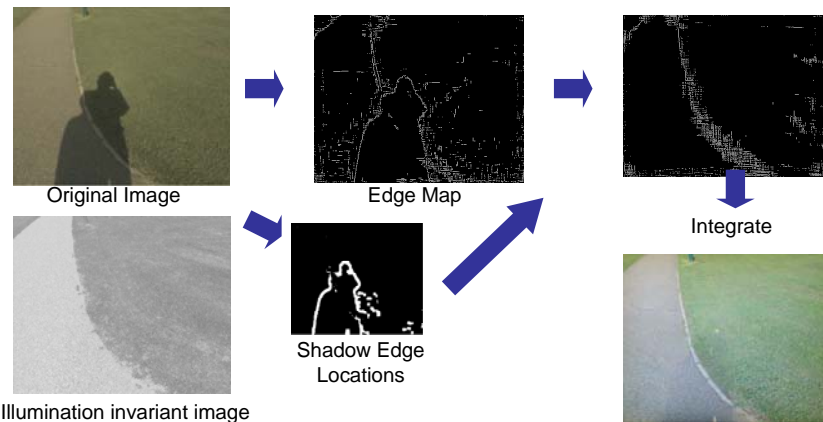
Illumination invariant image

- Assumptions

- Sensor response = delta functions R, G, B in wavelength spectrum
- Illumination restricted to Outdoor Illumination

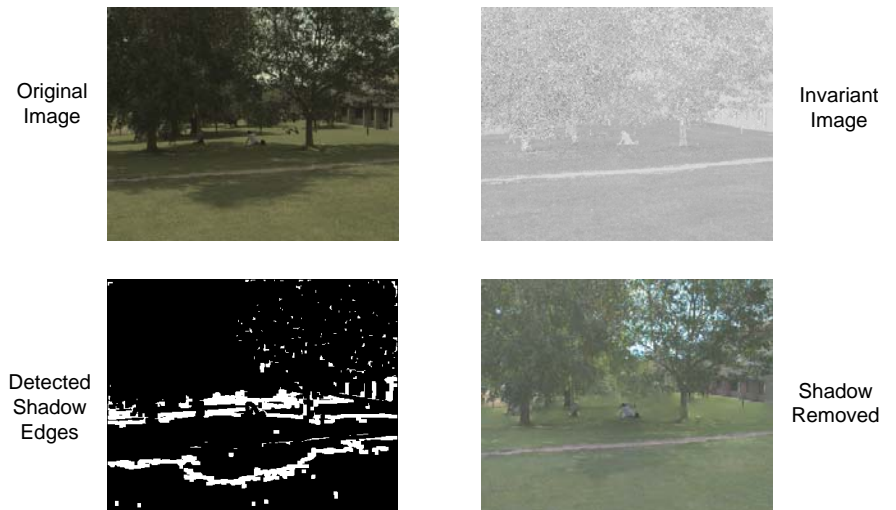
G. D. Finlayson, S.D. Hordley & M.S. Drew, Removing Shadows From Images, ECCV 2002

# Shadow Removal Using Illumination Invariant Image



G. D. Finlayson, S.D. Hordley & M.S. Drew, Removing Shadows From Images, ECCV 2002

# Illumination invariant image



G. D. Finlayson, S.D. Hordley & M.S. Drew, Removing Shadows From Images, ECCV 2002

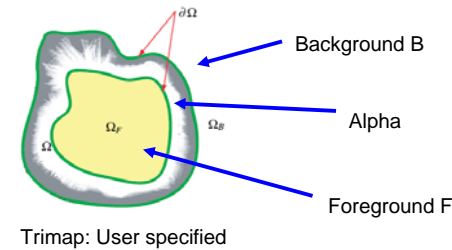
# Intrinsic Image

- Photo = Illumination Image \* **Intrinsic Image**
- Retinex [Land & McCann 1971, Horn 1974]
  - Illumination is smoothly varying
  - Reflectance, piece-wise constant, has strong edges
  - Keep strong image gradients, integrate to obtain reflectance

low-frequency attenuate more    high-frequency attenuate less



# Poisson Matting



Jian Sun, Jiaya Jia, Chi-Keung Tang, Heung-Yeung Shum, Poisson Matting, SIGGRAPH 2004

# Poisson Matting

$$I = \alpha F + (1 - \alpha)B$$

$$\nabla I = (F - B)\nabla\alpha + \alpha\nabla F + (1 - \alpha)\nabla B$$

Approximate: Assume F and B are smooth

$$\nabla I = (F - B)\nabla\alpha$$

$$\nabla\alpha \approx \frac{1}{F - B}\nabla I$$



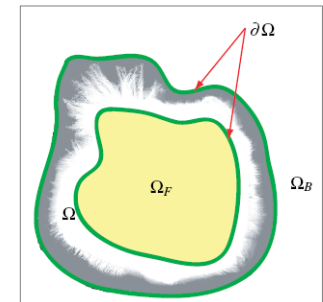
$$\Delta\alpha = \text{div}\left(\frac{\nabla I}{F - B}\right)$$

