Bilateral Filters

Digital Visual Effects, Spring 2008 Yung-Yu Chuang 2008/5/27

with slides by Fredo Durand, Ramesh Raskar, Sylvain Paris, Soonmin Bae



Announcements

- Final project proposal
- Project #3 artifacts voting



Bilateral filtering



[Ben Weiss, Siggraph 2006]



Image Denoising



noisy image



naïve denoising Gaussian blur



better denoising edge-preserving filter

Smoothing an image without blurring its edges.



- Diffusion, Bayesian, Wavelets...
 - All have their pros and cons.

- Bilateral filter
 - not always the best result [Buades 05] but often good
 - easy to understand, adapt and set up

Basic denoising



Noisy input Median 5x5

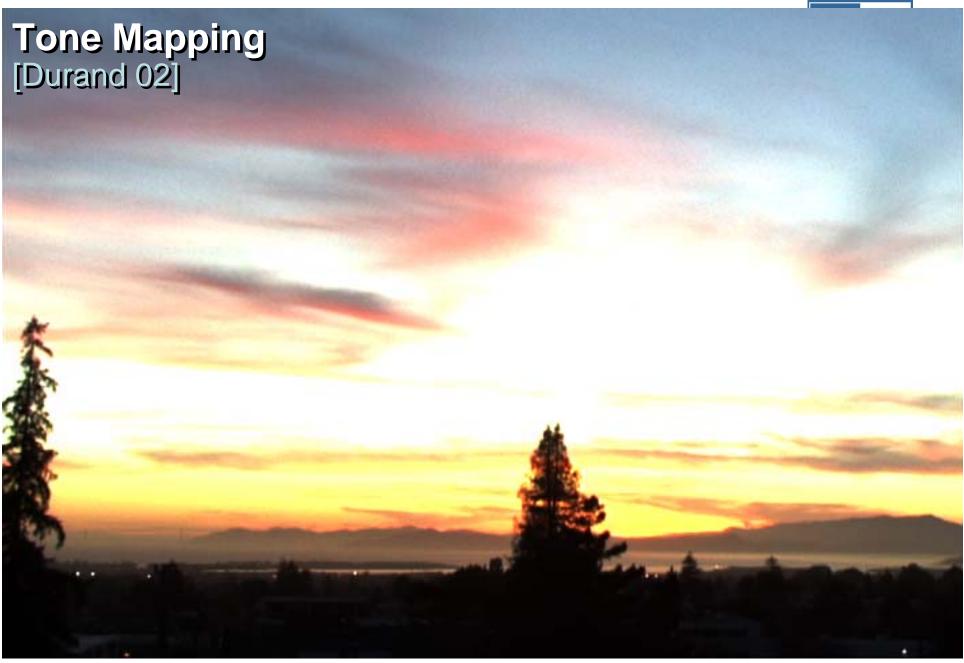
Basic denoising



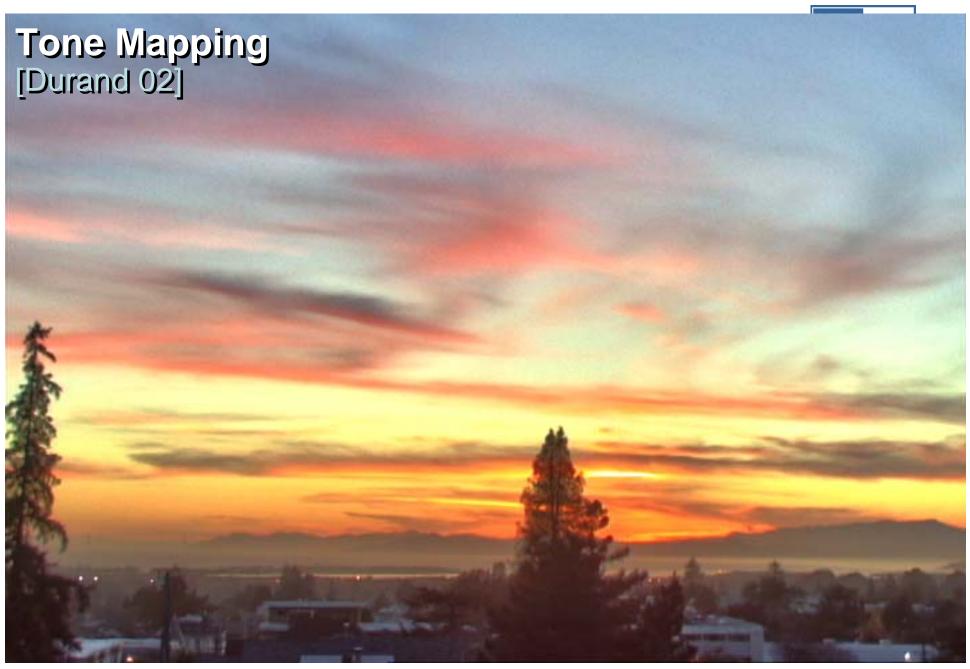
Noisy input

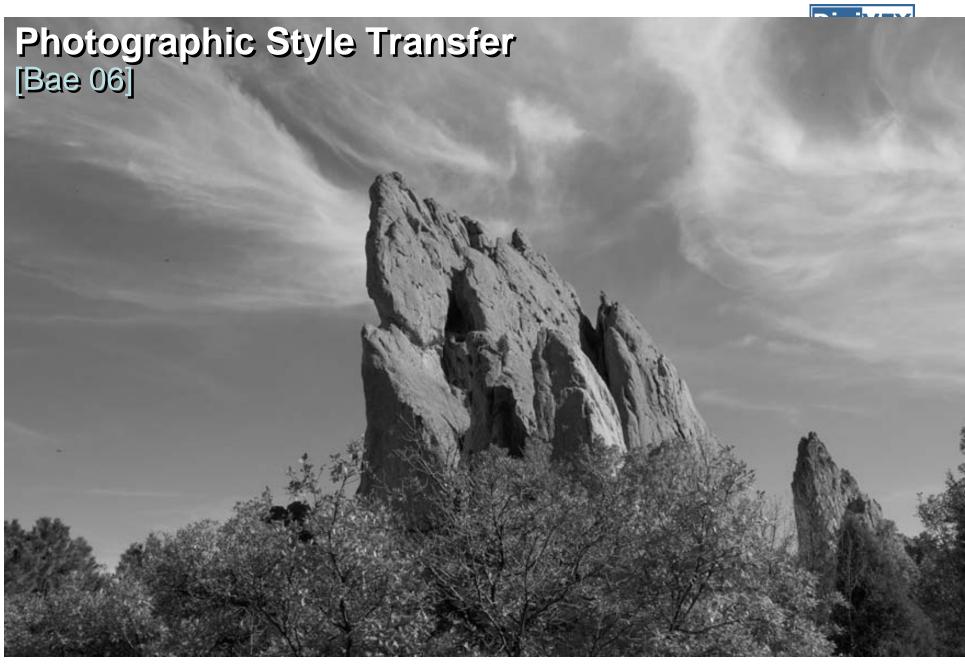
Bilateral filter 7x7 window

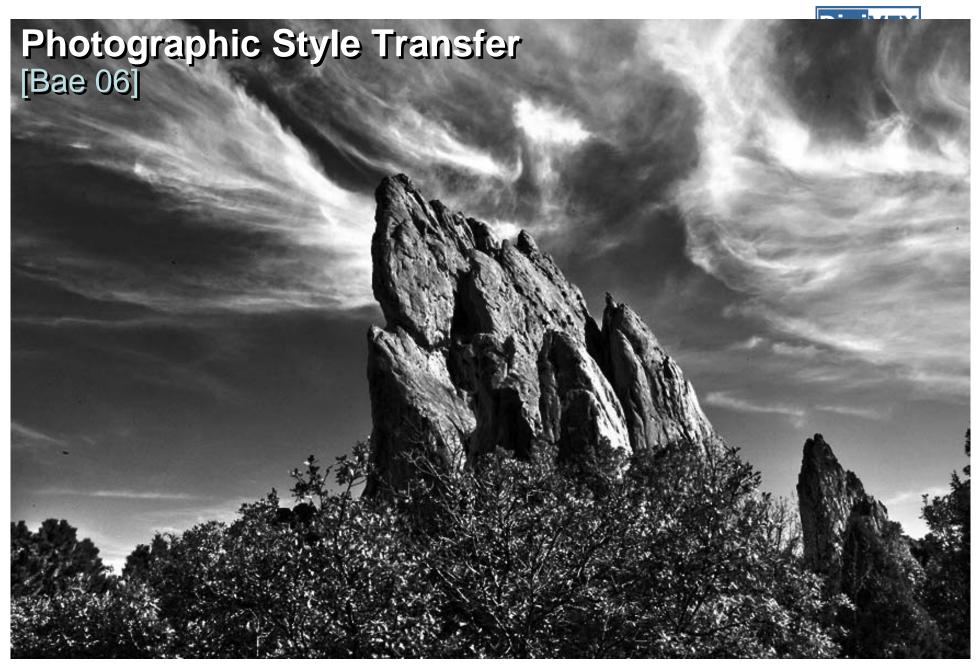




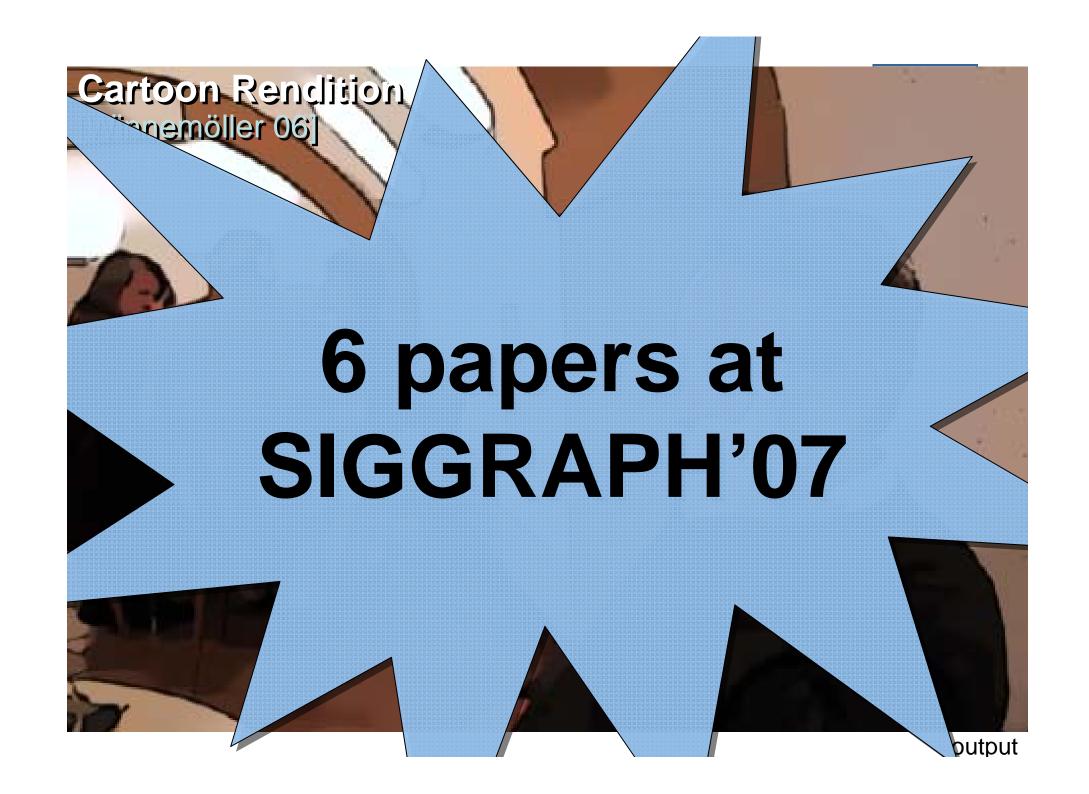
HDR input





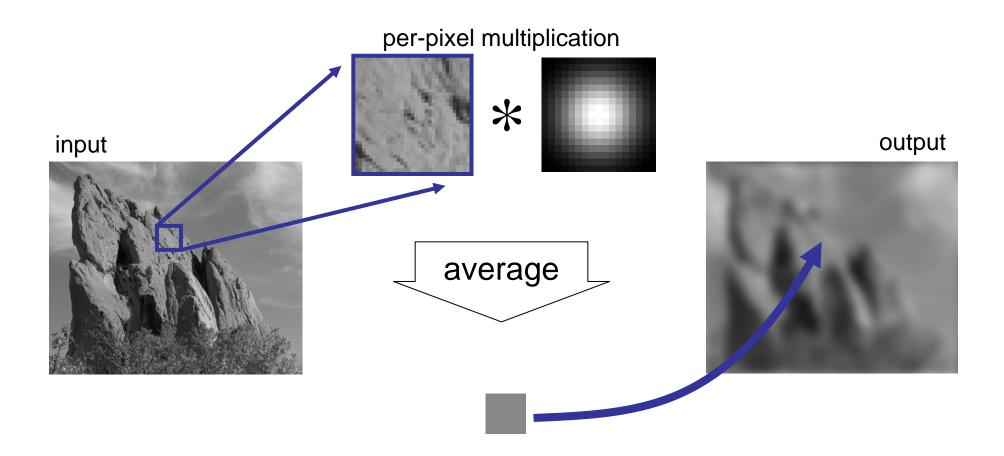


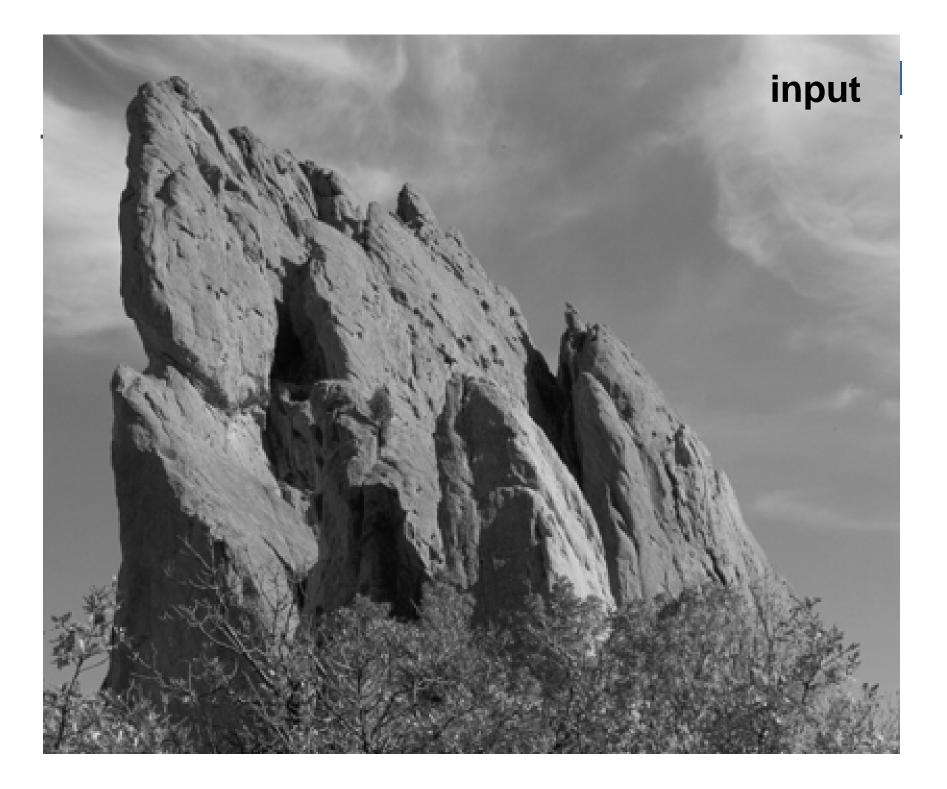












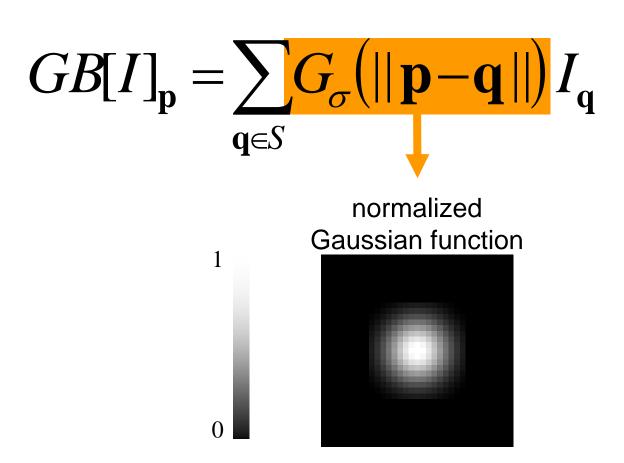


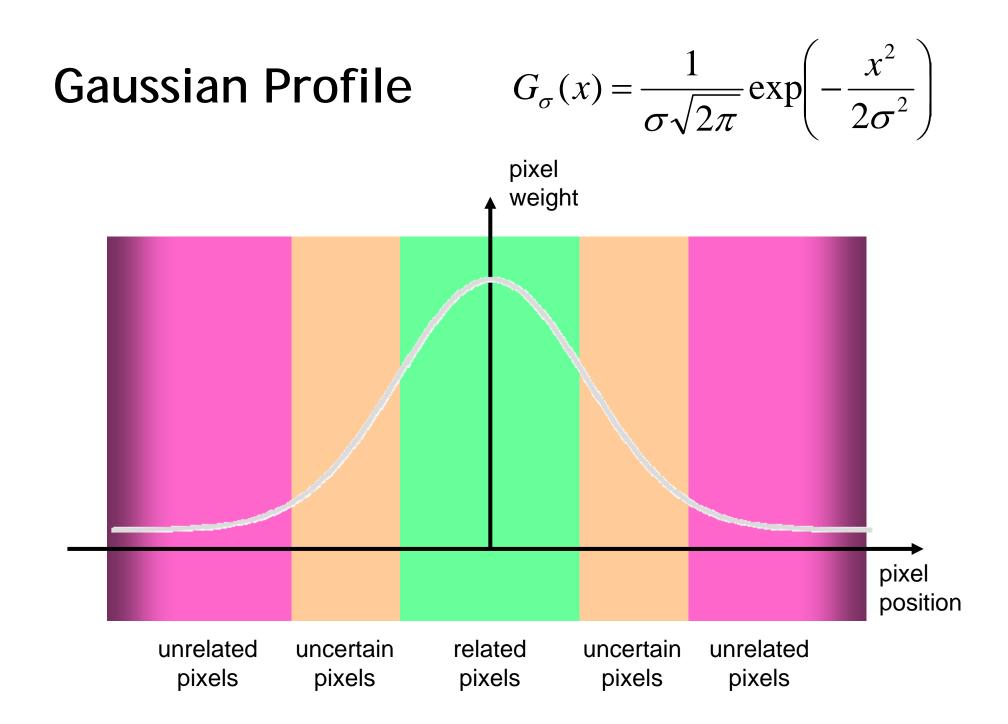


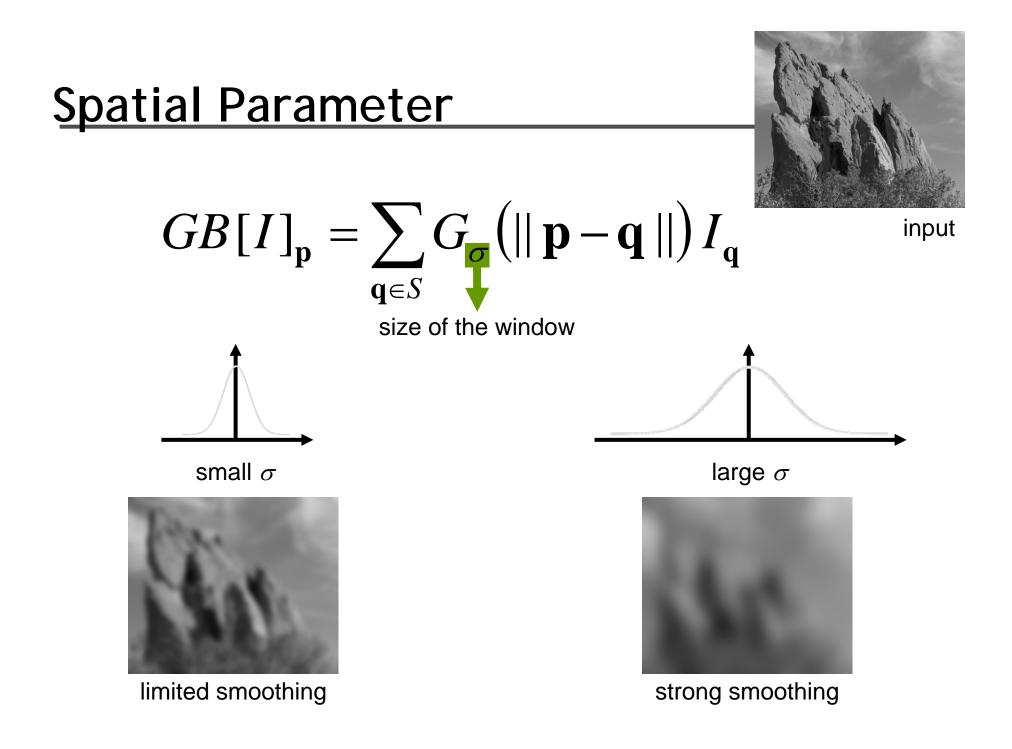


Equation of Gaussian Blur

Same idea: weighted average of pixels.









