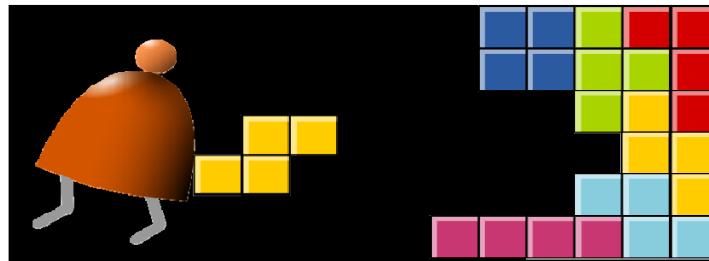


# Virtual Machine

## Part I: Stack Arithmetic

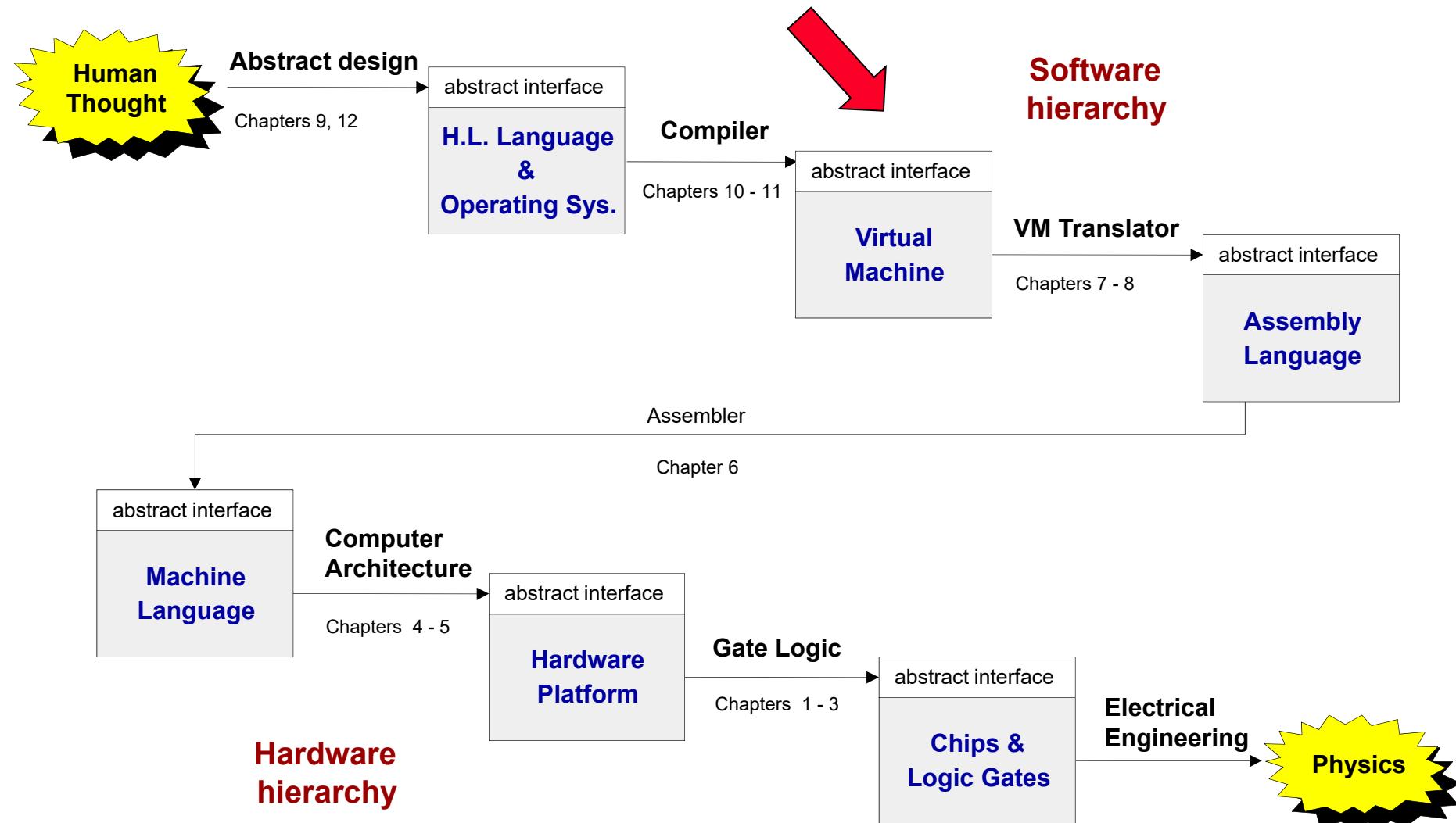


*Building a Modern Computer From First Principles*

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# Where we are at:

---



# Motivation

---

## Jack code (example)

```
class Main {  
    static int x;  
  
    function void main() {  
        // Inputs and multiplies two numbers  
        var int a, b, x;  
        let a = Keyboard.readInt("Enter a number");  
        let b = Keyboard.readInt("Enter a number");  
        let x = mult(a,b);  
        return;  
    }  
}  
  
// Multiplies two numbers.  
function int mult(int x, int y) {  
    var int result, j;  
    let result = 0; let j = y;  
    while ~(j = 0) {  
        let result = result + x;  
        let j = j - 1;  
    }  
    return result;  
}
```

## Our ultimate goal:

Translate high-level  
programs into  
executable code.

Compiler

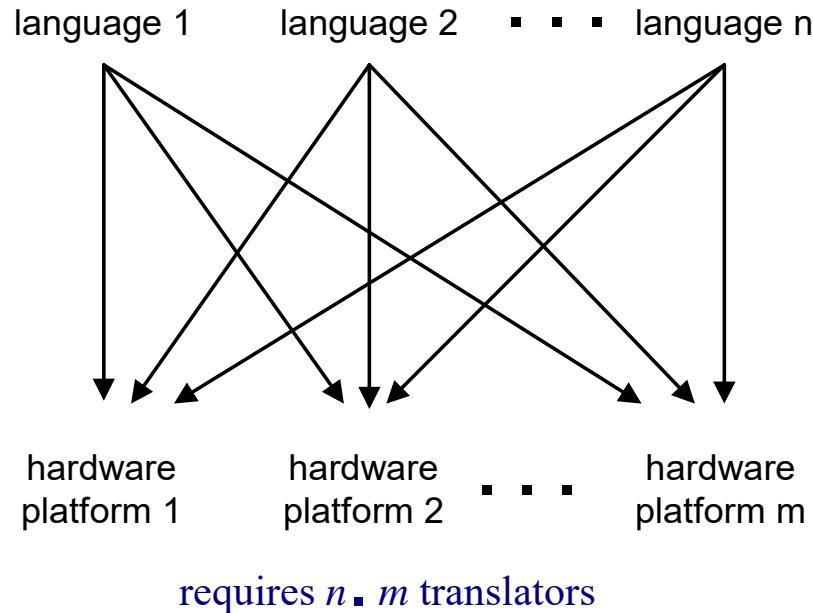
## Hack code

```
000000000010000  
1110111111001000  
000000000010001  
1110101010001000  
000000000010000  
1111110000010000  
0000000000000000  
1111010011010000  
0000000000010010  
1110001100000001  
000000000010000  
1111110000010000  
0000000000010001  
0000000000010000  
1110111111001000  
0000000000010001  
1110101010001000  
0000000000010000  
1111110000010000  
0000000000000000  
1111010011010000  
0000000000010010  
1110001100000001  
0000000000010000  
1111110000010000  
0000000000010001  
...
```

