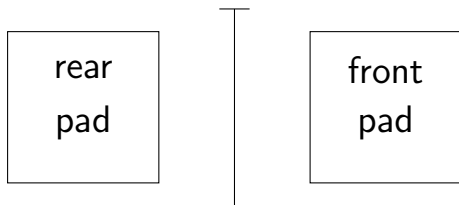


# What is a computer I

- Computers are complicated, but we can construct idealized computational models to do analysis
- Finite automata are the idealized model that we will discuss
- Example: automatic door

Fig 1.1

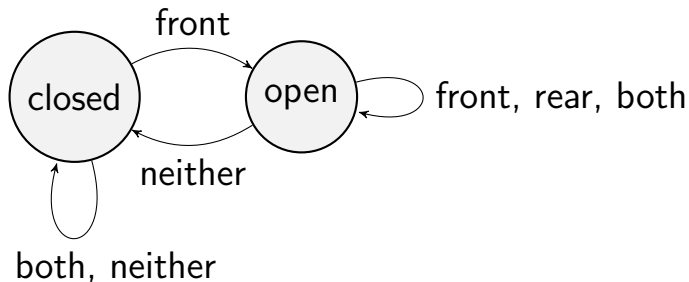


# What is a computer II

- Rules:  
When it moves, it cannot hit people
- We can use a simple graph to summarize all operations
- For example, if the door is open and some are in the front area, then the door should remain to be open

# What is a computer III

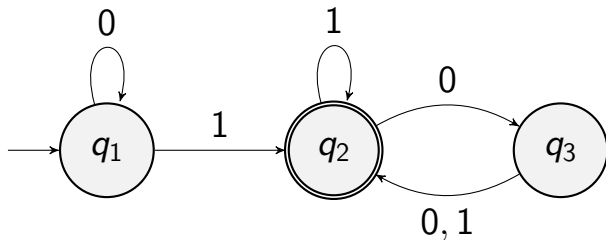
- Fig 1.2



- Single bit memory (open and closed)
- Automaton (single)  
automata (plural)
- This is a Latin word from Greek

# Examples of automata I

- Fig 1.4: a state diagram



states:  $q_1, q_2, q_3$

start state:  $q_1$

accept state  $q_2$  (double circle)

# Examples of automata II

- Example: running an input string 1101

$$q_1 \rightarrow q_2 \rightarrow q_2 \rightarrow q_3 \rightarrow q_2$$

This string is accepted

- Example: running 10

$$q_1 \rightarrow q_2 \rightarrow q_3$$

$q_3$  is not an accept state, so the string is rejected

- What are all strings accepted?

We will say what this set is

Unfortunately, it may not be always easy to know the set

# Formal definition I

We formally define a state diagram as a 5-tuple  $(Q, \Sigma, \delta, q_0, F)$

- $Q$ : set of states. It is a **finite** set
- $\Sigma$ : alphabet (i.e., set of characters in input string). It is a finite set
- $\delta : Q \times \Sigma \rightarrow Q$ : transition function  
This is the most complicated part of the definition. We explain the transition function by an example later
- $q_0 \in Q$ : start state

## Formal definition II

- $F \subset Q$ : set of accept states
- For the example given above,

$$Q = \{q_1, q_2, q_3\}$$

$$\Sigma = \{0, 1\}$$

$$q_0 = q_1$$

$$F = \{q_2\}$$

- The  $\delta$  function:

	0	1
$q_1$	$q_1$	$q_2$
$q_2$	$q_3$	$q_2$
$q_3$	$q_2$	$q_2$

# Formal definition III

- Language of  $M$ : all strings accepted by  $M$ . Denoted as

$$A = L(M)$$

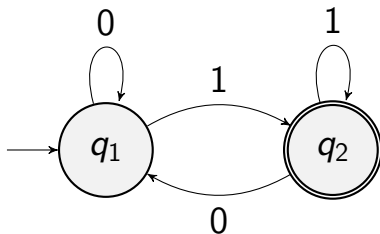
- Figure 1.4:

$$A = \{w \mid w : \text{at least one } 1, \text{ even } \neq 0 \\ \text{after the last } 1\}$$



# Example 1.7 I

- Figure 1.8



- $M = (\{q_1, q_2\}, \{0, 1\}, \delta, q_1, \{q_2\})$
- What is  $L(M)$  ? Anything ends with 1
- How to think about this ?

## Example 1.7 II

- Before the last input character, we must be at  $q_1$  or  $q_2$ . Then only if the last is 1 we can reach  $q_2$  to get accepted