Image stitching

Digital Visual Effects, Spring 2007 Yung-Yu Chuang 2007/4/3

with slides by Richard Szeliski, Steve Seitz, Matthew Brown and Vaclav Hlavac

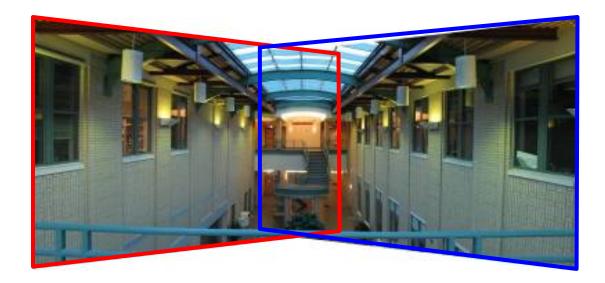


Stitching = alignment + blending

 f
 geometrical
 photometric
 registration
 registration







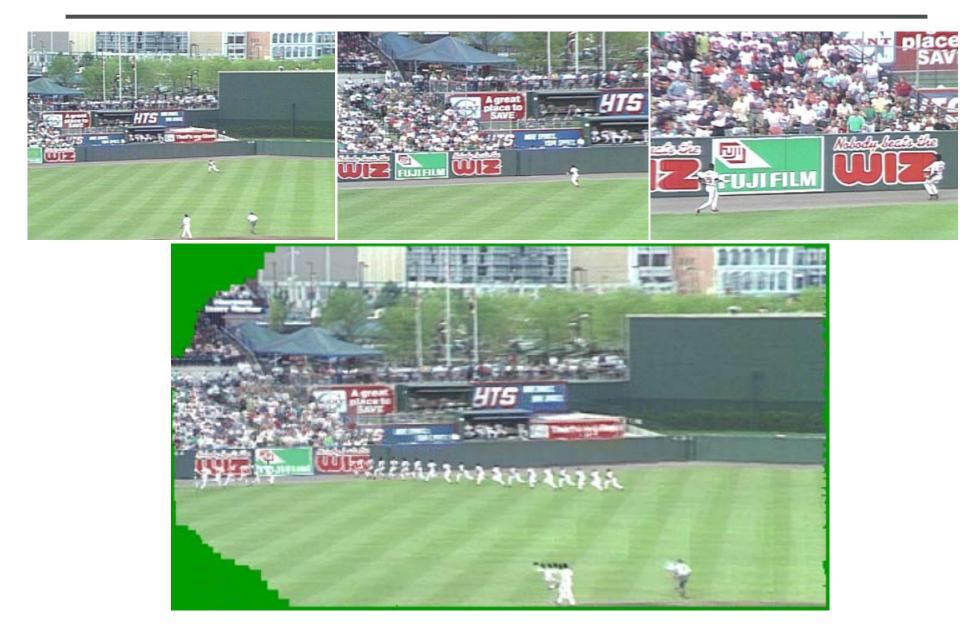


Applications of image stitching

- Video stabilization
- Video summarization
- Video compression
- Video matting
- Panorama creation

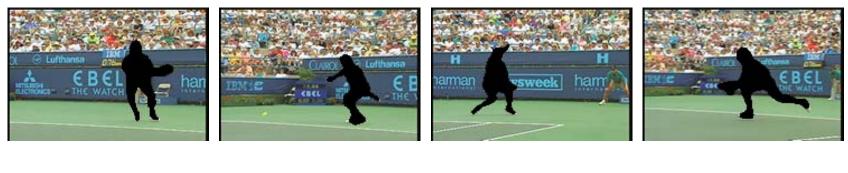


Video summarization





Video compression



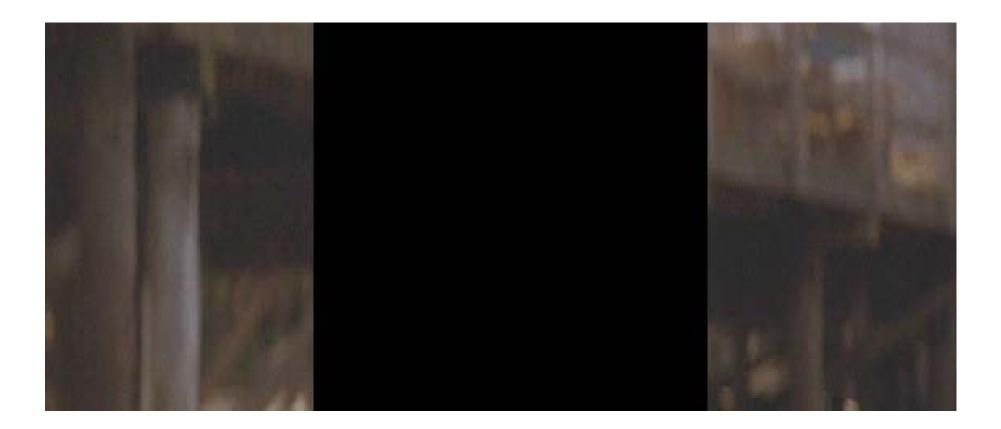






input video





remove foreground





estimate background

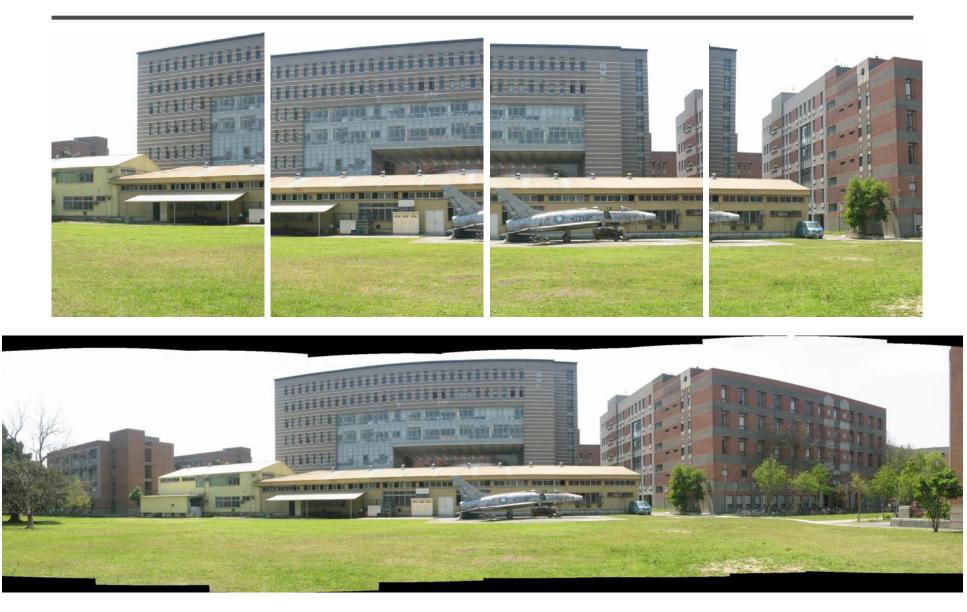




background estimation

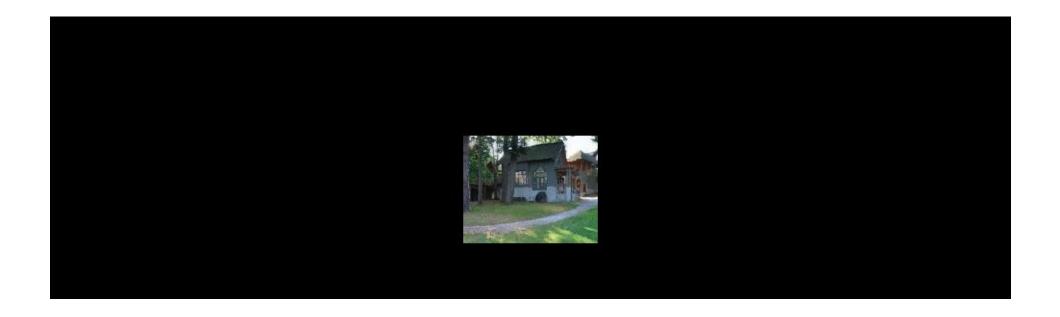


Panorama creation





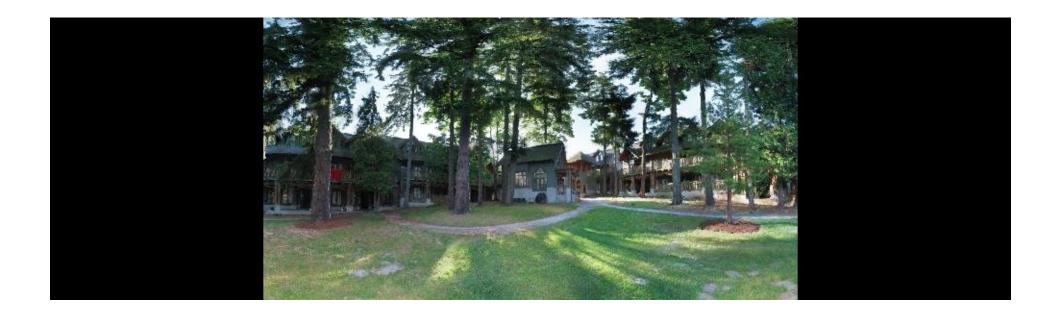
- Are you getting the whole picture?
 - Compact Camera FOV = 50 x 35°





Why panorama?