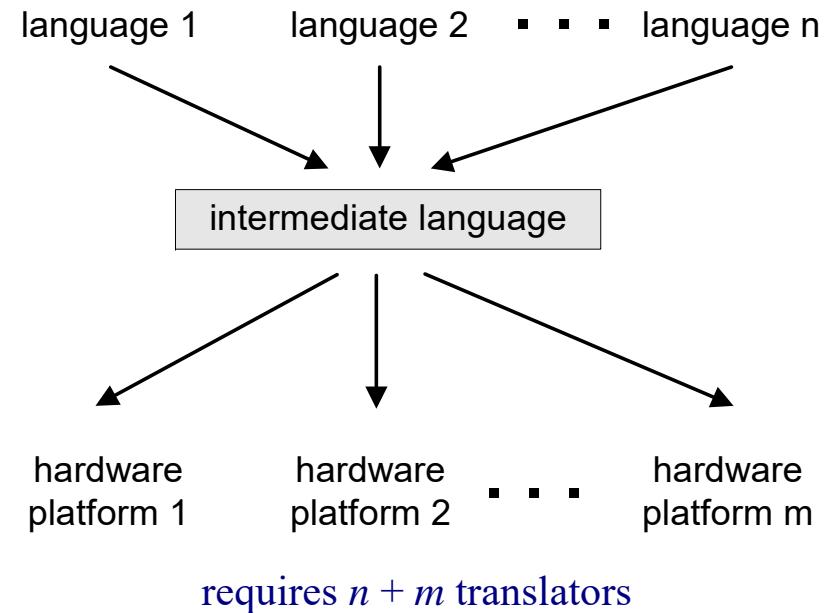
# Compilation models

---

## direct compilation:



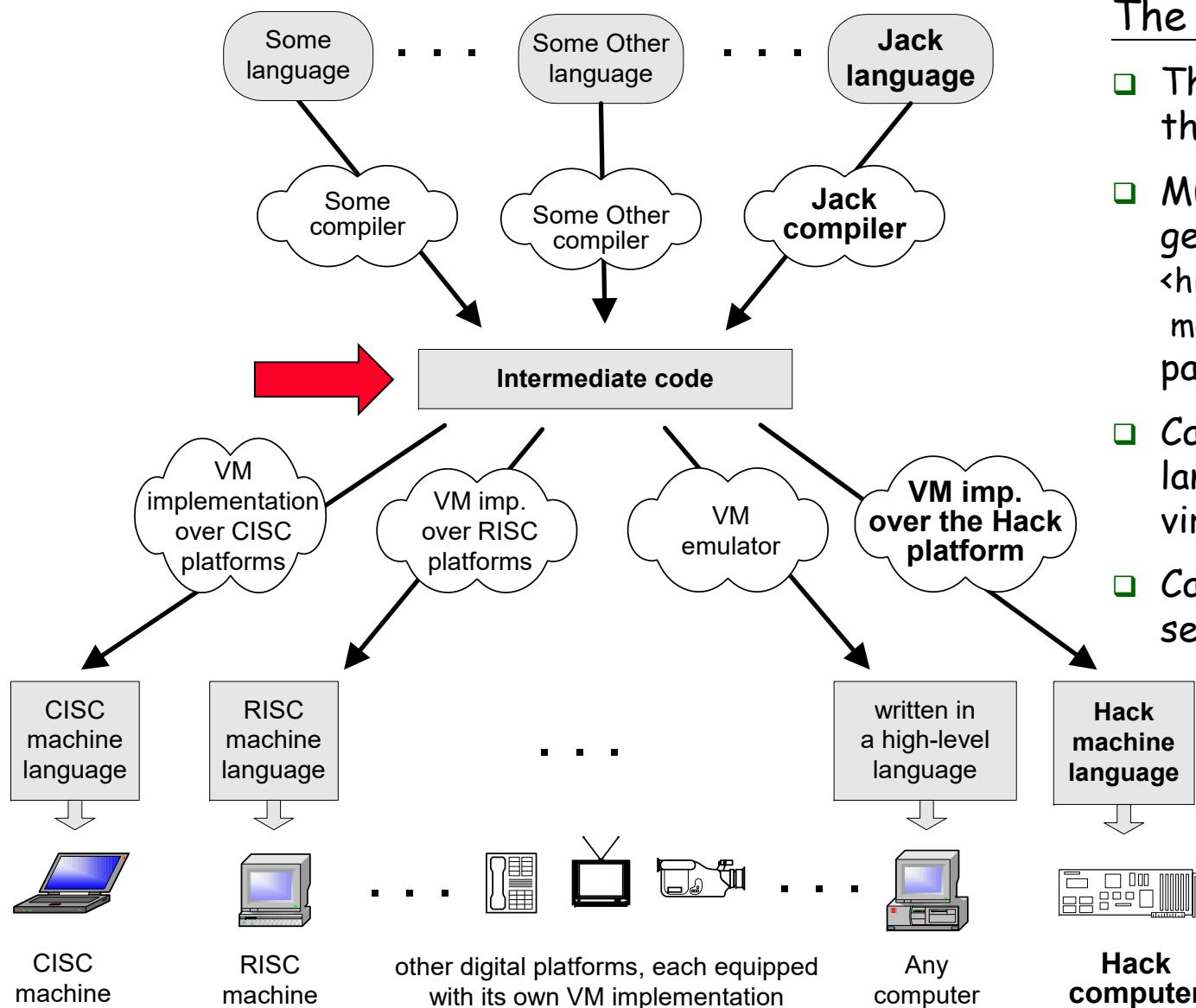
## 2-tier compilation:



## Two-tier compilation:

- ❑ First stage: depends only on the details of the source language
- ❑ Second stage: depends only on the details of the target language.

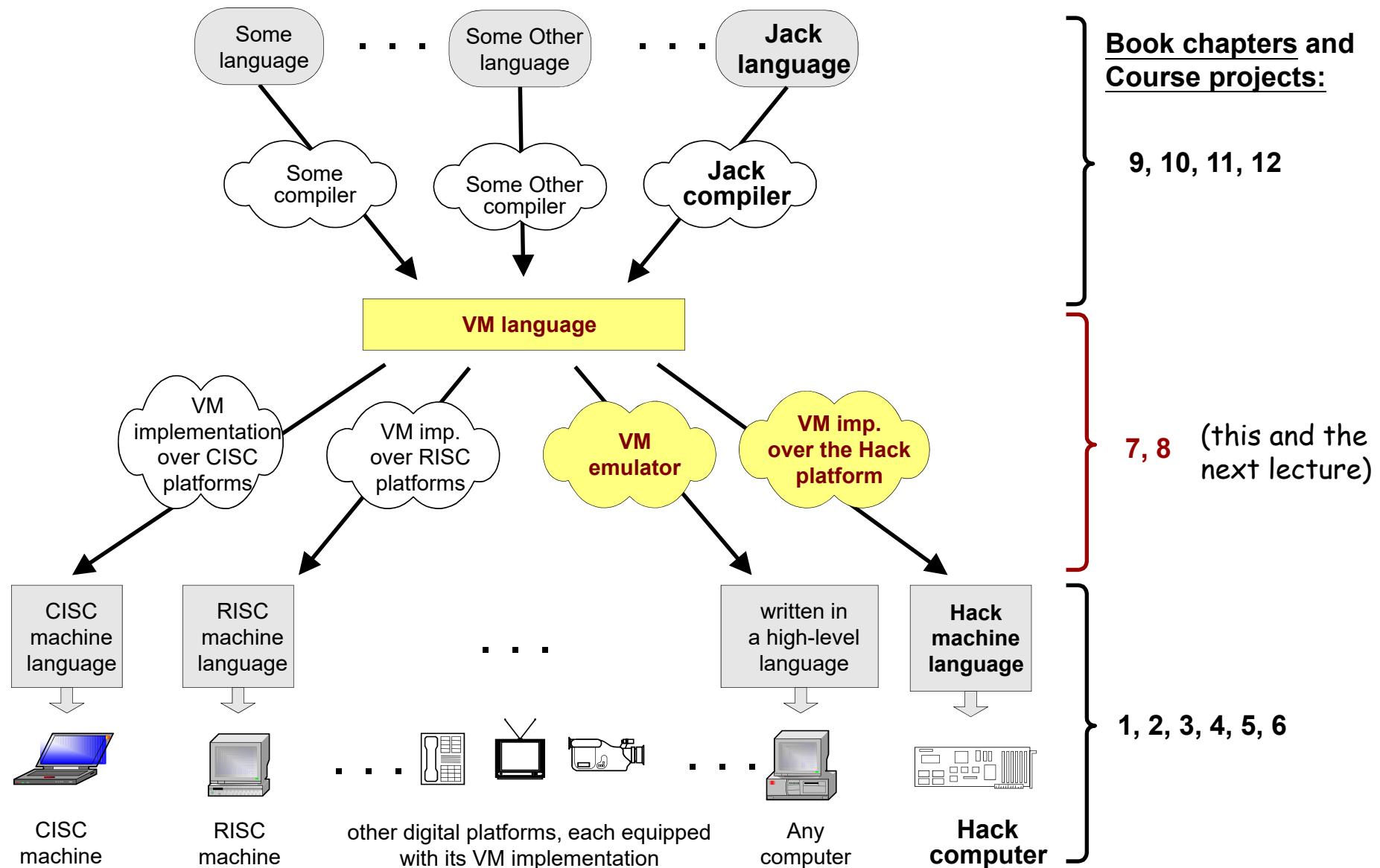
# The big picture



## The intermediate code:

- The interface between the 2 compilation stages
- Must be sufficiently general to support many <high-level language, machine-language> pairs
- Can be modeled as the language of an abstract virtual machine (VM)
- Can be implemented in several different ways.

# Focus of this lecture (yellow):



## Virtual machines

---

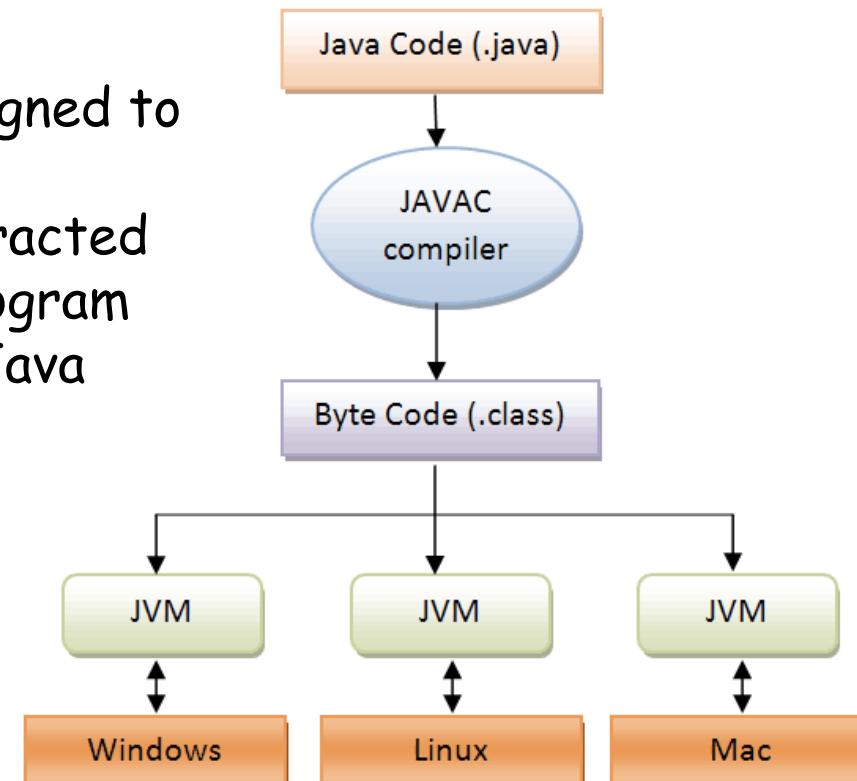
- A **virtual machine (VM)** is an emulation of a particular (real or hypothetical) computer system.
  - System virtual machine (full virtualization VMs): a complete substitute for the targeted real machine and a level of functionality required for the execution of a complete operating system, e.g., VirtualBox.



# Virtual machines

---

- A **virtual machine (VM)** is an emulation of a particular (real or hypothetical) computer system.
  - System virtual machine (full virtualization VMs): a complete substitute for the targeted real machine and a level of functionality required for the execution of a complete operating system, e.g., VirtualBox.
  - Process virtual machine: designed to execute a single computer program by providing an abstracted and platform-independent program execution environment, e.g., Java virtual machine (JVM).



# The VM model and language

---

## Perspective:

From here till the end of the next lecture we describe the VM model used in the Hack-Jack platform

Other VM models (like Java's JVM/JRE and .NET's IL/CLR) are similar in spirit, but differ in scope and details.

# The VM model and language

---

Several different ways to think about the notion of a virtual machine:

- **Abstract software engineering view:**  
the VM is an interesting abstraction that makes sense in its own right  
(a hypothetical machine closer to high-level language, but could still be built easily. Sometimes, no need to worry about how to implement it in hardware.)
- **Practical software engineering view:**  
the VM code layer enables “managed code” (e.g. enhanced security)
- **Pragmatic compiler writing view:**  
a VM architecture makes writing a compiler much easier  
(as we'll see later in the course)
- **Opportunistic empire builder view:**  
a VM architecture allows writing high-level code once and have it run on many target platforms with little or no modification.

# Hack virtual machine

---

Goal: Specify and implement a VM model and language:

<u>Arithmetic / Boolean commands</u>	<u>Program flow commands</u>
add	label (declaration)
sub	goto (label)
neg	if-goto (label)
eq	
gt	
lt	
and	
or	
not	
<u>Memory access commands</u>	<u>Function calling commands</u>
pop x (pop into x, which is a variable)	function (declaration)
push y (y being a variable or a constant)	call (a function)
	return (from a function)

Our game plan: (a) describe the VM abstraction (3 types of instructions)  
(b) propose how to implement it over the Hack platform.

