# Color and Radiometry

Digital Image Synthesis

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with slides by Pat Hanrahan and Matt Pharr

### **Basic radiometry**

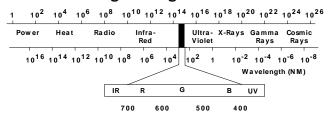


- pbrt is based on radiative transfer: study of the transfer of radiant energy based on radiometric principles and operates at the geometric optics level (light interacts with objects much larger than the light's wavelength)
- It is based on the particle model. Hence, diffraction and interference can't be easily accounted for.

#### Radiometry



- Radiometry: study of the propagation of electromagnetic radiation in an environment
- Four key quantities: flux, intensity, irradiance and radiance
- These radiometric quantities are described by their spectral power distribution (SPD)
- Human visible light ranges from 370nm to 730nm



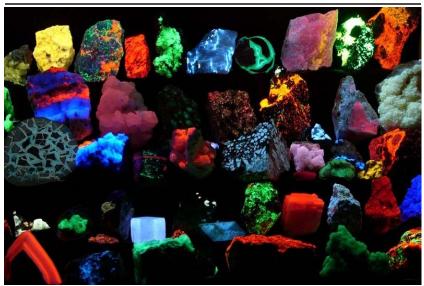
# Basic assumptions about light behavior



- **Linearity**: the combined effect of two inputs is equal to the sum of effects
- Energy conservation: scattering event can't produce more energy than they started with
- **Steady state**: light is assumed to have reached equilibrium, so its radiance distribution isn't changing over time.
- **No polarization:** we only care the frequency of light but not other properties (such as phases)
- No fluorescence or phosphorescence: behavior of light at a wavelength or time doesn't affect the behavior of light at other wavelengths or time

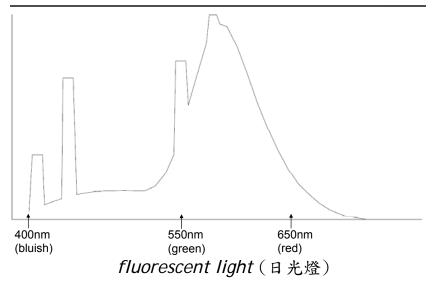
#### Fluorescent materials





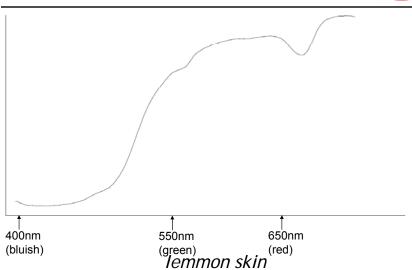
# Spectral power distribution





# Spectral power distribution





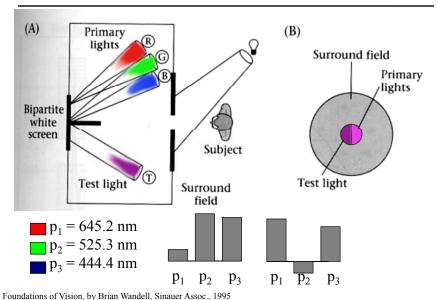
#### Color



- Need a compact, efficient and accurate way to represent functions like these
- Find proper basis functions to map the infinitedimensional space of all possible SPD functions to a low-dimensional space of coefficients
- For example,  $B(\lambda)=1$  is a trivial but bad approximation