Poisson Equation

F and B in tri-map using nearest pixels

# Poisson Matting

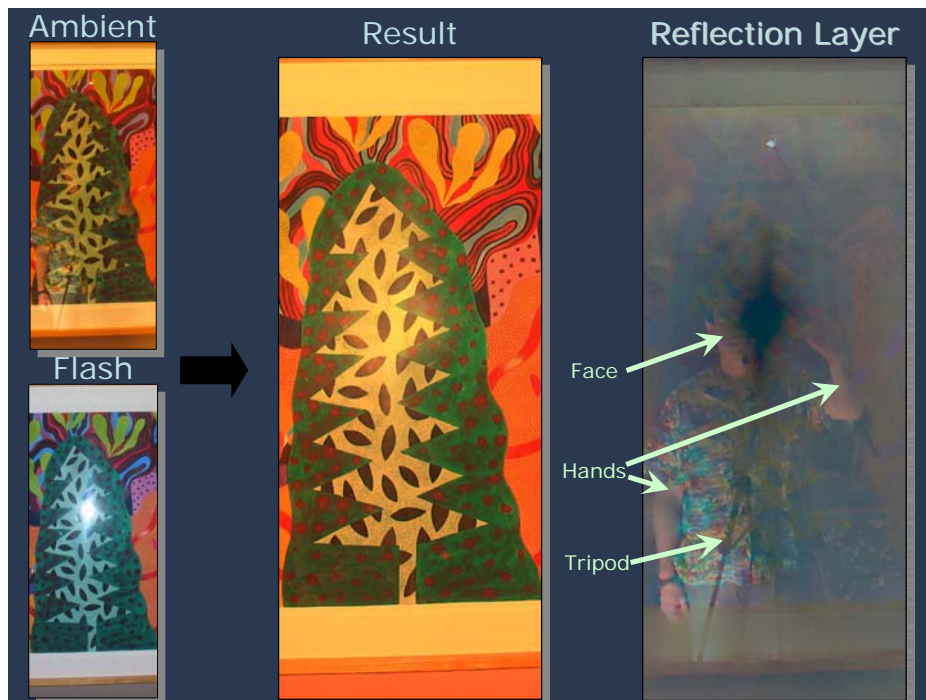
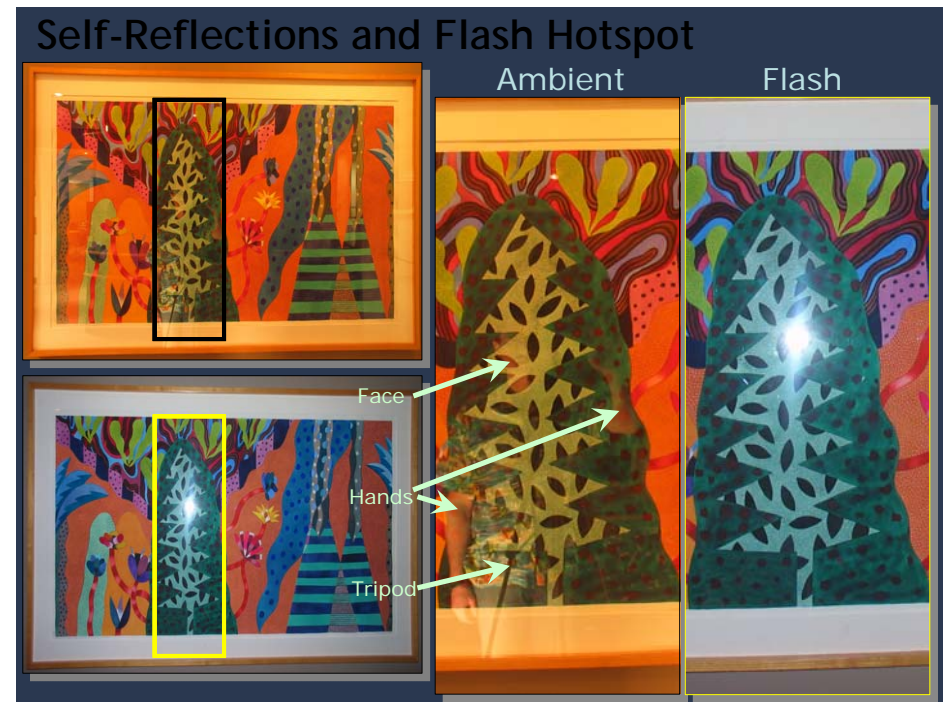
- Steps
  - Approximate F and B in trimap  $\Omega$
  - Solve for  $\alpha$      $\Delta\alpha = \text{div}\left(\frac{\nabla I}{F - B}\right)$
  - Refine F and B using  $\alpha$
  - Iterate