How to set σ

- Depends on the application.
- Common strategy: proportional to image size
 - e.g. 2% of the image diagonal
 - property: independent of image resolution

Properties of Gaussian Blur



- Weights independent of spatial location
 - linear convolution
 - well-known operation
 - efficient computation (recursive algorithm, FFT...)

Properties of Gaussian Blur

- Does smooth images
- But smoothes too much: edges are blurred.
 - Only spatial distance matters
 - No edge term





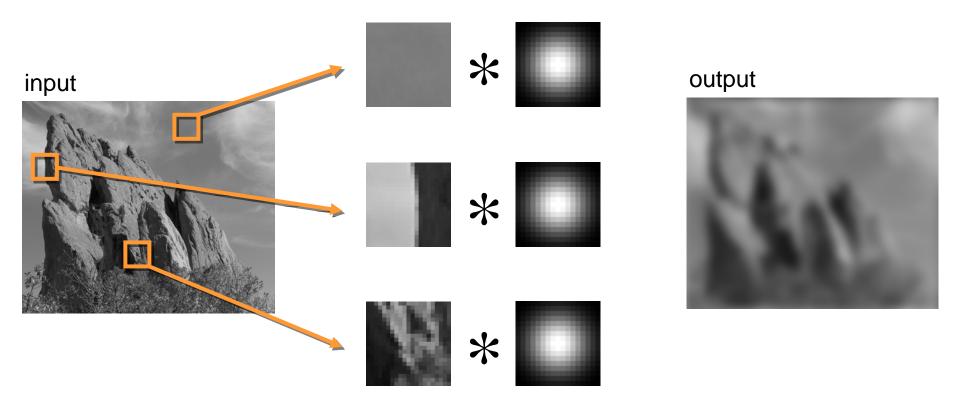


$$GB[I]_{\mathbf{p}} = \sum_{\mathbf{q}\in S} \frac{G_{\sigma}(\|\mathbf{p}-\mathbf{q}\|)}{S_{\mathbf{q}}} I_{\mathbf{q}}$$

input

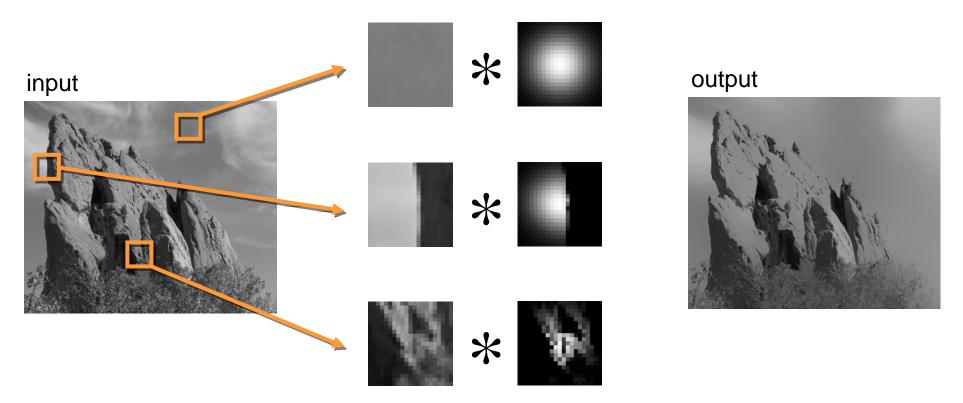


Blur Comes from Averaging across Edges



Same Gaussian kernel everywhere.





The kernel shape depends on the image content.



Bilateral Filter Definition

Same idea: weighted average of pixels.

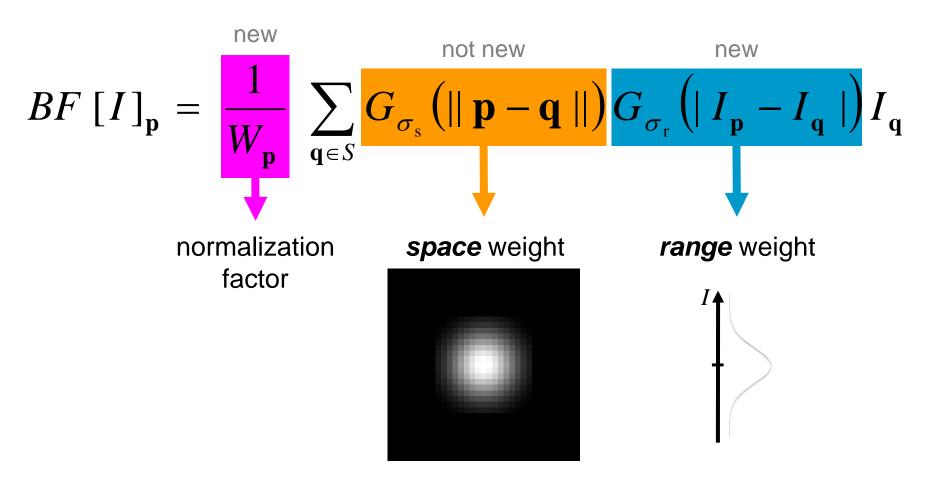


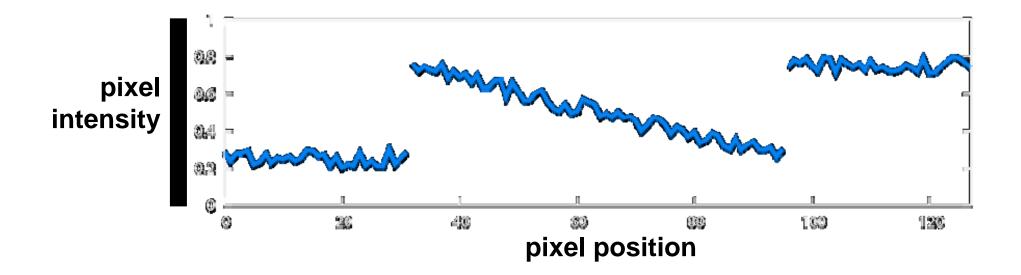
Illustration a 1D Image



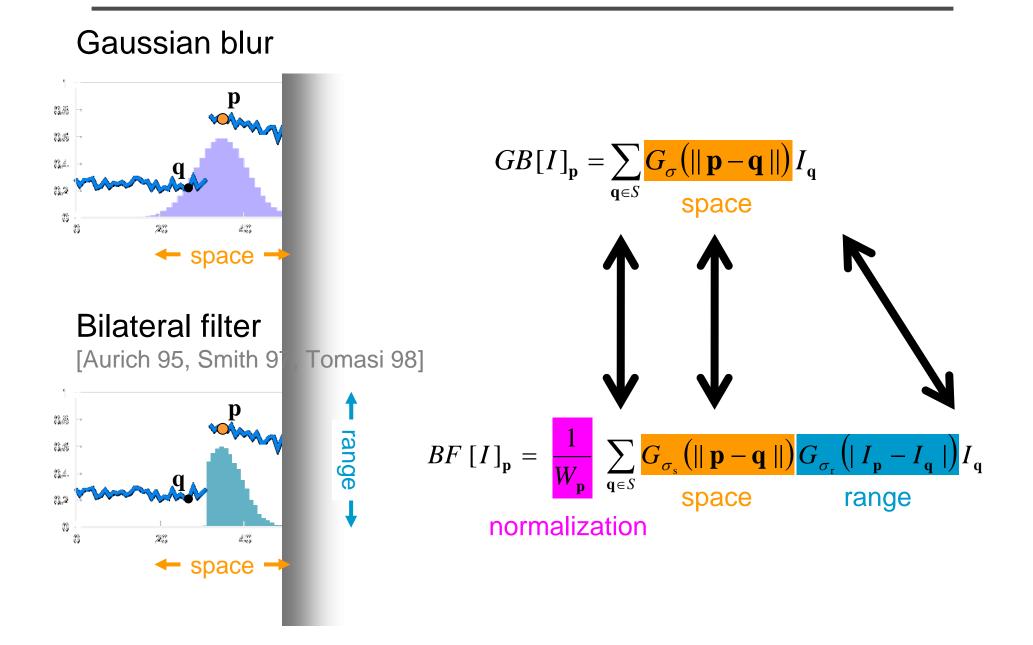
• 1D image = line of pixels



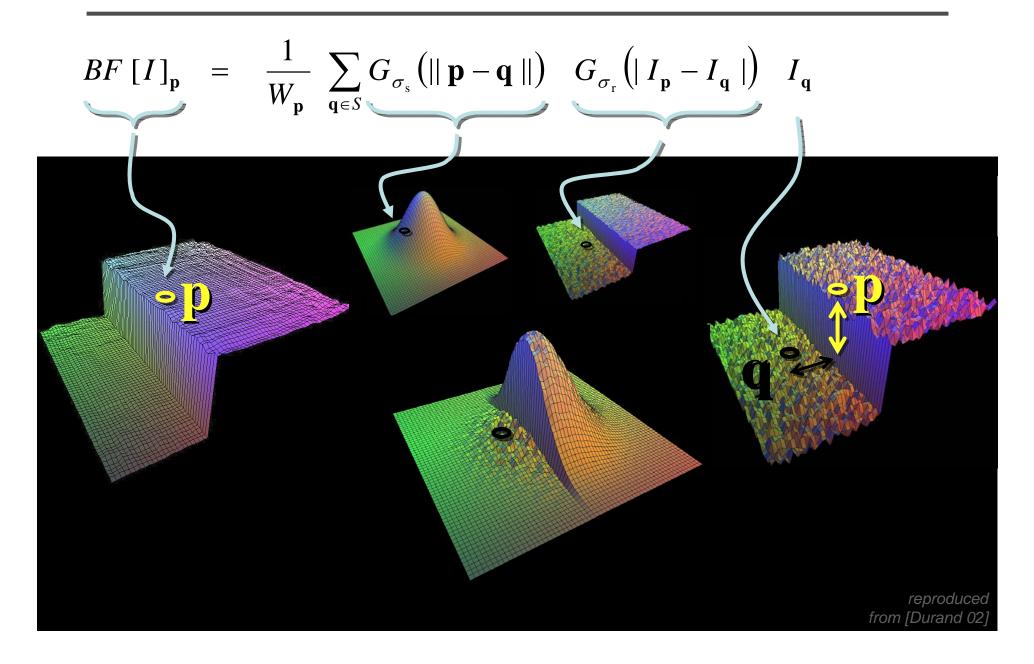
• Better visualized as a plot



Gaussian Blur and Bilateral Filter









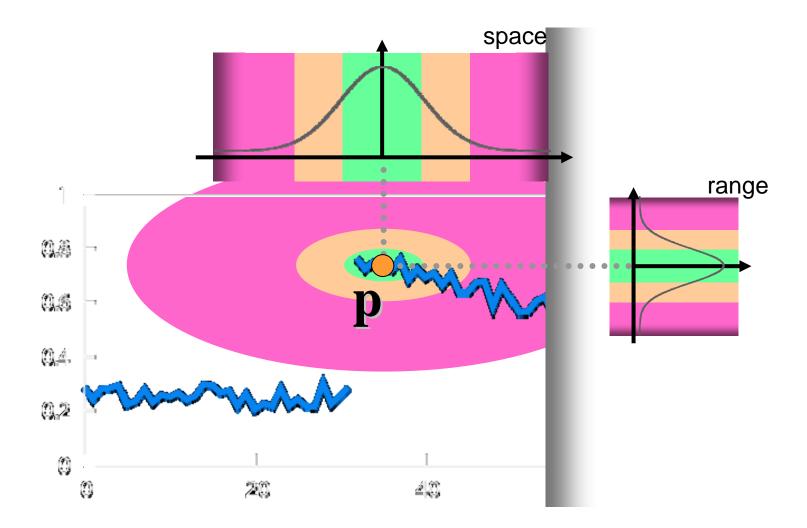
$$BF[I]_{\mathbf{p}} = \frac{1}{W_{\mathbf{p}}} \sum_{\mathbf{q} \in S} G_{\sigma_{s}} (\|\mathbf{p} - \mathbf{q}\|) G_{\sigma_{r}} (\|I_{\mathbf{p}} - I_{\mathbf{q}}\|) I_{\mathbf{q}}$$

- space σ_s : spatial extent of the kernel, size of the considered neighborhood.
- range $\sigma_{\rm r}$: "minimum" amplitude of an edge

Influence of Pixels



Only pixels close in space and in range are considered.





input

 $\sigma_{s} = 2$

Exploring the Parameter Space

 $\sigma_{\rm r} = \infty$ (Gaussian blur) $\sigma_{\rm r} = 0.1$ $\sigma_{\rm r} = 0.25$ $\sigma_{\rm s} = 6$ 8

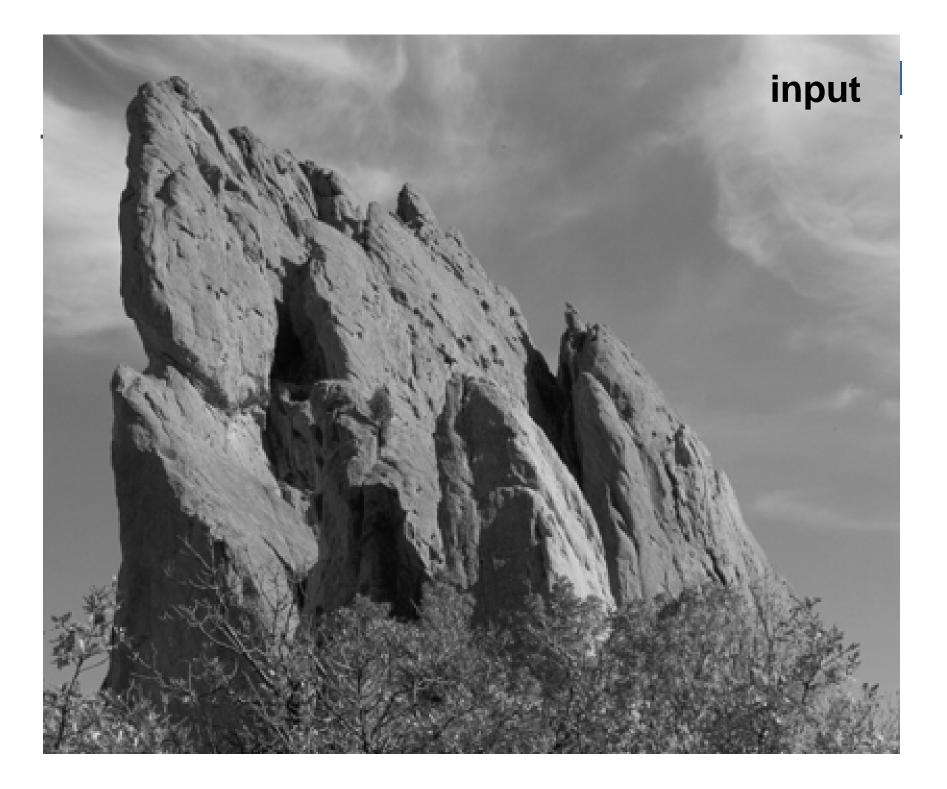
$$\sigma_{s} = 18$$



input

$$\sigma_{\rm r} = 0.1$$

$$\sigma_{\rm r} = 0.25$$
(Gaussian blur)
(Gaussian bl



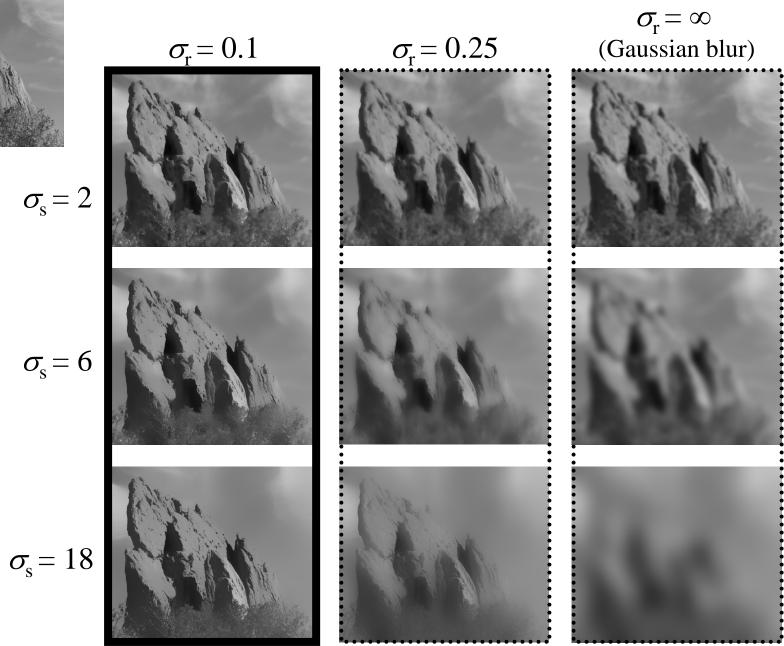


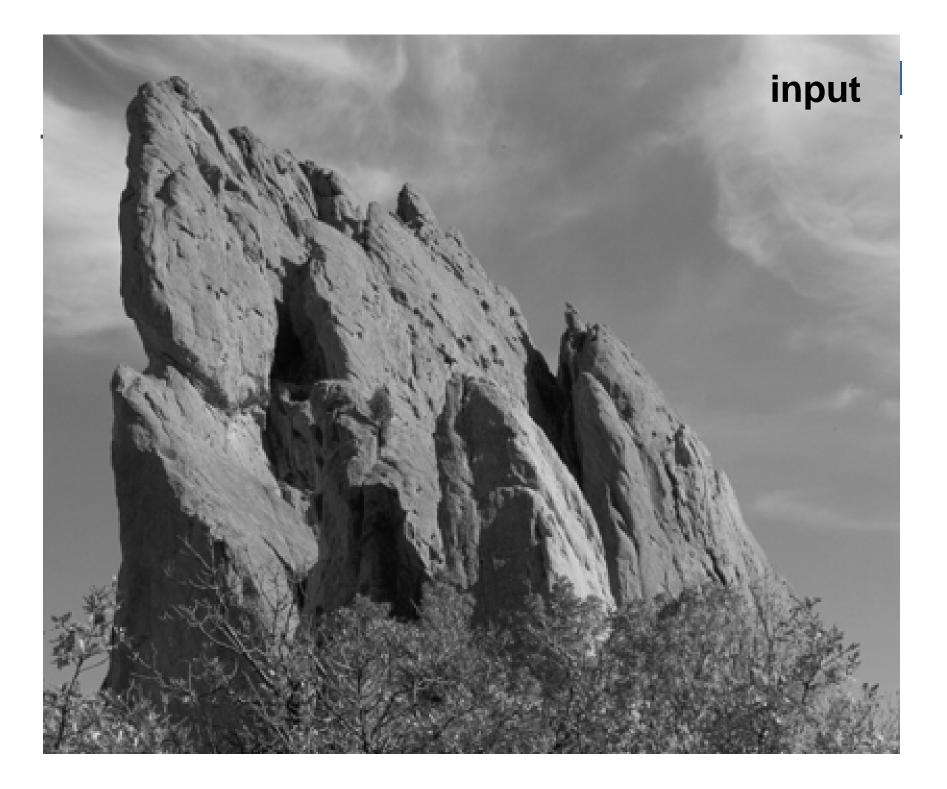






input













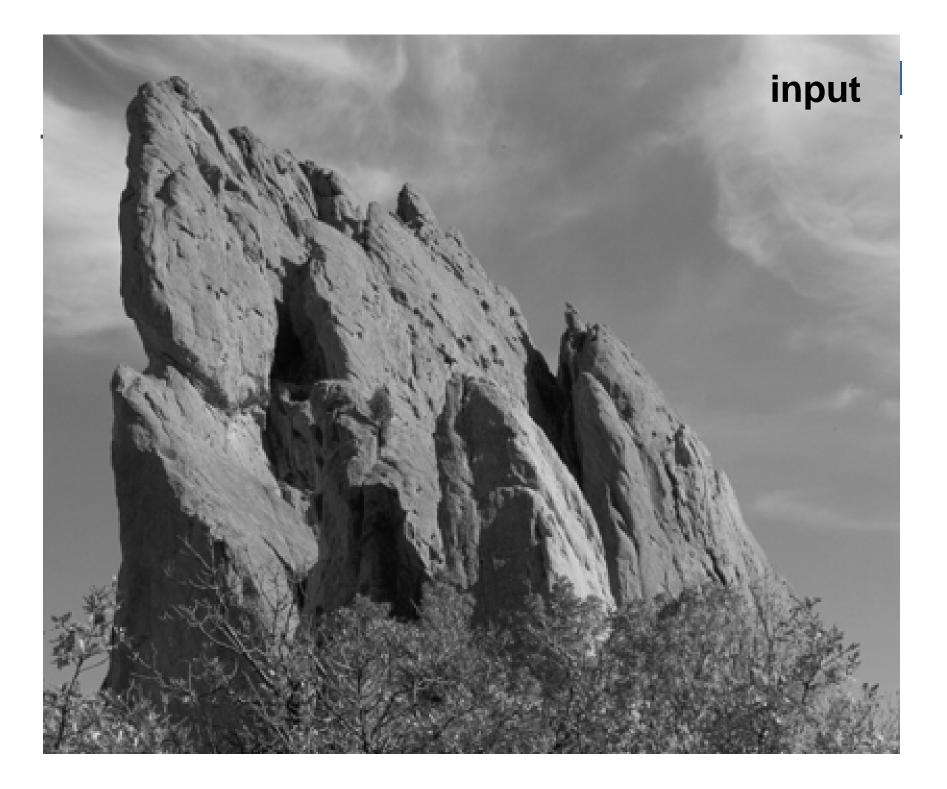
Depends on the application. For instance:

- space parameter: proportional to image size
 - e.g., 2% of image diagonal
- range parameter: proportional to edge amplitude
 - e.g., mean or median of image gradients
- independent of resolution and exposure



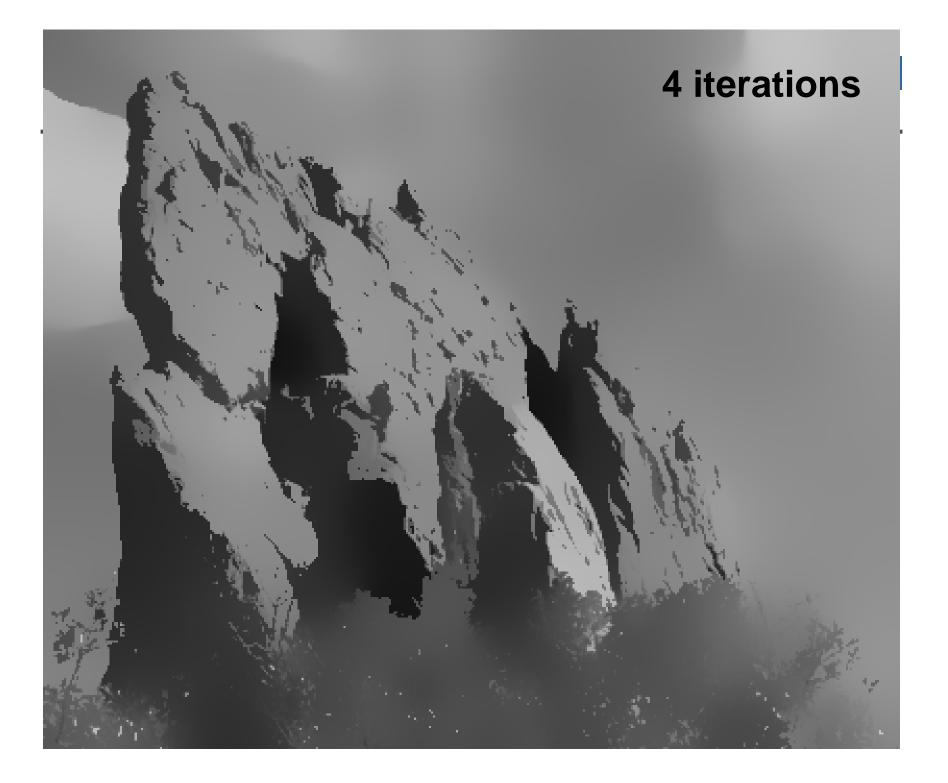
$$I_{(n+1)} = BF[I_{(n)}]$$

- Generate more piecewise-flat images
- Often not needed in computational photo, but could be useful for applications such as NPR.











Advantages of Bilateral Filter

- Easy to understand
 - Weighted mean of nearby pixels
- Easy to adapt
 - Distance between pixel values
- Easy to set up
 - Non-iterative

Hard to Compute



- Nonlinear $BF[I]_{\mathbf{p}} = \frac{1}{W_{\mathbf{p}}} \sum_{\mathbf{q} \in S} G_{\sigma_s} (\|\mathbf{p} \mathbf{q}\|) G_{\sigma_r} (|I_{\mathbf{p}} I_{\mathbf{q}}|) I_{\mathbf{q}}$
- Complex, spatially varying kernels
 - Cannot be precomputed, no FFT...



• Brute-force implementation is slow > 10min





- Slow but some accelerations exist:
 - [Elad 02]: Gauss-Seidel iterations
 - Only for many iterations

- [Durand 02, Weiss 06]: fast approximation
 - No formal understanding of accuracy versus speed
 - [Weiss 06]: Only box function as spatial kernel

A Fast Approximation of the Bilateral Filter using a Signal Processing Approach

Sylvain Paris and Frédo Durand

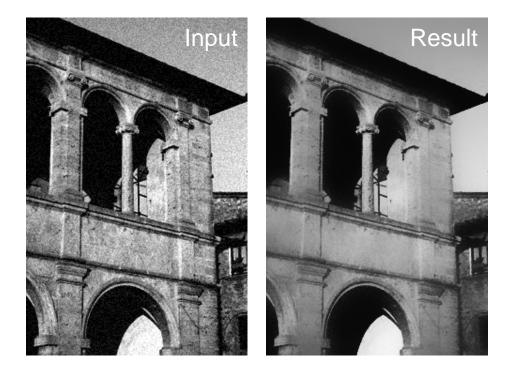
Computer Science and Artificial Intelligence Laboratory Massachusetts Institute of Technology





Definition of Bilateral Filter

- [Smith 97, Tomasi 98]
- Smoothes an image and preserves edges
- Weighted average of neighbors
- Weights
 - Gaussian on *space* distance
 - Gaussian on *range* distance
 - sum to 1

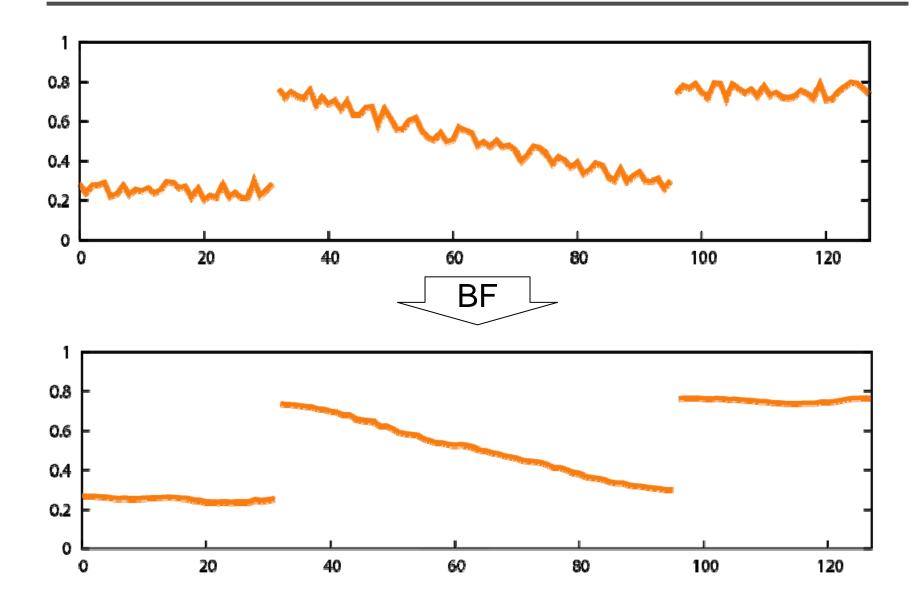


$$I_{\mathbf{p}}^{\mathrm{bf}} = \frac{1}{W_{\mathbf{p}}^{\mathrm{bf}}} \sum_{\mathbf{q} \in \mathcal{S}} G_{\sigma_{\mathrm{s}}}(\|\mathbf{p} - \mathbf{q}\|) G_{\sigma_{\mathrm{r}}}(|I_{\mathbf{p}} - I_{\mathbf{q}}|) I_{\mathbf{q}}$$



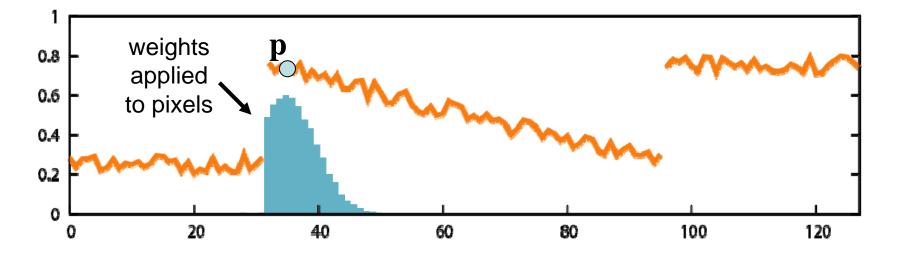
- Link with **linear filtering**
- Fast and accurate approximation





Intuition on 1D Signal Weighted Average of Neighbors

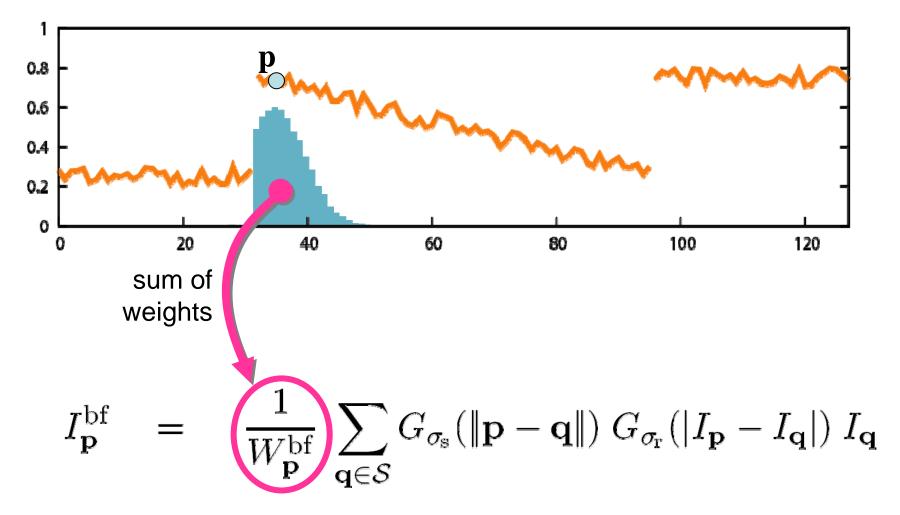




- Near and similar pixels have influence.
- Far pixels have no influence.
- Pixels with different value have no influence.

Link with Linear Filtering 1. Handling the Division





Handling the division with a **projective space**.



Formalization: Handling the Division

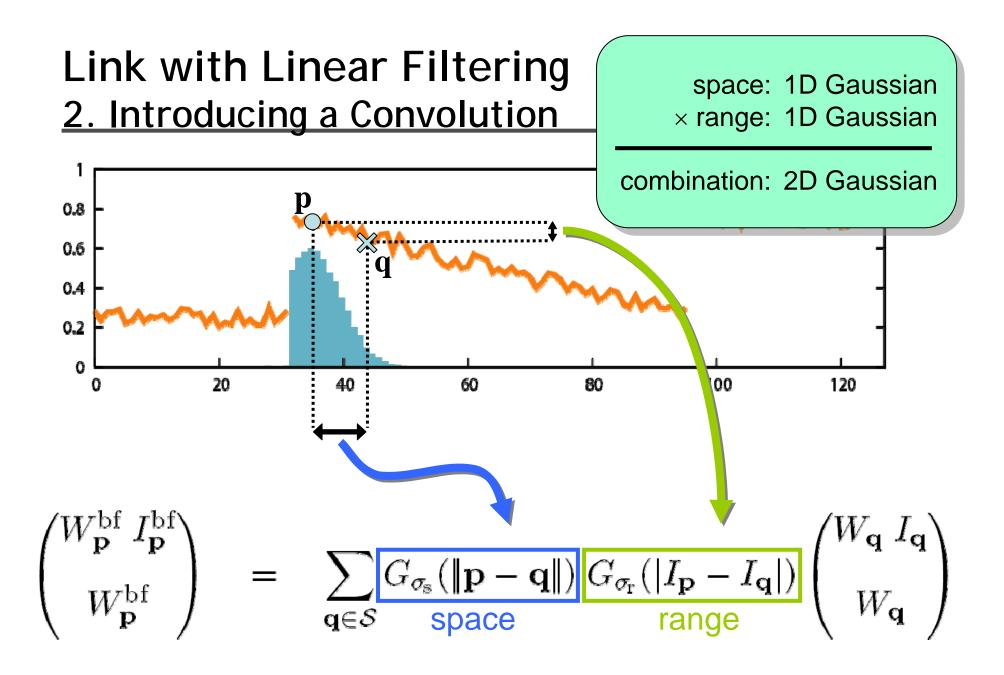
$$I_{\mathbf{p}}^{\mathrm{bf}} = \frac{1}{W_{\mathbf{p}}^{\mathrm{bf}}} \sum_{\mathbf{q}\in\mathcal{S}} G_{\sigma_{\mathrm{s}}}(\|\mathbf{p}-\mathbf{q}\|) G_{\sigma_{\mathrm{r}}}(|I_{\mathbf{p}}-I_{\mathbf{q}}|) I_{\mathbf{q}}$$
$$W_{\mathbf{p}}^{\mathrm{bf}} = \sum_{\mathbf{q}\in\mathcal{S}} G_{\sigma_{\mathrm{s}}}(\|\mathbf{p}-\mathbf{q}\|) G_{\sigma_{\mathrm{r}}}(|I_{\mathbf{p}}-I_{\mathbf{q}}|)$$

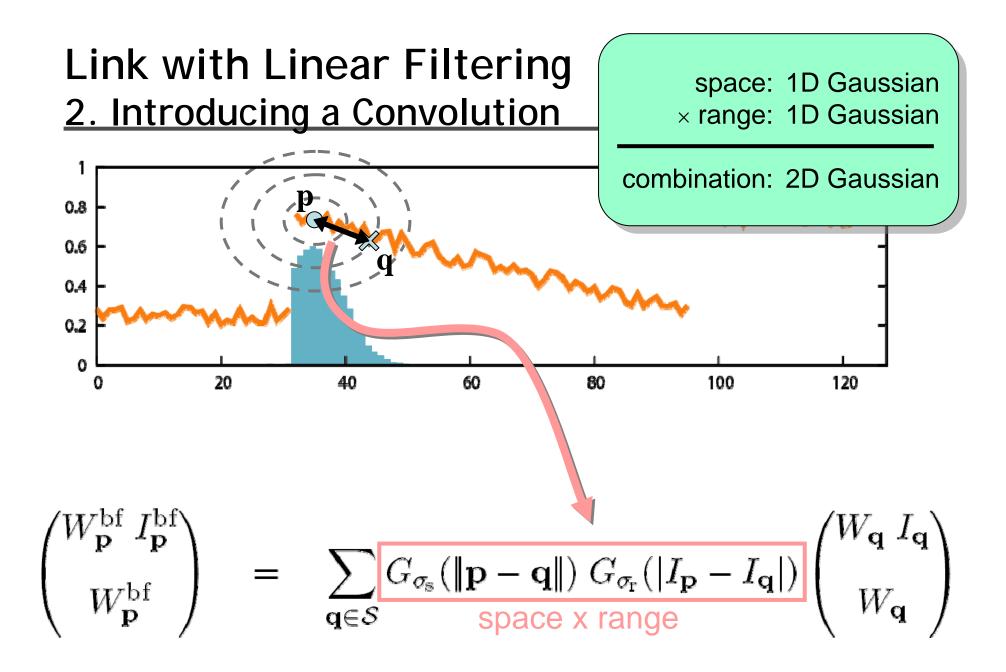
$$\begin{pmatrix}
W_{\mathbf{p}}^{\mathrm{bf}} I_{\mathbf{p}}^{\mathrm{bf}} \\
W_{\mathbf{p}}^{\mathrm{bf}}
\end{pmatrix} = \sum_{\mathbf{q}\in\mathcal{S}} G_{\sigma_{\mathrm{s}}}(\|\mathbf{p}-\mathbf{q}\|) G_{\sigma_{\mathrm{r}}}(|I_{\mathbf{p}}-I_{\mathbf{q}}|) \begin{pmatrix}
I_{\mathbf{q}} \\
1
\end{pmatrix}$$



$$\begin{pmatrix} W_{\mathbf{p}}^{\mathrm{bf}} I_{\mathbf{p}}^{\mathrm{bf}} \\ W_{\mathbf{p}}^{\mathrm{bf}} \end{pmatrix} = \sum_{\mathbf{q} \in \mathcal{S}} G_{\sigma_{\mathrm{s}}}(\|\mathbf{p} - \mathbf{q}\|) G_{\sigma_{\mathrm{r}}}(|I_{\mathbf{p}} - I_{\mathbf{q}}|) \begin{pmatrix} W_{\mathbf{q}} I_{\mathbf{q}} \\ W_{\mathbf{q}} \end{pmatrix} \text{ with } W_{\mathbf{q}} = 1$$

- Similar to homogeneous coordinates in projective space
- Division delayed until the end
- Next step: Adding a dimension to make a convolution appear

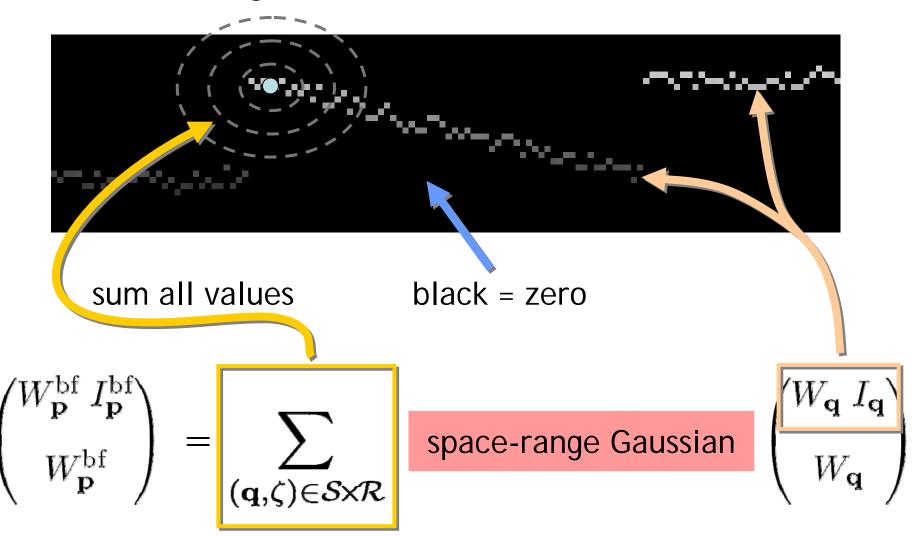




Corresponds to a 3D Gaussian on a 2D image.