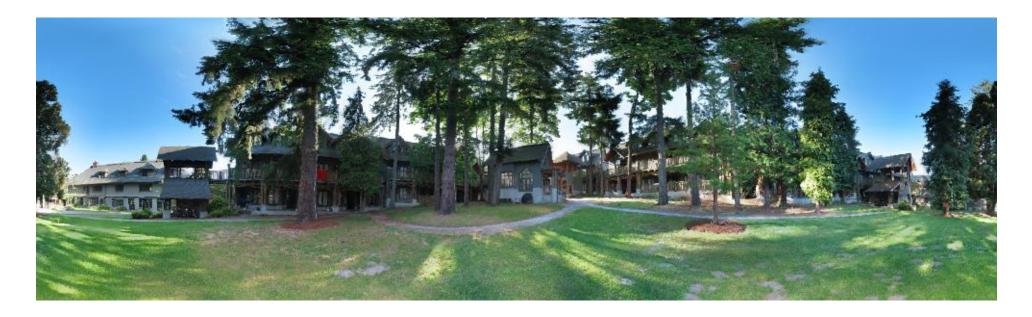
- Are you getting the whole picture?
 - Compact Camera FOV = 50 x 35°
 - Human FOV = $200 \times 135^{\circ}$





Why panorama?

- Are you getting the whole picture?
 - Compact Camera FOV = 50 x 35°
 - Human FOV = $200 \times 135^{\circ}$
 - Panoramic Mosaic = $360 \times 180^{\circ}$





- Like HDR, it is a topic of computational photography, seeking ways to build a better camera mostly in software.
- Most consumer cameras have a panorama mode
- Mars:

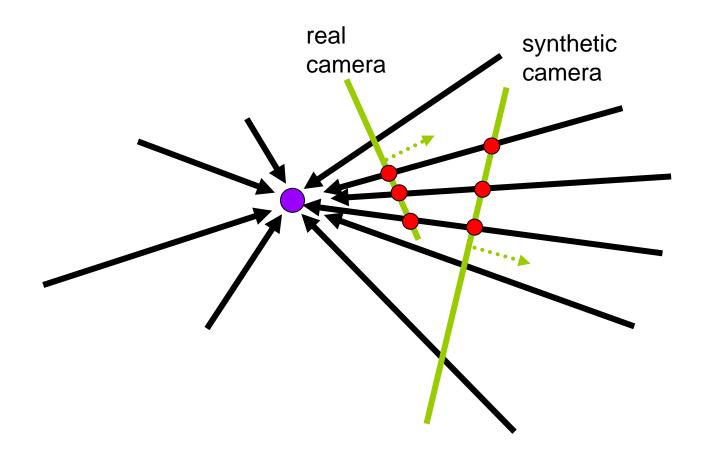
http://www.panoramas.dk/fullscreen3/f2_mars97.html

• Earth:

http://www.panoramas.dk/new-year-2006/taipei.html

A pencil of rays contains all views

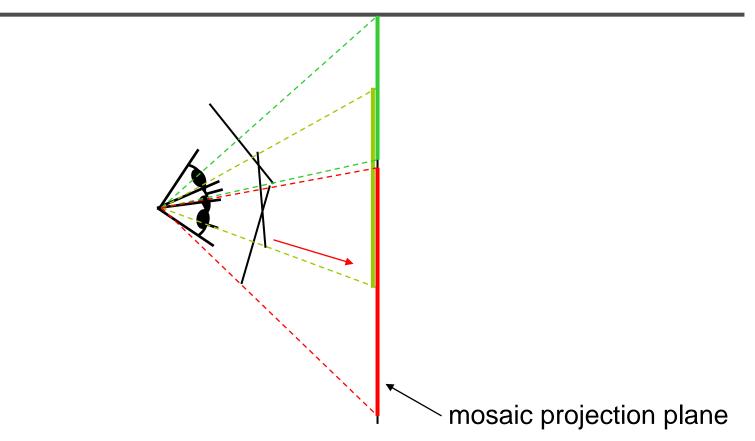




Can generate any synthetic camera view as long as it has **the same center of projection**!



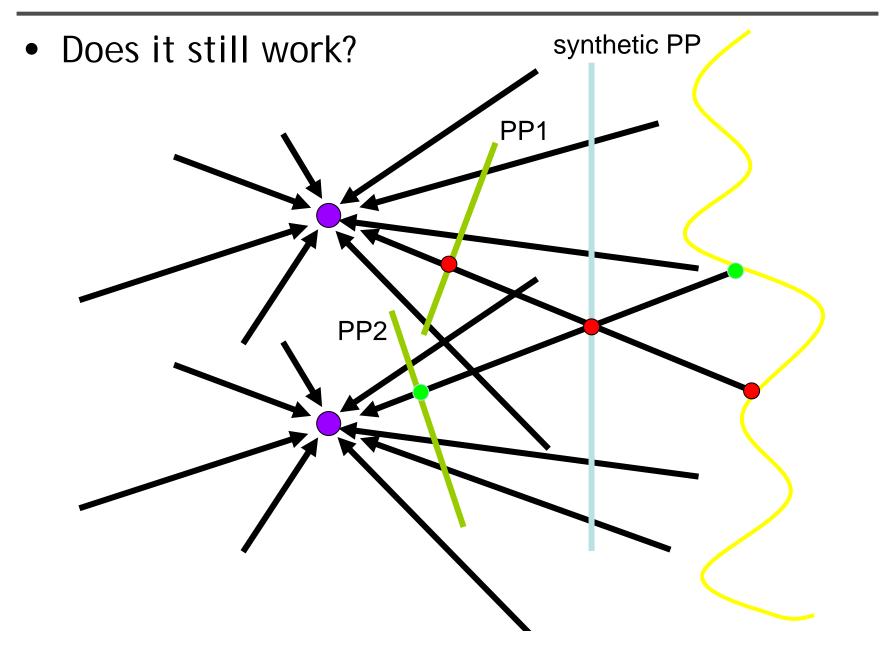
Mosaic as an image reprojection



- The images are reprojected onto a common plane
- The mosaic is formed on this plane
- Mosaic is a *synthetic wide-angle camera*

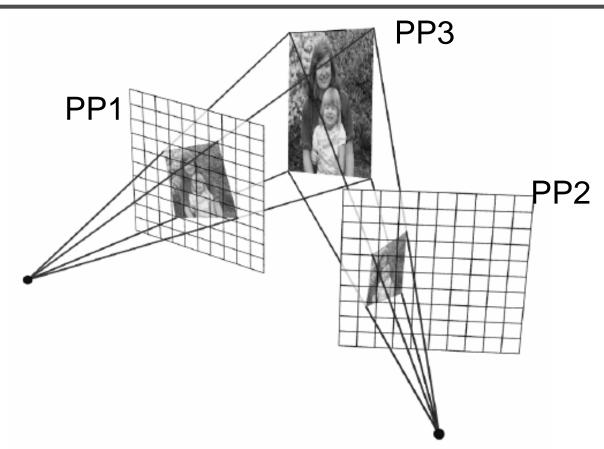
Changing camera center







Planar scene (or far away)



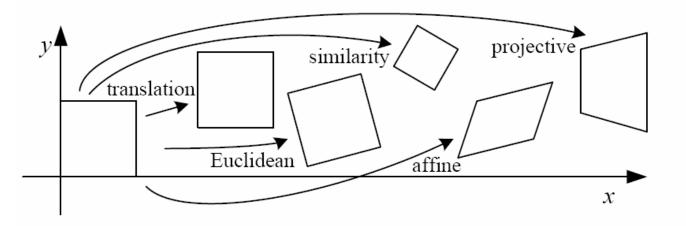
- PP3 is a projection plane of both centers of projection, so we are OK!
- This is how big aerial photographs are made



• Parametric models as the assumptions on the relation between two images.

