## Color and Radiometry

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## Radiometry



- Radiometry: study of the propagation of electromagnetic radiation in an environment
- Four key quantities: flux, intensity, irradiance and radiance
- These radiometric quantities are described by their spectral power distribution (SPD)
- Human visible light ranges from 370nm to 730nm





- pbrt is based on radiative transfer: study of the transfer of radiant energy based on radiometric principles and operates at the geometric optics level (light interacts with objects much larger than the light's wavelength)
- It is based on the particle model. Hence, diffraction and interference can't be easily accounted for.

## Basic assumptions about light behavior

- Linearity: the combined effect of two inputs is equal to the sum of effects
- Energy conservation: scattering event can't produce more energy than they started with
- Steady state: light is assumed to have reached equilibrium, so its radiance distribution isn't changing over time.
- No polarization: we only care the frequency of light but not other properties (such as phases)
- No fluorescence or phosphorescence: behavior of light at a wavelength or time doesn't affect the behavior of light at other wavelengths or time

#### Fluorescent materials





### Spectral power distribution











- Need a compact, efficient and accurate way to represent functions like these
- Find proper basis functions to map the infinitedimensional space of all possible SPD functions to a low-dimensional space of coefficients
- For example,  $B(\lambda)=1$  is a trivial but bad approximation

## **Color matching experiment**





Foundations of Vision, by Brian Wandell, Sinauer Assoc., 1995





Color matching experiment





#### Human Photoreceptors







**Metamers** 





tungsten (鎢絲) bulb

television monitor











Primary colors for addition (light sources)



Primary colors for subtraction (reflection)



- Vibration of atoms or electrons due to heat generates electromagnetic radiation as well. If its wavelength is within visible light (>1000K), it generates color as well.
- Color only depends on temperature, but not property of the object.
- Human body radiates IR light under room temperature.
- 2400-2900K: color temperature of incandescent light bulb



- In core/color.\*
- Not a plug-in, to use inline for performance
- Spectrum stores a fixed number of samples at a fixed set of wavelengths. Better for smooth functions. Why is this possible? Human vision system

```
#define COLOR_SAMPLE 3 We actually sample RGB
class COREDLL Spectrum {
  public:
```

<arithmetic operations>
private:

```
component-wise
+ - * / comparison...
```

```
float c[COLOR_SAMPLES];
```



- Tristimulus theory: all visible SPDs S can be accurately represented for human observers with three values,  $x_{\lambda}$ ,  $y_{\lambda}$  and  $z_{\lambda}$ .
- The basis are the *spectral matching curves*, X(λ), Y(λ) and Z(λ) determined by CIE (國際照明委員會).

$$\begin{aligned} x_{\lambda} &= \int_{\lambda} S(\lambda) X(\lambda) d\lambda \\ y_{\lambda} &= \int_{\lambda} S(\lambda) Y(\lambda) d\lambda \\ z_{\lambda} &= \int_{\lambda} S(\lambda) Z(\lambda) d\lambda \end{aligned}$$

#### **XYZ** basis





## XYZ color



- Good for representing visible SPD to human observer, but not good for spectral computation.
- A product of two SPD's XYZ values is likely different from the XYZ values of the SPD which is the product of the two original SPDs.
- Hence, we often have to convert our samples (RGB) into XYZ

```
void XYZ(float xyz[3]) const {
    xyz[0] = xyz[1] = xyz[2] = 0.;
    for (int i = 0; i < COLOR_SAMPLES; ++i) {
        xyz[0] += XWeight[i] * c[i];
        xyz[1] += YWeight[i] * c[i];
        xyz[2] += ZWeight[i] * c[i];
    }
}</pre>
```

#### **Conversion between XYZ and RGB**



```
float Spectrum::XWeight[COLOR_SAMPLES] = {
  0.412453f, 0.357580f, 0.180423f
};
float Spectrum::YWeight[COLOR_SAMPLES] = {
  0.212671f, 0.715160f, 0.072169f
};
float Spectrum::ZWeight[COLOR_SAMPLES] = {
  0.019334f, 0.119193f, 0.950227f
};
Spectrum FromXYZ(float x, float y, float z) {
  float c[3];
  c[0] = 3.240479f * x + -1.537150f * y + -
  0.498535f * z;
  c[1] = -0.969256f * x + 1.875991f * y +
  0.041556f * z;
  c[2] = 0.055648f * x + -0.204043f * y +
  1.057311f * z;
  return Spectrum(c);
}
```

#### **Conversion between XYZ and RGB**







non-directional

Flux: power, (W)

Irradiance: flux density per area, (W/m<sup>2</sup>)

<u>directional</u>

Intensity: flux density per solid angle Radiance: flux density per solid angle per area

# Flux (Φ)



- Radiant flux, power
- Total amount of energy passing through a surface per unit of time (J/s,W)



## Irradiance (E)







The solid angle subtended by a surface is defined as the surface area of a unit sphere covered by the surface's projection onto the sphere.

 $\Rightarrow$  sphere has  $4\pi$  steradians

## Intensity (I)



- Flux density per solid angle  $I = \frac{d\Phi}{d\omega}$  Intensity describes the directional distribution of light



![](_page_29_Picture_1.jpeg)

- Flux density per unit area per solid angle
  - $L = \frac{d\Phi}{d\omega dA^{\perp}}$
- Most frequently used, remains constant along ray.
- All other quantities can be derived from radiance

![](_page_29_Figure_6.jpeg)

![](_page_30_Picture_1.jpeg)

![](_page_30_Figure_2.jpeg)

![](_page_31_Picture_0.jpeg)

![](_page_31_Picture_1.jpeg)

Ν

 $L(\theta, \varphi)$  $E(\theta, \varphi)$ **∕**R

Radiance Environment Map Irradiance Environment Map

![](_page_32_Picture_1.jpeg)

![](_page_32_Figure_2.jpeg)

Goal: find out the relationship between  $d\omega$  and  $d\theta$ ,  $d\phi$ 

Why? In the integral,  $\int_{C^2} f(\omega) d\omega$ 

 $d\omega$  is uniformly divided. To convert the integral to  $\iint f(\theta, \phi) d\theta d\phi$ 

We have to find the relationship between  $d\omega$  and uniformly divided  $d\theta$  and  $d\phi$ .

![](_page_33_Picture_1.jpeg)

![](_page_33_Figure_2.jpeg)

![](_page_34_Figure_1.jpeg)

![](_page_34_Figure_2.jpeg)

![](_page_35_Picture_1.jpeg)

![](_page_35_Figure_2.jpeg)

![](_page_36_Picture_1.jpeg)

![](_page_36_Figure_2.jpeg)

If the total flux of the light source is  $\Phi$ , what is the intensity?

![](_page_37_Picture_1.jpeg)

![](_page_37_Figure_2.jpeg)

![](_page_38_Picture_1.jpeg)

![](_page_38_Figure_2.jpeg)

![](_page_39_Picture_1.jpeg)

![](_page_39_Figure_2.jpeg)