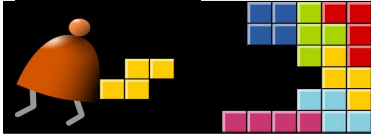


Machine (Assembly) Language



Building a Modern Computer From First Principles

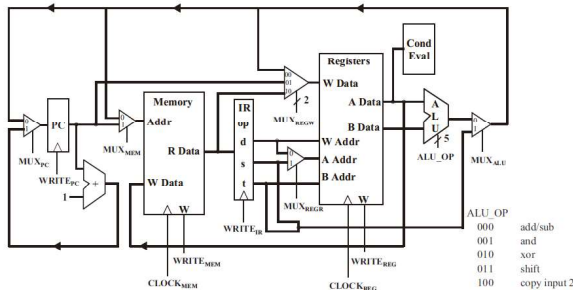
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Machine language

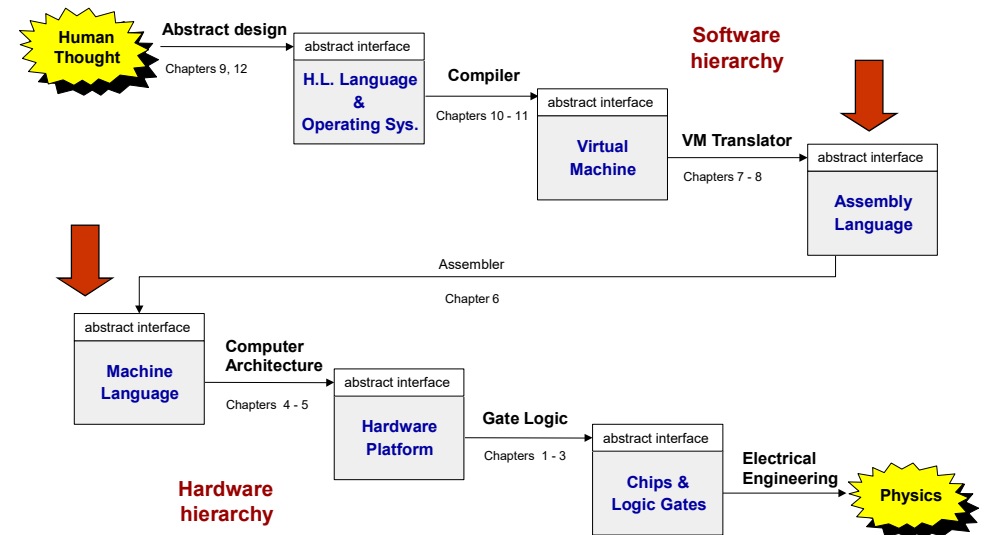
Abstraction - implementation duality:

- Machine language (= instruction set) can be viewed as a programmer-oriented abstraction of the hardware platform
- The hardware platform can be viewed as a physical means for realizing the machine language abstraction

#	Operation	Fmt	Pseudocode
0:	halt	1	exit(0)
1:	add	1	$R[d] \leftarrow R[s] + R[t]$
2:	subtract	1	$R[d] \leftarrow R[s] - R[t]$
3:	and	1	$R[d] \leftarrow R[s] \& R[t]$
4:	xor	1	$R[d] \leftarrow R[s] \wedge R[t]$
5:	shift left	1	$R[d] \leftarrow R[s] \ll R[t]$
6:	shift right	1	$R[d] \leftarrow R[s] \gg R[t]$
7:	load addr	2	$R[d] \leftarrow \text{addr}$
8:	load	2	$R[d] \leftarrow \text{mem}[\text{addr}]$
9:	store	2	$\text{mem}[\text{addr}] \leftarrow R[d]$
A:	load indirect	1	$R[d] \leftarrow \text{mem}[R[t]]$
B:	store indirect	1	$\text{mem}[R[t]] \leftarrow R[d]$
C:	branch zero	2	if $(R[d] == 0)$ pc \leftarrow addr
D:	branch positive	2	if $(R[d] > 0)$ pc \leftarrow addr
E:	jump register	1	pc $\leftarrow R[t]$
F:	jump and link	2	$R[d] \leftarrow$ pc; pc \leftarrow addr



Where we are at:



Machine language

Abstraction - implementation duality:

- Machine language (= instruction set) can be viewed as a programmer-oriented abstraction of the hardware platform
- The hardware platform can be viewed as a physical means for realizing the machine language abstraction

Another duality:

- Binary version: 0001 0001 0010 0011 (machine code)
- Symbolic version: ADD R1, R2, R3 (assembly)

Machine language

Abstraction - implementation duality:

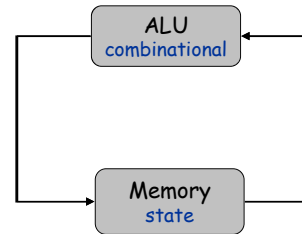
- Machine language (= instruction set) can be viewed as a programmer-oriented abstraction of the hardware platform
- The hardware platform can be viewed as a physical means for realizing the machine language abstraction

Another duality:

- Binary version
- Symbolic version

Loose definition:

- Machine language = an agreed-upon formalism for manipulating a memory using a processor and a set of registers
- Same spirit but different syntax across different hardware platforms.



Typical machine language commands (3 types)

- ALU operations
- Memory access operations
(addressing mode: how to specify operands)
 - Immediate addressing, LDA R1, 67 // R1=67
 - Direct addressing, LD R1, 67 // R1=M[67]
 - Indirect addressing, LDI R1, R2 // R1=M[R2]
- Flow control operations

Lecture plan

- Machine languages at a glance
- The Hack machine language:
 - Symbolic version
 - Binary version
- Perspective

(The assembler will be covered in chapter 6).

Typical machine language commands (a small sample)

```
// In what follows R1,R2,R3 are registers, PC is program counter,
// and addr is some value.

ADD R1,R2,R3    // R1 ← R2 + R3

ADDI R1,R2,addr // R1 ← R2 + addr

AND R1,R1,R2    // R1 ← R1 and R2 (bit-wise)

JMP addr        // PC ← addr

JEQ R1,R2,addr  // IF R1 == R2 THEN PC ← addr ELSE PC++

LOAD R1, addr   // R1 ← RAM[addr]

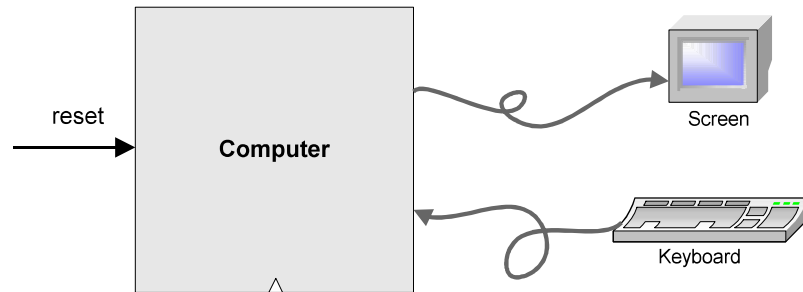
STORE R1, addr  // RAM[addr] ← R1

NOP             // Do nothing

// Etc. - some 50-300 command variants
```

The Hack computer

A 16-bit machine consisting of the following elements:



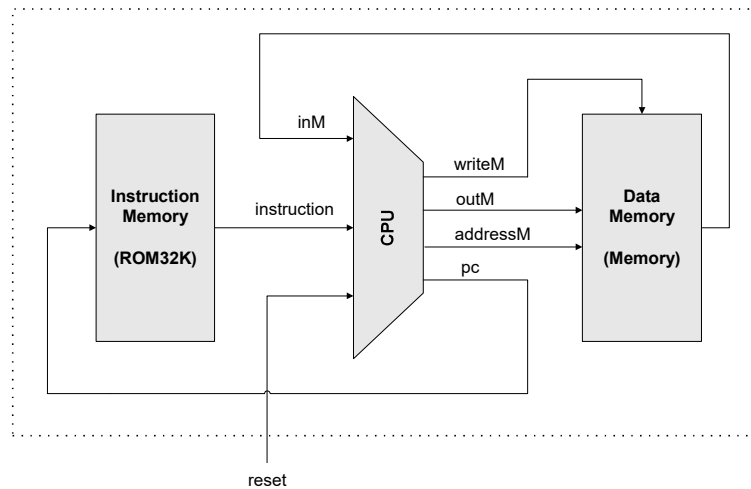
The Hack computer

- The ROM is loaded with a Hack program
- The reset button is pushed
- The program starts running