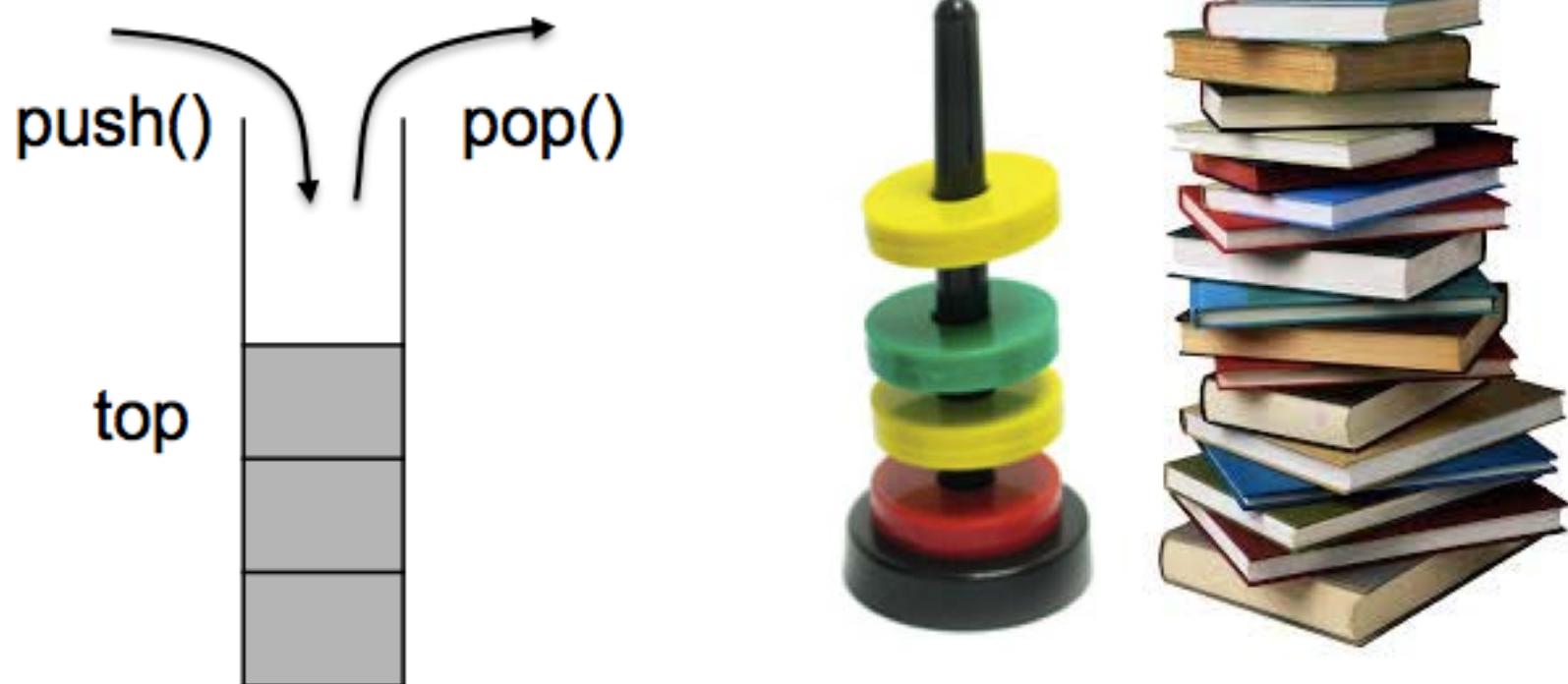
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# The stack

---

## The stack:

- A classical LIFO data structure
- Elegant and powerful
- Several hardware / software implementation options.

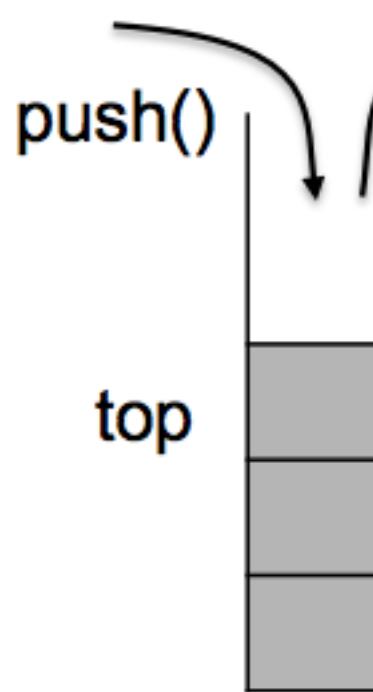


# The stack

---

## The stack:

- A classical LIFO data structure
- Elegant and powerful
- Several hardware / software implementation options.
- Several flavors: next empty/available, upward/downward



push(x)  
stack[top]=x;  
top++;

pop()  
top--;  
return stack[top];

peek(), empty()

## What is the stack good for?

---

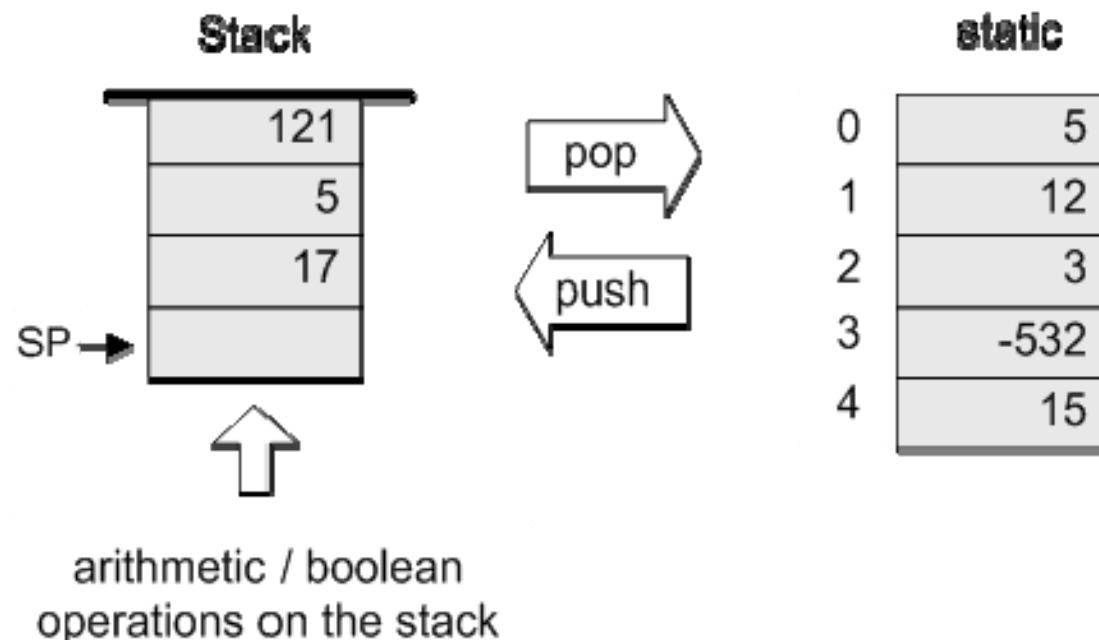
- Stack can be used for evaluating arithmetic expressions
- Expression:  $5 * (6+2) - 12/4$ 
  - Infix
  - Prefix
  - Postfix

Stack is also good for implementing function call structures, such as subroutines, local variables and recursive calls. Will discuss it later.

## Our VM model is *stack-oriented*

---

- All operations are done on a stack
- Data is saved in several separate memory segments
- All the memory segments behave the same
- One of the memory segments m is called static, and we will use it (as an arbitrary example) in the following examples:

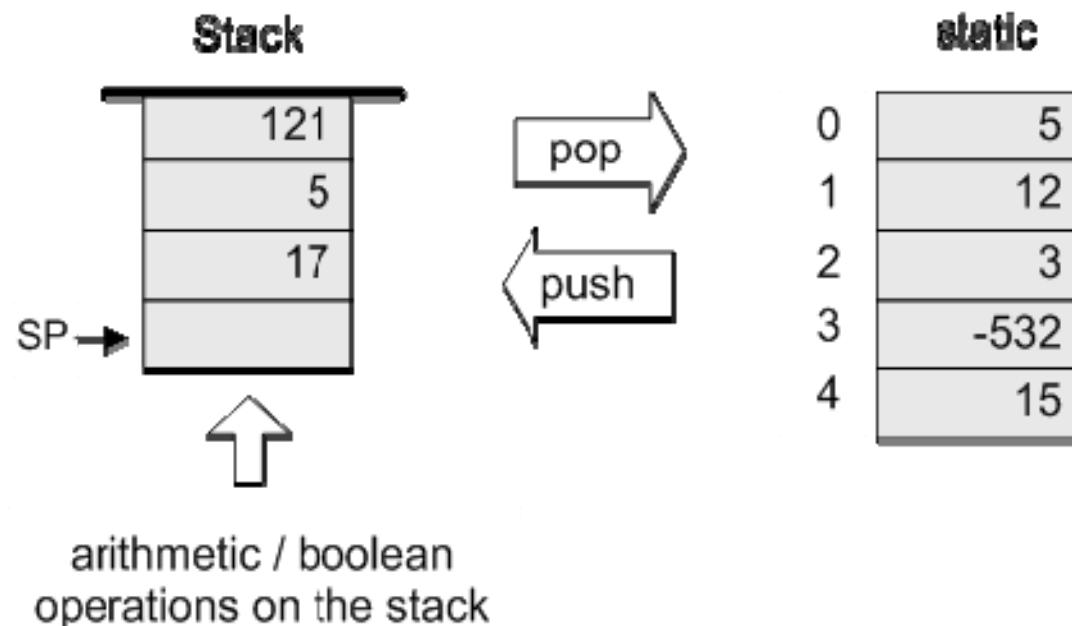


# Data types

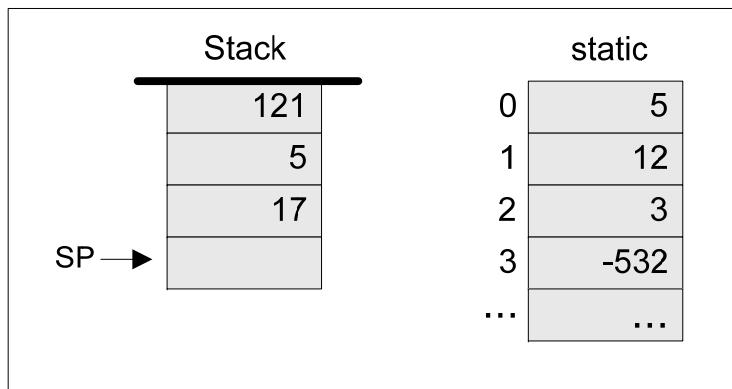
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Our VM model features a single 16-bit data type that can be used as:

