

# Tone mapping

Digital Visual Effects

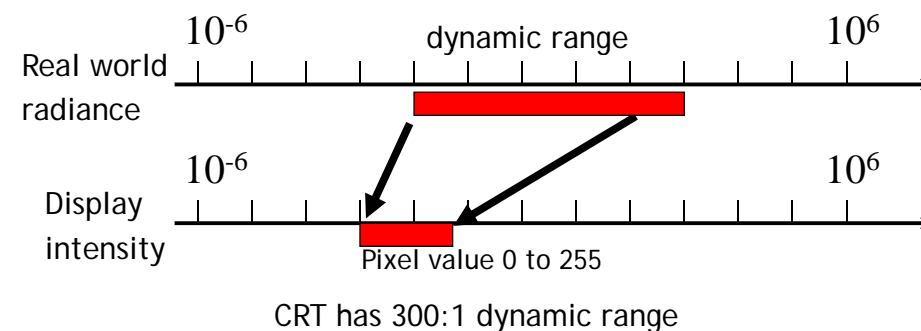
Yung-Yu Chuang

with slides by Fredo Durand, and Alexei Efros

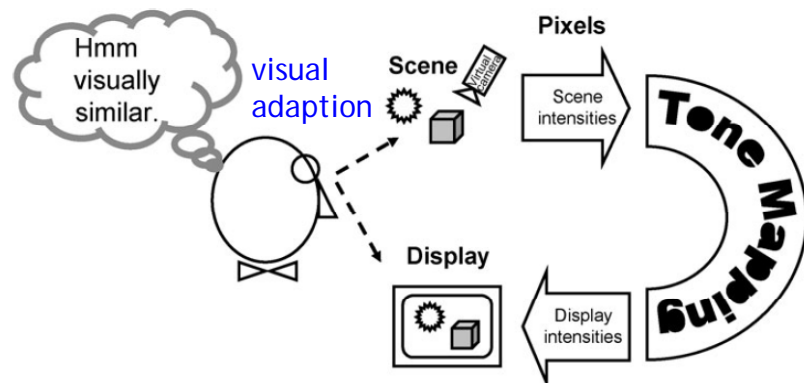
## Tone mapping

- How should we map scene luminances (up to 1:100,000) to display luminances (only around 1:100) to produce a satisfactory image?

Linear scaling?, thresholding?



## The ultimate goal is a visual match



We do not need to reproduce the true radiance as long as it gives us a visual match.

## Eye is not a photometer!



- Dynamic range along the visual pathway is only around 32:1.
- The key is adaptation

## Eye is not a photometer!



Are the headlights different in two images? Physically, they are the same, but perceptually different.

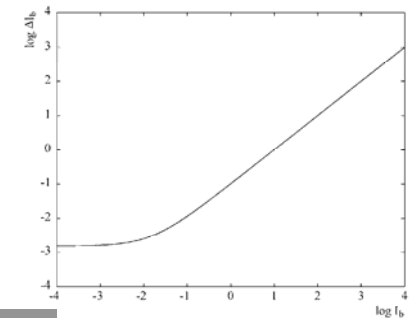
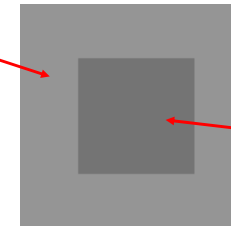
## We are more sensitive to contrast

- Weber's law

Just-noticeable  
Difference (JND)

$$\frac{\Delta I_b}{I_b} \sim 1\%$$

background  
intensity



## How humans deal with dynamic range

- We're more sensitive to contrast (multiplicative)
  - A ratio of 1:2 is perceived as the same contrast as a ratio of 100 to 200
  - Makes sense because illumination has a multiplicative effect
  - Use the log domain as much as possible
- Dynamic adaptation (very local in retina)
  - Pupil (not so important)
  - Neural
  - Chemical
- Different sensitivity to spatial frequencies

## Preliminaries

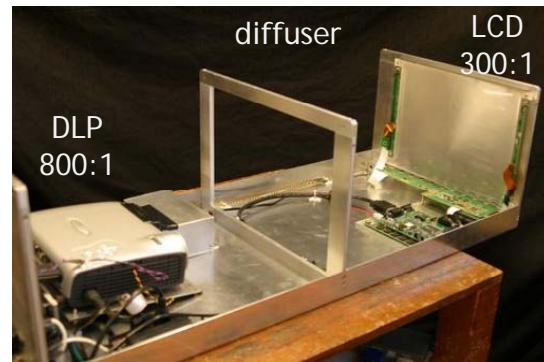
- For color images

$$\begin{bmatrix} R_d \\ G_d \\ B_d \end{bmatrix} = \begin{bmatrix} L_d \frac{R_w}{L_w} \\ L_d \frac{G_w}{L_w} \\ L_d \frac{B_w}{L_w} \end{bmatrix}$$

- Log domain is usually preferred.

## HDR Display

- Once we have HDR images (either captured or synthesized), how can we display them on normal displays?



Theoretically,  
240,000:1.

Due to imperfect  
optical depth,  
54,000:1 measured

HDR display system, Sunnybrook Technology, SIGGRAPH2004

## Sunnybrook HDR display

- Use Bright Source + Two 8-bit Modulators
  - Transmission multiplies together
  - Over 10,000:1 dynamic range possible

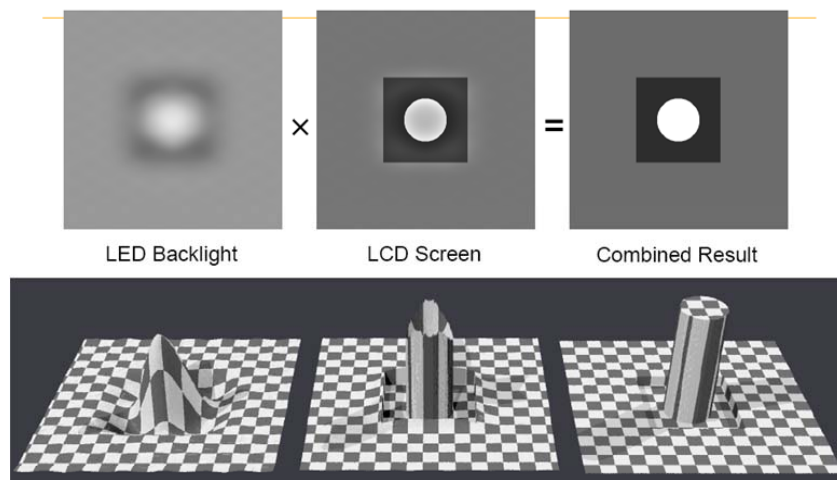


Low-res B&W backlight

High-res color foreground

Slide from the 2005 Siggraph course on HDR

## How it works



Slide from the 2005 Siggraph course on HDR

## Brightside HDR display



37"  
200000:1

Acquired  
by [Dolby](#)