The Hack computer

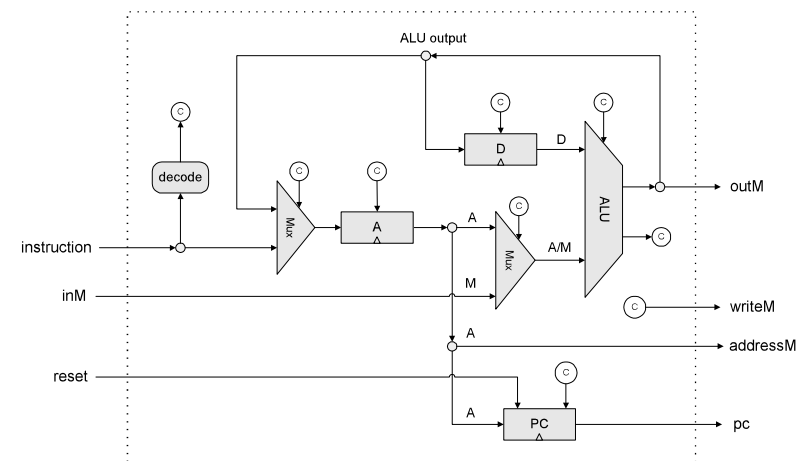
A 16-bit machine consisting of the following elements:



Both memory chips are 16-bit wide and have 15-bit address space.

The Hack computer (CPU)

A 16-bit machine consisting of the following elements:



The Hack computer

A 16-bit machine consisting of the following elements:

Data memory: **RAM** - an addressable sequence of registers

Instruction memory: **ROM** - an addressable sequence of registers

Registers: **D, A, M**, where **M** stands for **RAM[A]**

Processing: **ALU**, capable of computing various functions

Program counter: **PC**, holding an address

Control: The **ROM** is loaded with a sequence of 16-bit instructions, one per memory location, beginning at address 0. Fetch-execute cycle: later

Instruction set: Two instructions: A-instruction, C-instruction.

The A-instruction

```
@value // A ← value
```

Where *value* is either a number or a symbol referring to some number.

Why A-instruction?

In TOY, we store address in the instruction (fmt #2). But, it is impossible to pack a 15-bit address into a 16-bit instruction. So, we have the A-instruction for setting addresses if needed.

Example: @21

Effect:

- Sets the A register to 21
- RAM[21] becomes the selected RAM register M

The A-instruction

```
@value // A ← value
```

Used for:

- Entering a constant value
(**A = value**)

Coding example:

```
@17 // A = 17  
D = A // D = 17
```

- Selecting a RAM location
(**register = RAM[A]**)

```
@17 // A = 17  
D = M // D = RAM[17]  
M = -1 // RAM[17] = -1
```

- Selecting a ROM location
(**PC = A**)

```
@17 // A = 17  
JMP // fetch the instruction  
// stored in ROM[17]
```

The C-instruction

```
dest = comp ; jump
```

Both *dest* and *jump* are optional.

First, we compute something.

Next, optionally, we can store the result, or use it to jump to somewhere to continue the program execution.

comp:

```
0, 1, -1, D, A, !D, !A, -D, -A, D+1, A+1, D-1, A-1, D+A, D-A, A-D, D&A, D|A  
M, !M, -M, M+1, M-1, D+M, D-M, M-D, D&M, D|M
```

dest: null, A, D, M, MD, AM, AD, AMD

jump: null, JGT, JEQ, JLT, JGE, JNE, JLE, JMP

Compare to zero. If the condition holds, jump to ROM[A]

The C-instruction

dest = comp ; jump

- Computes the value of comp
- Stores the result in dest
- If (the condition jump compares to zero is true), goto the instruction at ROM[A].

Hack programming reference card

Hack commands:

A-command: @value // set A to value

C-command: dest = comp ; jump // dest = and ;jump
// are optional

Where:

comp =

0, 1, -1, D, A, !D, !A, -D, -A, D+1, A+1, D-1, A-1, D+A, D-A, A-D, D&A, D|A,
M, !M, -M, M+1, M-1, D+M, D-M, M-D, D&M, D|M

dest = M, D, A, MD, AM, AD, AMD, or null

jump = JGT, JEQ, JGE, JLT, JNE, JLE, JMP, or null

In the command dest = comp; jump, the jump materializes if (comp jump 0) is true. For example, in D=D+1,JLT, we jump if D+1 < 0.