Link with Linear Filtering 2. Introducing a Convolution

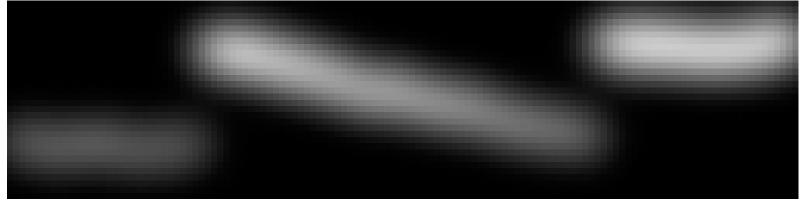




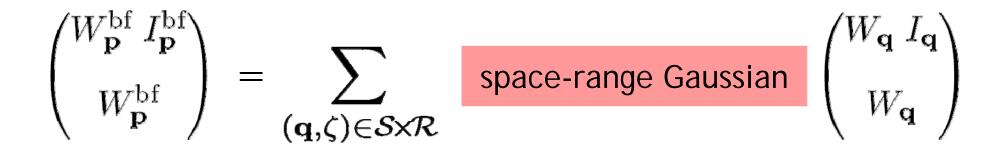
sum all values multiplied by kernel ⇒ convolution

Link with Linear Filtering 2. Introducing a Convolution



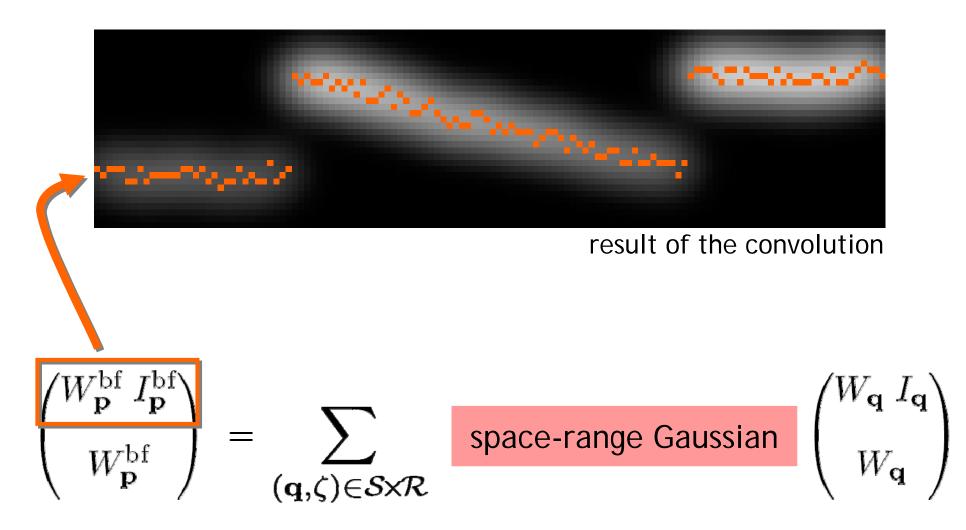


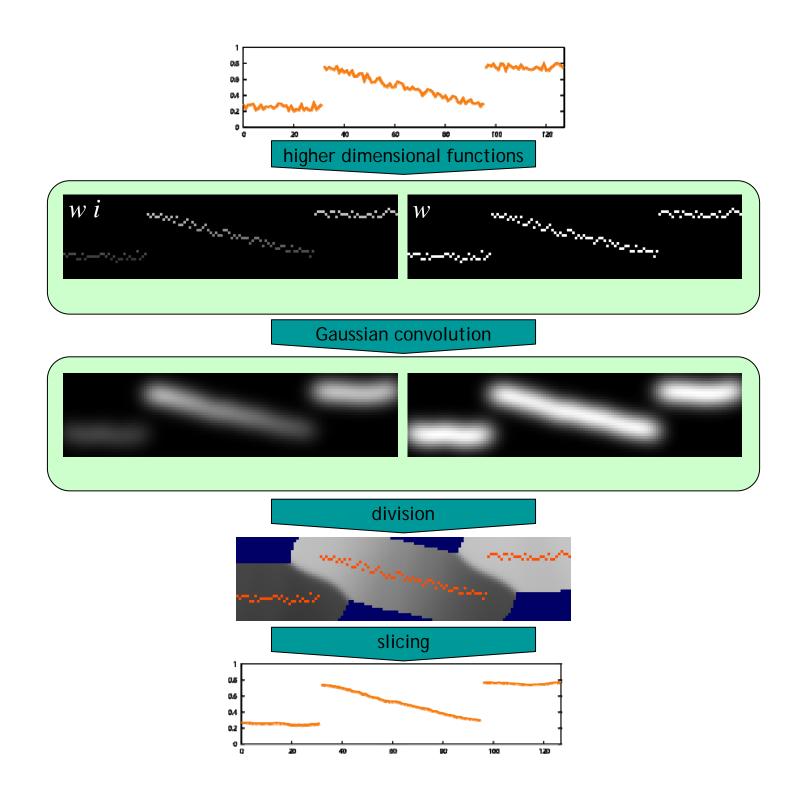
result of the convolution



Link with Linear Filtering 2. Introducing a Convolution





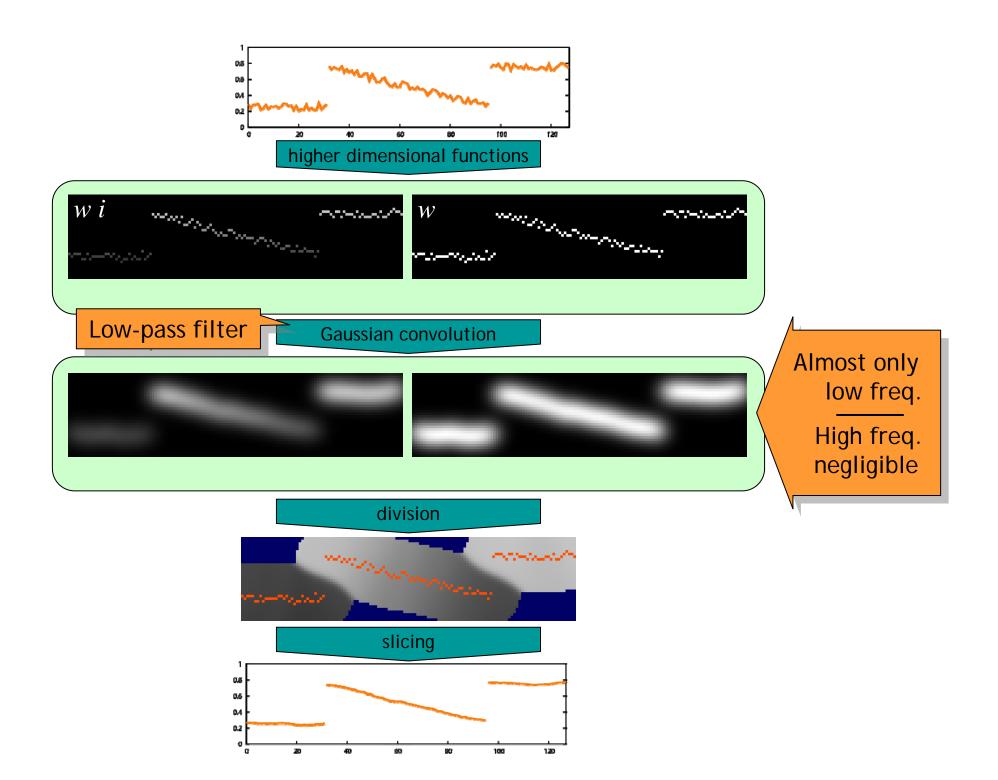


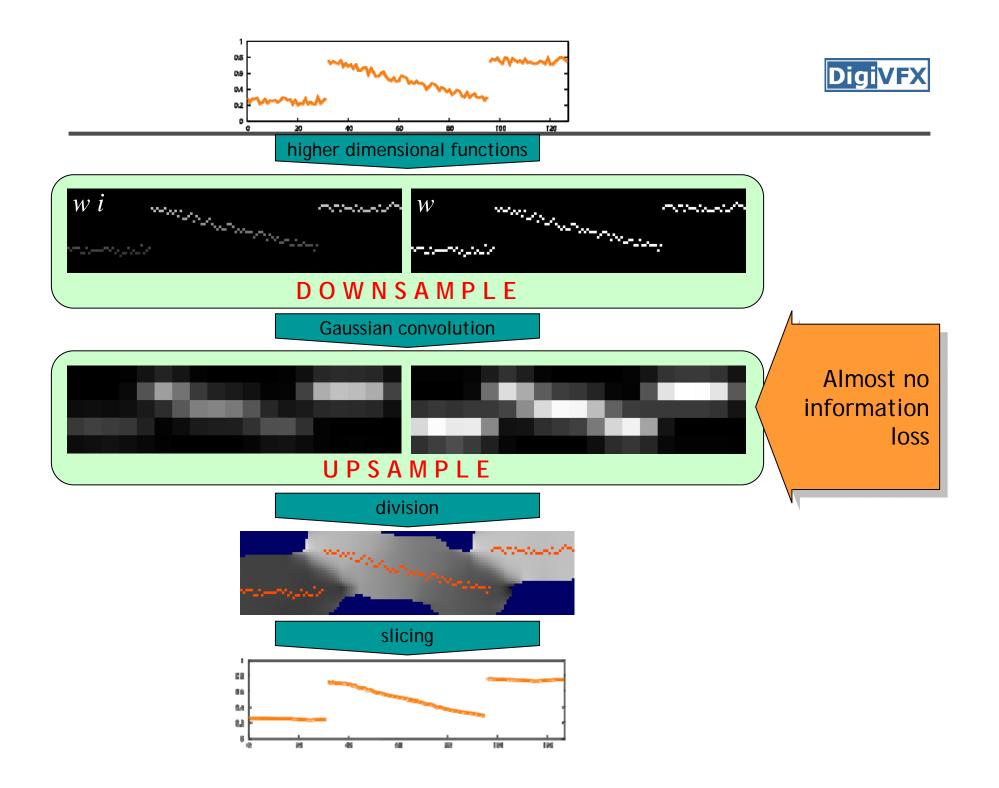
Reformulation: Summary



- 1. Convolution in higher dimension
 - expensive but well understood (linear, FFT, etc)
- 2. Division and slicing
 - nonlinear but simple and pixel-wise

Exact reformulation



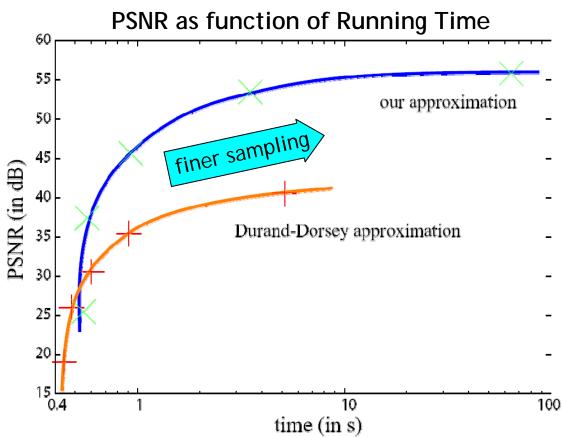




- Downsampling cuts frequencies above Nyquist limit
 - Less data to process
 - But induces error
- Evaluation of the approximation
 - Precision versus running time
 - Visual accuracy

Accuracy versus Running Time

- Finer sampling increases accuracy.
- More precise than previous work.





Digital photograph 1200 × 1600

- Straightforward
- implementation is
- over 10 minutes.

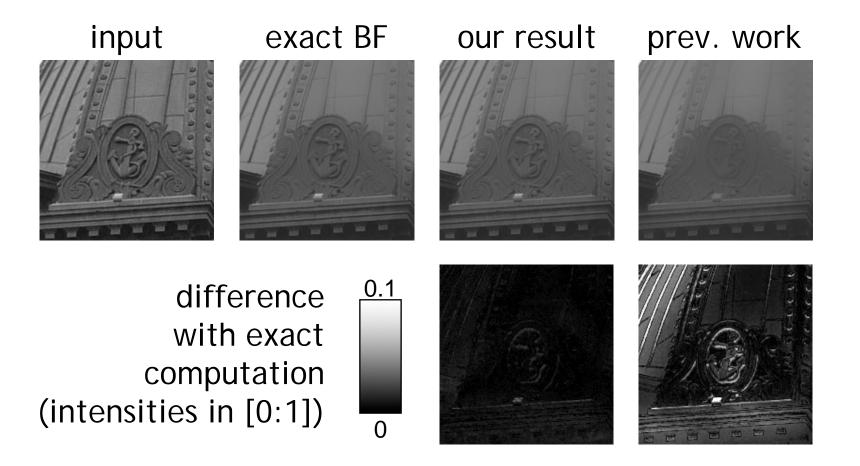


Visual Results

- Comparison with previous work [Durand 02]
 - running time = 1s for both techniques



 1200×1600





higher dimension ⇒ "better" computation

Practical gain

- Interactive running time
- Visually similar results
- Simple to code (100 lines)

Theoretical gain

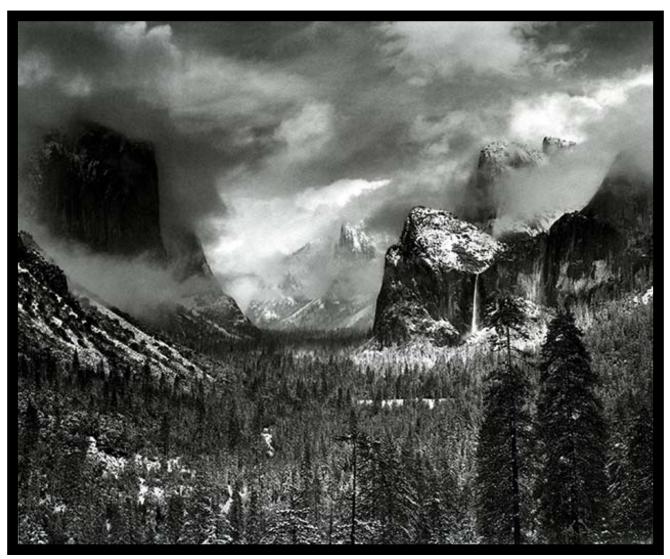
- Link with linear filters
- Separation linear/nonlinear
- Signal processing framework



Two-scale Tone Management for Photographic Look Soonmin Bae, Sylvain Paris, and Frédo Durand MIT CSAIL

SIGGRAPH2006

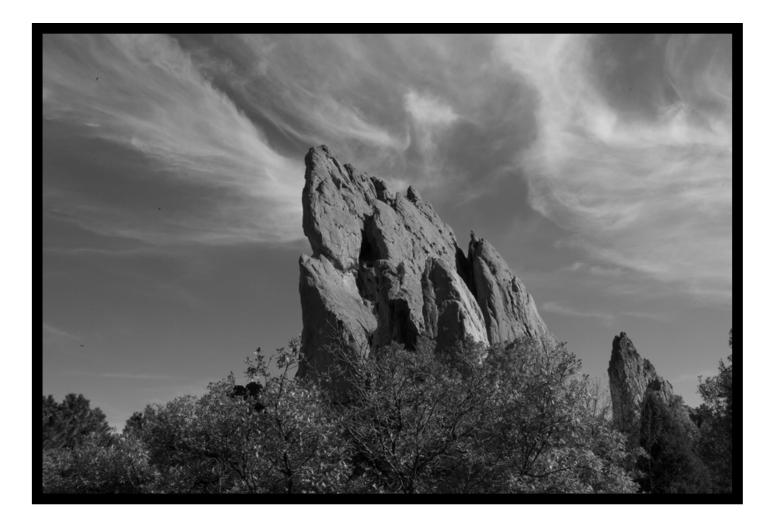




Ansel Adams, Clearing Winter Storm

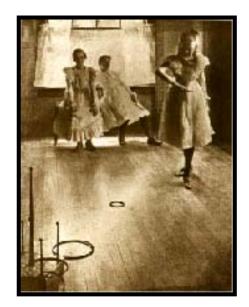
An Amateur Photographer







A Variety of Looks











- Control over photographic look
- Transfer "look" from a model photo

For example,

we want



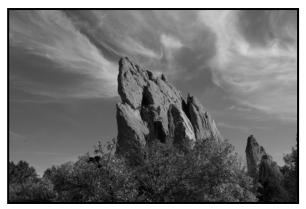
with the look of





Aspects of Photographic Look

- Subject choice
- Framing and composition
- ➔ Specified by input photos
- Tone distribution and contrast
- →Modified based on model photos



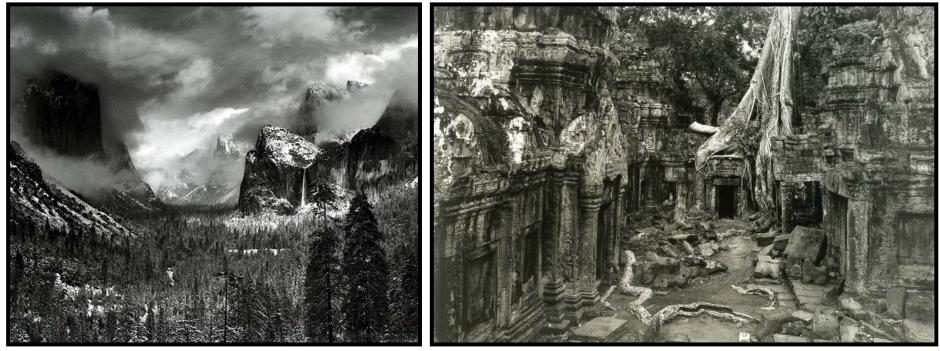
Input



Model







Kenro Izu



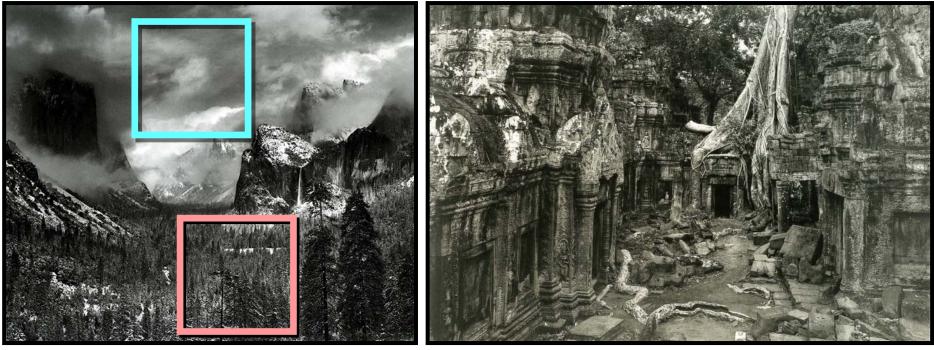


Kenro Izu

High Global Contrast

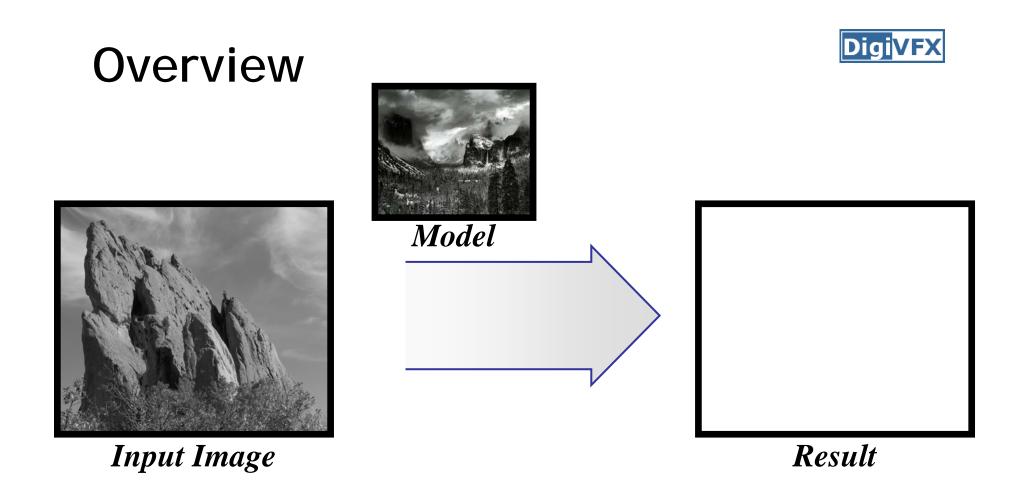
Low Global Contrast



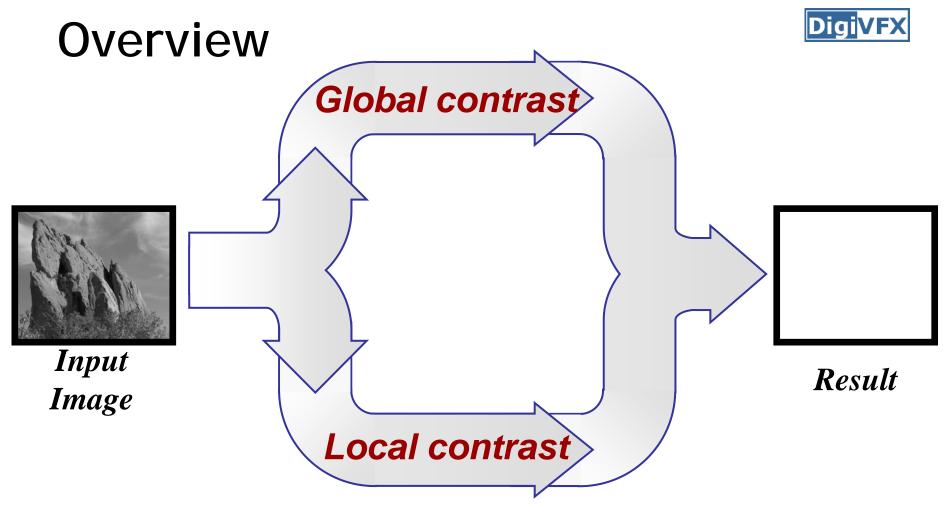


Kenro Izu

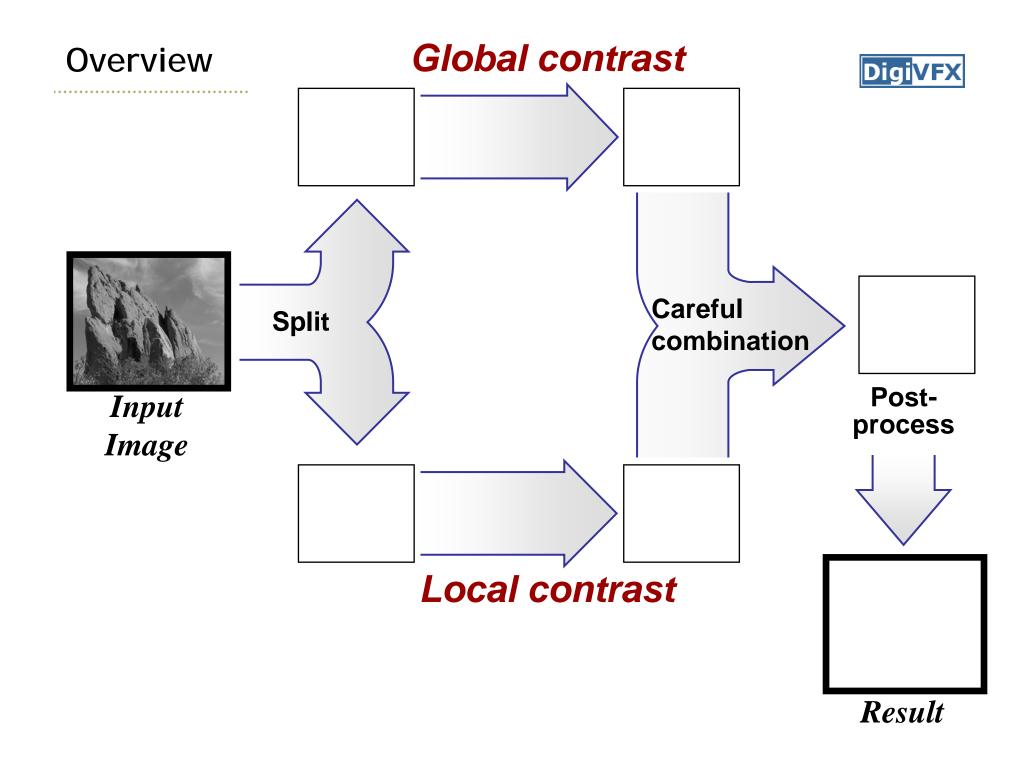
Variable amount of texture Texture everywhere