## Tone mapping operators

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- Spatial (global/local)
- Frequency domain
- Gradient domain
  
- 3 papers from SIGGRAPH 2002
  - ♦ Photographic Tone Reproduction for Digital Images
  - ♦ Fast Bilateral Filtering for the Display of High-Dynamic-Range Images
  - ♦ Gradient Domain High Dynamic Range Compression

## Photographic Tone Reproduction for Digital Images

Erik Reinhard Mike Stark  
Peter Shirley Jim Ferwerda  
SIGGRAPH 2002

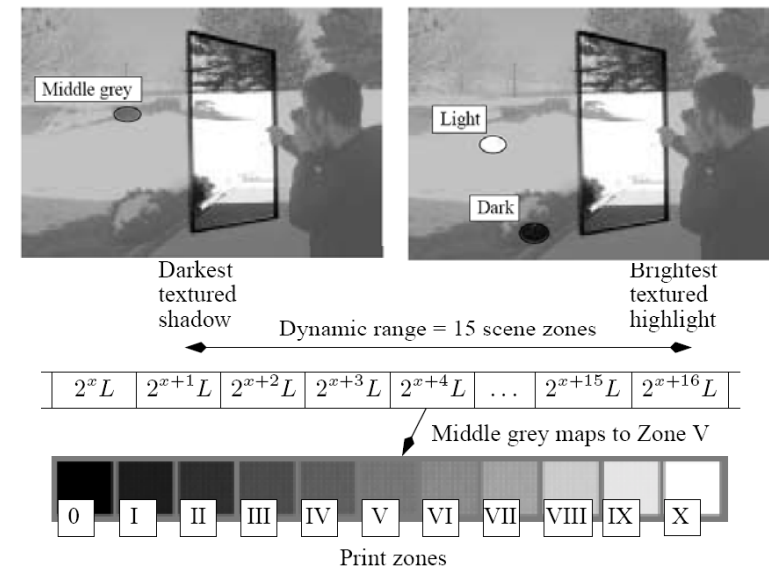
## Photographic tone reproduction

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- Proposed by Reinhard et. al. in SIGGRAPH 2002
- Motivated by traditional practice, zone system by Ansel Adams and dodging and burning
- It contains both global and local operators

## Zone system

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## The Zone system

- Formalism to talk about exposure, density
- Zone = intensity range, in powers of two
- In the scene, on the negative, on the print



Source: Ansel Adams

## The Zones

### The Zones

**0** Solid black; the same as the film rebate

**I** Nearly black; just different from Zone 0

**II** The first hint of texture

**III** Textured shadow; the first recognizable shadow detail

**IV** Average shadow value on Caucasian skin, foliage and buildings

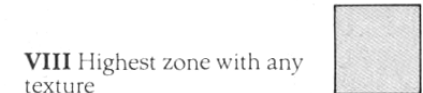
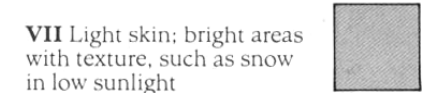
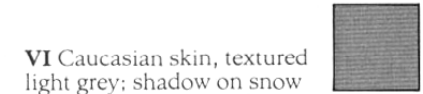
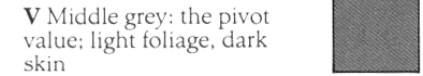
**V** Middle grey; the pivot value; light foliage, dark skin