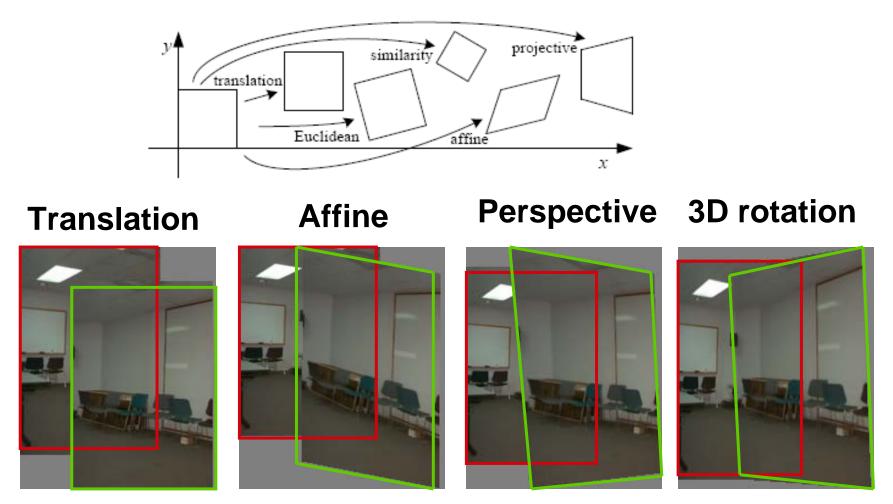


2D Motion models



Name	Matrix	# D.O.F.	Preserves:	Icon
translation	$igg[egin{array}{c c c c c c c c c c c c c c c c c c c $	2	orientation $+ \cdots$	
rigid (Euclidean)	$\left[egin{array}{c c} m{R} & t \end{array} ight]_{2 imes 3}$	3	lengths $+\cdots$	\bigcirc
similarity	$\left[\left[\left. s oldsymbol{R} \right oldsymbol{t} ight]_{2 imes 3} ight]$	4	angles $+ \cdots$	\Diamond
affine	$\left[egin{array}{c} oldsymbol{A} \end{array} ight]_{2 imes 3}$	6	parallelism $+\cdots$	
projective	$\left[egin{array}{c} ilde{H} \end{array} ight]_{3 imes 3}$	8	straight lines	



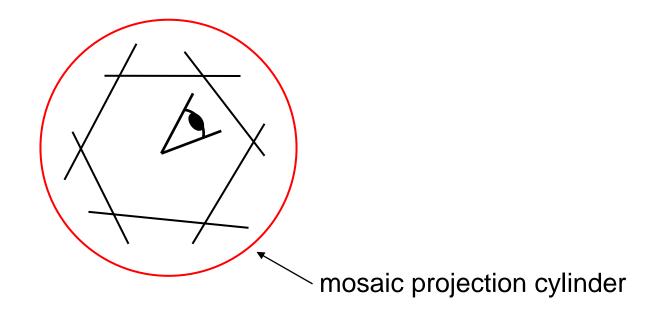


2 unknowns 6 unknowns 8 unknowns 3 unknowns

A case study: cylindrical panorama

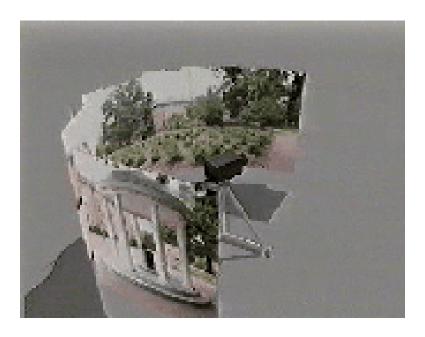


• What if you want a 360° field of view?





Cylindrical panoramas



- Steps
 - Reproject each image onto a cylinder
 - Blend
 - Output the resulting mosaic



- 1. Take pictures on a tripod (or handheld)
- 2. Warp to cylindrical coordinate
- 3. Compute pairwise alignments
- 4. Fix up the end-to-end alignment
- 5. Blending
- 6. Crop the result and import into a viewer