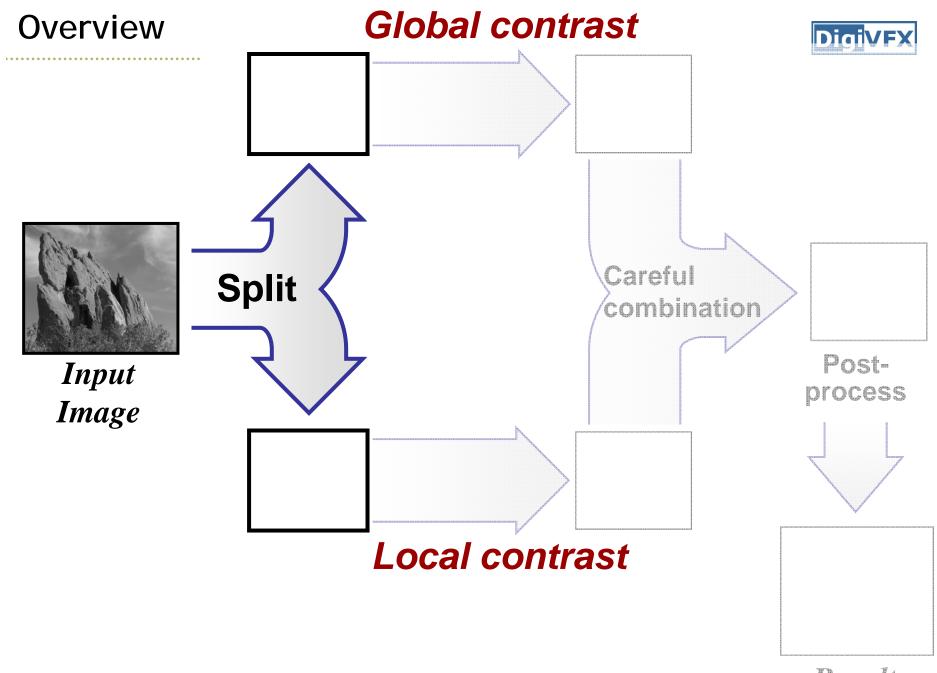


- Transfer look between photographs
 - Tonal aspects



• Separate global and local contrast





Result

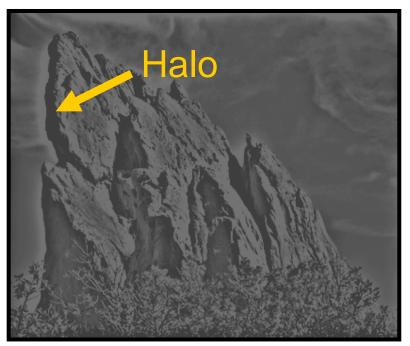
Split Global vs. Local Contrast



- Naïve decomposition: low vs. high frequency
 - Problem: introduce blur & halos



Low frequency Global contrast



High frequency Local contrast

Bilateral Filter



- Edge-preserving smoothing [Tomasi 98]
- We build upon tone mapping [Durand 02]



After bilateral filtering Global contrast



Residual after filtering Local contrast

Bilateral Filter



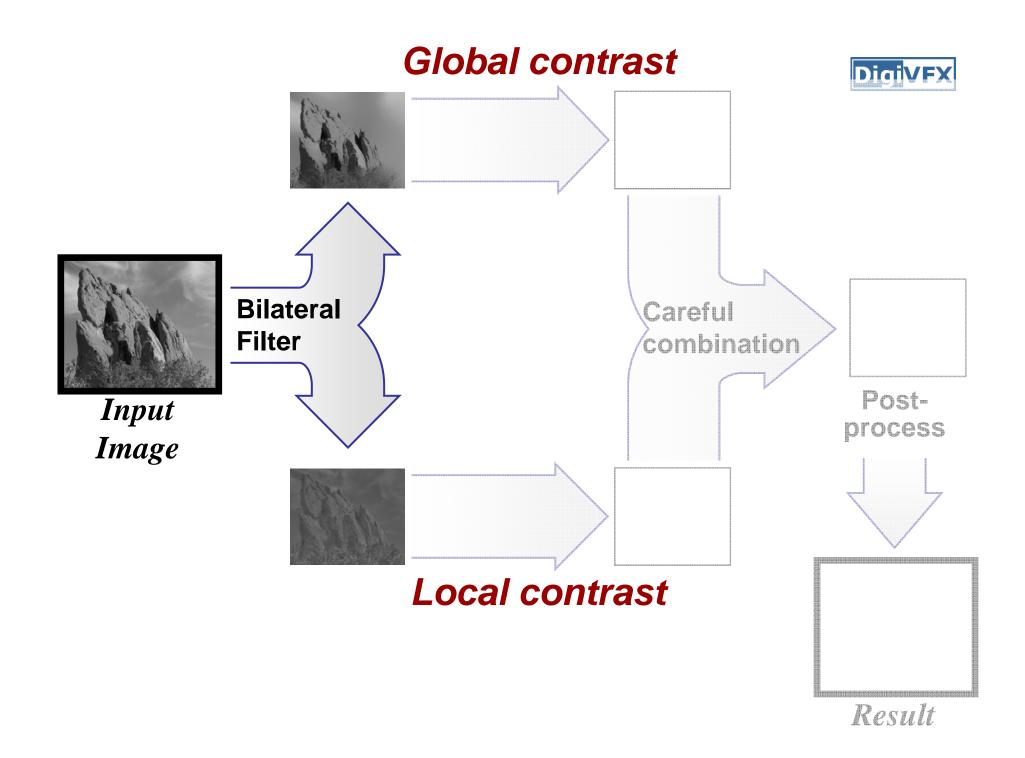
- Edge-preserving smoothing [Tomasi 98]
- We build upon tone mapping [Durand 02]

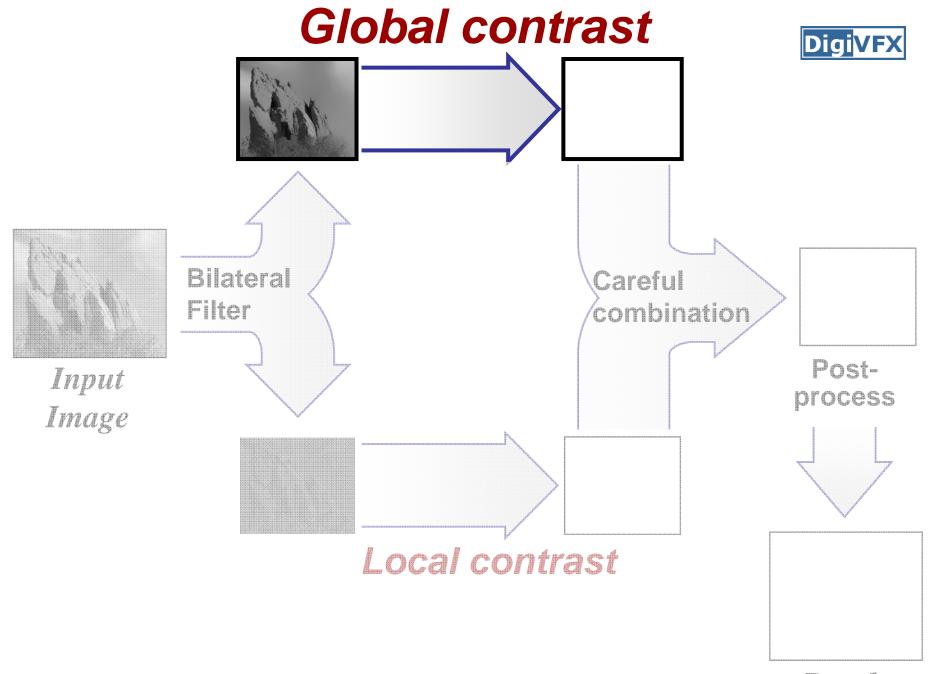


After bilateral filtering Global contrast



Residual after filtering Local contrast







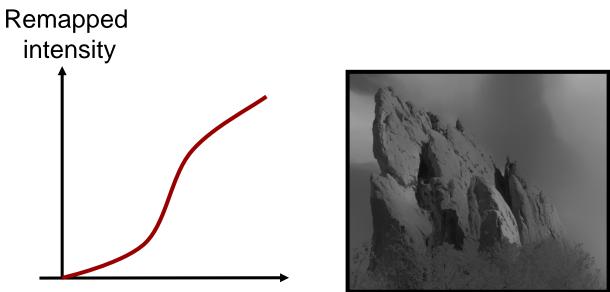
Global Contrast



• Intensity remapping of base layer



Input base

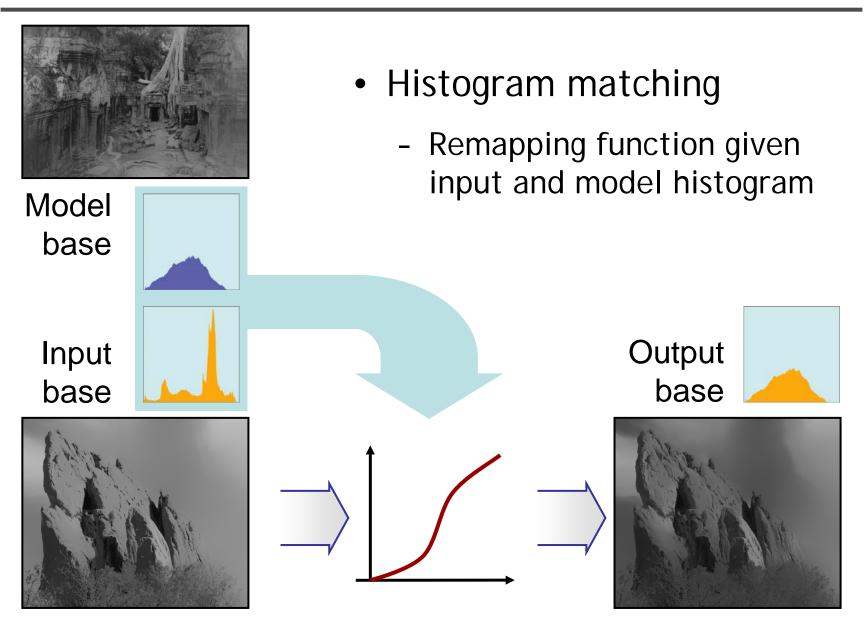


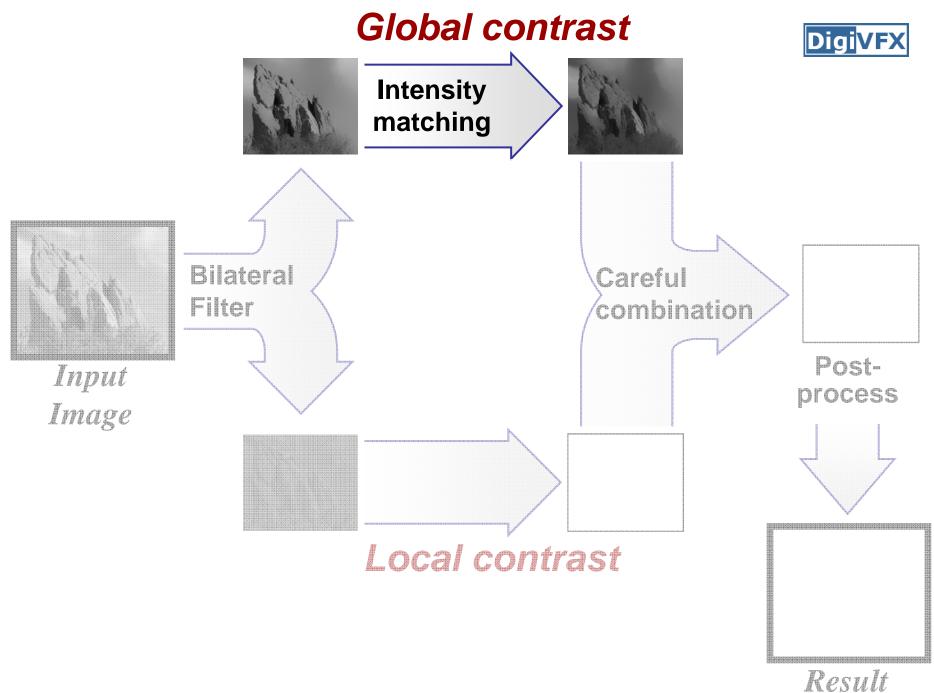
Input intensity

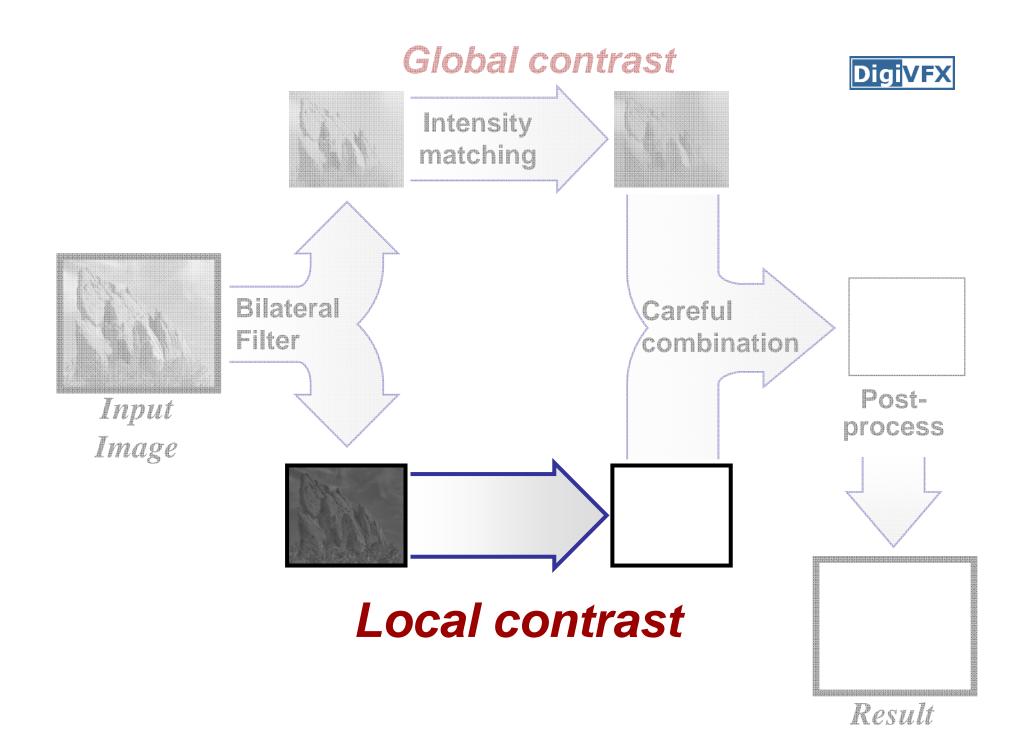
After remapping

Global Contrast (Model Transfer)



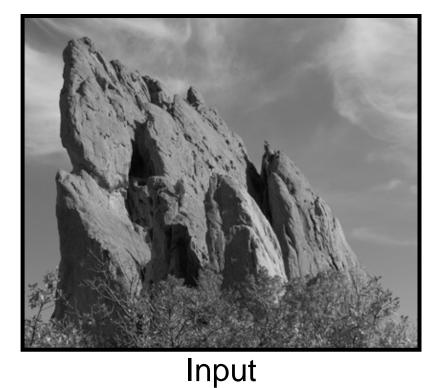


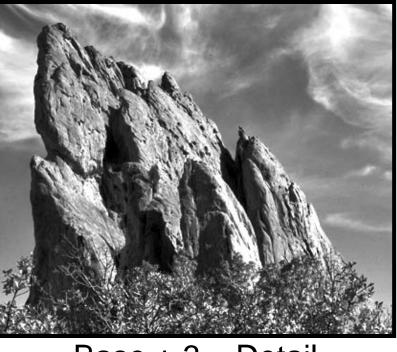






- Uniform control:
 - Multiply all values in the detail layer

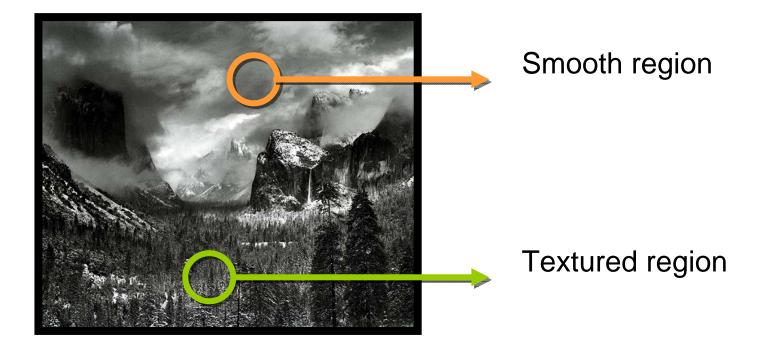




Base + $3 \times$ Detail

The amount of local contrast is not uniform

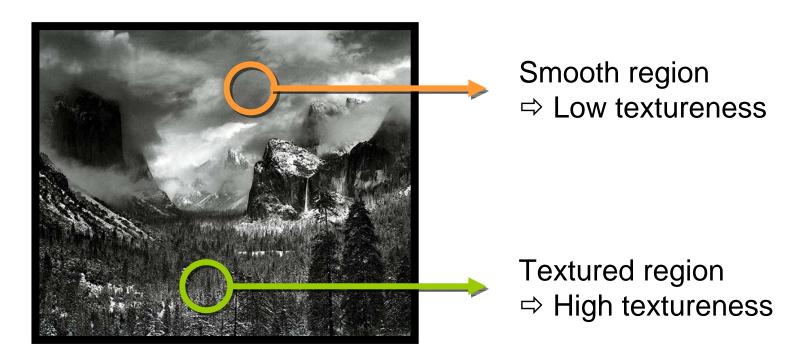




Local Contrast Variation

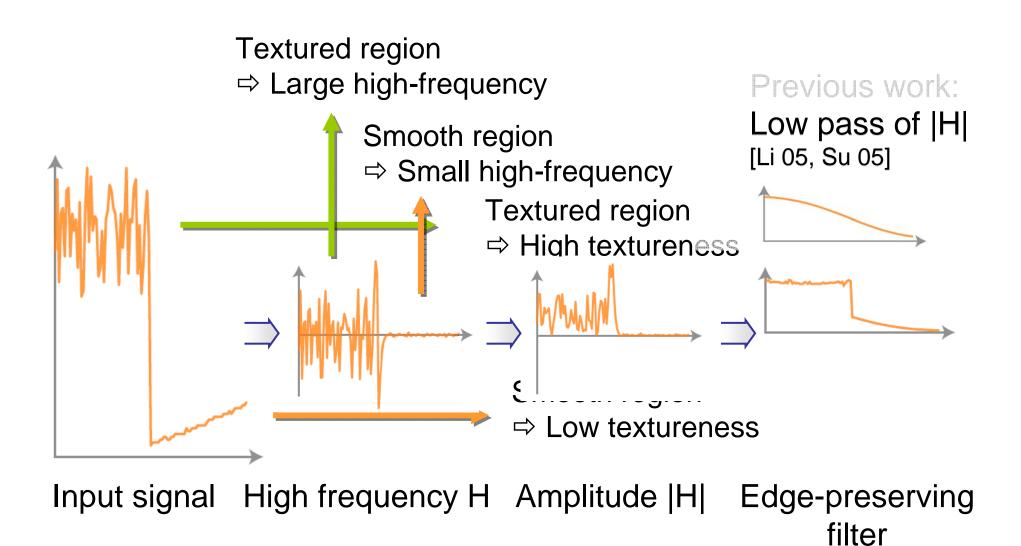


- We define "textureness": amount of local contrast
 - at each pixel based on surrounding region