**VI** Caucasian skin, textured light grey; shadow on snow

**VII** Light skin; bright areas with texture, such as snow in low sunlight

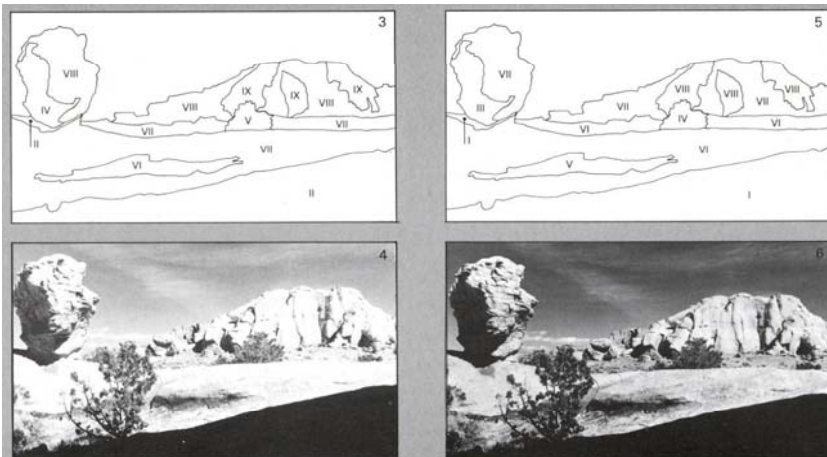
**VIII** Highest zone with any texture

**IX** Pure untextured white



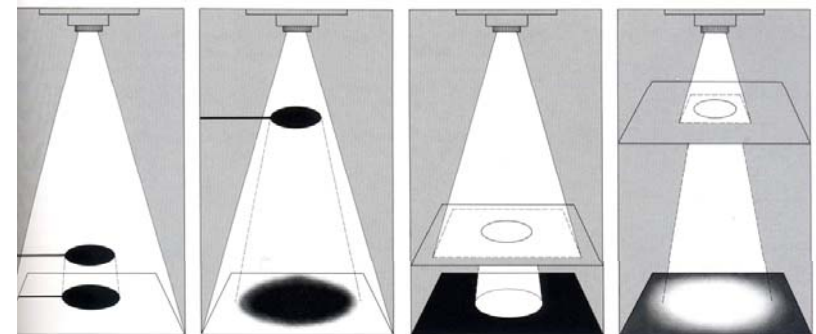
## The Zone system

- You decide to put part of the system in a given zone

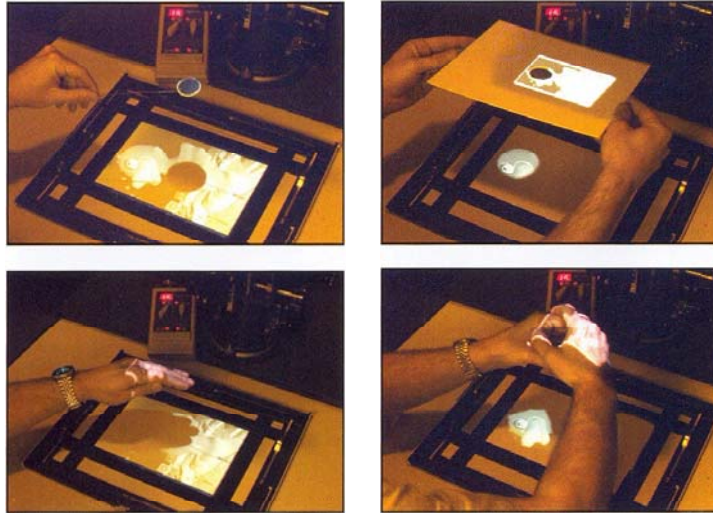


## Dodging and burning

- During the print
- Hide part of the print during exposure
  - Makes it brighter



## Dodging and burning

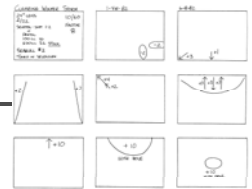


dodging

burning

From Photography by London et al.

## Dodging and burning



- Must be done for every single print!



Straight print

After dodging and burning

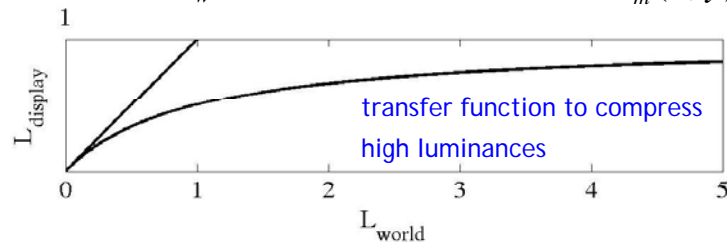
## Global operator

$$\bar{L}_w = \exp\left(\frac{1}{N} \sum_{x,y} \log(\delta + L_w(x,y))\right)$$

Approximation of scene's key (how light or dark it is).  
Map to 18% of display range for average-key scene

User-specified; high key or low key

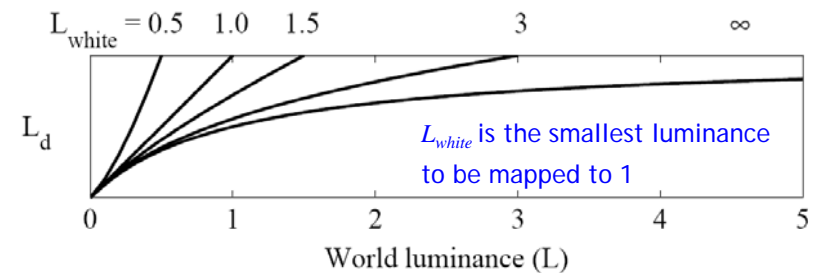
$$L_m(x,y) = \frac{a}{L_w} L_w(x,y) \quad L_d(x,y) = \frac{L_m(x,y)}{1 + L_m(x,y)}$$



## Global operator

It seldom reaches 1 since the input image does not have infinitely large luminance values.

$$L_d(x,y) = \frac{L_m(x,y) \left(1 + \frac{L_m(x,y)}{L_{white}^2(x,y)}\right)}{1 + L_m(x,y)}$$





low key (0.18)

high key (0.5)

## Dodging and burning (local operators)

- Area receiving a different exposure is often bounded by sharp contrast
- Find largest surrounding area without any sharp contrast

$$L_s^{blur}(x, y) = L_m(x, y) \otimes G_s(x, y)$$

$$V_s(x, y) = \frac{L_s^{blur}(x, y) - L_{s+1}^{blur}(x, y)}{2^\phi a/s^2 + L_s^{blur}}$$

$$s_{\max} : |V_{s_{\max}}(x, y)| < \varepsilon$$

## Dodging and burning (local operators)

$$L_d(x, y) = \frac{L_m(x, y)}{1 + L_{s_{\max}}^{blur}(x, y)}$$

- A darker pixel (smaller than the blurred average of its surrounding area) is divided by a larger number and become darker (dodging)
- A brighter pixel (larger than the blurred average of its surrounding area) is divided by a smaller number and become brighter (burning)
- Both increase the contrast

## Dodging and burning



Simple operator

Dodging-and-burning

## Frequency domain

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- First proposed by Oppenheim in 1968!
- Under simplified assumptions,

image = illuminance \* reflectance  
low-frequency attenuate more    high-frequency attenuate less



## Oppenheim

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- Taking the logarithm to form density image
- Perform FFT on the density image
- Apply frequency-dependent attenuation filter

$$s(f) = (1 - c) + c \frac{kf}{1 + kf}$$

- Perform inverse FFT
- Take exponential to form the final image

## Fast Bilateral Filtering for the Display of High-Dynamic-Range Images

Frédo Durand & Julie Dorsey

SIGGRAPH 2002

### A typical photo

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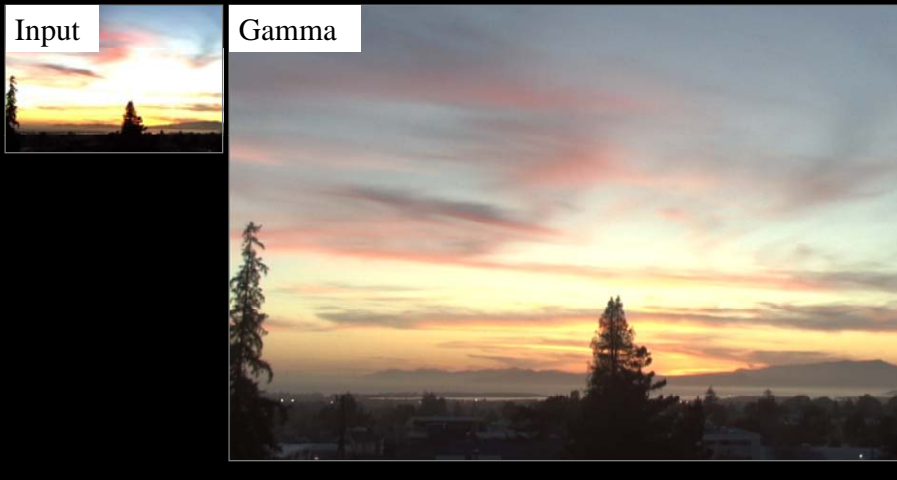
- Sun is overexposed
- Foreground is underexposed