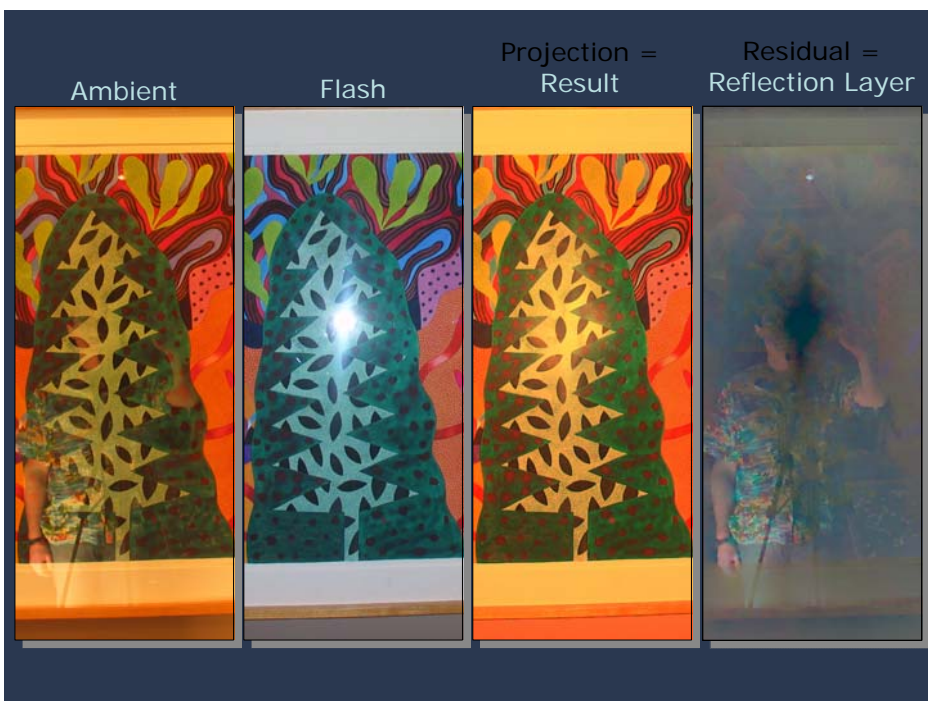
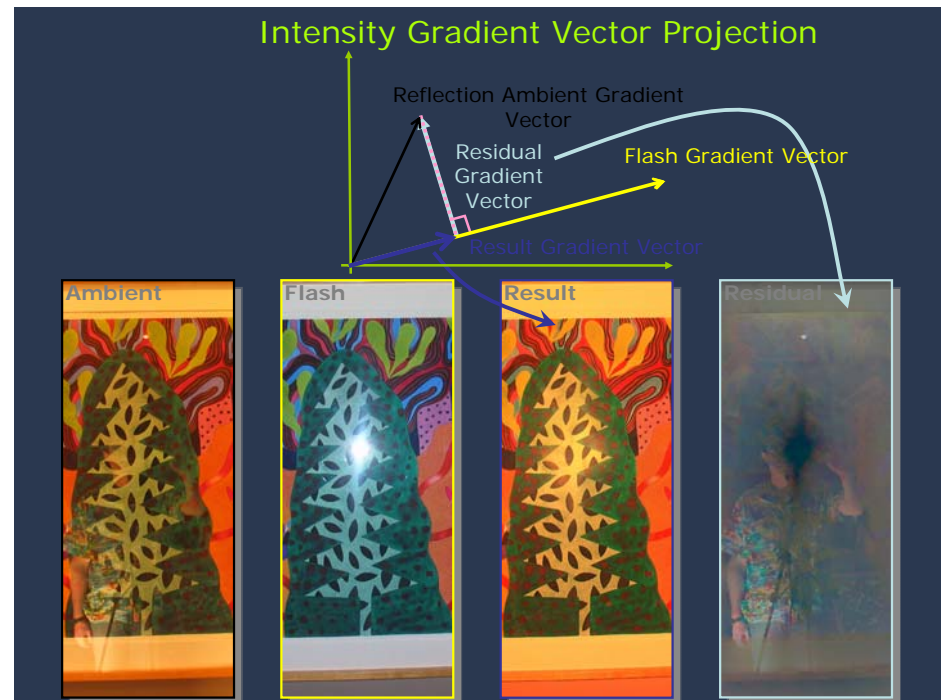
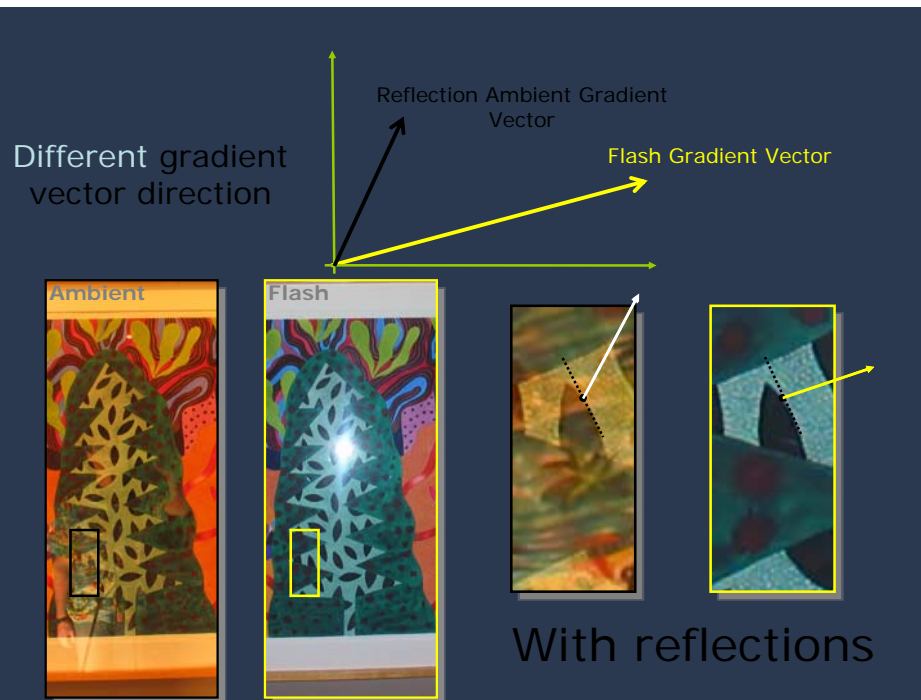