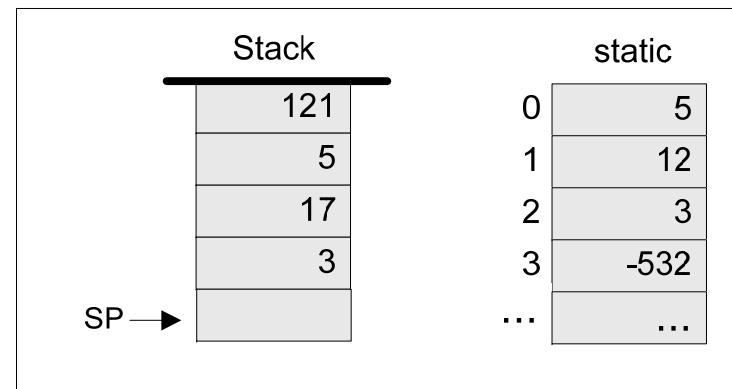
- an integer value (16-bit 2's complement: -32768, ... , 32767)
- a Boolean value (0 and -1, standing for true and false)
- a pointer (memory address)



# Memory access operations

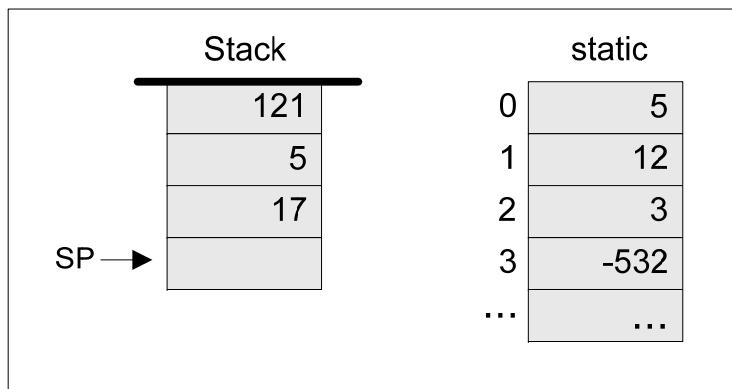


push  
static 2

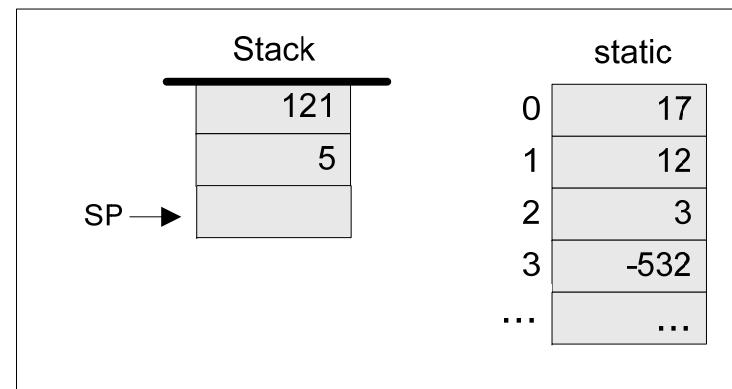


(before)

(after)



pop  
static 0

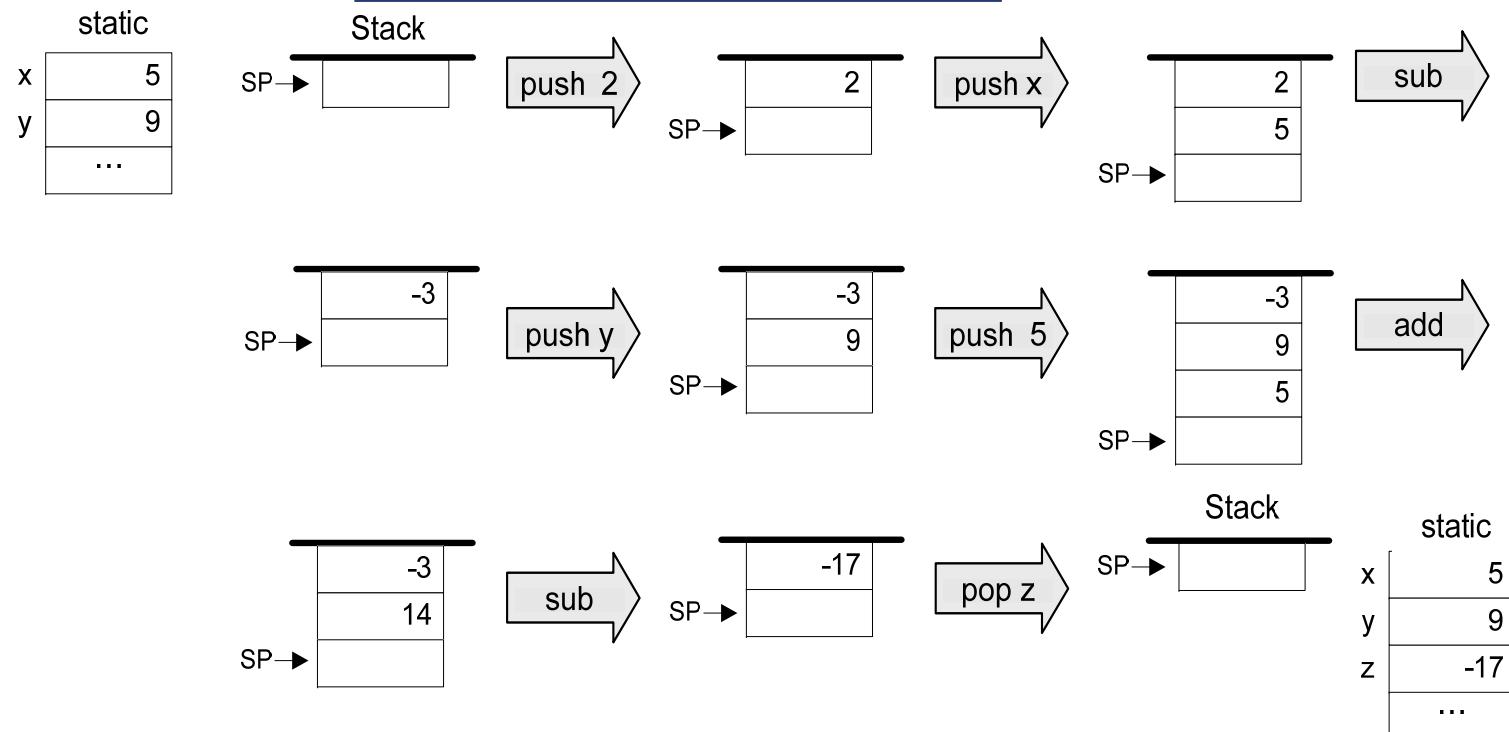


# Evaluation of arithmetic expressions

VM code (example)

```
// z=(2-x)-(y+5)
push 2
push x
sub
push y
push 5
add
sub
pop z
```

(suppose that  
x refers to static 0,  
y refers to static 1,  
z refers to static 2)

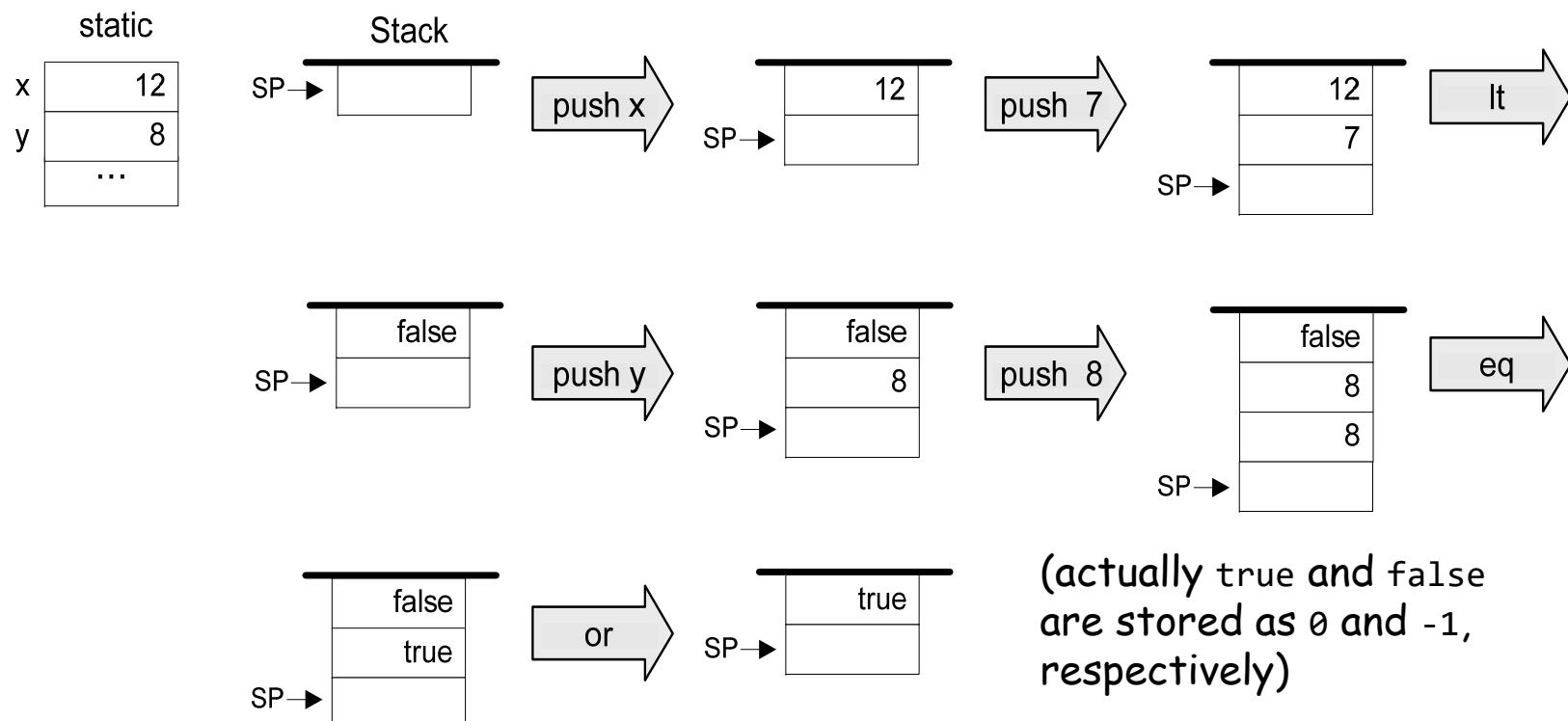


# Evaluation of Boolean expressions

VM code (example)

```
// (x<7) or (y=8)
push x
push 7
lt
push y
push 8
eq
or
```

(suppose that  
x refers to static 0,  
y refers to static 1)



# Arithmetic and Boolean commands in the VM language (wrap-up)

Command	Return value (after popping the operand/s)	Comment
add	$x + y$	Integer addition (2's complement)
sub	$x - y$	Integer subtraction (2's complement)
neg	$-y$	Arithmetic negation (2's complement)
eq	true if $x = y$ and false otherwise	Equality
gt	true if $x > y$ and false otherwise	Greater than
lt	true if $x < y$ and false otherwise	Less than
and	$x \text{ And } y$	Bit-wise
or	$x \text{ Or } y$	Bit-wise
not	$\text{Not } y$	Bit-wise

Stack

SP →

## The VM's Memory segments

---

A VM program is designed to provide an interim abstraction of a program written in some high-level language.