## Gamma compression

- $X \rightarrow X^\gamma$
- Colors are washed-out



## Gamma compression on intensity

- Colors are OK, but details (intensity high-frequency) are blurred



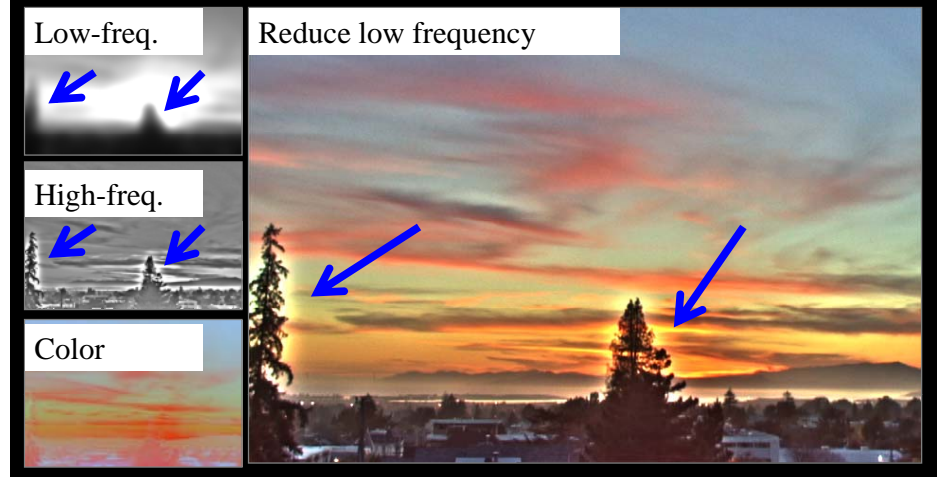
## Chiu et al. 1993

- Reduce contrast of low-frequencies
- Keep high frequencies



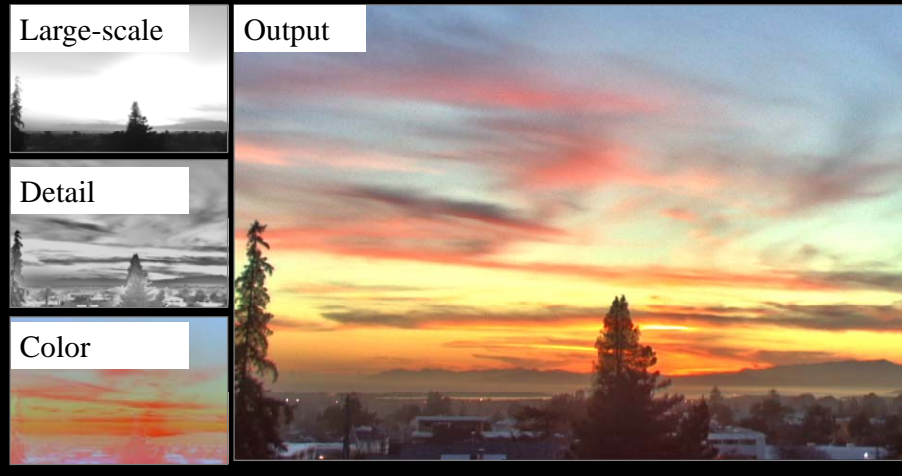
## The halo nightmare

- For strong edges
- Because they contain high frequency



## Durand and Dorsey

- Do not blur across edges
- Non-linear filtering



## Edge-preserving filtering

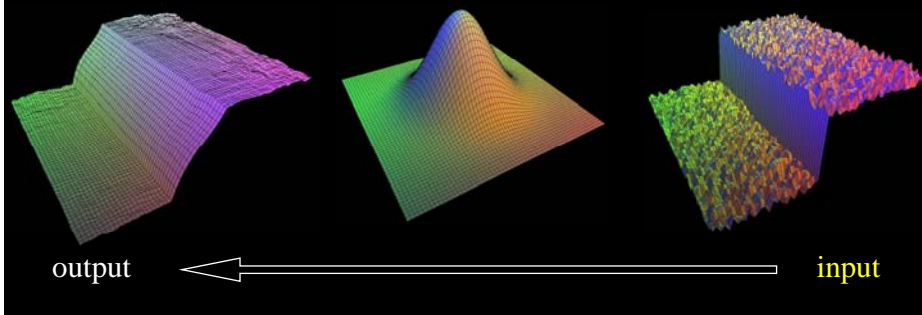
- Blur, but not across edges



- Anisotropic diffusion [Perona & Malik 90]
  - Blurring as heat flow
  - LCIS [Tumblin & Turk]
- Bilateral filtering [Tomasi & Manduci, 98]