# Gradient Domain Manipulations: Overview DigiVEX

- (A) Per pixel
- (B) Corresponding gradients in two images
- (C) Corresponding gradients in multiple images
- (D) Combining gradients along seams





# Image Fusion for Context Enhancement and Video Surrealism

Ramesh Raskar

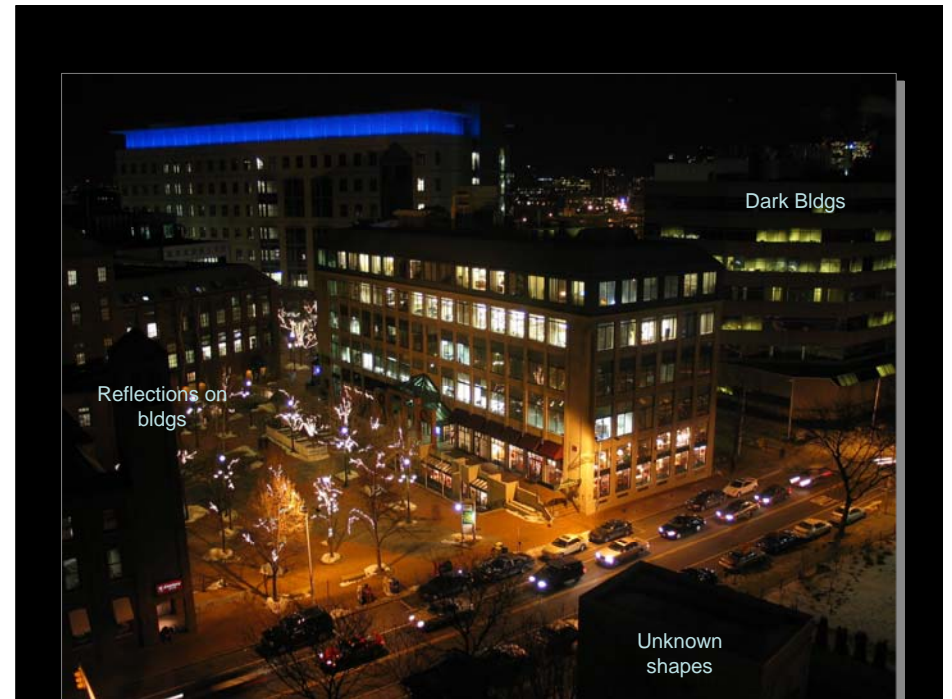
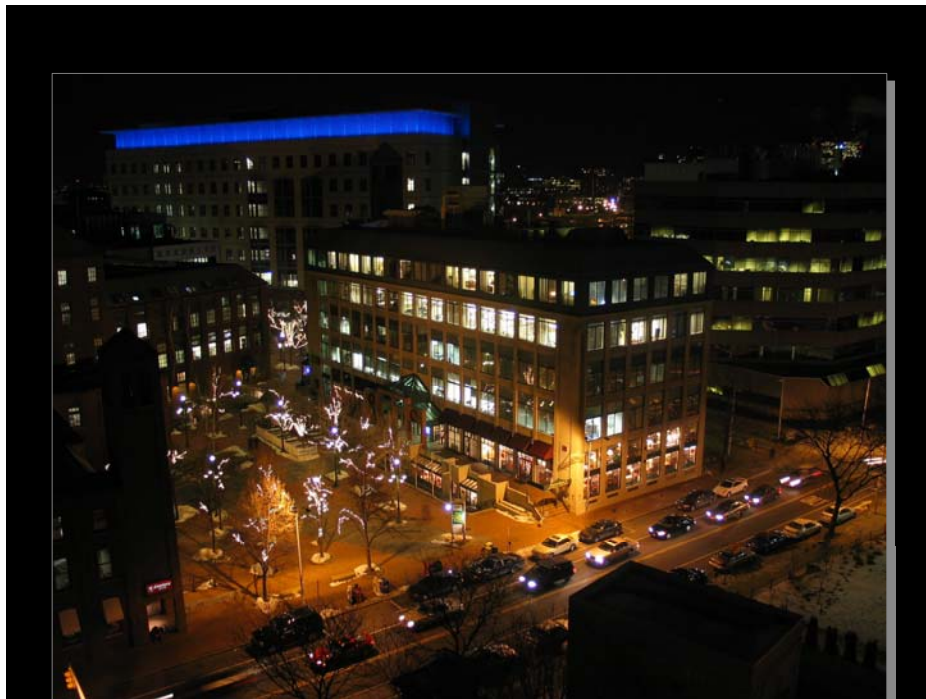
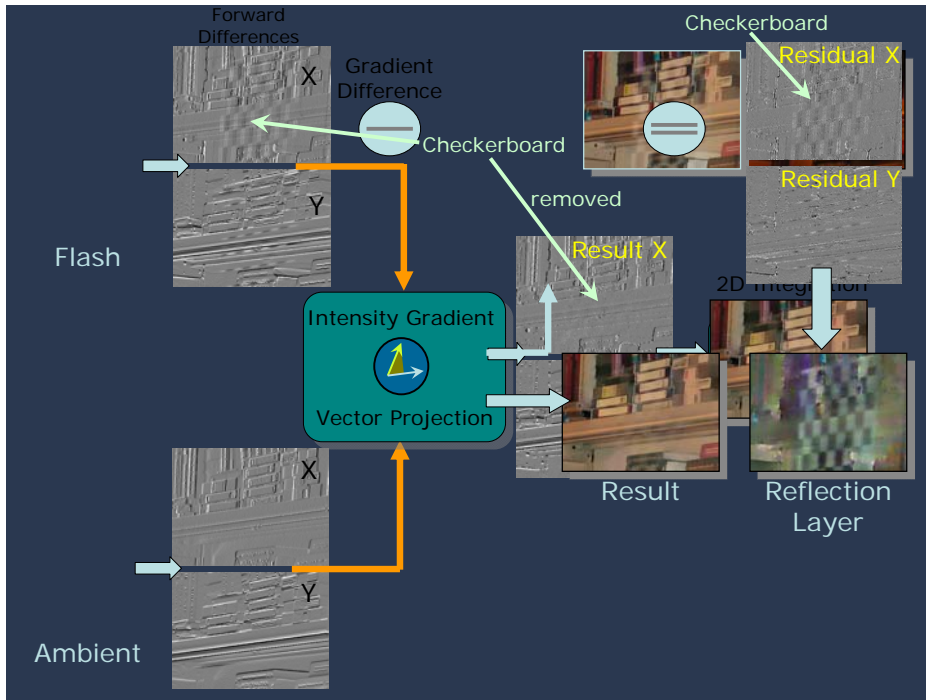
Adrian Ilie