Taking pictures





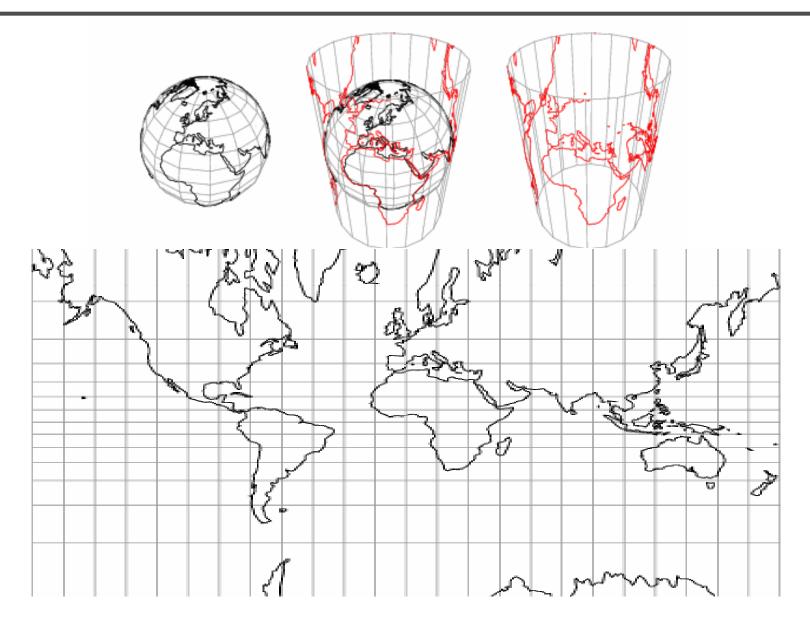
Kaidan panoramic tripod head



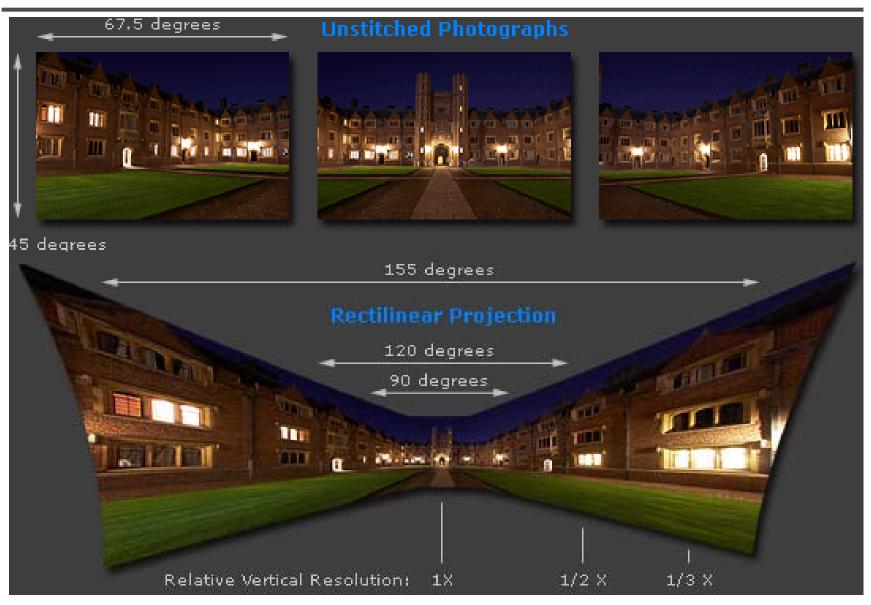
Translation model





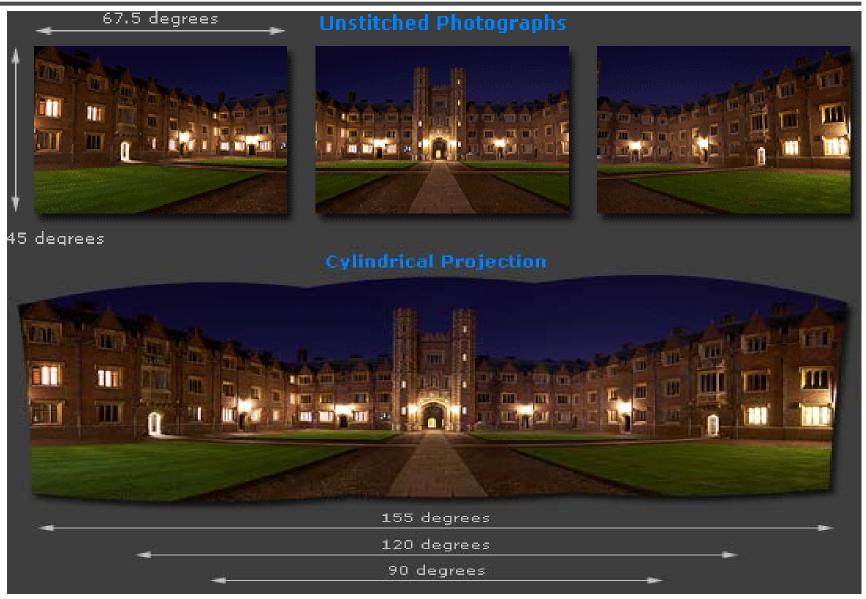






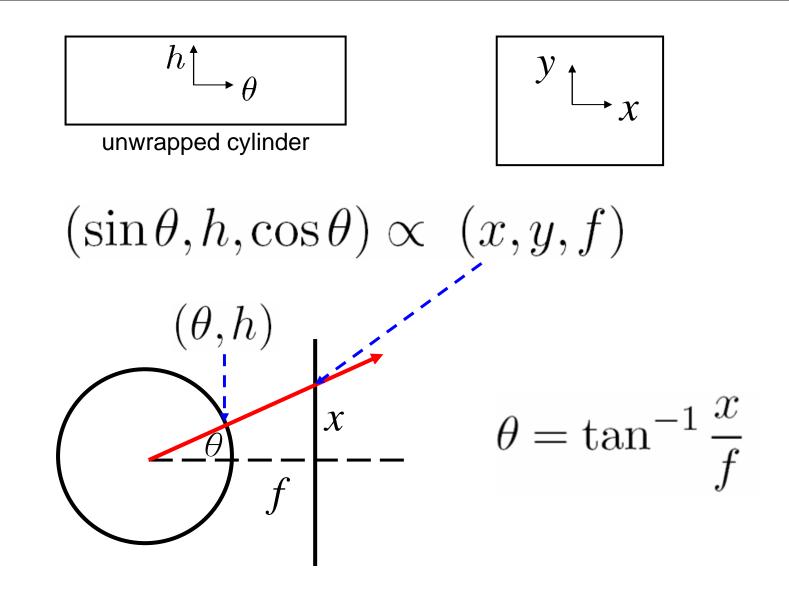
Adopted from http://www.cambridgeincolour.com/tutorials/image-projections.htm