The C-instruction

dest = comp ; jump

comp:

0, 1, -1, D, A, !D, !A, -D, -A, D+1, A+1, D-1, A-1, D+A, D-A, A-D, D&A, D|A
M, !M, -M, M+1, M-1, D+M, D-M, M-D, D&M, D|M

dest: null, A, D, M, MD, AM, AD, AMD

jump: null, JGT, JEQ, JLT, JGE, JNE, JLE, JMP

Example: set the D register to -1

D = -1

Example: set RAM[300] to the value of the D register minus 1

@300

M = D-1

Example: if ((D-1) == 0) goto ROM[56]

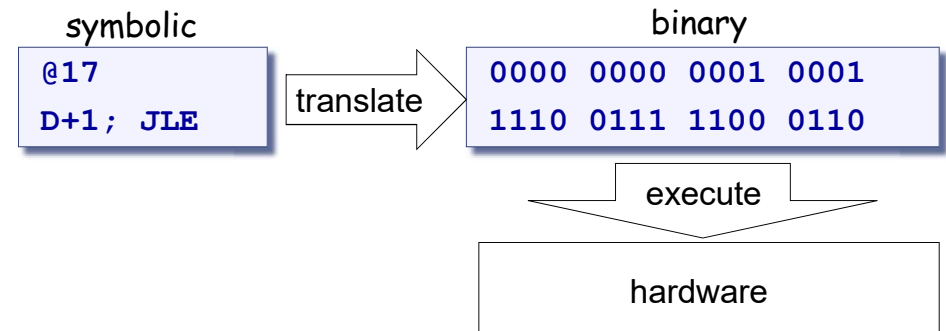
@56

D-1; JEQ

The Hack machine language

Two ways to express the same semantics:

- Binary code (machine language)
- Symbolic language (assembly)



The A-instruction

symbolic

@value

- value is a non-negative decimal number $\leq 2^{15}-1$ or
- A symbol referring to such a constant

binary

0value

- value is a 15-bit binary number

Example

@21

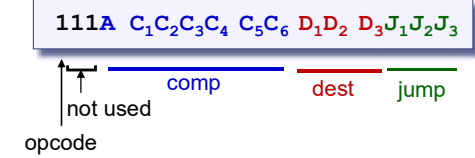
0000 0000 0001 0101

The C-instruction

symbolic

dest = comp ; jump

binary



The C-instruction

111A C₁C₂C₃C₄ C₅C₆ D₁D₂ D₃J₁J₂J₃

	comp			dest			jump		
(when a=D) comp	c1	c2	c3	c4	c5	c6	(when a=1) comp		
0	1	0	1	0	1	0			
1	1	1	1	1	1	1			
-1	1	1	1	0	1	0			
D	0	0	1	1	0	0			
A	1	1	0	0	0	0	M		
!D	0	0	1	1	0	1			
!A	1	1	0	0	0	1	!M		
-D	0	0	1	1	1	1			
-A	1	1	0	0	1	1	-M		
D+1	0	1	1	1	1	1			
A+1	1	1	0	1	1	1	M+1		
D-1	0	0	1	1	1	0			
A-1	1	1	0	0	1	0	M-1		
D+A	0	0	0	0	1	0	D+M		
D-A	0	1	0	0	1	1	D-M		
A-D	0	0	0	1	1	1	M-D		
D&A	0	0	0	0	0	0	D&M		
D A	0	1	0	1	0	1	D M		

The C-instruction

111A C₁C₂C₃C₄ C₅C₆ D₁D₂ D₃J₁J₂J₃

	A D M			
dest	d	d	d	effect: the value is stored in:
null	0	0	0	the value is not stored
M	0	0	1	RAM[A]
D	0	1	0	D register
DM	0	1	1	D register and RAM[A]
A	1	0	0	A register
AM	1	0	1	A register and RAM[A]
AD	1	1	0	A register and D register
ADM	1	1	1	A register, D register, and RAM[A]