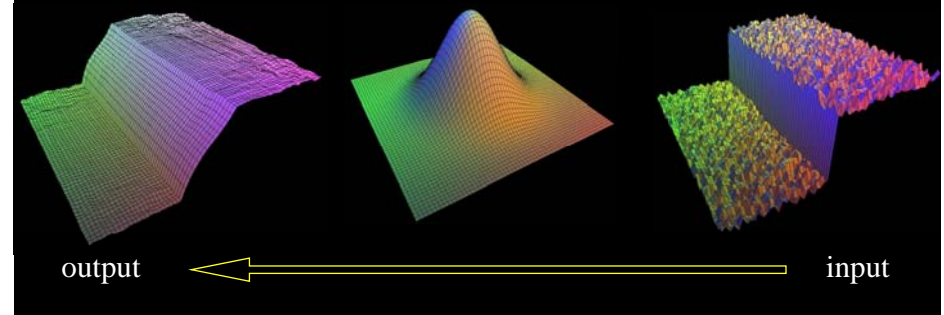
## Start with Gaussian filtering

- Here, input is a step function + noise



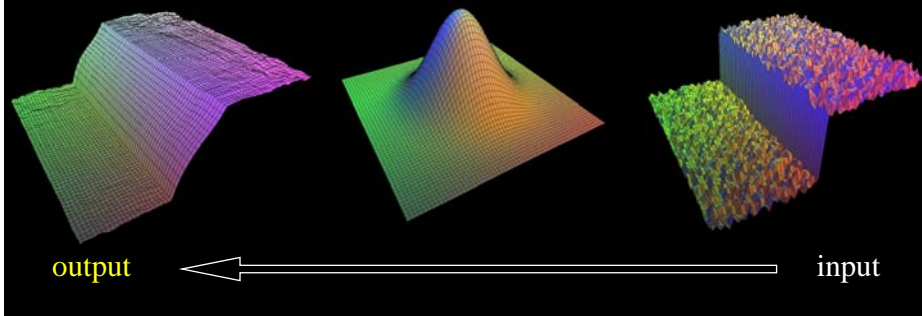
## Start with Gaussian filtering

- Spatial Gaussian f

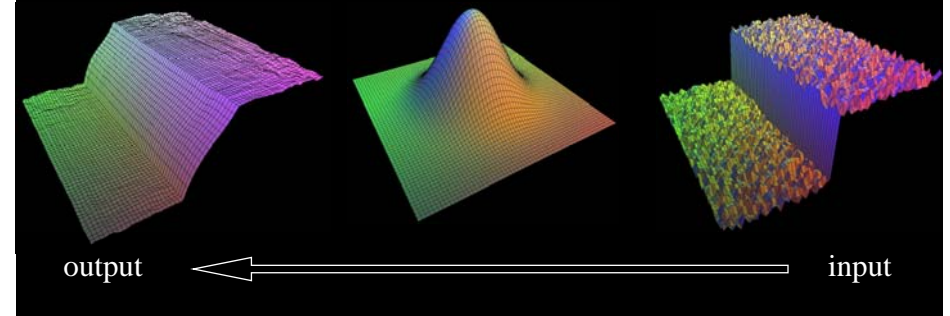


## Start with Gaussian filtering

- Output is blurred

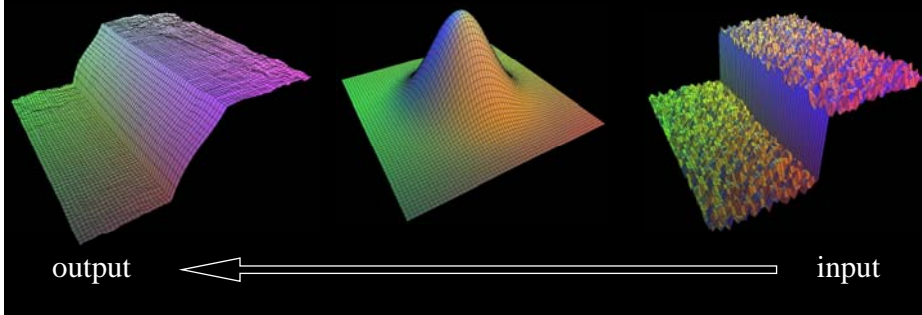


## Gaussian filter as weighted average



## The problem of edges

- Here, “pollutes” our estimate  $J(x)$
- It is too different



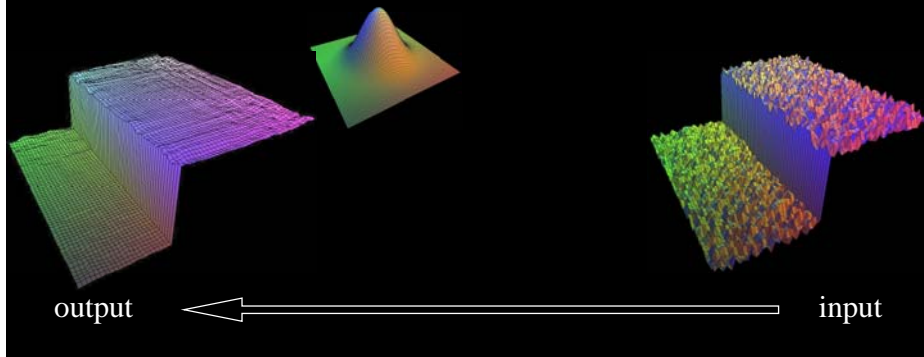
## Principle of Bilateral filtering

- [Tomasi and Manduchi 1998]
- Penalty  $g$  on the intensity difference



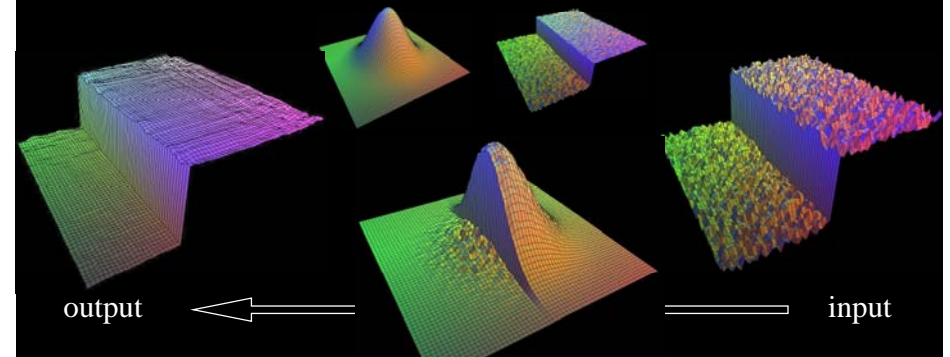
## Bilateral filtering

- [Tomasi and Manduchi 1998]
- Spatial Gaussian  $f$



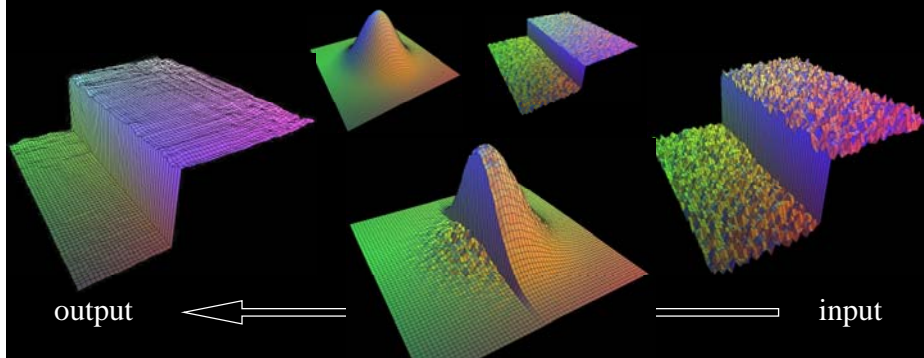
## Bilateral filtering

- [Tomasi and Manduchi 1998]
- Spatial Gaussian  $f$
- Gaussian  $g$  on the intensity difference