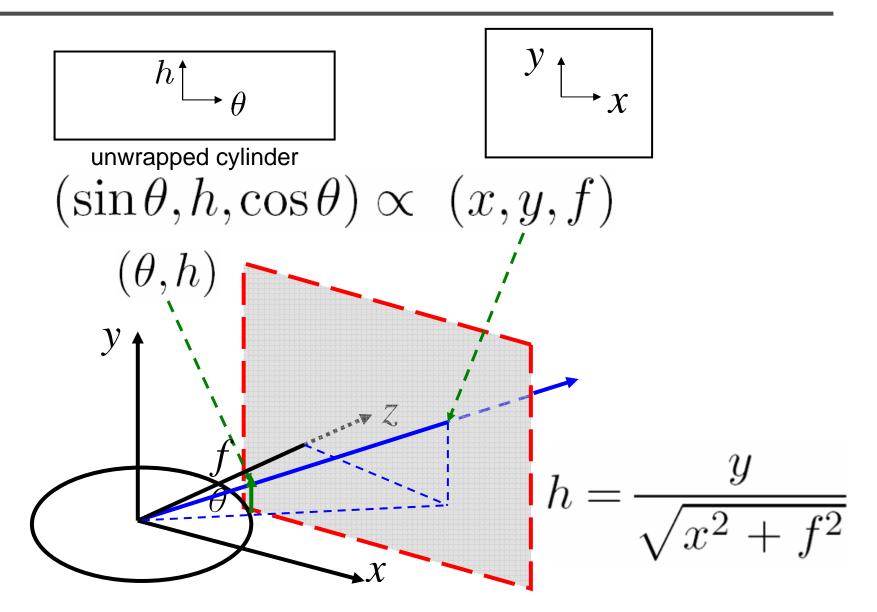


Adopted from http://www.cambridgeincolour.com/tutorials/image-projections.htm

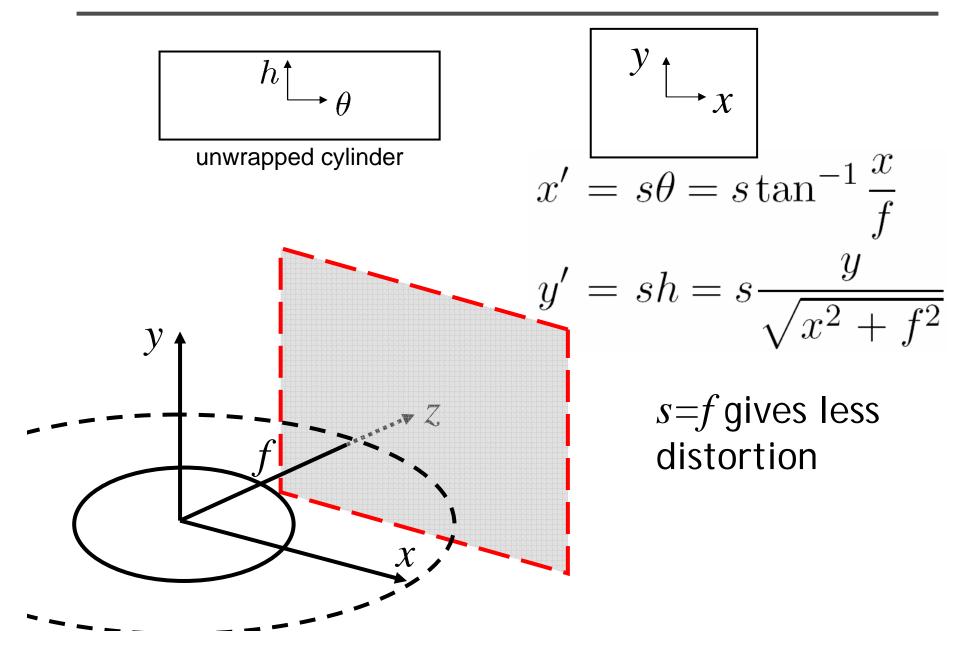














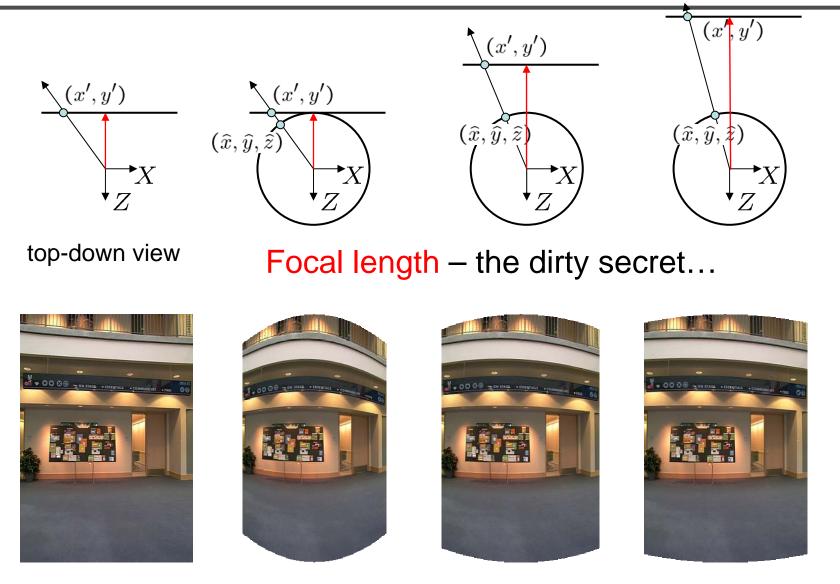


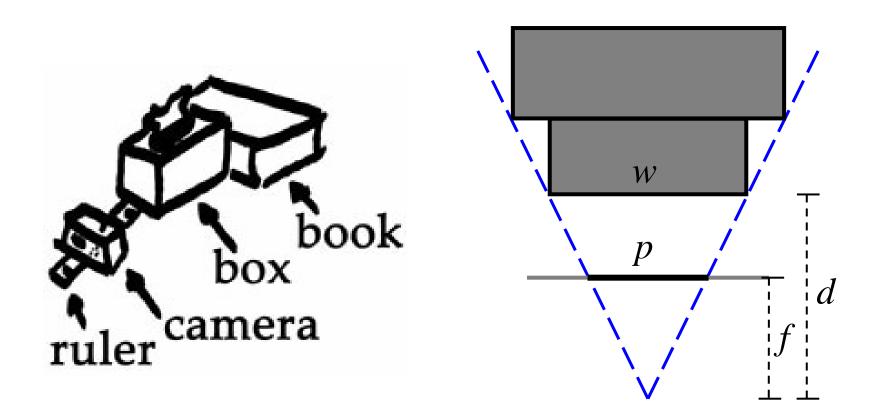
Image 384x300

f = 180 (pixels)

f = 280

f = 380





Or, you can use other software, such as AutoStich, to help.



Input images





Cylindrical warping

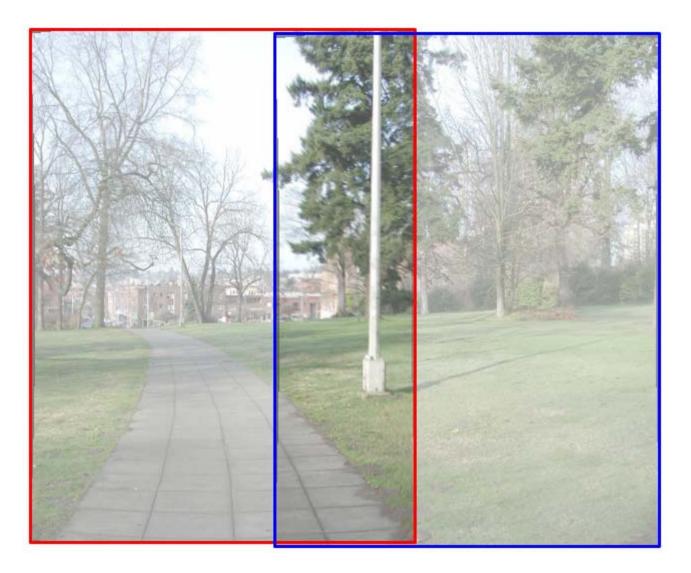


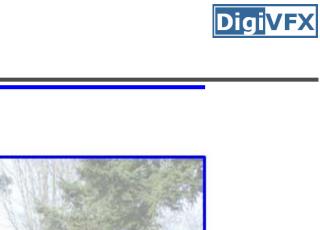


• Why blending: parallax, lens distortion, scene motion, exposure difference

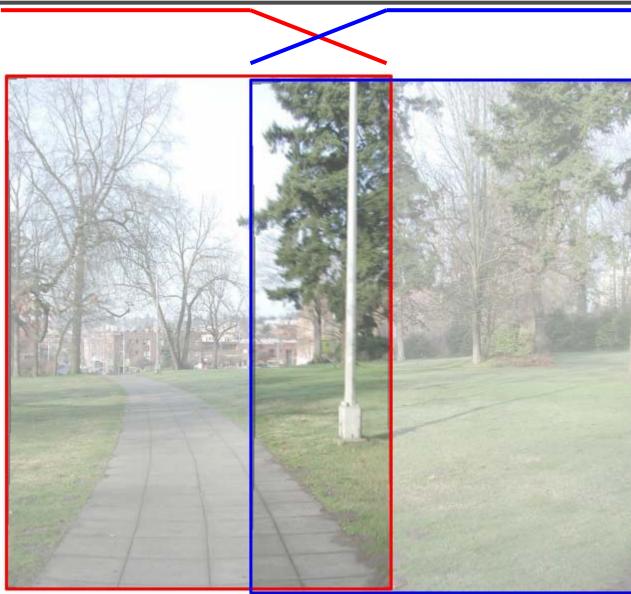


Blending





Blending



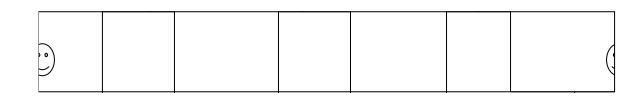


Blending



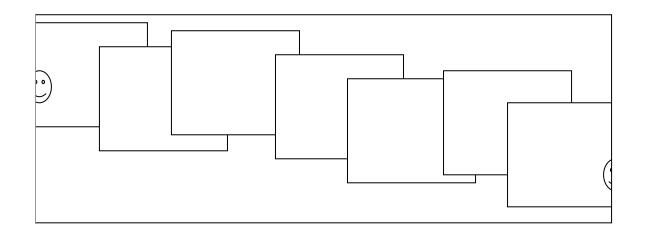
Assembling the panorama





• Stitch pairs together, blend, then crop

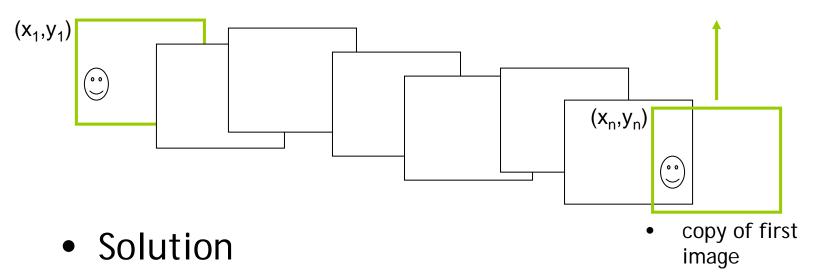




- Error accumulation
 - small errors accumulate over time



Problem: Drift



- add another copy of first image at the end
- there are a bunch of ways to solve this problem
 - add displacement of (y₁ y_n)/(n -1) to each image after the first
 - compute a global warp: y' = y + ax
 - run a big optimization problem, incorporating this constraint
 - best solution, but more complicated
 - known as "bundle adjustment"

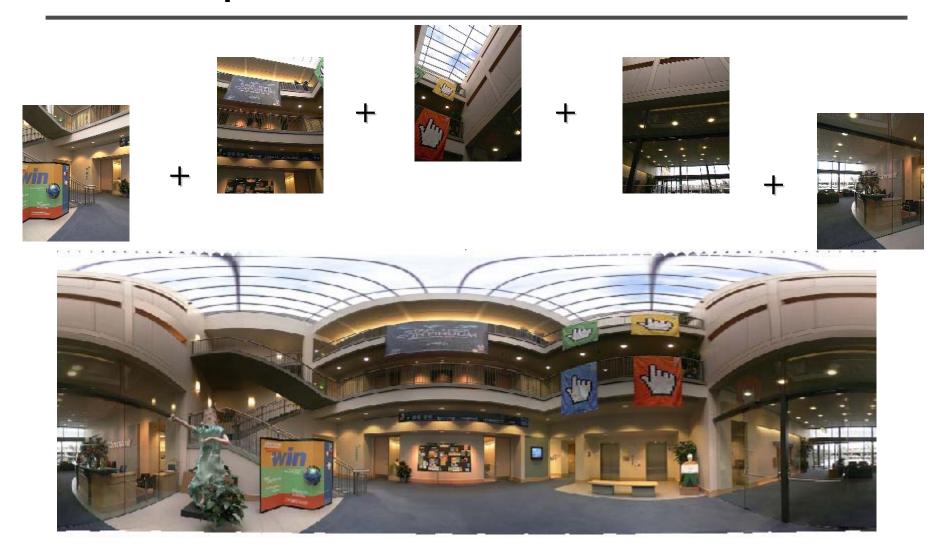








Viewer: panorama



example: http://www.cs.washington.edu/education/courses/cse590ss/01wi/projects/project1/students/dougz/index.html

Viewer: texture mapped model





example: http://www.panoramas.dk/

Cylindrical panorama



- 1. Take pictures on a tripod (or handheld)
- 2. Warp to cylindrical coordinate
- 3. Compute pairwise alignments
- 4. Fix up the end-to-end alignment
- 5. Blending
- 6. Crop the result and import into a viewer



Determine pairwise alignment?