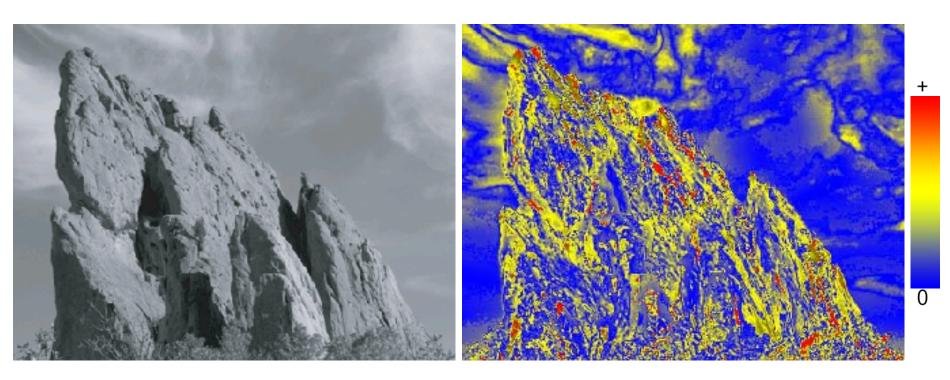


"Textureness": 1D Example





Textureness

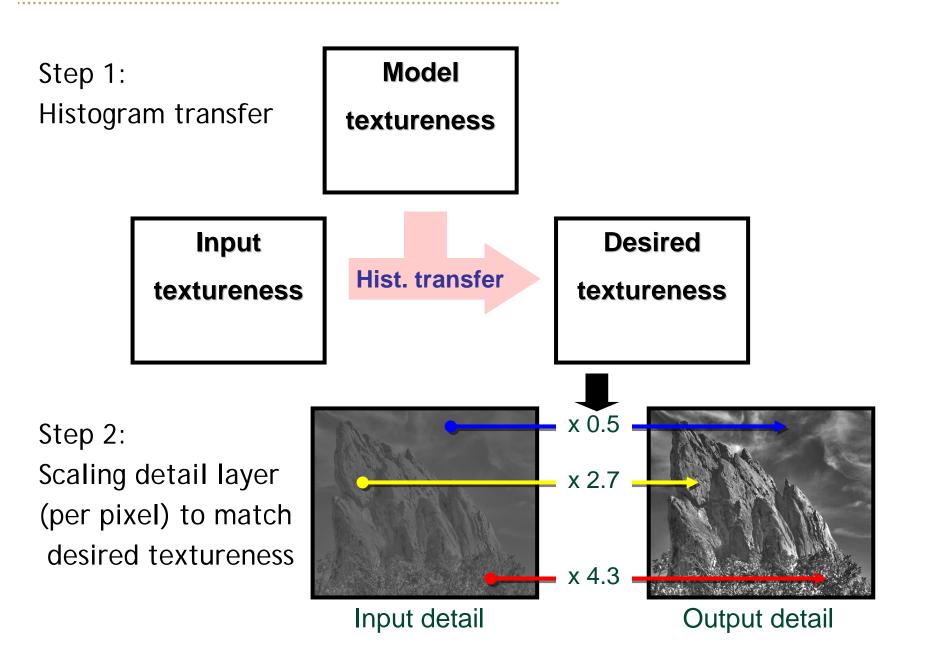


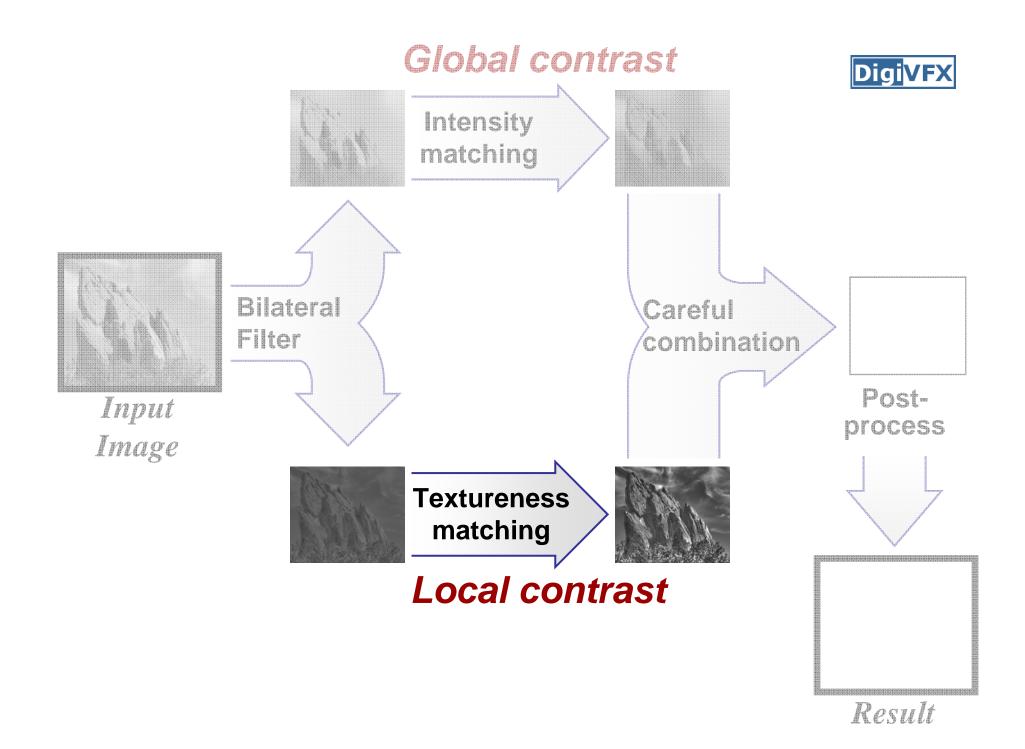
Input

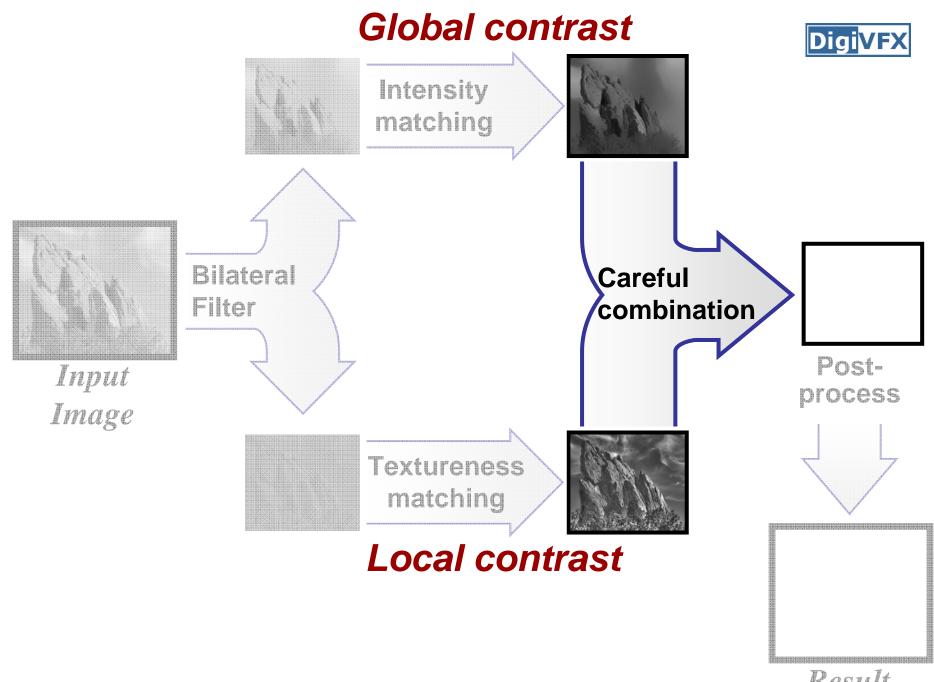
Textureness

Textureness Transfer









Result

A Non Perfect Result



Decoupled and large modifications (up to 6x)
 →Limited defects may appear



input (HDR)





result after global and local adjustments

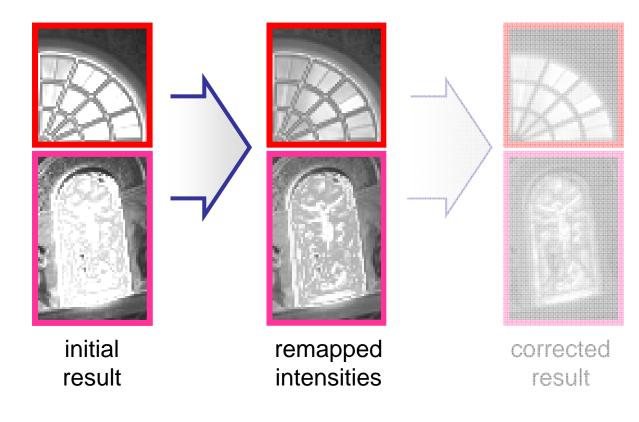








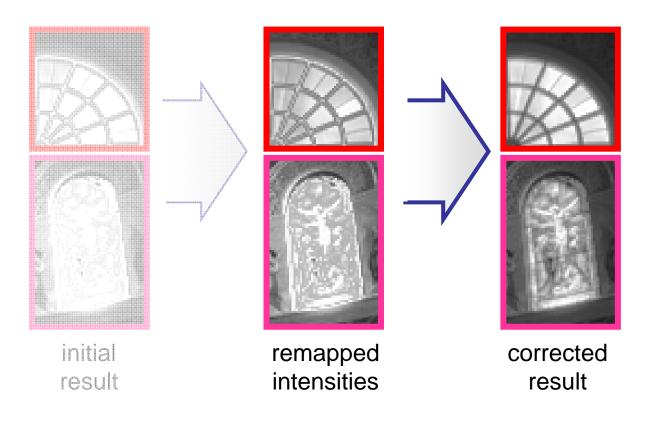
- Some intensities may be outside displayable range.
- → Compress histogram to fit visible range.





Preserving Details

- 1. In the gradient domain:
 - Compare gradient amplitudes of input and current
 - Prevent extreme reduction & extreme increase
- 2. Solve the Poisson equation.





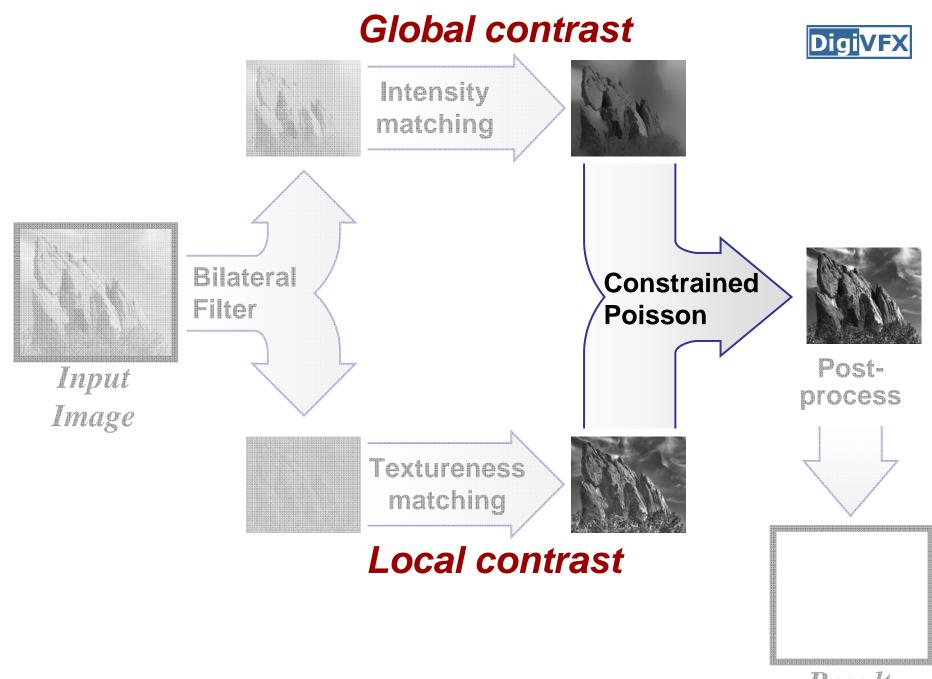
Effect of Detail Preservation

uncorrected result

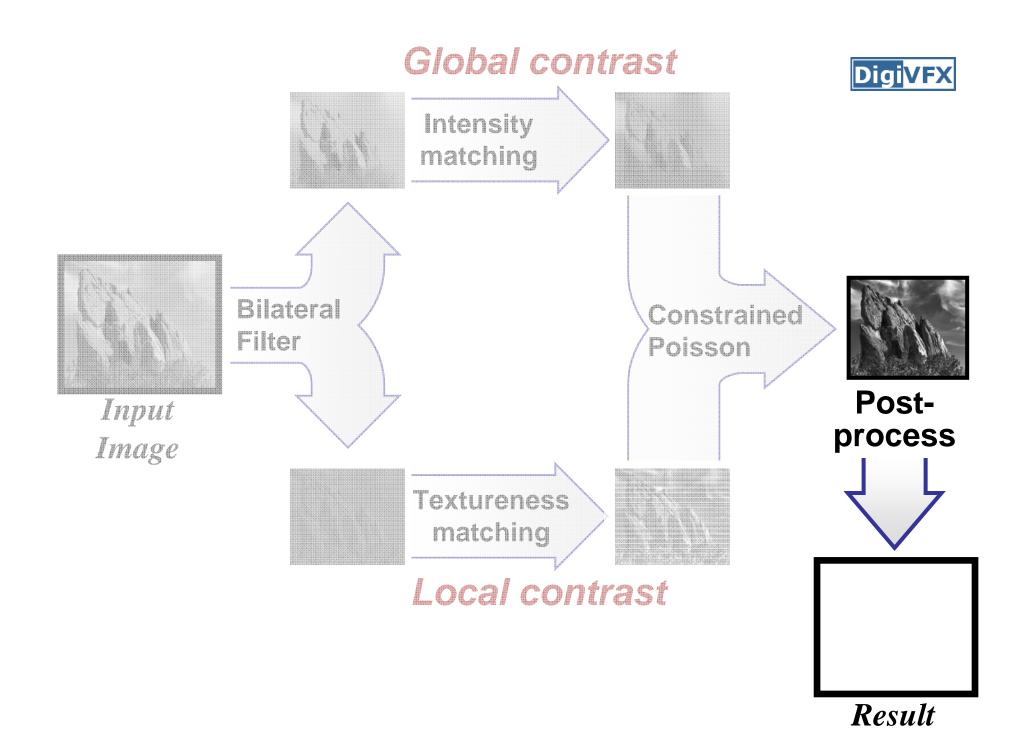


corrected result



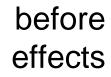


Result



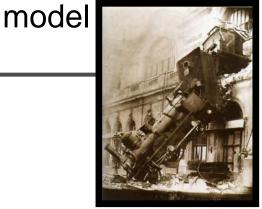
Additional Effects

- **Soft focus** (high frequency manipulation)
- Film grain (texture synthesis [Heeger 95])
- Color toning (chrominance = f (luminance))