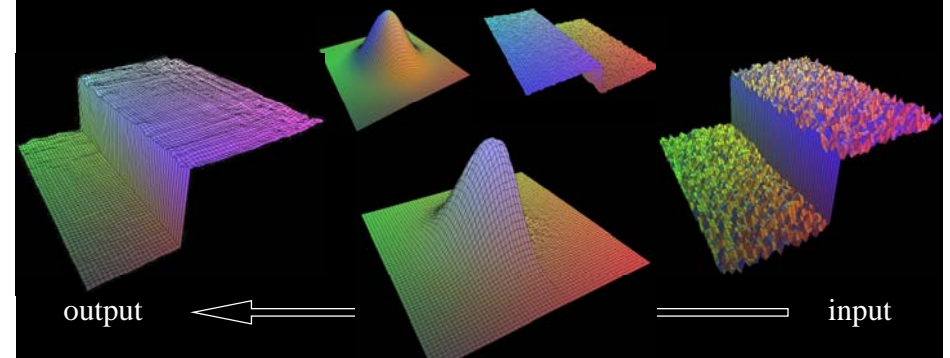
## Normalization factor

- [Tomasi and Manduchi 1998]
- $k(x) =$



## Bilateral filtering is non-linear

- [Tomasi and Manduchi 1998]
- The weights are different for each output pixel



# Contrast reduction

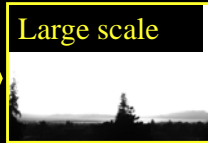
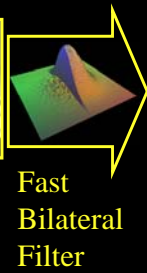


Contrast too high!

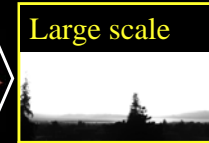
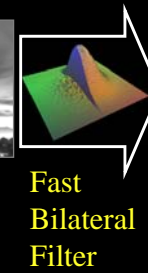
# Contrast reduction