- Feature-based methods: only use feature points to estimate parameters
- We will study the "Recognising panorama" paper published in ICCV 2003
- Run SIFT for each image, find feature matches.

Determine pairwise alignment

- p'=Mp, where M is a transformation matrix, p and p' are feature matches
- It is possible to use more complicated models such as affine or perspective
- For example, assume M is a 2x2 matrix

$$\begin{pmatrix} x' \\ y' \end{pmatrix} = \begin{pmatrix} m_{11} & m_{12} \\ m_{21} & m_{22} \end{pmatrix} \begin{pmatrix} x \\ y \end{pmatrix}$$

• Find M with the least square error

$$\sum_{i=1}^n (Mp - p')^2$$



Determine pairwise alignment

$$\begin{pmatrix} x' \\ y' \end{pmatrix} = \begin{pmatrix} m_{11} & m_{12} \\ m_{21} & m_{22} \end{pmatrix} \begin{pmatrix} x \\ y \end{pmatrix}$$

$$x_1 m_{11} + y_1 m_{12} = x_1$$
$$x_1 m_{21} + y_1 m_{22} = y_1$$

• Overdetermined system

$$\begin{pmatrix} x_1 & y_1 & 0 & 0 \\ 0 & 0 & x_1 & y_1 \\ x_2 & y_2 & 0 & 0 \\ \vdots & \vdots & \vdots & \vdots \\ x_n & y_n & 0 & 0 \\ 0 & 0 & x_n & y_n \end{pmatrix} \begin{pmatrix} m_{11} \\ m_{12} \\ m_{21} \\ m_{22} \end{pmatrix} = \begin{pmatrix} x_1 \\ y_1 \\ x_2 \\ \vdots \\ m_{21} \\ m_{22} \end{pmatrix}$$



Given an overdetermined system

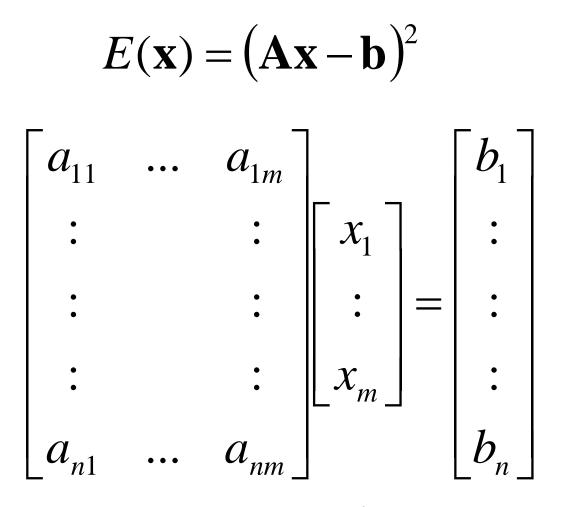
$\mathbf{A}\mathbf{x} = \mathbf{b}$

the normal equation is that which minimizes the sum of the square differences between left and right sides

$\mathbf{A}^{\mathrm{T}}\mathbf{A}\mathbf{x} = \mathbf{A}^{\mathrm{T}}\mathbf{b}$

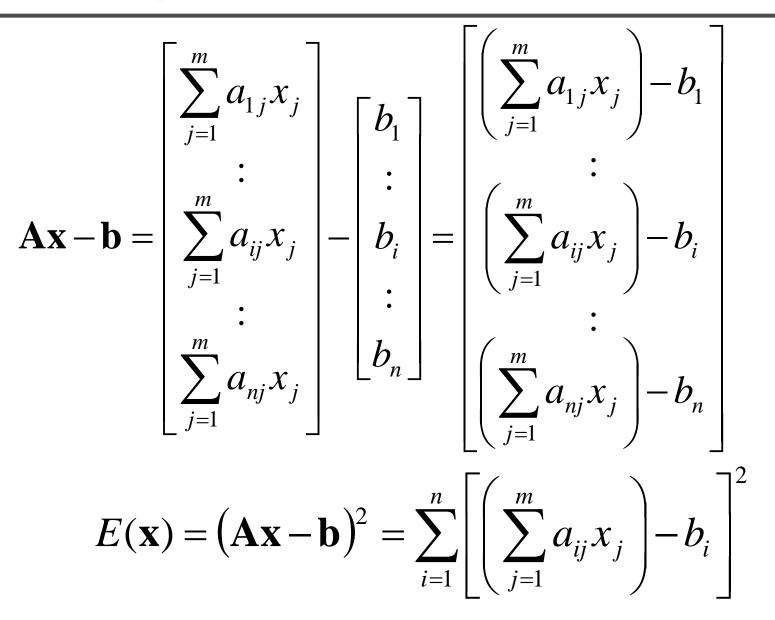
Why?





nXm, *n* equations, *m* variables







$$E(\mathbf{x}) = (\mathbf{A}\mathbf{x} - \mathbf{b})^2 = \sum_{i=1}^n \left[\left(\sum_{j=1}^m a_{ij} x_j \right) - b_i \right]^2$$
$$0 = \frac{\partial E}{\partial x_1} = \sum_{i=1}^n 2 \left[\left(\sum_{j=1}^m a_{ij} x_j \right) - b_i \right] a_{i1}$$
$$= 2 \sum_{i=1}^n a_{i1} \sum_{j=1}^m a_{ij} x_j - 2 \sum_{i=1}^n a_{i1} b_i$$

$$0 = \frac{\partial E}{\partial \mathbf{x}} = 2(\mathbf{A}^{\mathrm{T}}\mathbf{A}\mathbf{x} - \mathbf{A}^{\mathrm{T}}\mathbf{b}) \rightarrow \mathbf{A}^{\mathrm{T}}\mathbf{A}\mathbf{x} = \mathbf{A}^{\mathrm{T}}\mathbf{b}$$



$$(\mathbf{A}\mathbf{x} - \mathbf{b})^{2}$$

= $(\mathbf{A}\mathbf{x} - \mathbf{b})^{T} (\mathbf{A}\mathbf{x} - \mathbf{b})$
= $((\mathbf{A}\mathbf{x})^{T} - \mathbf{b}^{T})(\mathbf{A}\mathbf{x} - \mathbf{b})$
= $(\mathbf{x}^{T}\mathbf{A}^{T} - \mathbf{b}^{T})(\mathbf{A}\mathbf{x} - \mathbf{b})$
= $\mathbf{x}^{T}\mathbf{A}^{T}\mathbf{A}\mathbf{x} - \mathbf{b}^{T}\mathbf{A}\mathbf{x} - \mathbf{x}^{T}\mathbf{A}^{T}\mathbf{b} + \mathbf{b}^{T}\mathbf{b}$
= $\mathbf{x}^{T}\mathbf{A}^{T}\mathbf{A}\mathbf{x} - (\mathbf{A}^{T}\mathbf{b})^{T}\mathbf{x} - (\mathbf{A}^{T}\mathbf{b})^{T}\mathbf{x} + \mathbf{b}^{T}\mathbf{b}$
 $\frac{\partial E}{\partial \mathbf{x}} = 2\mathbf{A}^{T}\mathbf{A}\mathbf{x} - 2\mathbf{A}^{T}\mathbf{b}$

Determine pairwise alignment?