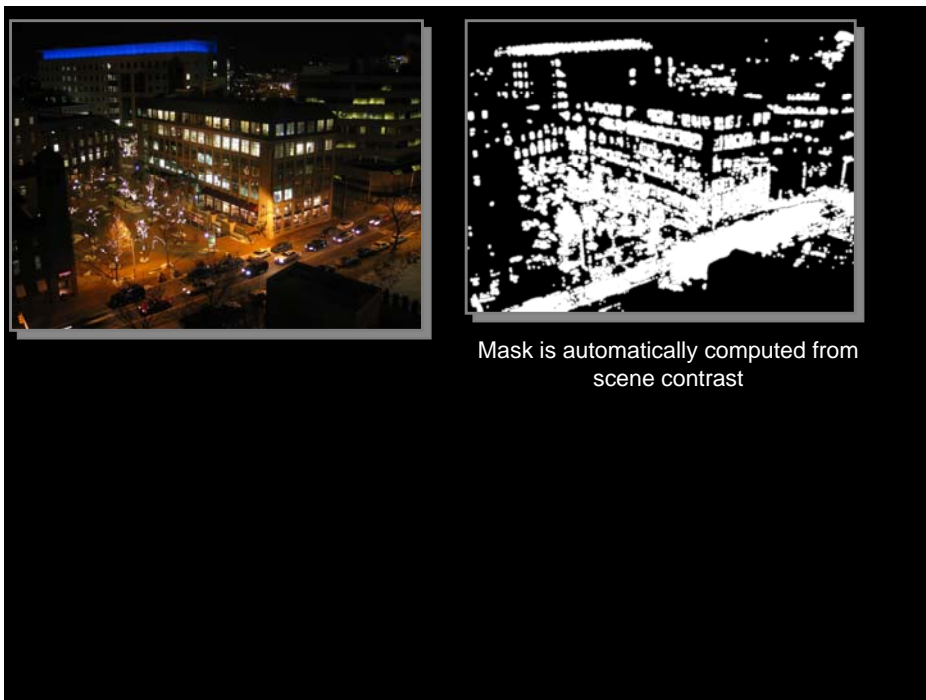
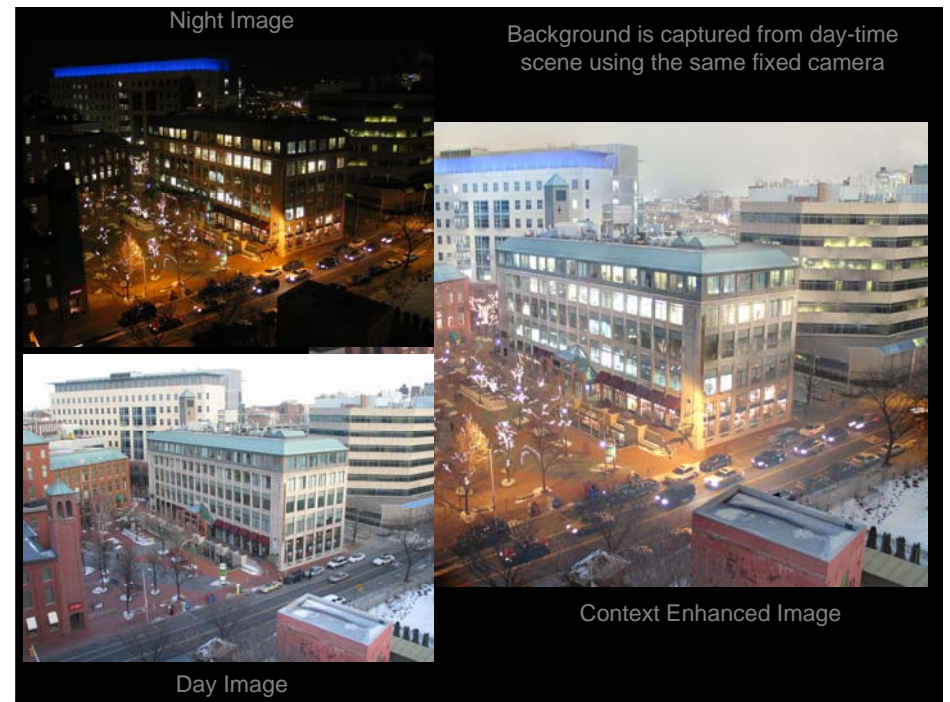
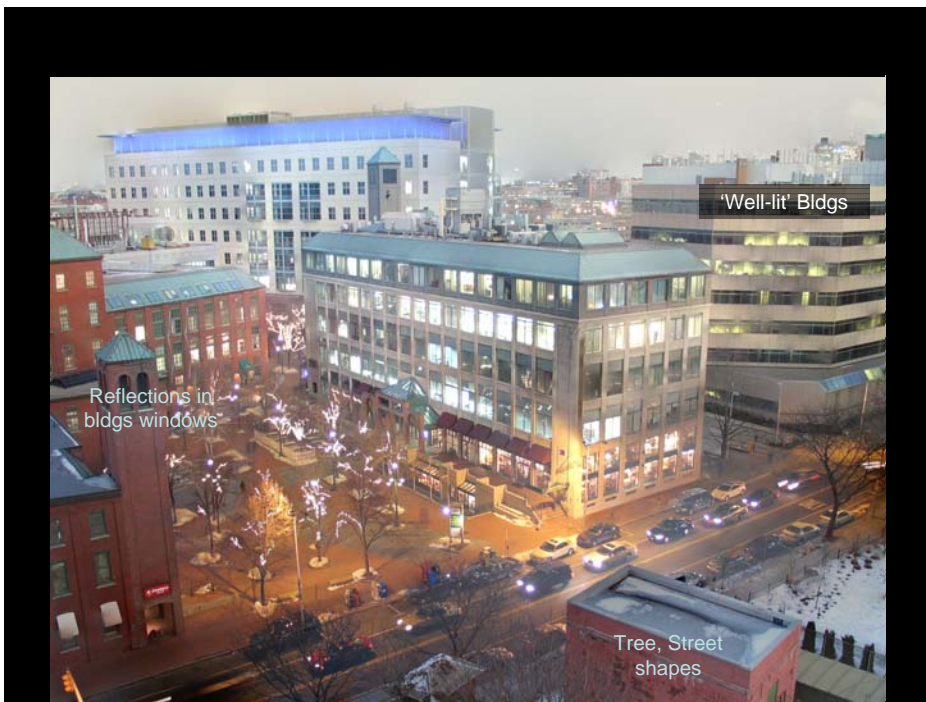
Jingyi Yu