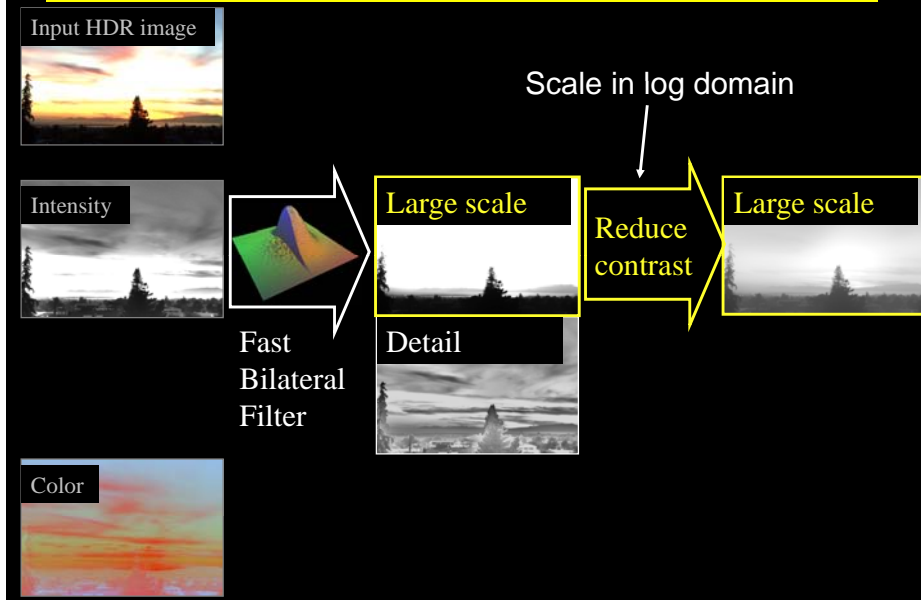
# Contrast reduction



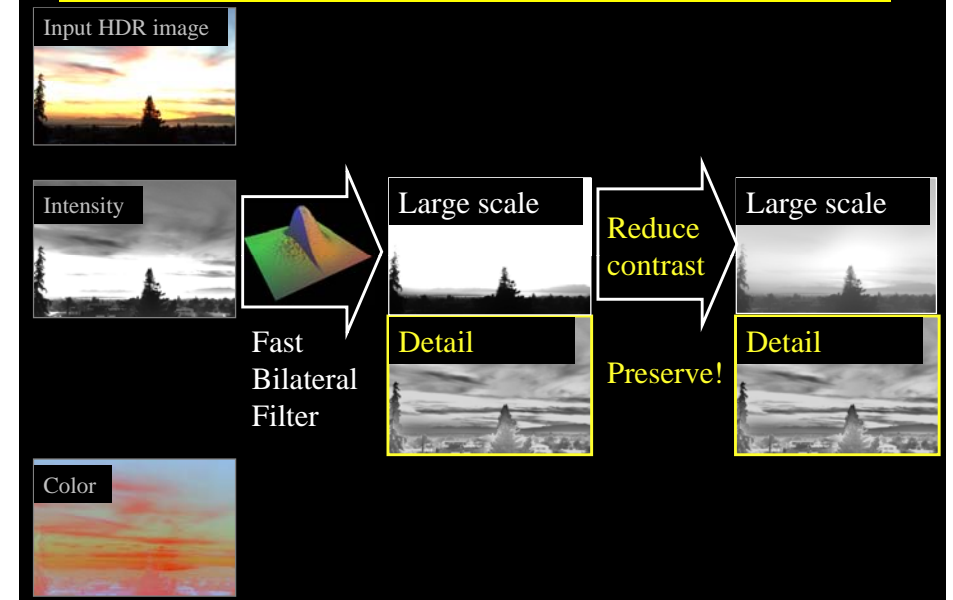
# Contrast reduction



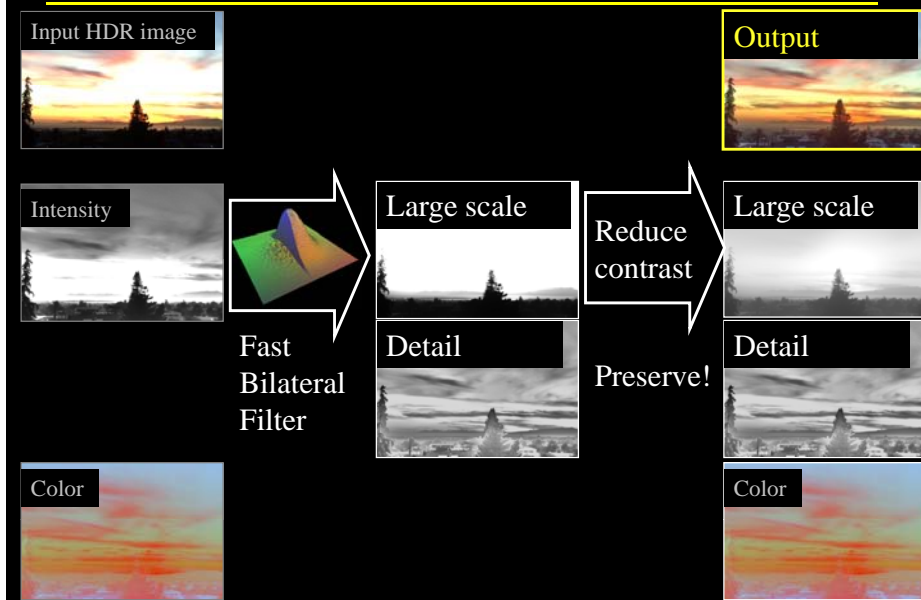
## Contrast reduction



## Contrast reduction



## Contrast reduction



## Bilateral filter is slow!

- Compared to Gaussian filtering, it is much slower because the kernel is not fixed.
- Durand and Dorsey proposed an approximate approach to speed up
- Paris and Durand proposed an even-faster approach in ECCV 2006. We will cover this one when talking about computational photography.



Oppenheim

bilateral

## Gradient Domain High Dynamic Range Compression

Raanan Fattal Dani Lischinski Michael Werman

SIGGRAPH 2002

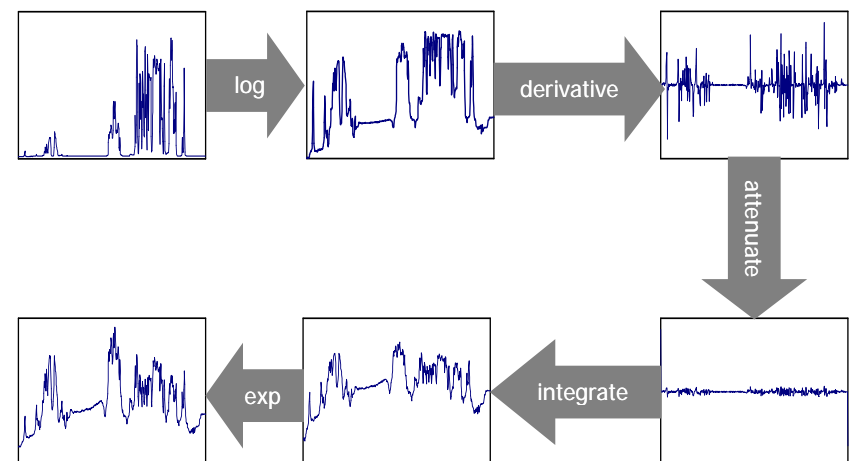
### Log domain

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- Logarithm is a crude approximation to the perceived brightness
- Gradients in log domain correspond to ratios (local contrast) in the luminance domain

### The method in 1D

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## The method in 2D

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- Given: a log-luminance image  $H(x,y)$
- Compute an *attenuation map*  $\Phi(\|\nabla H\|)$
- Compute an attenuated gradient field  $\mathbf{G}$ :

$$G(x, y) = \nabla H(x, y) \cdot \Phi(\|\nabla H\|)$$

- Problem:  $\mathbf{G}$  may not be integrable!

## Solution

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- Look for image  $\mathbf{I}$  with gradient closest to  $\mathbf{G}$  in the least squares sense.
- $\mathbf{I}$  minimizes the integral:  $\iint F(\nabla I, \mathbf{G}) dx dy$

$$F(\nabla I, \mathbf{G}) = \|\nabla I - \mathbf{G}\|^2 = \left(\frac{\partial I}{\partial x} - G_x\right)^2 + \left(\frac{\partial I}{\partial y} - G_y\right)^2$$

$$\longrightarrow \frac{\partial^2 I}{\partial x^2} + \frac{\partial^2 I}{\partial y^2} = \frac{\partial G_x}{\partial x} + \frac{\partial G_y}{\partial y} \quad \text{Poisson equation}$$

## Solving Poisson equation

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- No analytical solution
- Multigrid method
- Conjugate gradient method

Solve  $\frac{\partial^2 I}{\partial x^2} + \frac{\partial^2 I}{\partial y^2} = \frac{\partial G_x}{\partial x} + \frac{\partial G_y}{\partial y}$

$G_x(x, y) - G_x(x-1, y) + G_y(x, y) - G_y(x, y-1)$

$I(x+1, y) + I(x-1, y) + I(x, y+1) + I(x, y-1) - 4I(x, y)$

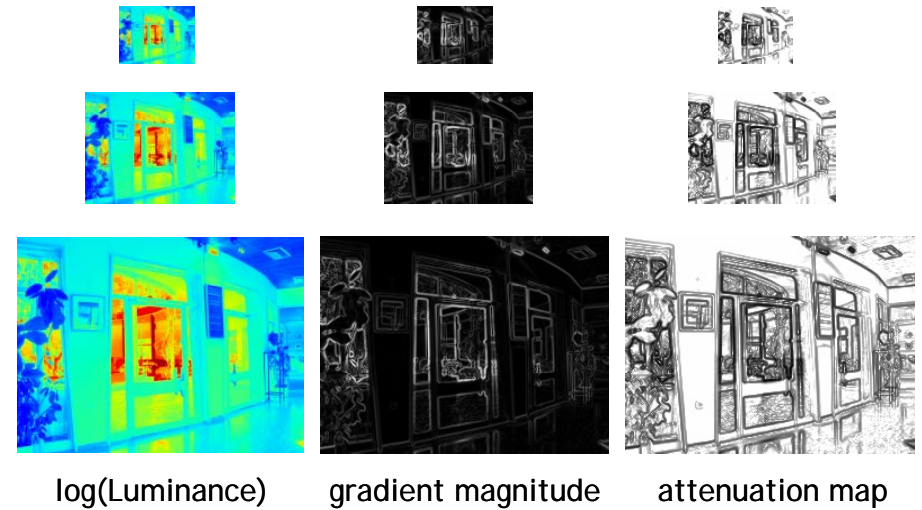
$$\begin{bmatrix} \dots & 1 & \dots & 1 & -4 & 1 & \dots & 1 & \dots \end{bmatrix} \begin{bmatrix} \mathbf{I} \end{bmatrix} = \begin{bmatrix} \end{bmatrix}$$