The C-instruction

111A C₁C₂C₃C₄ C₅C₆ D₁D₂ D₃J₁J₂J₃

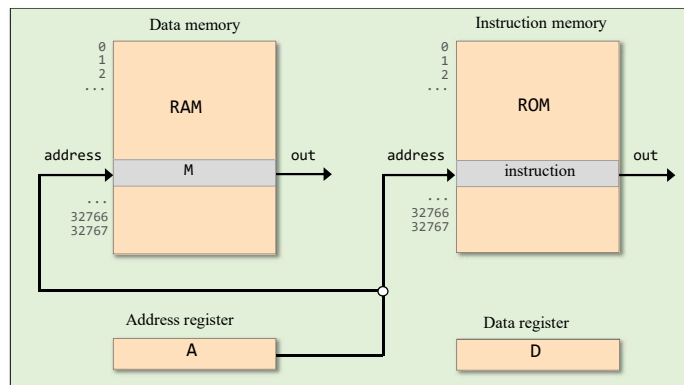
comp dest jump

< = >
jump j j j effect:

null	0	0	0	no jump
JGT	0	0	1	if <i>comp</i> > 0 jump
JEQ	0	1	0	if <i>comp</i> = 0 jump
JGE	0	1	1	if <i>comp</i> ≥ 0 jump
JLT	1	0	0	if <i>comp</i> < 0 jump
JNE	1	0	1	if <i>comp</i> ≠ 0 jump
JLE	1	1	0	if <i>comp</i> ≤ 0 jump
JMP	1	1	1	Unconditional jump

Working with registers and memory

- D: data register
- A: address/data register
- M: the currently selected memory cell, $M=RAM[A]$



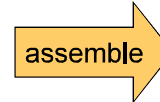
Hack assembly/machine language

Source code (example)

```
// Computes 1+...+RAM[0]
// And stored the sum in RAM[1]
@i
M=1 // i = 1
@sum
M=0 // sum = 0
(LOOP)
@i // if i>RAM[0] goto WRITE
D=M
@R0
D=D-M
@WRITE
D;JGT
@i // sum += i
D=M
@sum
M=D+M
@i // i++
M=M+1
@LOOP // goto LOOP
0;JMP
(WRITE)
@sum
D=M
@R1
M=D // RAM[1] = the sum
(END)
@END
0;JMP
```

Target code

```
000000000010000
111011111001000
000000000010001
111010100010000
000000000010000
111110000010000
000000000000000
111010011010000
000000000010010
111001100000001
000000000010000
111110000100000
000000000010001
1111000010001000
000000000010000
111110111001000
000000000001000
111010100000111
000000000010001
111110000100000
000000000000001
111001100001000
000000000010110
11101010000111
```



Hack assembler
or CPU emulator

We will focus on writing the assembly code.

Hack programming exercises

Exercise: Implement the following tasks using Hack commands:

1. Set D to A-1
2. Set both A and D to A + 1
3. Set D to 19
4. D++
5. D=RAM[17]
6. Set RAM[5034] to D - 1
7. Set RAM[53] to 171
8. Add 1 to RAM[7], and store the result in D.

Hack programming exercises

Exercise: Implement the following tasks using Hack commands:

1. Set **D** to **A-1**
2. Set both **A** and **D** to **A + 1**
3. Set **D** to 19
4. **D++**
5. **D=RAM[17]**
6. Set **RAM[5034]** to **D - 1**
7. Set **RAM[53]** to 171
8. Add 1 to **RAM[7]**, and store the result in **D**.

1. **D = A-1**
2. **AD=A+1**
3. **@19**
D=A
4. **D=D+1**
5. **@17**
D=M
6. **@5034**
M=D-1
7. **@171**
D=A
@53
M=D
8. **@7**
D=M+1

Terminate properly

- To avoid malicious code, you could terminate your program with an infinite loop, such as

```
@6
0; JMP
```

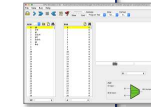
```
00: @0
01: D=M
02: @1
03: D=D+M
04: @2
05: M=D
```

A simple program: add two numbers (demo)

Add.asm (example)

```
// Computes: RAM[2] = RAM[0] + RAM[1]
// D = RAM[0]
@0
D=M
// D = D + RAM[1]
@1
D=D+M
// RAM[2] = D
@2
M=D
```