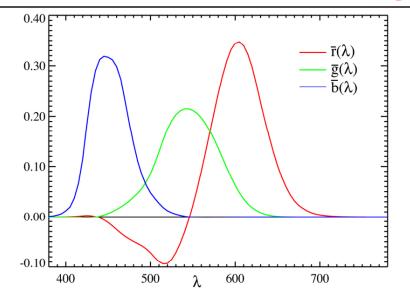
# Color matching experiment





# Color matching experiment

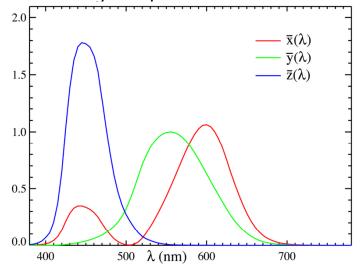




# Color matching experiment

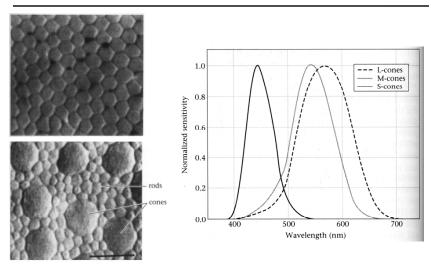


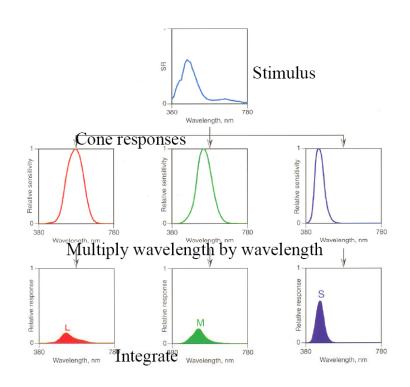
• To avoid negative parameters



# **Human Photoreceptors**

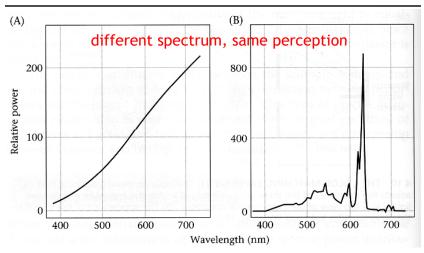






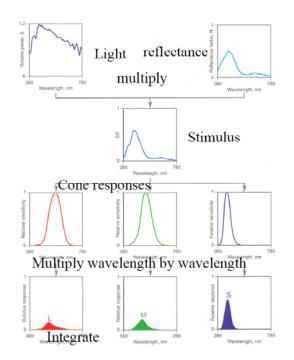
#### **Metamers**





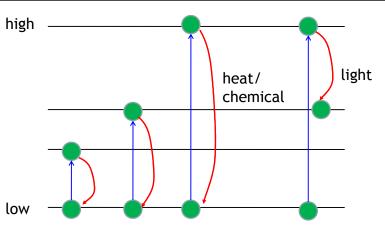
tungsten (鎢絲) bulb

television monitor



# Why reflecting different colors



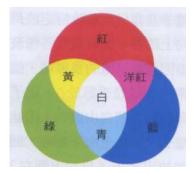


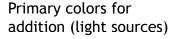
Light with specific wavelengths are absorbed.

Fluorescent

#### **Primary colors**









Primary colors for subtraction (reflection)

#### Heat generates light



- Vibration of atoms or electrons due to heat generates electromagnetic radiation as well. If its wavelength is within visible light (>1000K), it generates color as well.
- Color only depends on temperature, but not property of the object.
- Human body radiates IR light under room temperature.
- 2400-2900K: color temperature of incandescent light bulb

#### Spectrum



- In core/color.\*
- Not a plug-in, to use inline for performance
- Spectrum stores a fixed number of samples at a fixed set of wavelengths. Better for smooth functions. Why is this possible? Human vision system

#### Human visual system

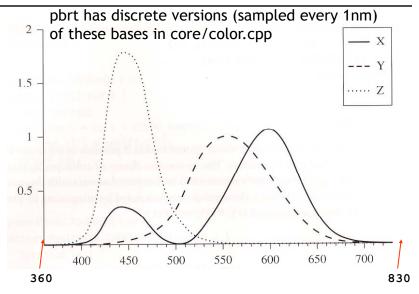


- Tristimulus theory: all visible SPDs S can be accurately represented for human observers with three values,  $x_{\lambda}$ ,  $y_{\lambda}$  and  $z_{\lambda}$ .
- The basis are the *spectral matching curves*,  $X(\lambda)$ ,  $Y(\lambda)$  and  $Z(\lambda)$  determined by CIE (國際照明委員會).

$$x_{\lambda} = \int_{\lambda} S(\lambda) X(\lambda) d\lambda$$
$$y_{\lambda} = \int_{\lambda} S(\lambda) Y(\lambda) d\lambda$$
$$z_{\lambda} = \int_{\lambda} S(\lambda) Z(\lambda) d\lambda$$

#### XYZ basis





#### XYZ color



- Good for representing visible SPD to human observer, but not good for spectral computation.
- A product of two SPD's XYZ values is likely different from the XYZ values of the SPD which is the product of the two original SPDs.
- Hence, we often have to convert our samples (RGB) into XYZ

```
void XYZ(float xyz[3]) const {
  xyz[0] = xyz[1] = xyz[2] = 0.;
  for (int i = 0; i < COLOR_SAMPLES; ++i) {
    xyz[0] += XWeight[i] * c[i];
    xyz[1] += YWeight[i] * c[i];
    xyz[2] += ZWeight[i] * c[i];
}
}</pre>
```

#### Conversion between XYZ and RGB



```
float Spectrum::XWeight[COLOR SAMPLES] = {
  0.412453f, 0.357580f, 0.180423f
};
float Spectrum::YWeight[COLOR SAMPLES] = {
  0.212671f, 0.715160f, 0.072169f
};
float Spectrum::ZWeight[COLOR_SAMPLES] = {
  0.019334f, 0.119193f, 0.950227f
Spectrum FromXYZ(float x, float y, float z) {
  float c[3];
  c[0] = 3.240479f * x + -1.537150f * y + -
  0.498535f * z;
  c[1] = -0.969256f * x + 1.875991f * y +
  0.041556f * z;
  c[2] = 0.055648f * x + -0.204043f * y +
  1.057311f * z;
  return Spectrum(c);
```

#### Conversion between XYZ and RGB



# **Basic quantities**



non-directional

Flux: power, (W)

Irradiance: flux density per area, (W/m²)

directional

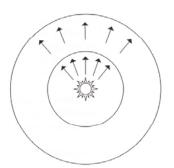
Intensity: flux density per solid angle

Radiance: flux density per solid angle per area

# Flux (Φ)



- Radiant flux, power
- Total amount of energy passing through a surface per unit of time (J/s,W)