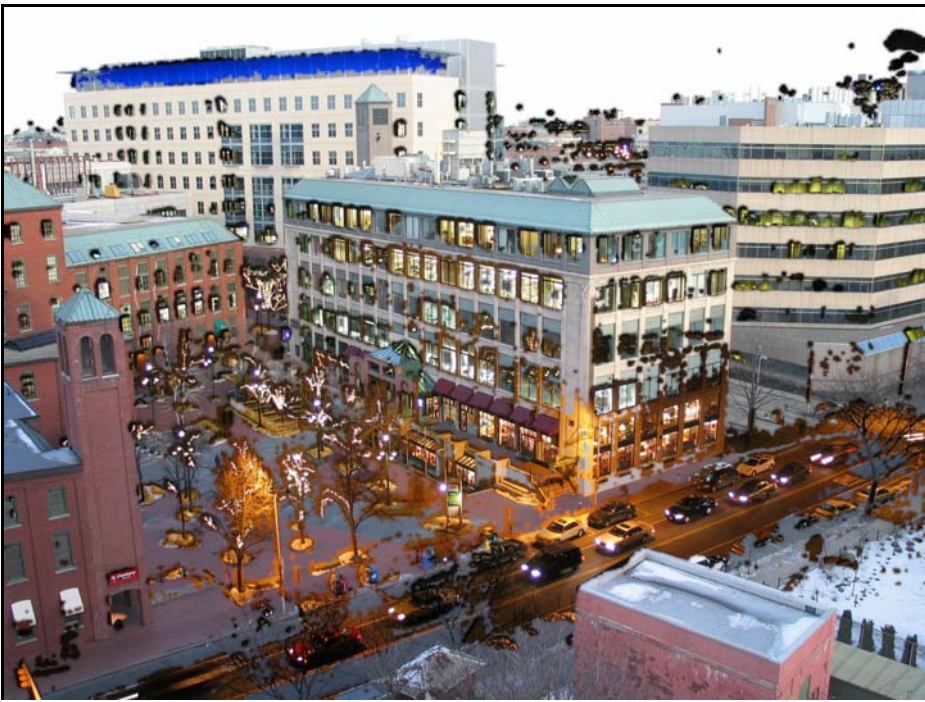
*Mitsubishi Electric  
Research Labs,  
(MERL)*