Load into the CPU emulator



Binary

```
0000000000000000
1000010010001101
0000000000000001
1010011001100001
0000000000000010
1110010010010011
```

Execute

When loading a symbolic program into the CPU emulator, the emulator translates it into binary code (using a built-in assembler)

Built-in symbols

symbol	value
R0	0
R1	1
R2	2
...	...
R15	15
SCREEN	16384
KBD	24576

symbol	value
SP	0
LCL	1
ARG	2
THIS	3
THAT	4

- R0, R1, ..., R15 : virtual registers
- SCREEN and KBD : base address of I/O memory maps
- Others: used in the implementation of the Hack Virtual Machine
- Note that Hack assembler is case-sensitive, R5 != r5

Branching

```
// Program: branch.asm
// if R0>0
//   R1=1
// else
//   R1=0
```

Branching

```
// Program: branch.asm
// if R0>0
//   R1=1
// else
//   R1=0

@R0
D=M          // D=RAM[0]

@8
D; JGT       // If R0>0 goto 8

@R1
M=0          // R1=0
@10
0; JMP       // go to end

@R1
M=1          // R1=1

@10
0; JMP
```

Branching

```
// Program: branch.asm
// if R0>0
//   R1=1
// else
//   R1=0

@R0
D=M          // D=RAM[0]

@8
D; JGT       // If R0>0 goto 8

@R1
M=0          // R1=0
@10
0; JMP       // go to end

@R1
M=1          // R1=1

@10
0; JMP
```

Branching with labels

```
// Program: branch.asm
// if R0>0
//   R1=1
// else
//   R1=0

@R0
D=M          // D=RAM[0]

@POSTIVE ← refer a label
D; JGT       // If R0>0 goto 8

@R1
M=0          // R1=0
@END
0; JMP       // go to end

(POSTIVE) ← declare a label
@R1
M=1          // R1=1

(END)
@10
0; JMP
```

0	@0
1	D=M
2	@8
3	D; JGT
4	@1
5	M=0
6	@10
7	0; JMP
8	@1
9	M=1
10	@10
11	0; JMP
12	
13	
14	
15	
16	

IF logic – Hack style

High level:

```
if condition {
  code block 1
} else {
  code block 2
}
code block 3
```

Hack convention:

- True is represented by -1
- False is represented by 0

Hack:

```
D ← condition
@IF_TRUE
D;JEQ
code block 2
@END
0;JMP
(IF_TRUE)
code block 1
(END)
code block 3
```

Coding examples (practice)

Exercise: Implement the following tasks using Hack commands:

- goto 50
- if D==0 goto 112
- if D<9 goto 507
- if RAM[12] > 0 goto 50
- if sum>0 goto END
- if x[i]<=0 goto NEXT.

Coding examples (practice)

Exercise: Implement the following tasks using Hack commands:

- | | | |
|---------------------------|---------|---------|
| 1. goto 50 | 1. @50 | 5. @sum |
| | 0; JMP | D=M |
| 2. if D==0 goto 112 | 2. @112 | @END |
| | D; JEQ | D: JGT |
| 3. if D<9 goto 507 | 3. @9 | 6. @i |
| | D=D-A | D=M |
| 4. if RAM[12] > 0 goto 50 | @507 | @x |
| | D; JLT | A=D+M |
| 5. if sum>0 goto END | 4. @12 | D=M |
| | D=M | @NEXT |
| | @50 | D; JLE |
| | D; JGT | |

variables

```
// Program: swap.asm
// temp = R1
// R1 = R0
// R0 = temp
```

variables

```
// Program: swap.asm
// temp = R1
// R1 = R0
// R0 = temp

    @R1
    D=M
    @temp
    M=D           // temp = R1

    @R0
    D=M
    @R1
    M=D           // R1 = R0

    @temp
    D=M
    @R0
    M=D           // R0 = temp

(END)
@END
0;JMP
```

- When a symbol is encountered, the assembler looks up a symbol table
- If it is a new label, assign a number (address of the next available memory cell) to it.
- For this example, temp is assigned with 16.
- If the symbol exists, replace it with the number recorded in the table.
- With symbols and labels, the program is easier to read and debug. Also, it can be relocated.