Modern OO languages normally feature the following variable kinds:

### Class level:

- Static variables (class-level variables)
- Private variables (aka "object variables" / "fields" / "properties")

### Method level:

- Local variables
- Argument variables

When translated into the VM language,

The static, private, local and argument variables are mapped by the compiler on the four memory segments static, this, local, argument

In addition, there are four additional memory segments, whose role will be presented later: that, constant, pointer, temp.

---

## Memory segments and memory access commands

---

The VM abstraction includes 8 separate memory segments named:  
static, this, local, argument, that, constant, pointer, temp

As far as VM programming commands go, all memory segments look and behave the same

To access a particular segment entry, use the following generic syntax:

### Memory access VM commands:

- ❑ pop *memorySegment index*
- ❑ push *memorySegment index*

Where *memorySegment* is static, this, local, argument, that, constant, pointer, or temp

And *index* is a non-negative integer

(In all our code examples thus far, *memorySegment* was static)

The different roles of the eight memory segments will become relevant when we'll talk about the compiler

At the VM abstraction level, all memory segments are treated the same way.

## VM programming

---

VM programs are normally written by *compilers*, not by humans

However, compilers are written by humans ...

In order to write or optimize a compiler, it helps to first understand the spirit of the compiler's target language - the VM language

So, we'll now see an example of a VM program

# VM programming

---

The example includes three new VM commands:

- ❑ `function functionSymbol // function declaration`
- ❑ `label labelSymbol // label declaration`
- ❑ `if-goto labelSymbol // pop x  
// if x=true, jump to execute the  
// command after labelSymbol  
// else proceed to execute the next  
// command in the program`

For example, to effect `if (x > n) goto loop`, we can use the following VM commands:

```
push x
push n
gt
if-goto loop      // Note that x, n, and the truth value
                  // were removed from the stack.
```

## High-level code

```
function mult (x,y) {  
    int result, j;  
    result = 0;  
    j = y;  
    while ~(j = 0) {  
        result = result + x;  
        j = j - 1;  
    }  
    return result;  
}
```

## Pseudo code

```
...  
loop:  
    if (j=0) goto end  
    result=result+x  
    j=j-1  
    goto loop  
end:  
...
```

## VM code (first approx.)

```
function mult(x,y)  
    push 0  
    pop result  
    push y  
    pop j  
label loop  
    push j  
    push 0  
    eq  
    if-goto end  
    push result  
    push x  
    add  
    pop result  
    push j  
    push 1  
    sub  
    pop j  
    goto loop  
label end  
    push result  
    return
```

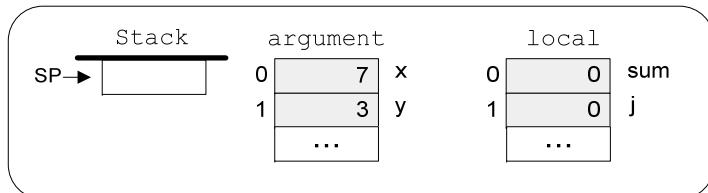
## VM code

```
function mult 2  
    push constant 0  
    pop local 0  
    push argument 1  
    pop local 1  
label loop  
    push local 1  
    push constant 0  
    eq  
    if-goto end  
    push local 0  
    push argument 0  
    add  
    pop local 0  
    push local 1  
    push constant 1  
    sub  
    pop local 1  
    goto loop  
label end  
    push local 0  
    return
```

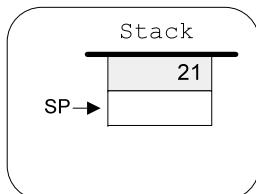
## High-level code

```
function mult (x,y) {  
    int result, j;  
    result = 0;  
    j = y;  
    while ~(j = 0) {  
        result = result + x;  
        j = j - 1;  
    }  
    return result;  
}
```

Just after `mult(7,3)` is entered:



Just after `mult(7,3)` returns:



## VM code (first approx.)

```
function mult(x,y)  
    push 0  
    pop result  
    push y  
    pop j  
label loop  
    push j  
    push 0  
    eq  
    if-goto end  
    push result  
    push x  
    add  
    pop result  
    push j  
    push 1  
    sub  
    pop j  
    goto loop  
label end  
    push result  
    return
```

## VM code

```
function mult 2  
    push constant 0  
    pop local 0  
    push argument 1  
    pop local 1  
label loop  
    push local 1  
    push constant 0  
    eq  
    if-goto end  
    push local 0  
    push argument 0  
    add  
    pop local 0  
    push local 1  
    push constant 1  
    sub  
    pop local 1  
    goto loop  
label end  
    push local 0  
    return
```

# VM programming: multiple functions

---

## Compilation:

- ❑ A Jack application is a set of 1 or more class files (just like .java files).
- ❑ When we apply the Jack compiler to these files, the compiler creates a set of 1 or more .vm files (just like .class files). Each method in the Jack app is translated into a VM function written in the VM language
- ❑ Thus, a VM file consists of one or more VM functions.

# VM programming: multiple functions

---

## Execution:

- ❑ At any given point of time, only one VM function is executing (the “current function”), while 0 or more functions are waiting for it to terminate (the functions up the “calling hierarchy”)
- ❑ For example, a main function starts running; at some point we may reach the command call factorial, at which point the factorial function starts running; then we may reach the command call mult, at which point the mult function starts running, while both main and factorial are waiting for it to terminate

The stack: a global data structure, used to save and restore the resources (memory segments) of all the VM functions up the calling hierarchy (e.g. main and factorial). The tip of this stack is the working stack of the current function (e.g. mult).

# VM programming: multiple functions (files)

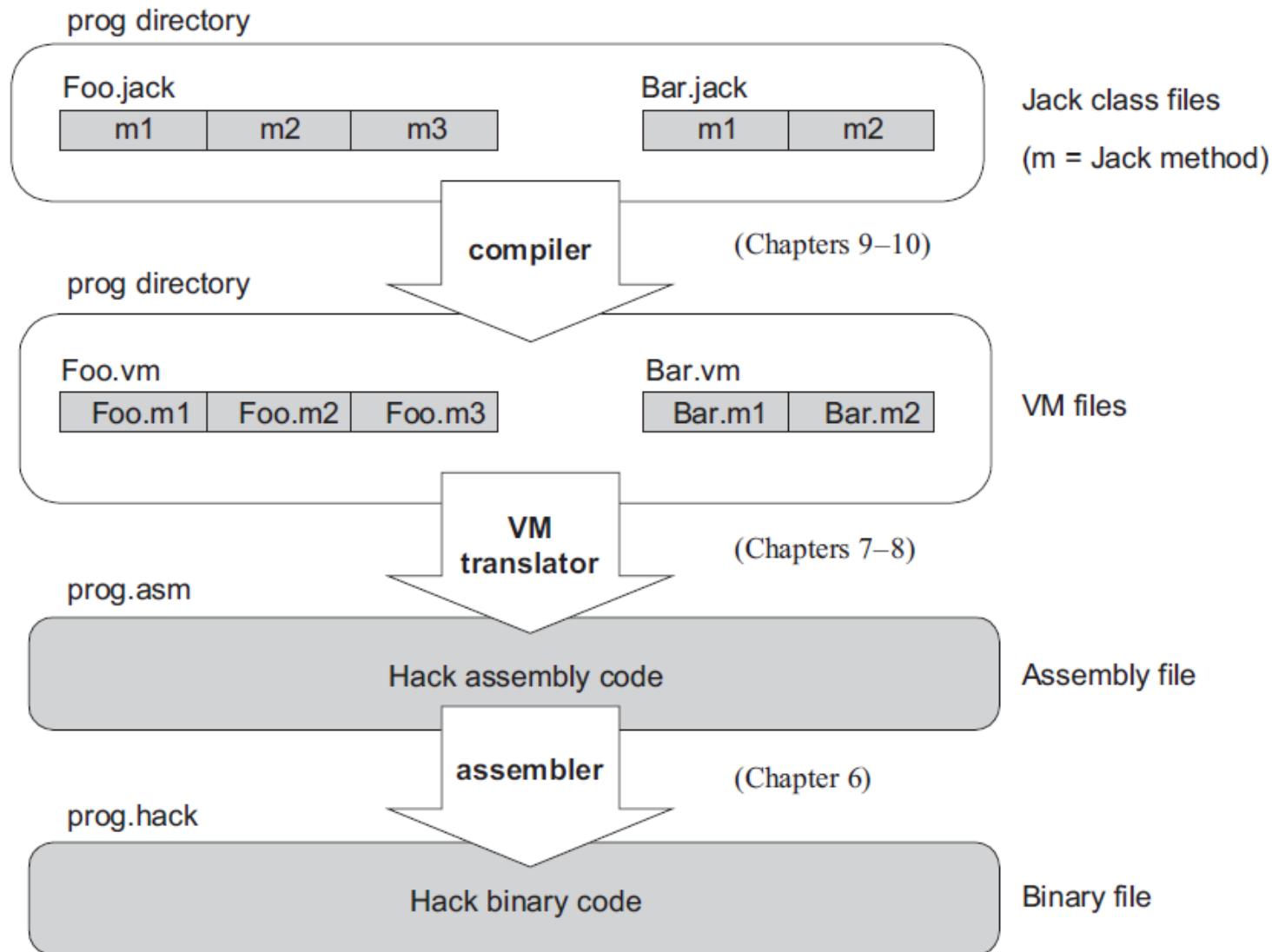


Figure 7.8 Program elements in the Jack-VM-Hack platform.