### Irradiance (E)

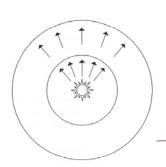


• Area density of flux (W/m<sup>2</sup>)  $E = \frac{d\Phi}{dA}$ 

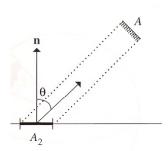
$$=\frac{\Phi}{4\pi r^2}$$

$$E = \frac{\Phi}{}$$

Lambert's law
$$E = \frac{\Phi \cos \theta}{4}$$



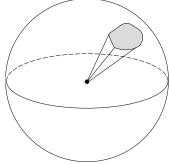




# Angles and solid angles



- Angle  $\theta = \frac{l}{r}$ 
  - $\Rightarrow$  circle has  $2\pi$  radians
- Solid angle  $\Omega = \frac{A}{R^2}$



The solid angle subtended by a surface is defined as the surface area of a unit sphere covered by the surface's projection onto the sphere.

 $\Rightarrow$  sphere has  $4\pi$  steradians

### Intensity (I)

- Flux density per solid angle  $I = \frac{d\Phi}{d\omega}$
- Intensity describes the directional distribution of light

$$I(\omega) \equiv \frac{d\Phi}{d\omega}$$

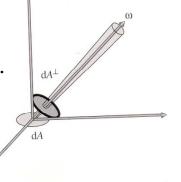
# Radiance (L)



• Flux density per unit area per solid angle

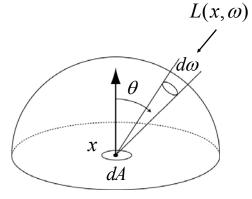
$$L = \frac{d\Phi}{d\omega dA^{\perp}}$$

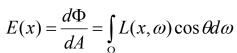
- Most frequently used, remains constant along ray.
- All other quantities can be derived from radiance



### Calculate irradiance from radiance

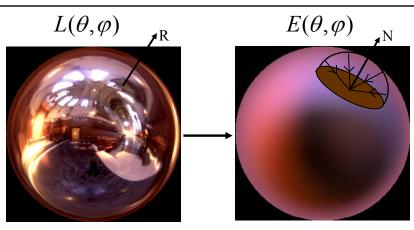








# **Irradiance Environment Maps**

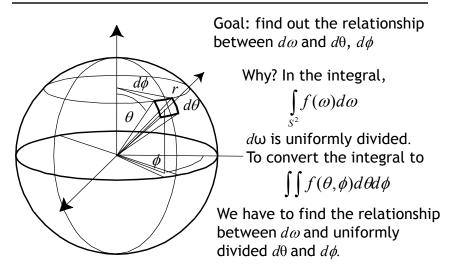


Radiance Environment Map

Irradiance Environment Map

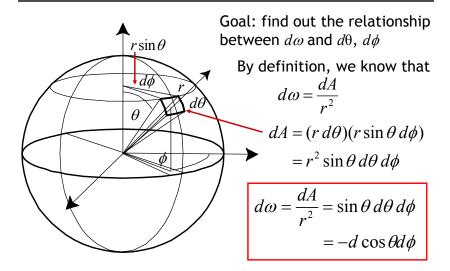
#### Differential solid angles





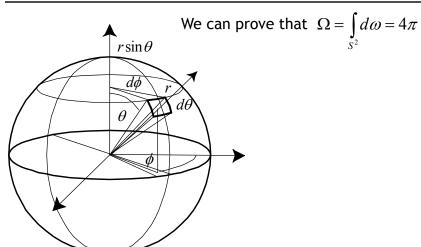
### Differential solid angles





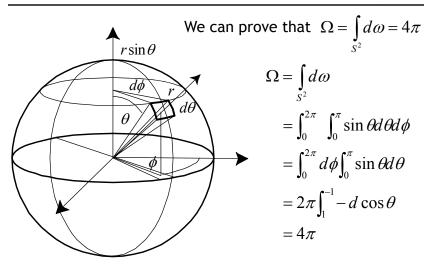
### Differential solid angles





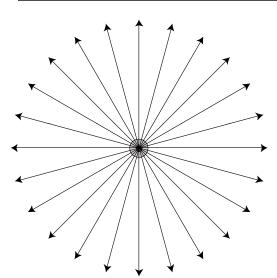
### Differential solid angles





### Isotropic point source

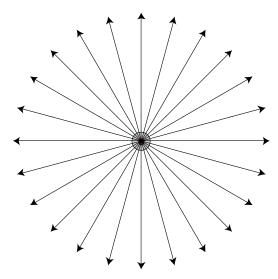




If the total flux of the light source is  $\Phi$ , what is the intensity?

### Isotropic point source





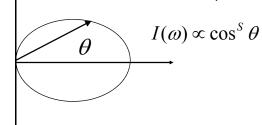
If the total flux of the light source is  $\Phi$ , what is the intensity?

$$\Phi = \int_{S^2} I \, d\omega$$
$$= 4\pi I$$
$$I = \frac{\Phi}{4\pi}$$

### Warn's spotlight



If the total flux is  $\Phi$ , what is the intensity?



# Warn's spotlight



If the total flux is  $\Phi$ , what is the intensity?