Hack program (exercise)

Exercise: Implement the following tasks using Hack commands:

1. `sum = 0`
2. `j = j + 1`
3. `q = sum + 12 - j`
4. `arr[3] = -1`
5. `arr[j] = 0`
6. `arr[j] = 17`

Hack program (exercise)

Exercise: Implement the following tasks using Hack commands:

- | | | | |
|----------------------------------|----------------------|----------------------|--------------------|
| 1. <code>sum = 0</code> | 1. <code>@sum</code> | 4. <code>@arr</code> | 6. <code>@j</code> |
| | <code>M=0</code> | <code>D=M</code> | <code>D=M</code> |
| 2. <code>j = j + 1</code> | 2. <code>@j</code> | <code>@3</code> | <code>@arr</code> |
| | <code>M=M+1</code> | <code>A=D+A</code> | <code>D=D+M</code> |
| 3. <code>q = sum + 12 - j</code> | 3. <code>@sum</code> | <code>M=-1</code> | <code>@ptr</code> |
| | <code>D=M</code> | 5. <code>@j</code> | <code>M=D</code> |
| 4. <code>arr[3] = -1</code> | <code>D=M</code> | <code>D=M</code> | <code>@17</code> |
| | <code>@12</code> | <code>@arr</code> | <code>D=A</code> |
| 5. <code>arr[j] = 0</code> | <code>D=D+A</code> | <code>@arr</code> | <code>D=A</code> |
| | <code>@j</code> | <code>A=D+M</code> | <code>@ptr</code> |
| 6. <code>arr[j] = 17</code> | <code>D=D-M</code> | <code>M=0</code> | <code>A=M</code> |
| | <code>@q</code> | | <code>M=D</code> |
| | <code>M=D</code> | | |

WHILE logic – Hack style

High level:

```
while condition {
    code block 1
}
Code block 2
```

Hack:

```
(LOOP)
    D ← condition
    @END
    D;JNE
    code block 1
    @LOOP
    0;JMP
(END)
    code block 2
```

Hack convention:

- True is represented by -1
- False is represented by 0

Complete program example

C language code:

```
// Adds 1+...+100.
int i = 1;
int sum = 0;
while (i <= 100){
    sum += i;
    i++;
}
```

Hack assembly convention:

- Variables: lower-case
- Labels: upper-case
- Commands: upper-case

Example

```
// for (i=0; i<n; i++)
//     arr[i] = -1;
```

Pseudo code:

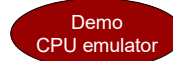
Complete program example

Pseudo code:

```
i = 1;
sum = 0;
LOOP:
    if (i>100) goto END
    sum += i;
    i++;
    goto LOOP
END:
```

Hack assembly convention:

- Variables: lower-case
- Labels: upper-case
- Commands: upper-case



Example

```
// for (i=0; i<n; i++)
//     arr[i] = -1;
```

Pseudo code:

```
i = 0
(LLOOP)
    if (i-n)>=0 goto END
    arr[i] = -1
    i++
    goto LOOP
(ENDEL)
```

Example

```
// for (i=0; i<n; i++)
//   arr[i] = -1;
    @i
    M=0
(LLOOP)
    @i
    D=M
    @n
    D=D-M
    @END
    D; JGE

    @arr
    D=M
    @i
    A=D+M
    M=-1

    @i
    M=M+1

    @LOOP
    0; JMP
(ENDD)
```

Pseudo code:

```
i = 0
(LLOOP)
    if (i-n)>=0 goto END
    arr[i] = -1
    i++
    goto LOOP
(ENDD)
```

Perspective

- Hack is a simple machine language
- User friendly syntax: $D=D+A$ instead of `ADD D,D,A`
- Hack is a " $\frac{1}{2}$ -address machine": any operation that needs to operate on the RAM must be specified using two commands: an `A`-command to address the RAM, and a subsequent `C`-command to operate on it
- A Macro-language can be easily developed
 - $D=D+M[XXX] \Rightarrow @XXX$ followed by $D=D+M$
 - $GOTO\ YYY \Rightarrow @YYY$ followed by `0; JMP`
- A Hack assembler is needed and will be discussed and developed later in the course.