# VM programming: multiple functions (memory)

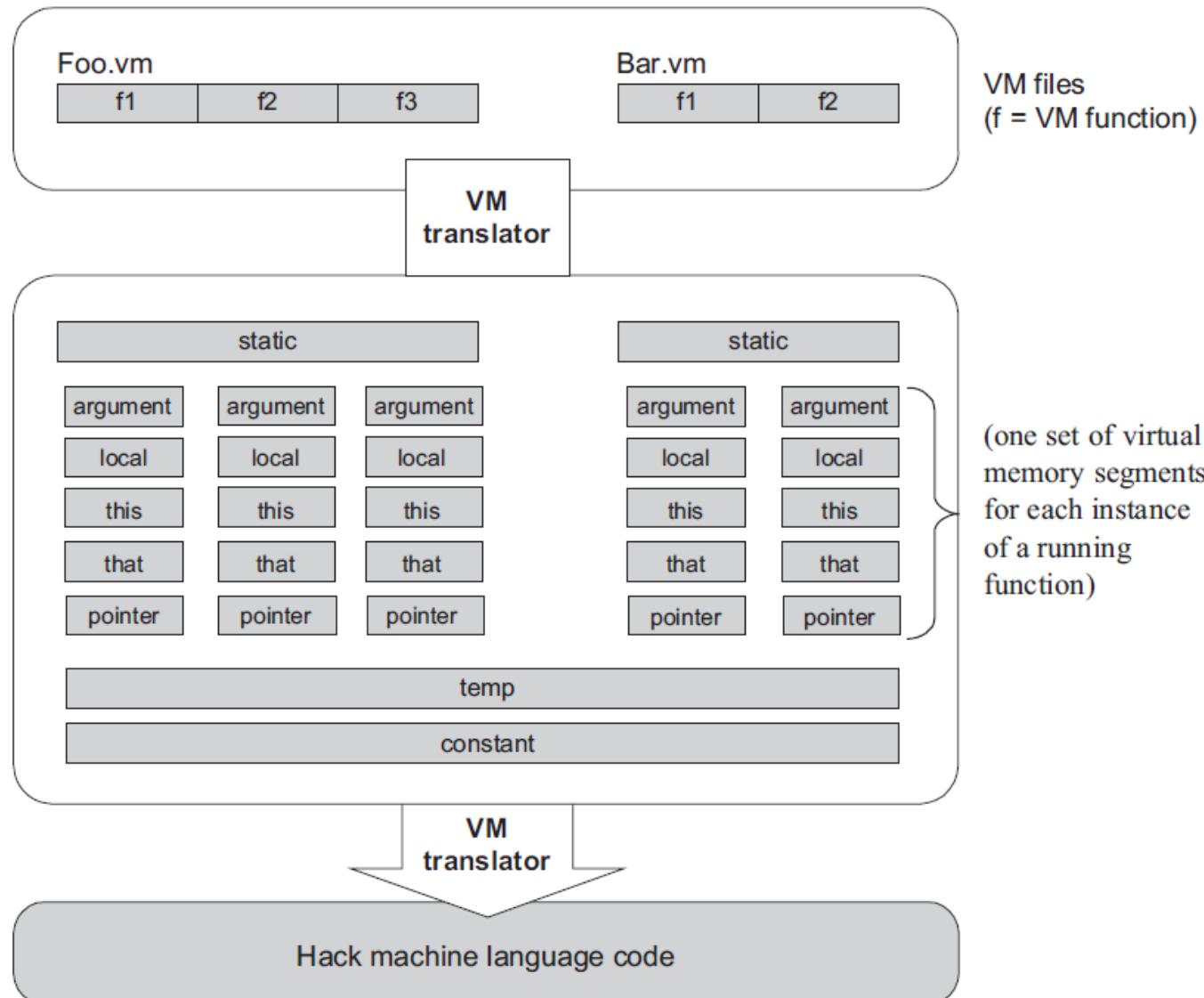
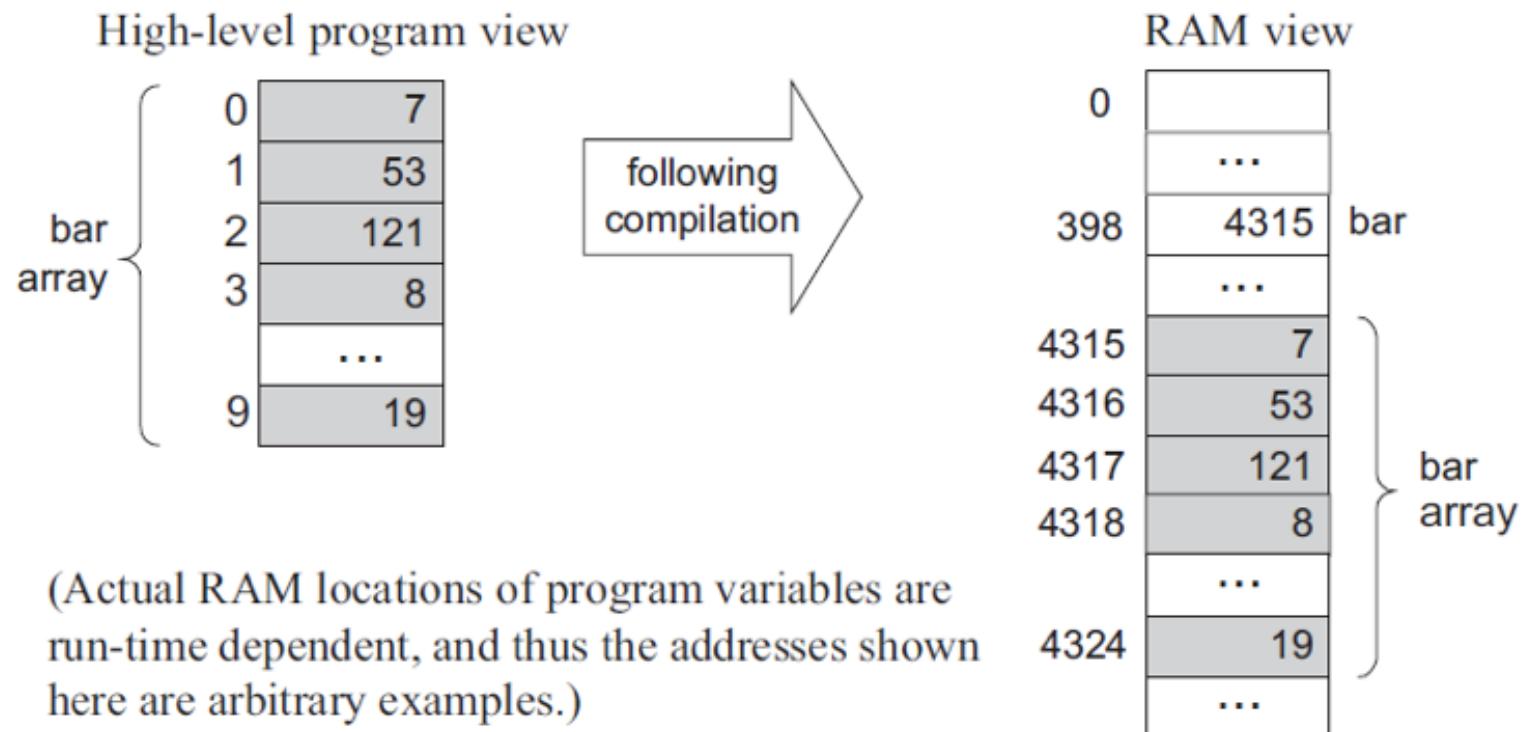


Figure 7.7 The virtual memory segments are maintained by the VM implementation.

# Handling array

---

```
int foo() {      // some language, not Jack  
    int bar[10];  
  
    ...  
  
    bar[2] = 19;  
}
```



# Handling array

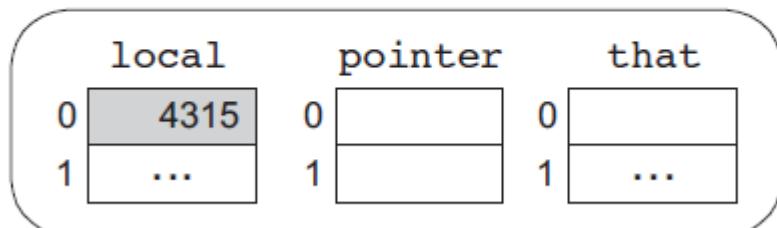
## VM code

```
/* Assume that the bar array is the first local variable declared in the
high-level program. The following VM code implements the operation
bar[2]=19, i.e., *(bar+2)=19. */
push local 0          // Get bar's base address
push constant 2
add
pop  pointer 1        // Set that's base to (bar+2)
push constant 19
pop  that 0           // *(bar+2)=19
...
...
```

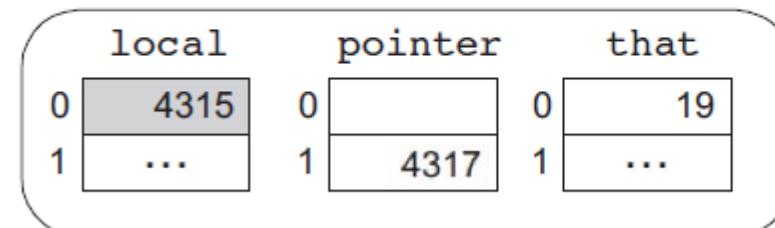
Alternative

```
push local 0
pop pointer 1
push constant 19
pop that 2
```

Virtual memory segments  
just before the bar[2]=19 operation:



Virtual memory segments  
just after the bar[2]=19 operation:

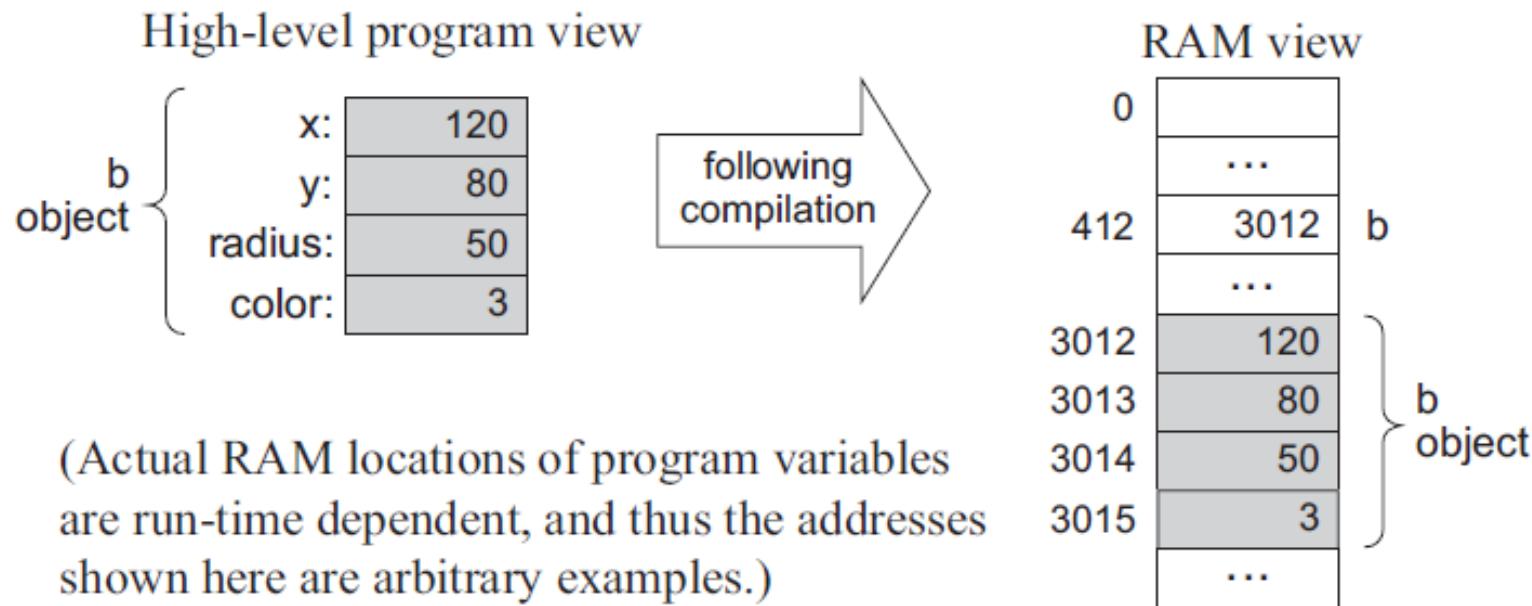


(that 0  
is now  
aligned with  
RAM[4317])