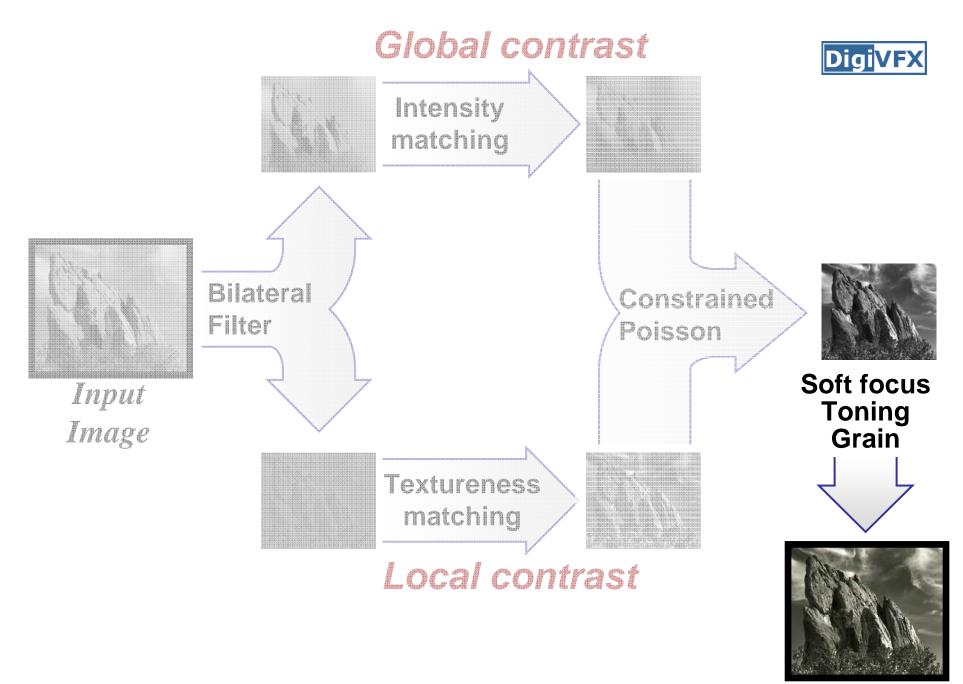




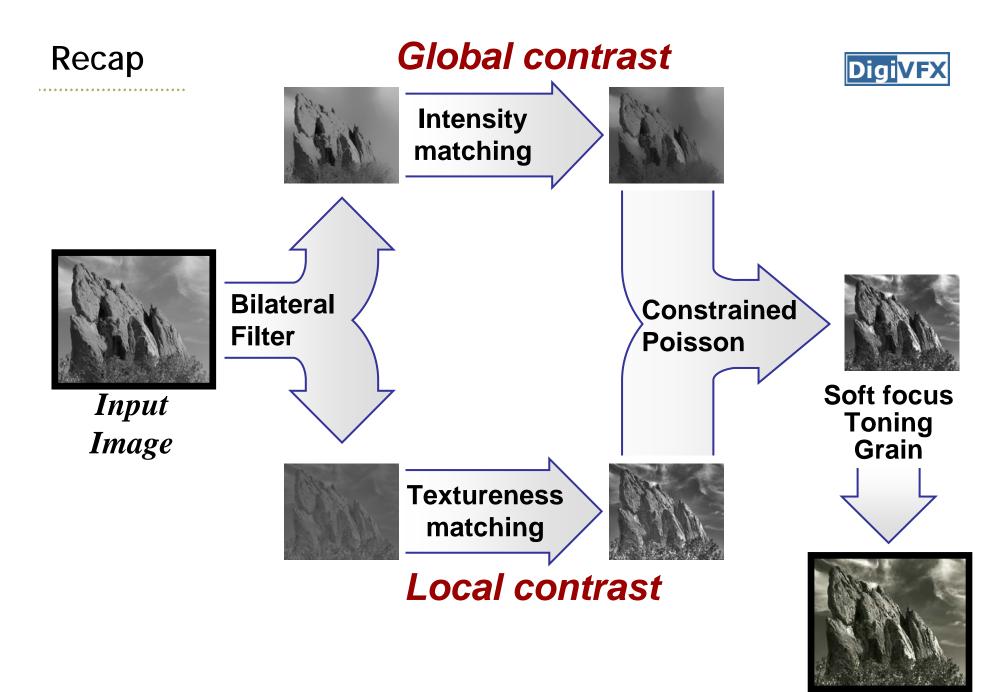




after effects



Result



Result

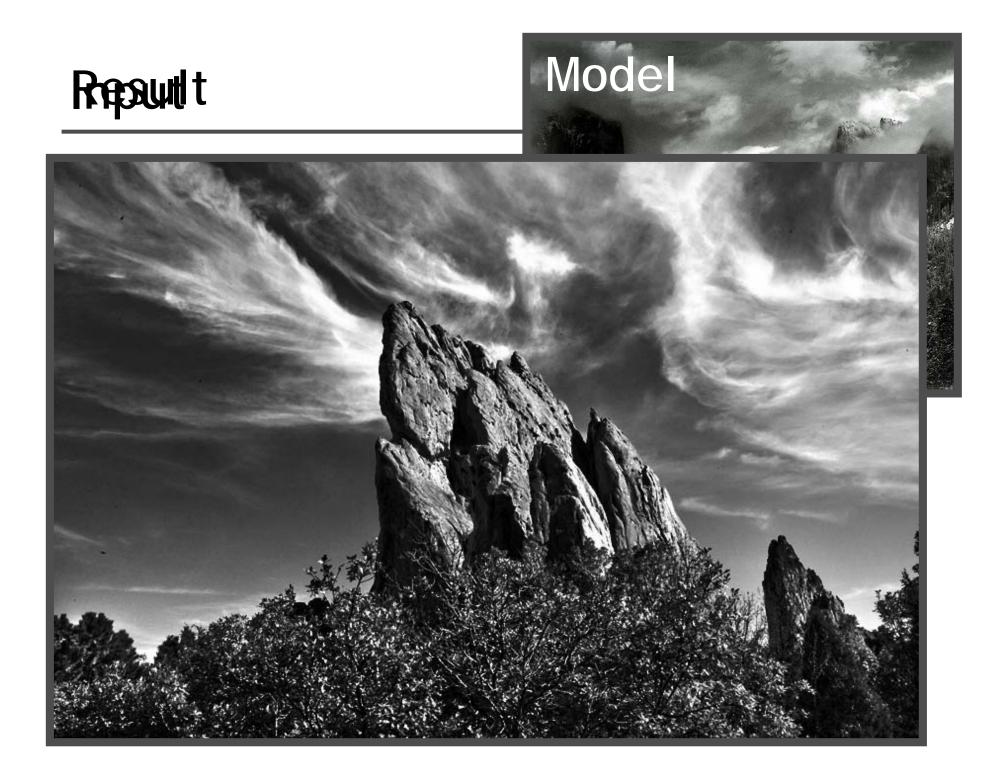


User provides input and model photographs.

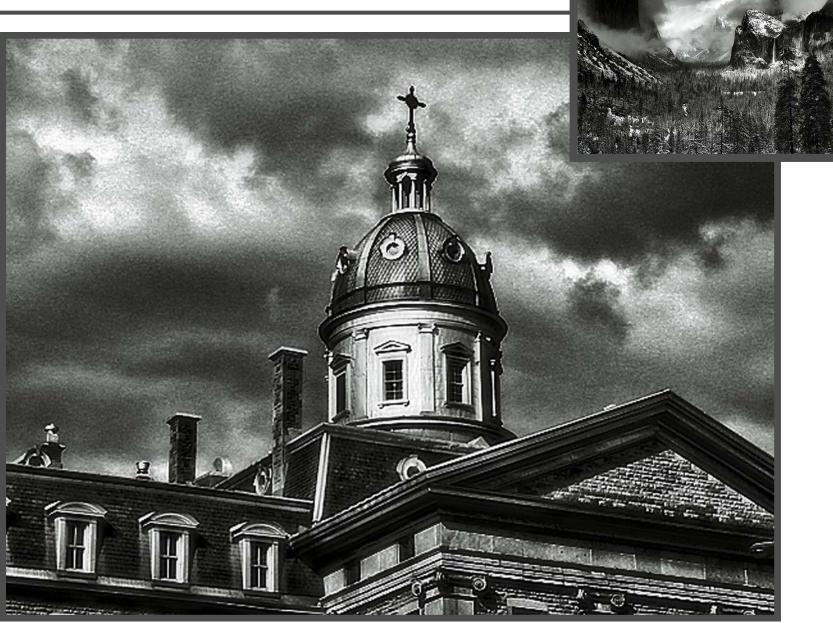
→ Our system automatically produces the result.

Running times:

- 6 seconds for 1 MPixel or less
- 23 seconds for 4 MPixels
- multi-grid Poisson solver and fast bilateral filter [Paris 06]

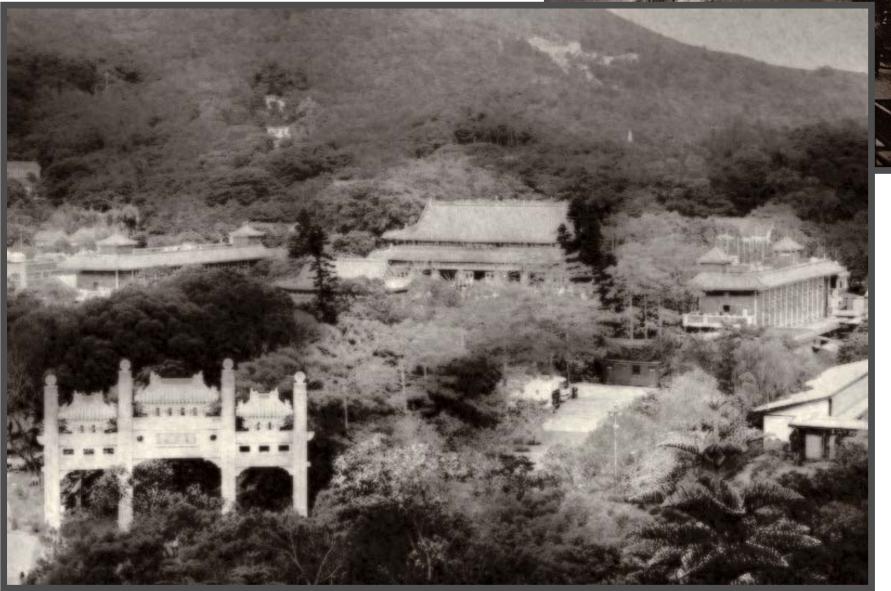


Repsult t

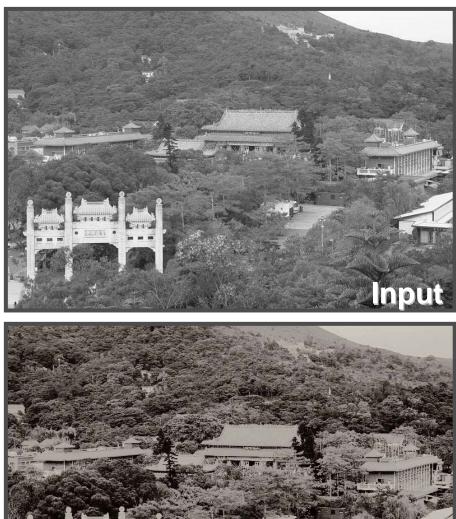


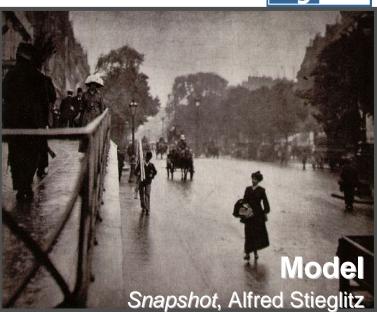
Repsult t





Comparison with Naïve Histogram Matching

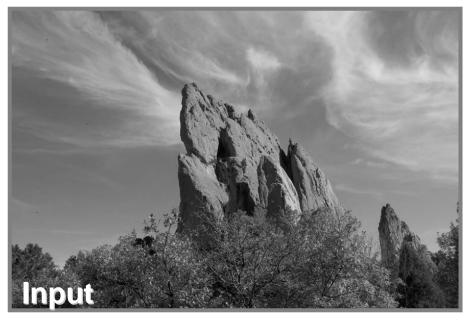




Local contrast, sharpness unfaithful

Naïve Histogram Matching

Comparison with Naïve Histogram Matching





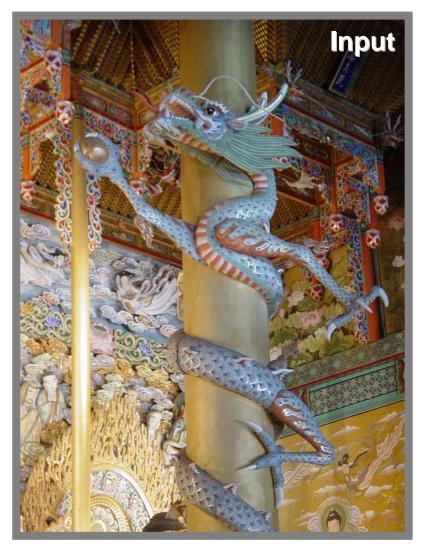


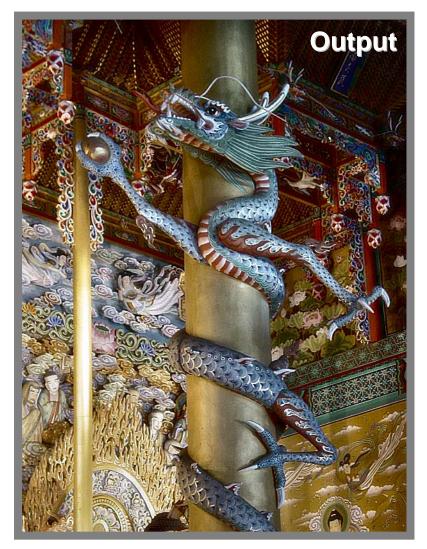




Color Images

• Lab color space: modify only luminance

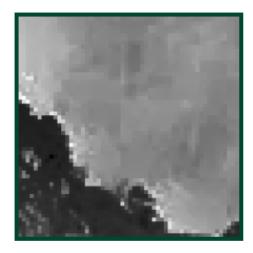






Limitations

- Noise and JPEG artifacts
 - amplified defects



- Can lead to unexpected results if the image content is too different from the model
 - Portraits, in particular, can suffer





- Transfer "look" from a model photo
- Two-scale tone management
 - Global and local contrast
 - New edge-preserving textureness
 - Constrained Poisson reconstruction
 - Additional effects

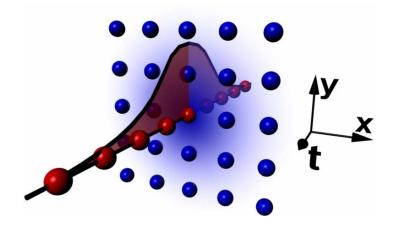
Video Enhancement Using Per Pixel Exposures (Bennett, 06)



From this video:

ASTA: <u>A</u>daptive <u>S</u>patio-<u>T</u>emporal <u>A</u>ccumulation Fi









$$J_p = \frac{1}{k_p} \sum_{q \in \Omega} I_q f(||p - q||) g(||I_p - I_q||)$$

$$J_p = \frac{1}{k_p} \sum_{q \in \Omega} I_q f(||p-q||) g(||\tilde{I}_p - \tilde{I}_q||)$$

Flash / No-Flash Photo Improvement (Petschnigg04) (Eisemann04)

Merge best features: warm, cozy candle light (no-flash) low-noise, detailed flash image





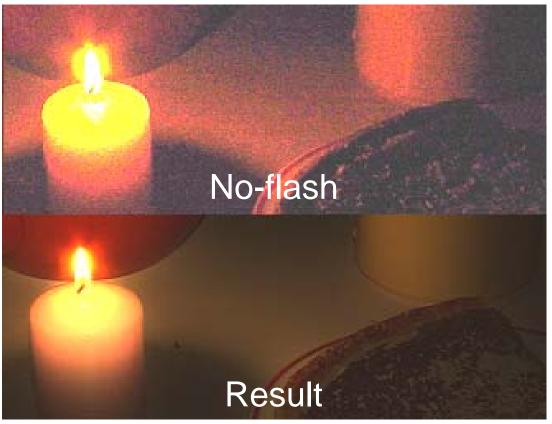
Basic approach of both flash/noflash papers

Remove noise + details from image A,

Keep as image A Lighting

Obtain noise-free details from image B,

Discard Image B Lighting



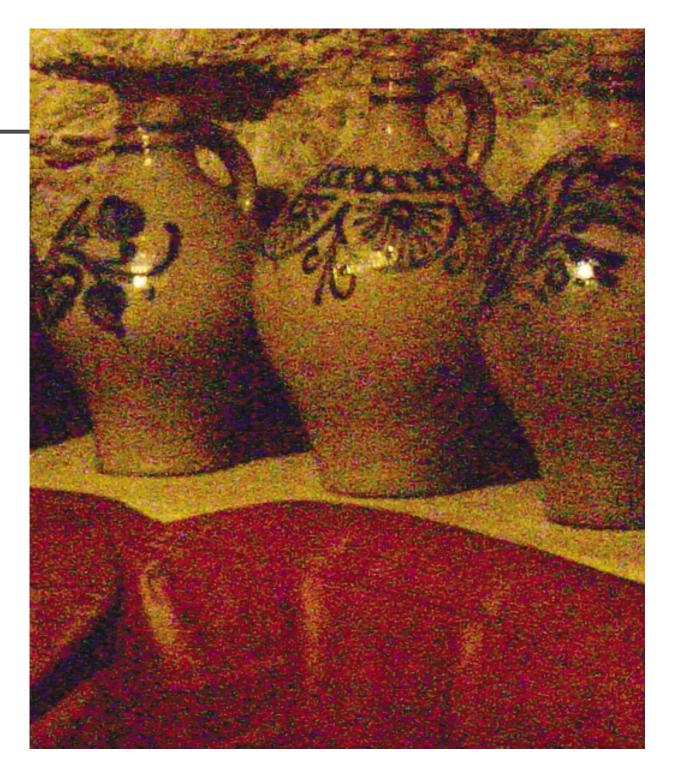
Petschnigg:

• Flash



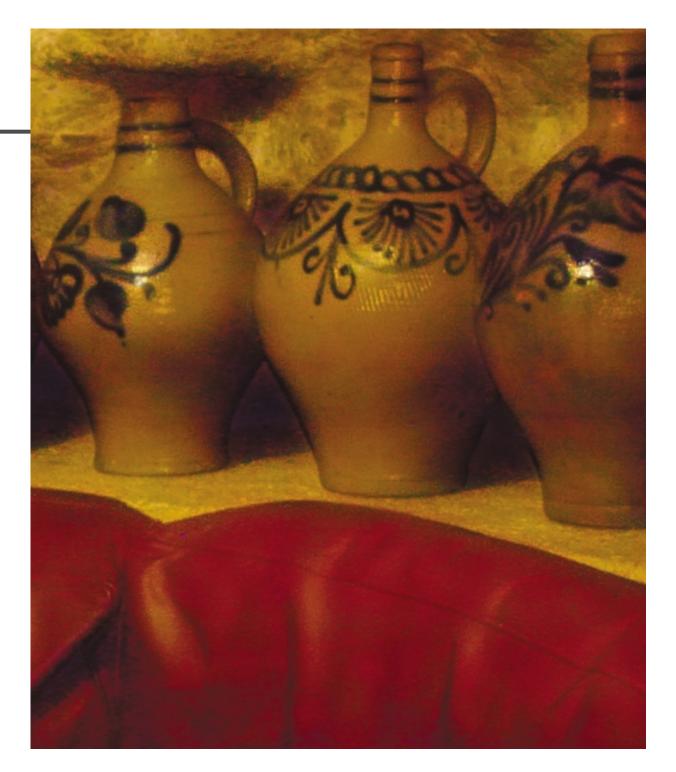
Petschnigg:

• No Flash,



Petschnigg:

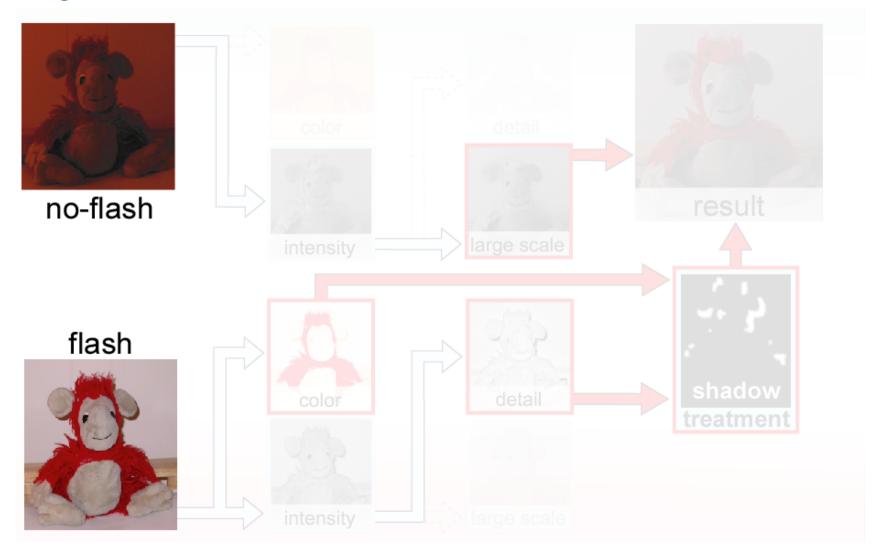
• Result





Our Approach

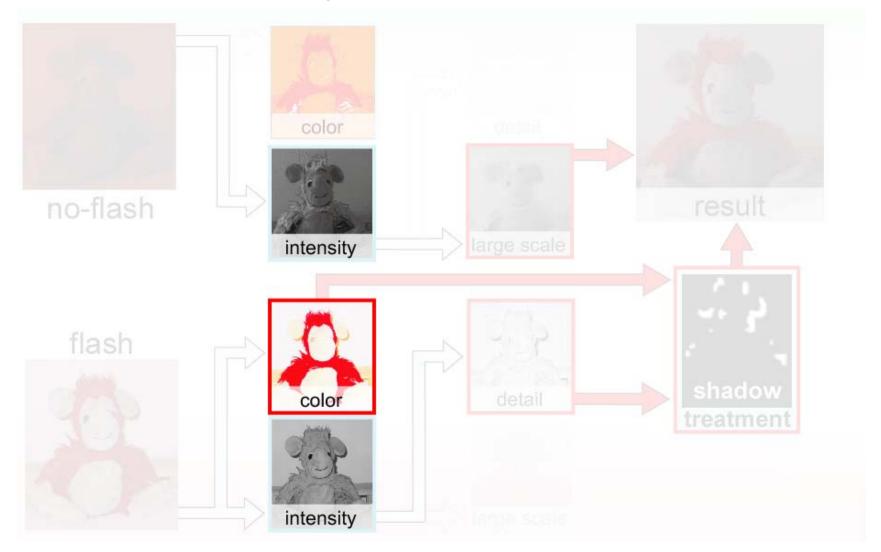
Registration



Our Approach



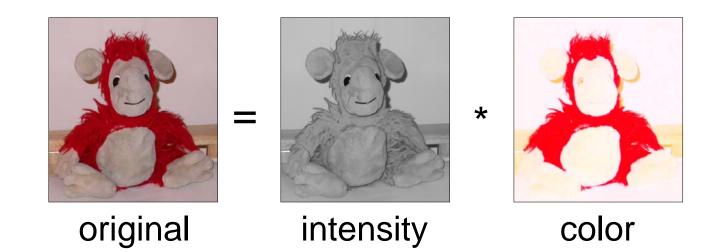
Decomposition





Decomposition

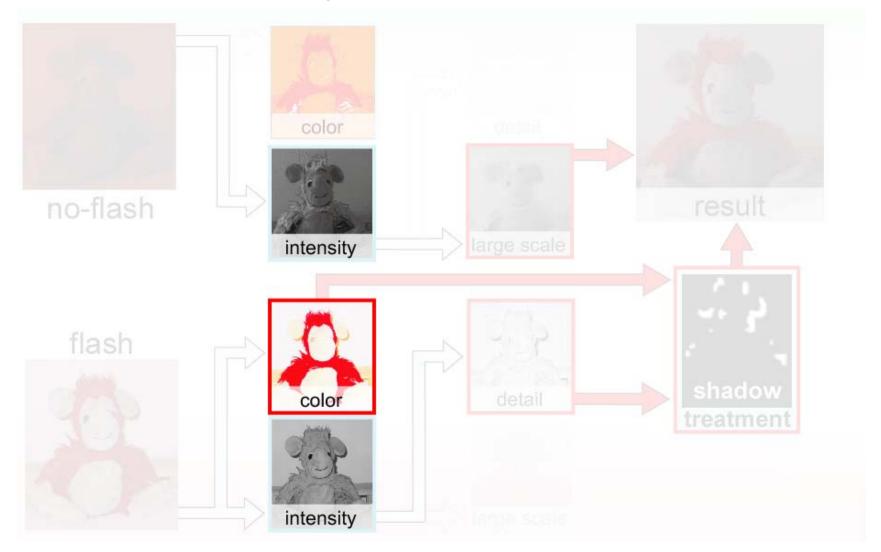
Color / Intensity:



Our Approach

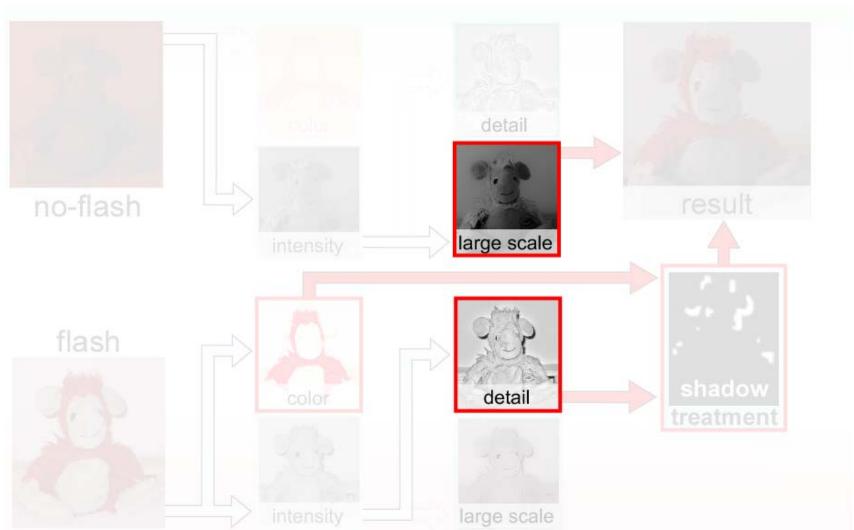


Decomposition



Our Approach





Decoupling

Decoupling



- Lighting : Large-scale variation
- Lightinge Langelscale variation
- Texture : Small-scale variation

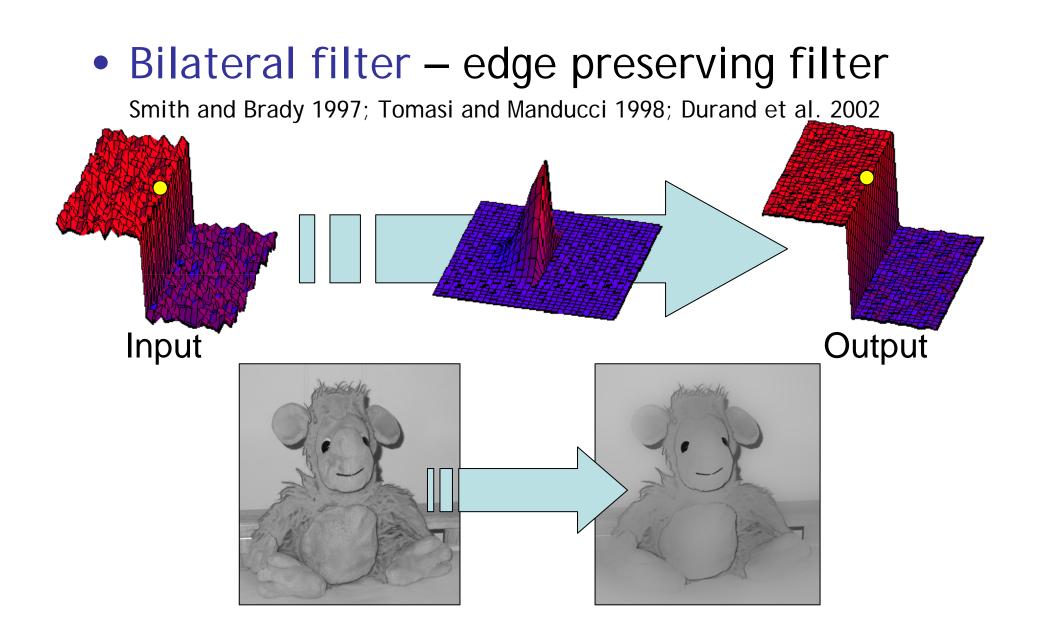








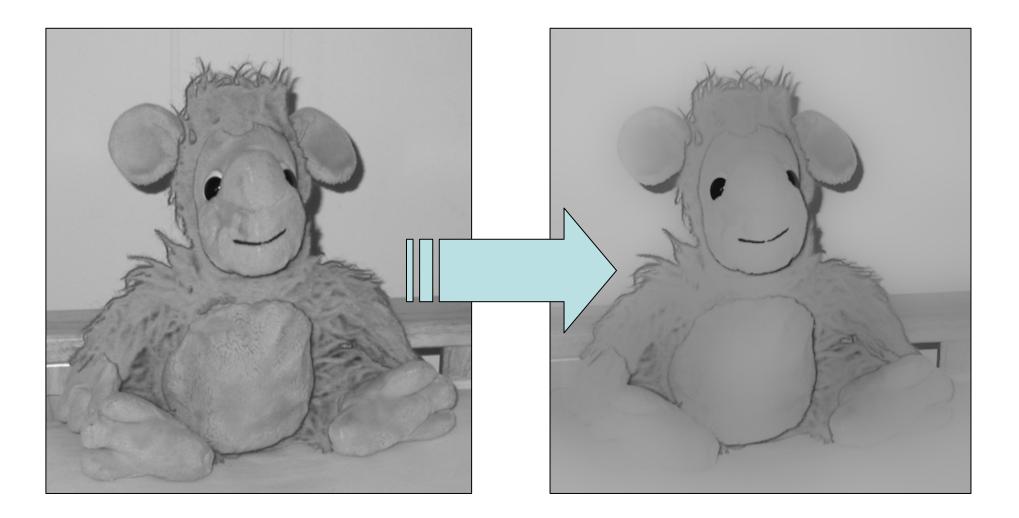






Large-scale Layer

• Bilateral filter

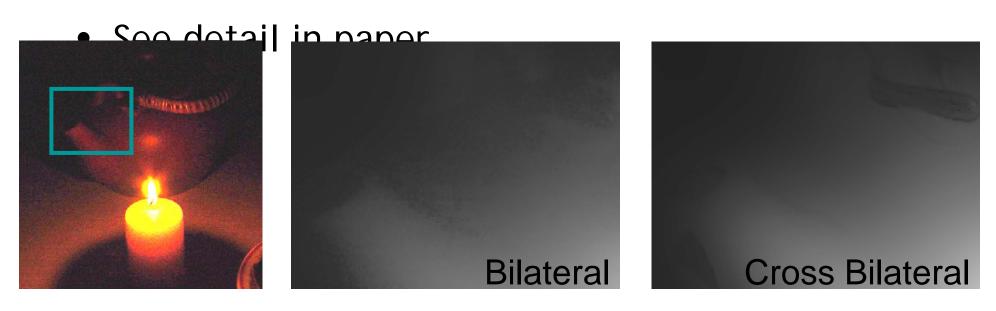


Cross Bilateral Filter



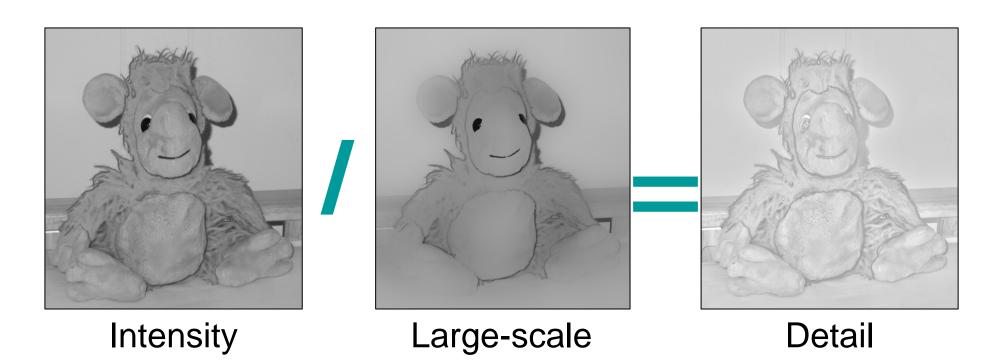
- Similar to joint bilateral filter by Petschnigg et al.
- When no-flash image is too noisy
- Borrow similarity from flash image

edge stopping from flash image





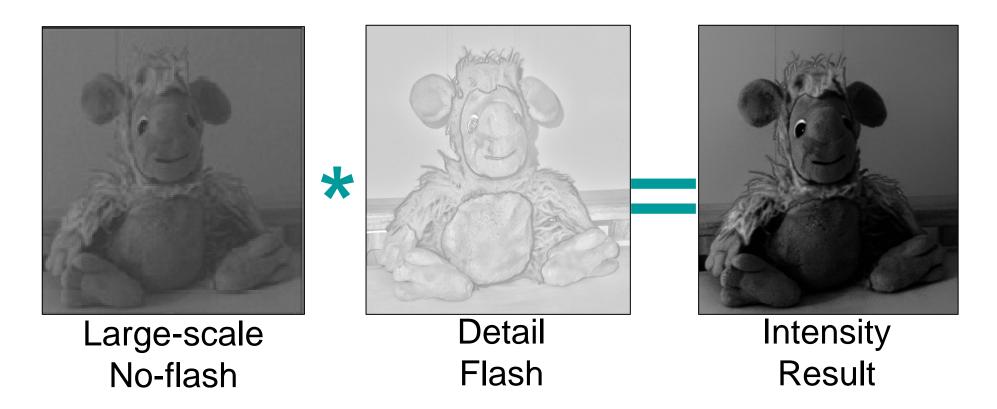
Detail Layer



Recombination: Large scale * Detail = Intensity

Recombination





Recombination: Large scale * Detail = Intensity

Recombination

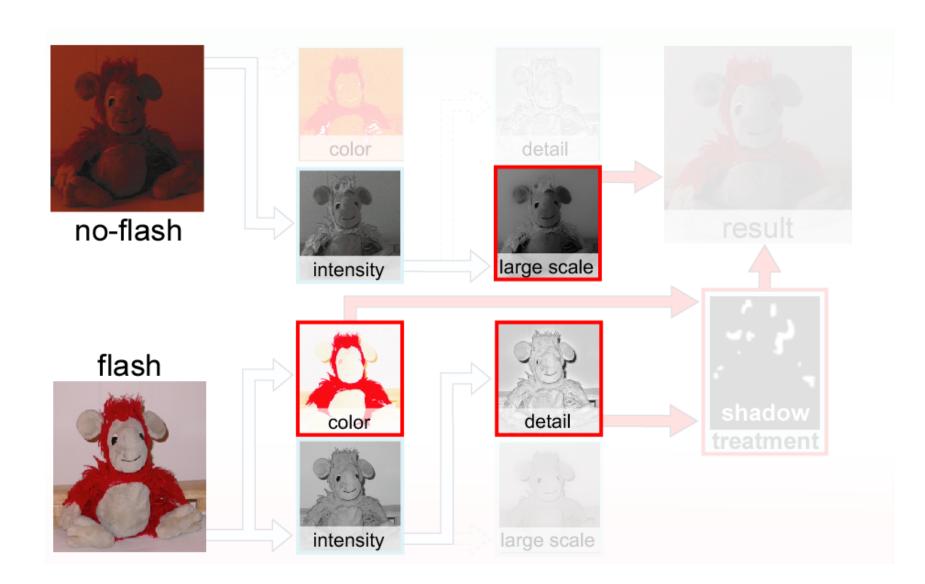




Recombination: Intensity * Color = Original



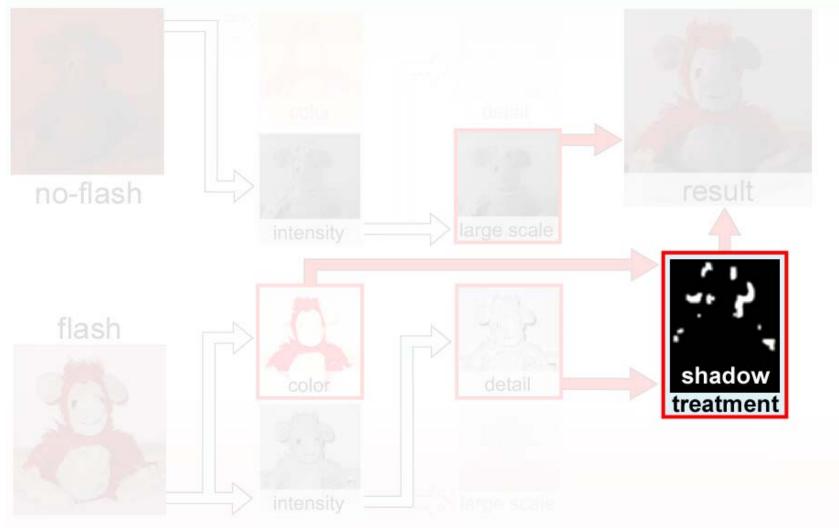
Our Approach



Our Approach



Shadow Detection/Treatment



Results





No-flash







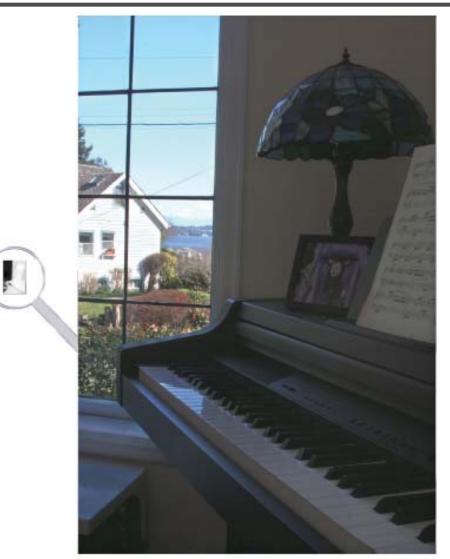


$$J_p = \frac{1}{k_p} \sum_{q \in \Omega} I_q f(||p - q||) g(||I_p - I_q||)$$

$$J_p = \frac{1}{k_p} \sum_{q \in \Omega} I_q f(||p - q||) g(||\tilde{I}_p - \tilde{I}_q||)$$

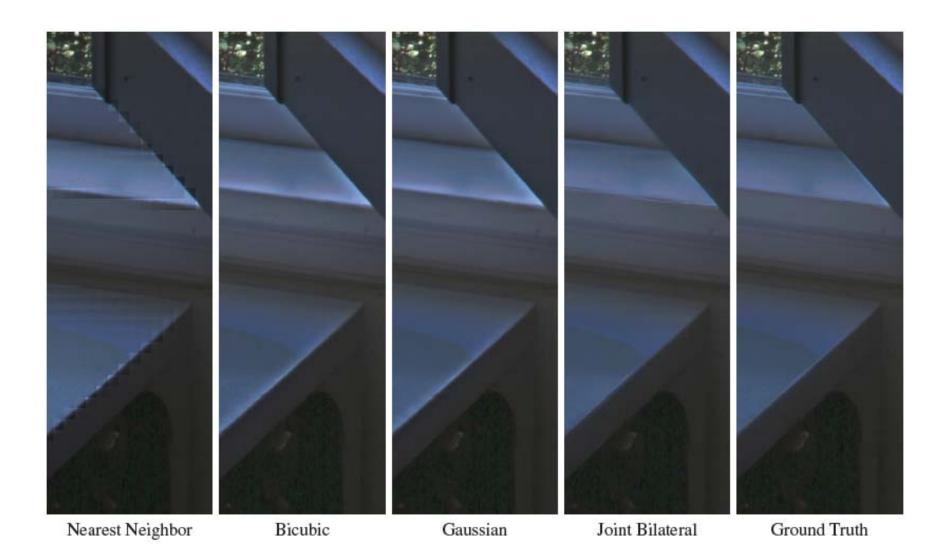
$$\tilde{S}_p = \frac{1}{k_p} \sum_{q_{\downarrow} \in \Omega} S_{q_{\downarrow}} f(||p_{\downarrow} - q_{\downarrow}||) g(||\tilde{I}_p - \tilde{I}_q||)$$



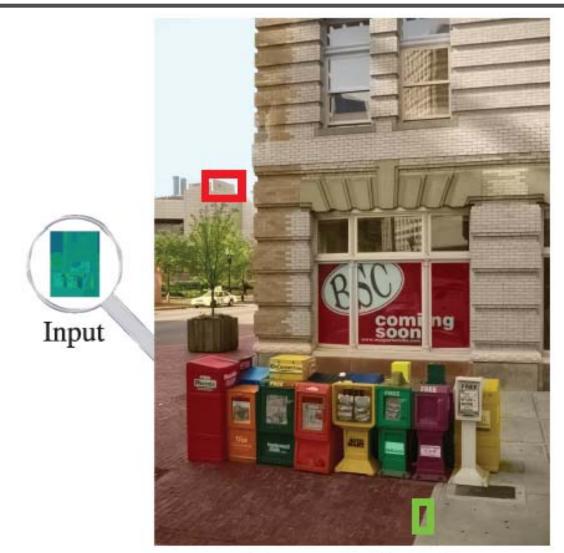


Upsampled Result



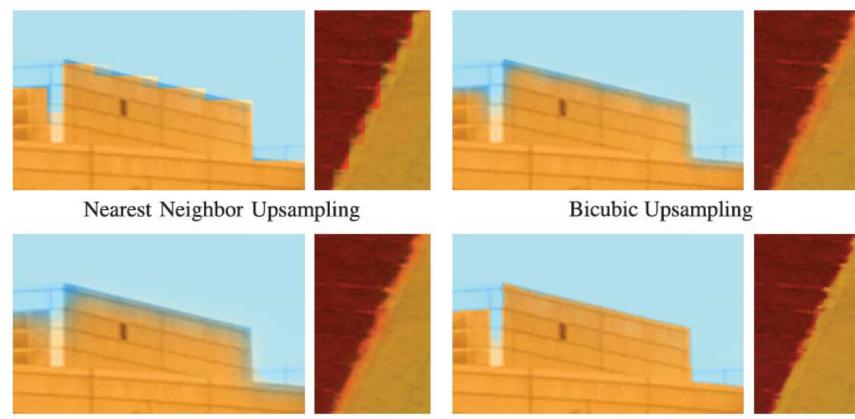






Upsampled Result





Gaussian Upsampling

Joint Bilateral Upsampling





Input Images





Nearest Neighbor

Bicubic

Gaussian

Joint Bilateral





Upsampled Result

References

- Patrick Perez, Michel Gangnet, Andrew Blake, <u>Poisson Image</u> <u>Editing</u>, SIGGRAPH 2003.
- Dani Lischinski, Zeev Farbman, Matt Uytendaelle and Richard Szeliski. <u>Interactive Local Adjustment of Tonal Values</u>. SIGGRAPH 2006.
- Carsten Rother, Andrew Blake, Vladimir Kolmogorov, <u>GrabCut</u> -<u>Interactive Foreground Extraction Using Iterated Graph Cuts</u>, SIGGRAPH 2004.
- Aseem Agarwala, Mira Dontcheva, Maneesh Agrawala, Steven Drucker, Alex Colburn, Brian Curless, David H. Salesin, Michael F. Cohen, <u>Interactive Digital Photomontage</u>, SIGGRAPH 2004.
- Sylvain Paris and Fredo Durand. <u>A Fast Approximation of the</u> <u>Bilateral Filter using a Signal Processing Approach</u>. ECCV 2006.
- Soonmin Bae, Sylvain Paris and Fredo Durand. <u>Two-scale Tone</u> <u>Management for Photographic Look</u>. SIGGRAPH 2006.