- p'=Mp, where M is a transformation matrix, p and p' are feature matches
- For translation model, it is easier.

$$E = \sum_{i=1}^{n} \left[\left(m_1 + x_i - x_i^{'} \right)^2 + \left(m_2 + y_i - y_i^{'} \right)^2 \right]$$

$$0 = \frac{\partial E}{\partial m_1}$$

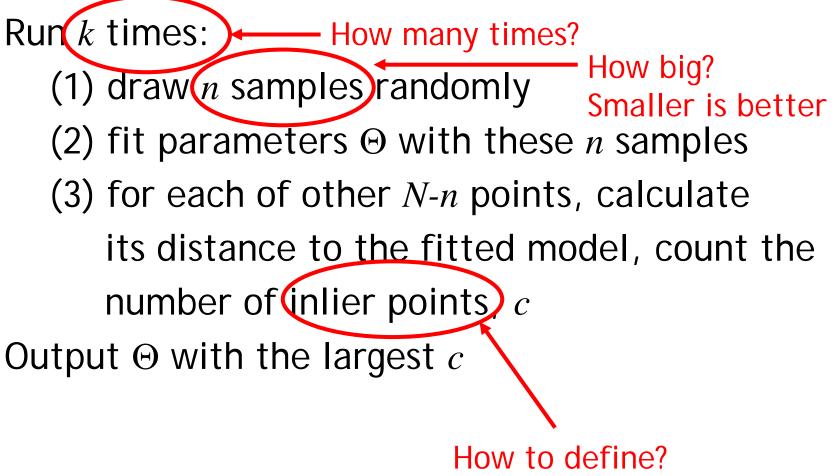
• What if the match is false? Avoid impact of outliers.



- RANSAC = Random Sample Consensus
- an algorithm for robust fitting of models in the presence of many data outliers
- Compare to robust statistics
- Given N data points x_i, assume that mjority of them are generated from a model with parameters Θ, try to recover Θ.



RANSAC algorithm



Depends on the problem.



p: probability of real inliers

P: probability of success after k trials

$$P = 1 - (1 - p^{n})^{k}$$

n samples are all inliers
a failure
failure after k trials
$$k = \frac{\log(1 - P)}{\log(1 - p^{n})}$$
 for $P = 0.99$
$$\frac{n p k}{3 0.5 35}$$