# Handling objects

---

```
Class Ball {      // some language, not Jack  
    int x, y, radius, color;  
    int SetR(int r) {radius = r;}  
}  
  
Ball b;  
  
b.SetR(10);
```



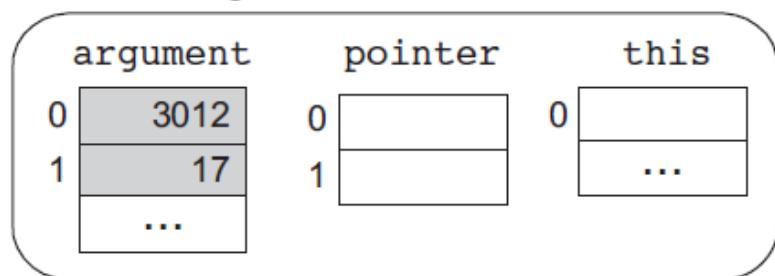
# Handling objects

*VM code*

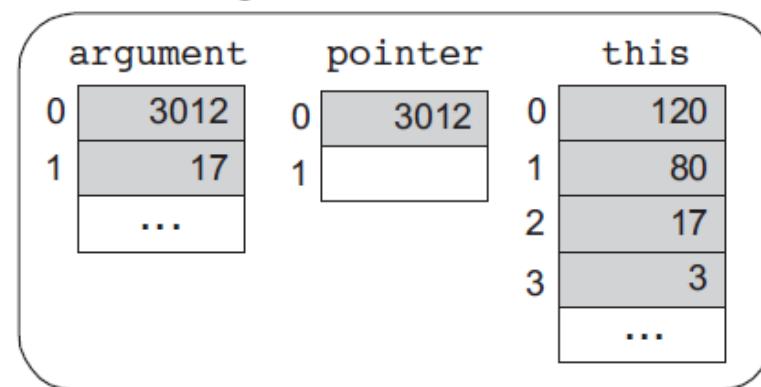
```
/* Assume that the b object and the r integer were passed to the function as
   its first two arguments. The following code implements the operation
   b.radius=r. */

push argument 0 // Get b's base address
pop pointer 0    // Point the this segment to b
push argument 1 // Get r's value
pop this 2       // Set b's third field to r
...
...
```

Virtual memory segments just before  
the operation `b.radius=17`:



Virtual memory segments just after  
the operation `b.radius=17`:



(`this 0`  
is now  
aligned with  
RAM[3012])

# Lecture plan

Summary: Hack VM has the following instructions and eight memory segments.

## Arithmetic / Boolean commands

add

sub

neg

eq

gt

lt

and

or

not

Chapter 7

## Memory access commands

pop x (pop into x, which is a variable)

push y (y being a variable or a constant)

## Program flow commands

label (declaration)

goto (label)

if-goto (label)

Chapter 8

## Function calling commands

function (declaration)

call (a function)

return (from a function)

Method: (a) specify the abstraction (stack, memory segments, commands)

→ (b) how to implement the abstraction over the Hack platform.

## Implementation of VM on Hack

---

- Each VM instruction must be translated into a set of Hack assembly code
- VM segments need to be realized on the host memory

# Implementation

---

## VM implementation options:

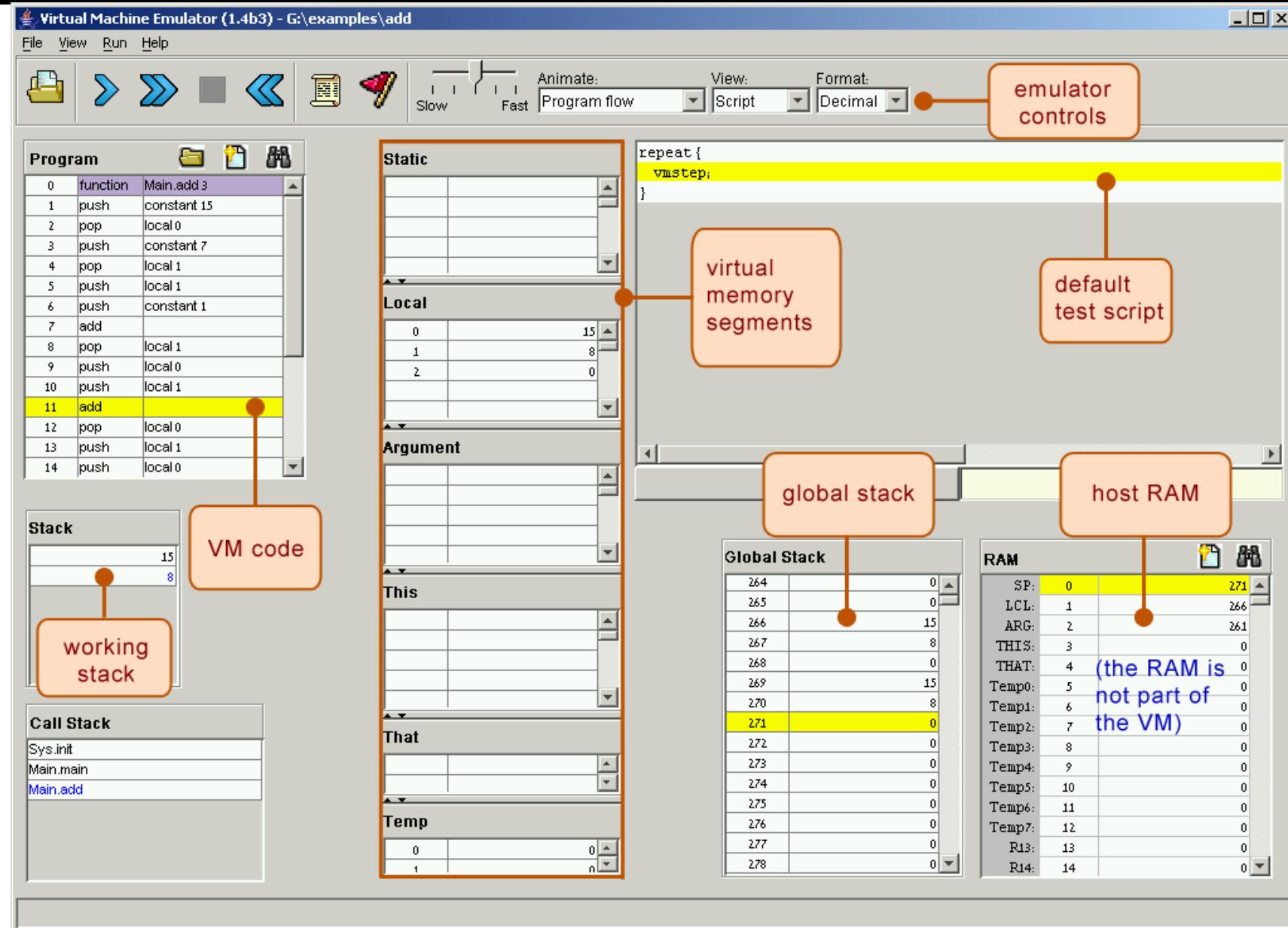
- Emulator-based (e.g. emulate the VM model using Java)
- Translator-based (e.g. translate VM programs into the Hack machine language)
- Hardware-based (realize the VM model using dedicated memory and registers)

## Two well-known translator-based implementations:

JVM: Javac translates Java programs into bytecode;  
The JVM translates the bytecode into  
the machine language of the host computer

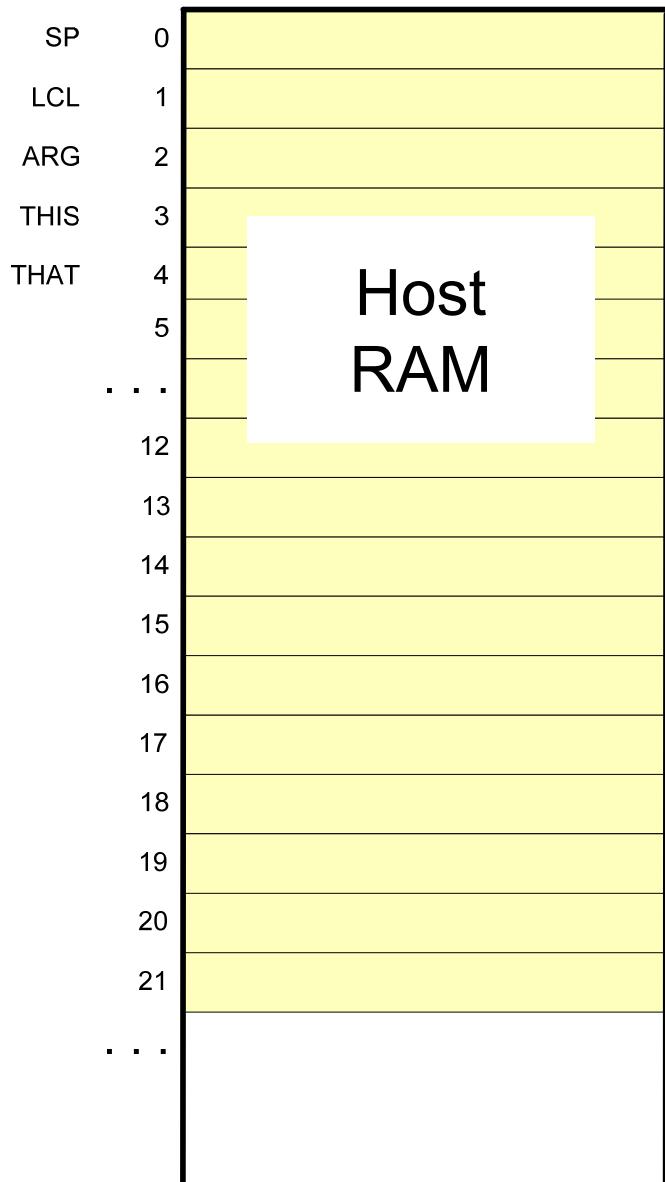
CLR: C# compiler translates C# programs into IL code;  
The CLR translates the IL code into  
the machine language of the host computer.