*UNC Chapel Hill*

*MIT*







DigiVFX

Nighttime image

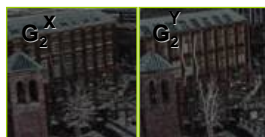
Gradient field



Importance image W



Daytime image



Gradient field



DigiVFX

## Reconstruction from Gradient Field

- Problem: minimize error  $|\nabla I' - G|$
- Estimate  $I'$  so that

$$G = \nabla I'$$

- Poisson equation

$$\nabla^2 I' = \text{div } G$$

- Full multigrid solver



# Poisson Image Editing: Inserting Objects

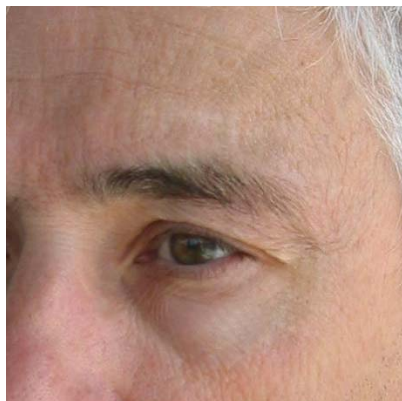
- Precise selection: tedious and unsatisfactory
- Alpha-Matting: powerful but involved
- **Seamless cloning**: loose selection but no seams?



# Smooth Correction: Copying Gradients

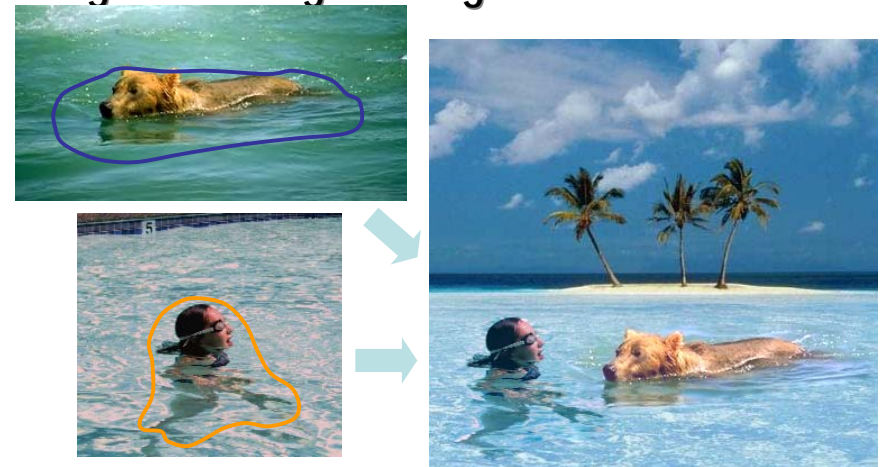


# Conceal



Copy Background gradients (user strokes)

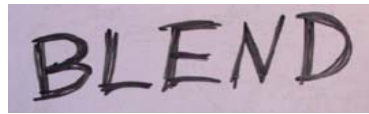
# Compose: Copy gradients from Source Images to Target Image