 $\frac{6 0.6 97}{6 0.5 293}$

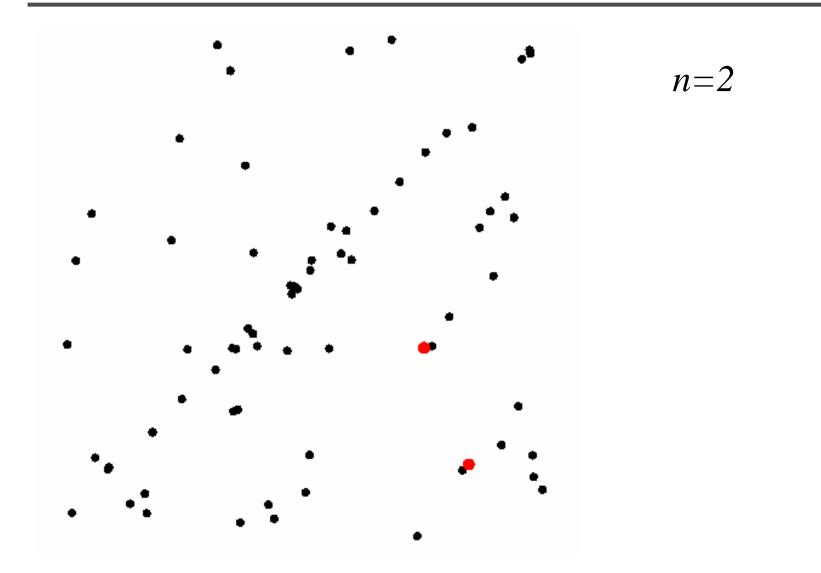


Example: line fitting



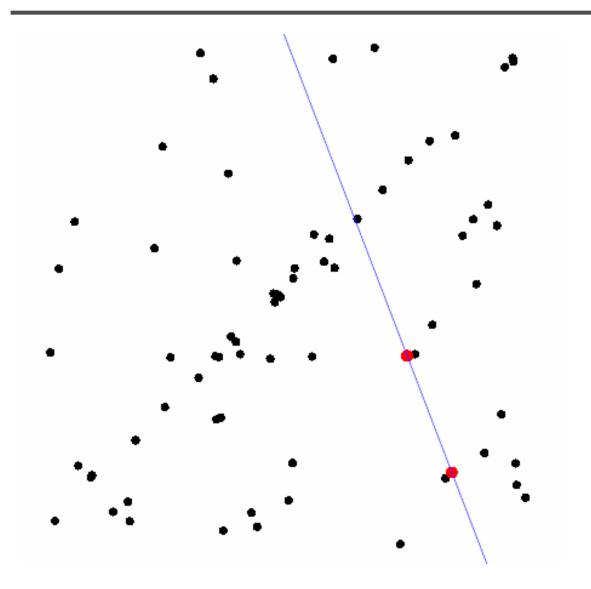
Example: line fitting





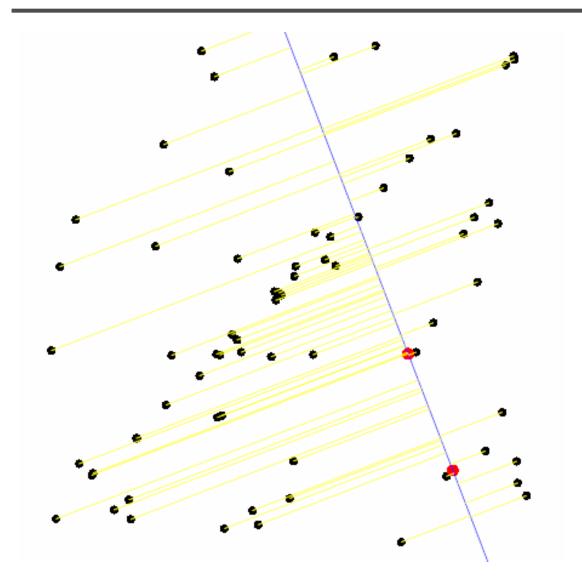


Model fitting



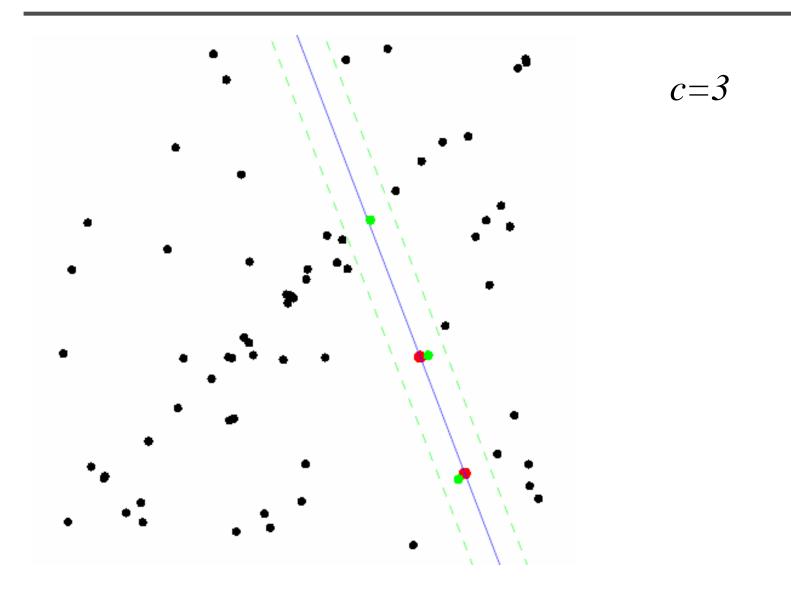


Measure distances



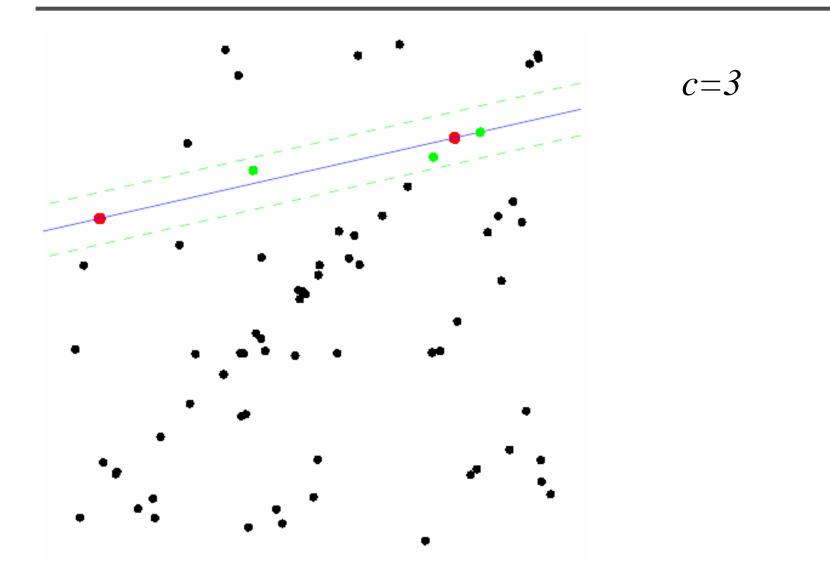


Count inliers



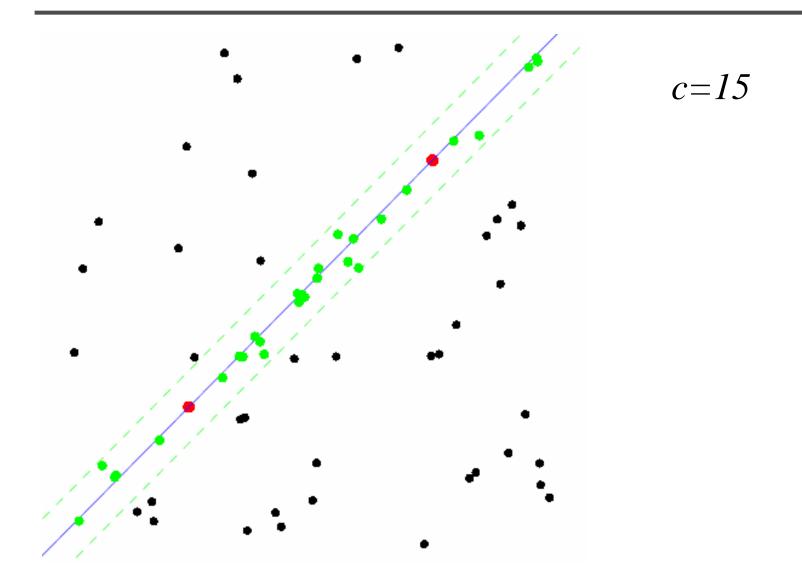


Another trial



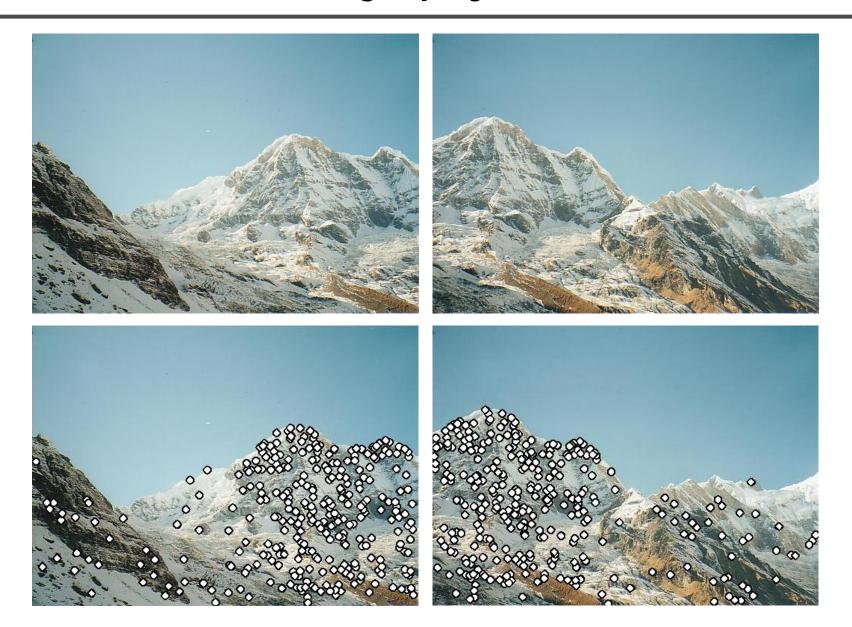






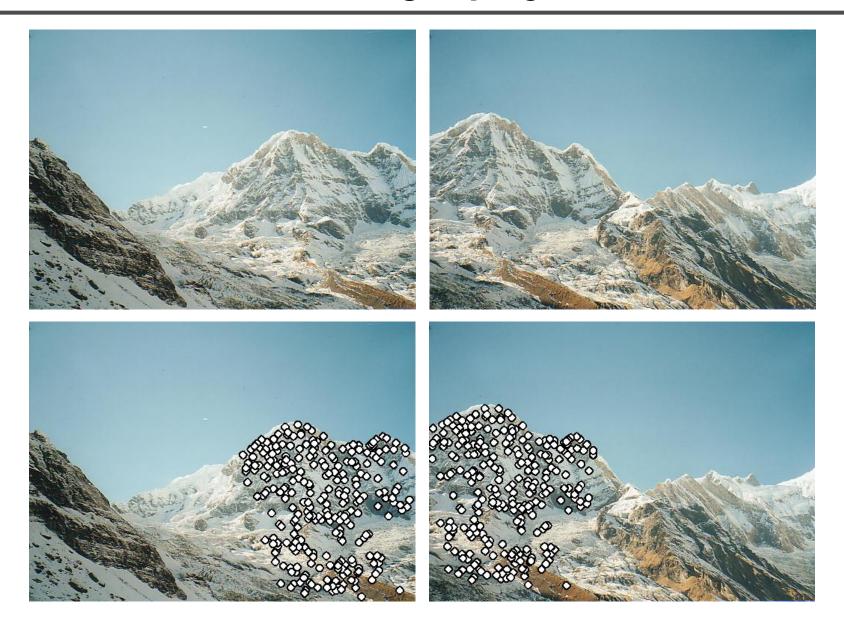
RANSAC for Homography





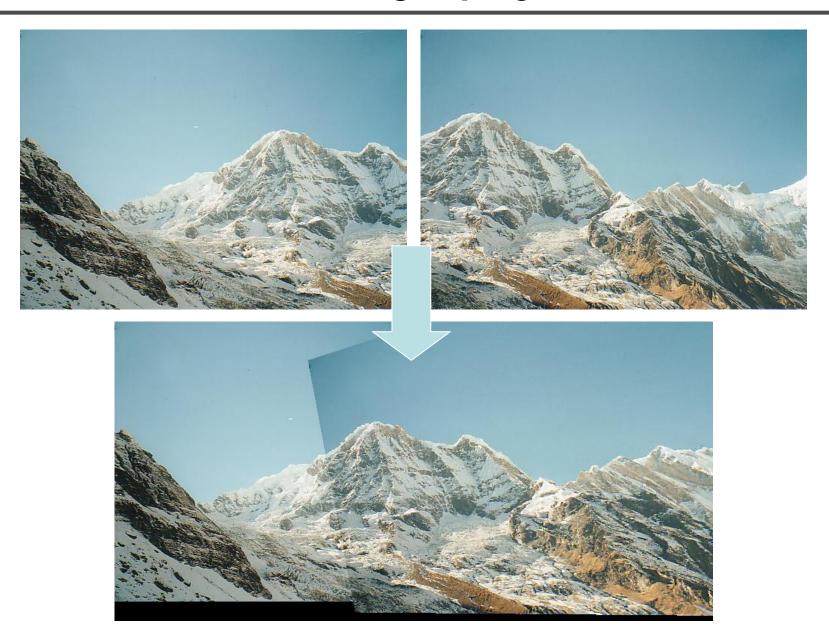
RANSAC for Homography





RANSAC for Homography







Applications of panorama in VFX

- Background plates
- Image-based lighting

Spiderman 2 (background plate)











http://www.cgnetworks.com/story_custom.php?story_id=2195&page=4