# Software implementation: VM emulator (part of the course software suite)



# VM implementation on the Hack platform (memory)

---



The stack: a global data structure, used to save and restore the resources of all the VM functions up the calling hierarchy.

The tip of this stack is the working stack of the current function

static, constant, temp, pointer:

Global memory segments, all functions see the same four segments

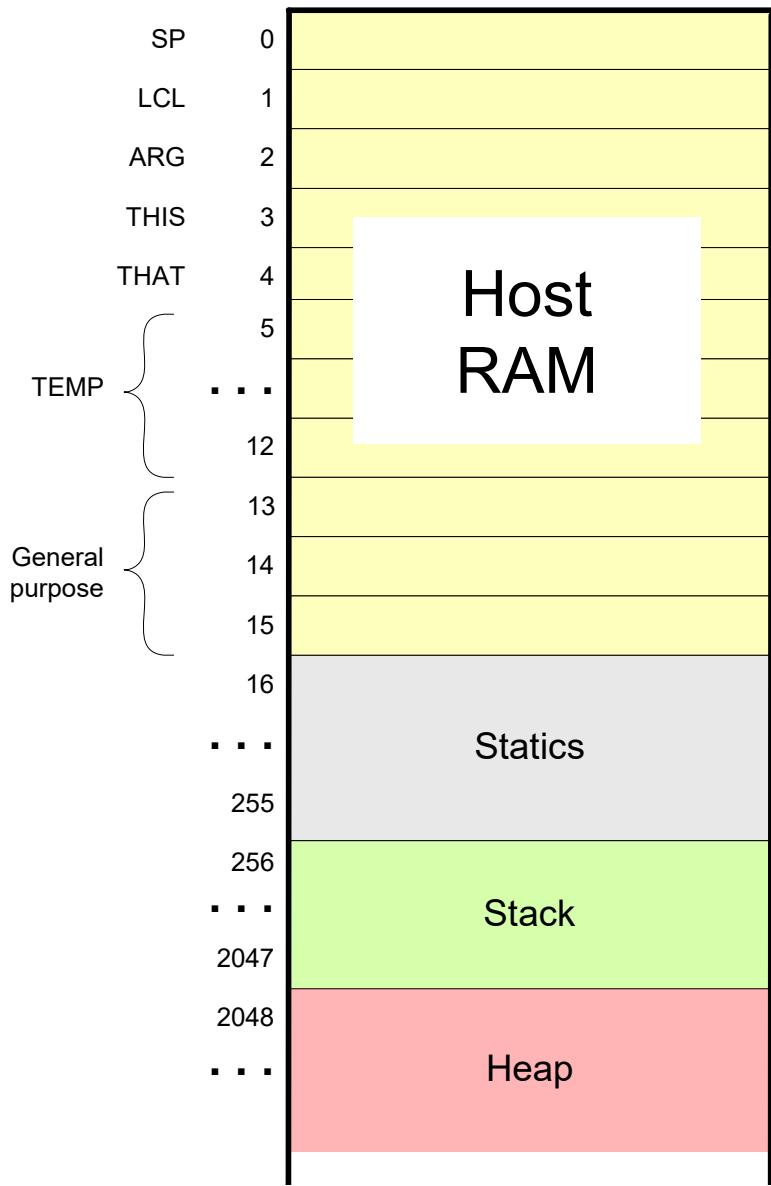
local, argument, this, that:

these segments are local at the function level; each function sees its own, private copy of each one of these four segments

The challenge:

represent all these logical constructs on the same single physical address space -- the host RAM.

# VM implementation on the Hack platform (memory)



**Basic idea:** the mapping of the stack and the global segments on the RAM is easy (fixed); the mapping of the function-level segments is dynamic, using pointers

The stack: mapped on RAM[ 256 ... 2047 ];  
The stack pointer is kept in RAM address SP

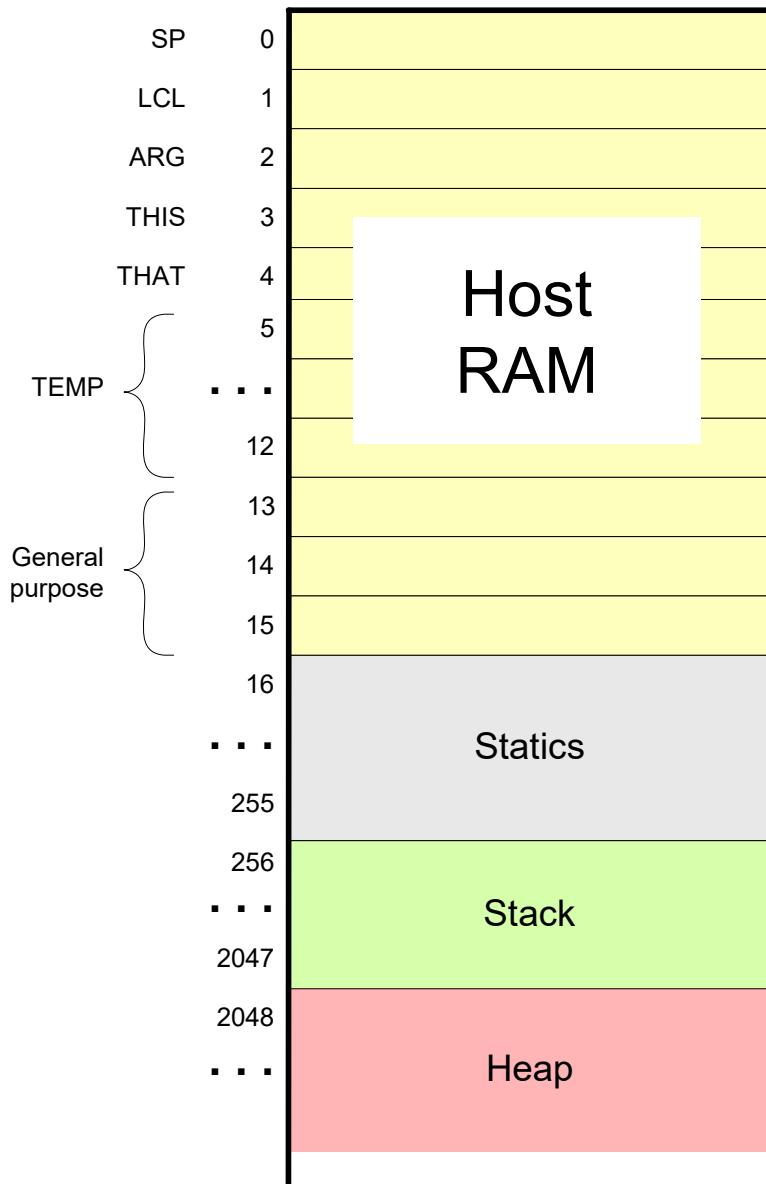
static: mapped on RAM[ 16 ... 255 ];  
each segment reference static  $i$  appearing in a VM file named  $f$  is compiled to the assembly language symbol  $f.i$  (recall that the assembler further maps such symbols to the RAM, from address 16 onward)

local,argument,this,that: these method-level segments are mapped somewhere from address 2048 onward, in an area called "heap". The base addresses of these segments are kept in RAM addresses LCL, ARG, THIS, and THAT. Access to the  $i$ -th entry of any of these segments is implemented by accessing RAM[ segmentBase +  $i$  ]

constant: a truly a virtual segment:  
access to constant  $i$  is implemented by supplying the constant  $i$ .

pointer: discussed later.

# VM implementation on the Hack platform (memory)



## Practice exercises

Now that we know how the memory segments are mapped on the host RAM, we can write Hack commands that realize the various VM commands. for example, let us write the Hack code that implements the following VM commands:

- ❑ push constant 1
- ❑ pop static 7 (suppose it appears in a VM file named f)
- ❑ push constant 5
- ❑ add
- ❑ pop local 2
- ❑ eq

## Tips:

1. The implementation of any one of these VM commands requires several Hack assembly commands involving pointer arithmetic (using commands like A=M)
2. If you run out of registers (you have only two ...), you may use R13, R14, and R15.

## VM implementation on the Hack platform (translator)

---

□ push constant 1

@1

D=A

@SP

A=M

M=D

@SP

M=M+1

□ add

@SP

AM=M-1

D+M

A=A-1

M=M+D

□ pop local 2

@LCL

D=M

@2

D=D+A

@R15

M=D

@SP

AM=M-1

D=M

@R15

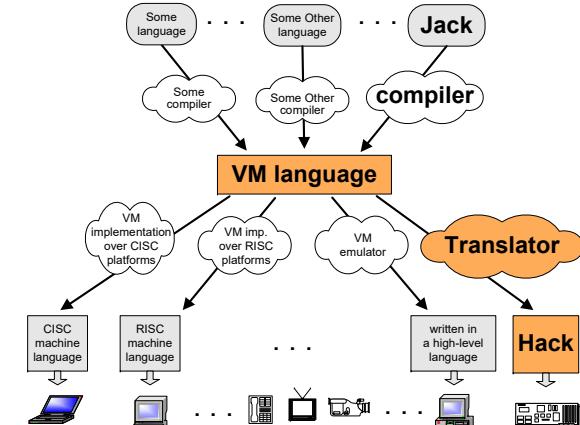
A=M

M=D

# Perspective

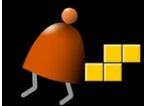
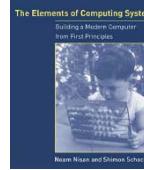
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- In this lecture we began the process of building a compiler
- Modern compiler architecture:
  - Front-end (translates from a high-level language to a VM language)
  - Back-end (translates from the VM language to the machine language of some target hardware platform)
- Brief history of virtual machines:
  - 1970's: p-Code
  - 1990's: Java's JVM
  - 2000's: Microsoft .NET
- A full blown VM implementation typically also includes a common software library (can be viewed as a mini, portable OS).
- We will build such a mini OS later in the course.



# The big picture

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<ul style="list-style-type: none"><li><input type="checkbox"/> JVM</li><li><input type="checkbox"/> Java</li><li><input type="checkbox"/> Java compiler</li><li><input type="checkbox"/> JRE</li></ul>	<ul style="list-style-type: none"><li><input type="checkbox"/> CLR</li><li><input type="checkbox"/> C#</li><li><input type="checkbox"/> C# compiler</li><li><input type="checkbox"/> .NET base class library</li></ul>	<ul style="list-style-type: none"><li><input checked="" type="checkbox"/> VM</li><li><input checked="" type="checkbox"/> Jack</li><li><input checked="" type="checkbox"/> Jack compiler</li><li><input checked="" type="checkbox"/> Mini OS</li></ul>	<ul style="list-style-type: none"><li><input checked="" type="checkbox"/> 7, 8</li><li><input checked="" type="checkbox"/> 9</li><li><input checked="" type="checkbox"/> 10, 11</li><li><input checked="" type="checkbox"/> 12</li></ul>
			(Book chapters and Course projects)