Source Images

Target Image

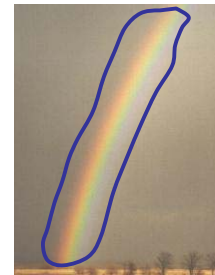
## Transparent Cloning



$$\mathbf{v} = \frac{\nabla f^* + \nabla g}{\sqrt{|\nabla f^*|^2 + |\nabla g|^2}}$$

Largest variation from source and destination at each point

## Compose (transparent)

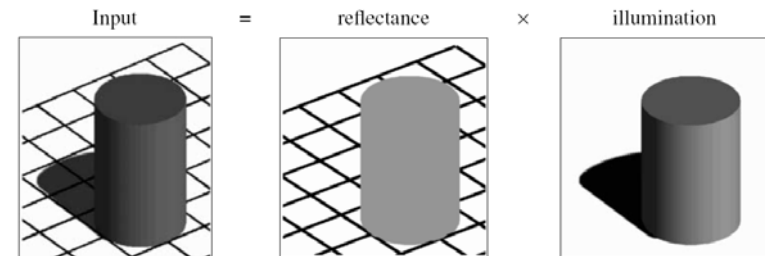


## Gradient Domain Manipulations: Overview

- (A) Per pixel
- (B) Corresponding gradients in two images
- (C) Corresponding gradients in multiple images
- (D) Combining gradients along seams

## Intrinsic images: Median of Gradient operator

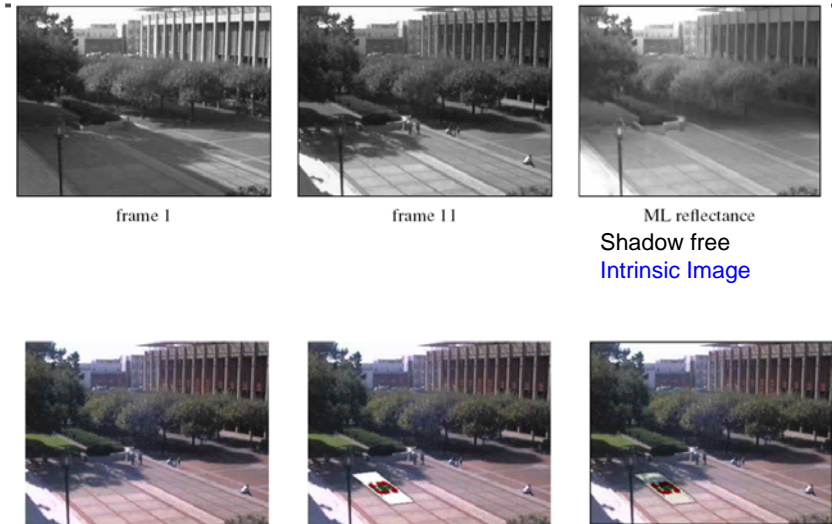
- $I = L * R$
- L = illumination image
- R = reflectance image



# Intrinsic images

- Use multiple images under different illumination
- Assumption
  - Illumination image gradients = Laplacian PDF
  - Under Laplacian PDF, Median = ML estimator
- At each pixel, take Median of gradients across images
- Integrate to remove shadows

Yair Weiss, "Deriving intrinsic images from image sequences", ICCV 2001



Result = Illumination Image \* (Label in Intrinsic Image)

# Specularity Reduction in Active Illumination



Line Specularity Point Specularity Area Specularity

Multiple images with same viewpoint, varying illumination  
How do we remove highlights?



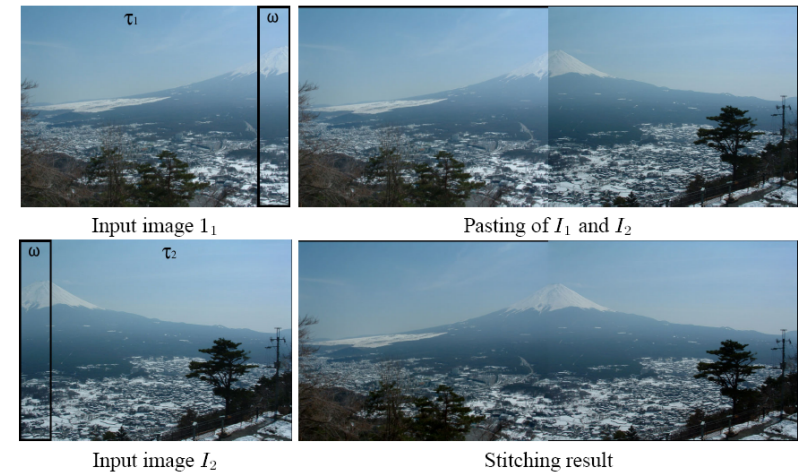
Specularity Reduced Image



## Gradient Domain Manipulations: Overview

- (A) Per pixel
- (B) Corresponding gradients in two images
- (C) Corresponding gradients in multiple images
- (D) [Combining gradients along seams](#)

## Seamless Image Stitching



Anat Levin, Assaf Zomet, Shmuel Peleg and Yair Weiss, "Seamless Image Stitching in the Gradient Domain", ECCV 2004