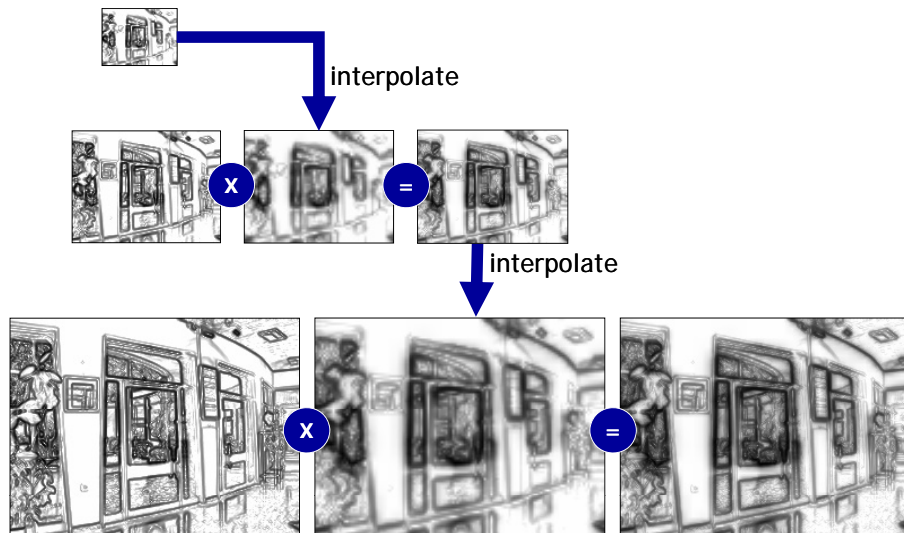
## Attenuation

- Any dramatic change in luminance results in large luminance gradient at some scale
- Edges exist in multiple scales. Thus, we have to detect and attenuate them at multiple scales
- Construct a Gaussian pyramid  $H_i$

$$\text{Attenuation } \varphi_k(x, y) = \left( \frac{\|\nabla H_k(x, y)\|}{\alpha} \right)^{\beta-1} \quad \beta \sim 0.8$$
$$\alpha = 0.1\overline{\nabla H}$$



## Multiscale gradient attenuation



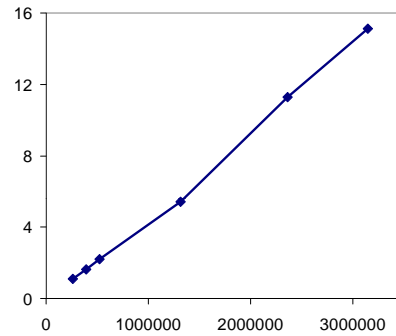
## Final gradient attenuation map



## Performance

- Measured on 1.8 GHz Pentium 4:

- 512 x 384: 1.1 sec
- 1024 x 768: 4.5 sec



- Can be accelerated using processor-optimized libraries.

## Informal comparison



Gradient domain  
[Fattal et al.]

Bilateral  
[Durand et al.]

Photographic  
[Reinhard et al.]

## Informal comparison



Gradient domain  
[Fattal et al.]

Bilateral  
[Durand et al.]

Photographic  
[Reinhard et al.]

## Informal comparison



Gradient domain  
[Fattal et al.]

Bilateral  
[Durand et al.]

Photographic  
[Reinhard et al.]

# Evaluation of Tone Mapping Operators using a High Dynamic Range Display

Patrick Ledda Alan Chalmers  
Tom Troscinko Helge Seetzen

SIGGRAPH 2005

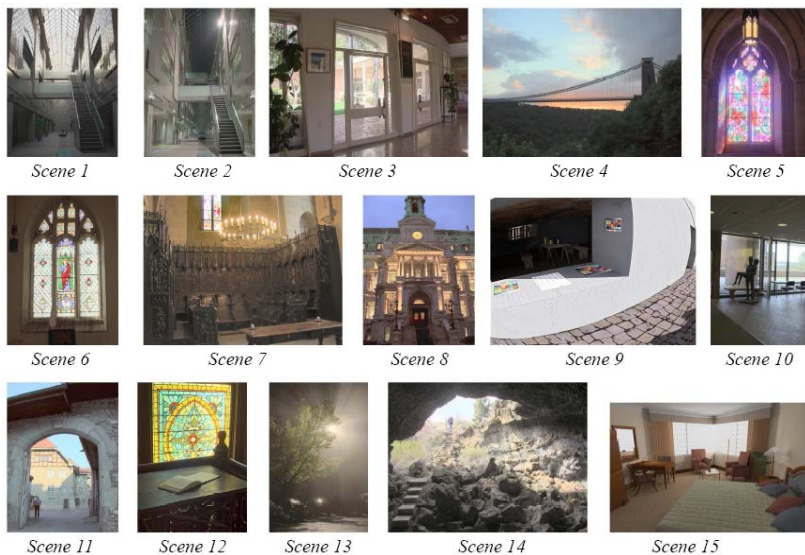
## Six operators

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- H: histogram adjustment
- B: bilateral filter
- P: photographic reproduction
- I: iCAM
- L: logarithm mapping
- A: local eye adaption

## 23 scenes

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## Experiment setting

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## Preference matrix

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- Ranking is easier than rating.
- 15 pairs for each person to compare. A total of 345 pairs per subject.

	<i>tmo</i> <sub>1</sub>	<i>tmo</i> <sub>2</sub>	<i>tmo</i> <sub>3</sub>	<i>tmo</i> <sub>4</sub>	<i>tmo</i> <sub>5</sub>	<i>tmo</i> <sub>6</sub>	Score
<i>tmo</i> <sub>1</sub>	-	1	0	0	1	1	3
<i>tmo</i> <sub>2</sub>	0	-	0	1	1	0	2
<i>tmo</i> <sub>3</sub>	1	1	-	1	1	1	5
<i>tmo</i> <sub>4</sub>	1	0	0	-	0	0	1
<i>tmo</i> <sub>5</sub>	0	0	0	1	-	1	2
<i>tmo</i> <sub>6</sub>	0	1	0	1	0	-	2

preference matrix (*tmo*<sub>2</sub>->*tmo*<sub>4</sub>, *tom*<sub>2</sub> is better than *tmo*<sub>4</sub>)

## Statistical measurements

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- Statistical measurements are used to evaluate:
  - Agreement: whether most agree on the ranking between two tone mapping operators.
  - Consistency: no cycle in ranking. If all are confused in ranking some pairs, it means they are hard to compare. If someone is inconsistent alone, his ranking could be dropped.

## Overall similarity

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- Scene 8



	<i>P</i>	<i>H</i>	<i>B</i>	<i>L</i>	<i>I</i>	<i>A</i>	Total
<i>P</i>	-	24	46	42	10	32	154
<i>H</i>	24	-	44	32	8	12	120
<i>B</i>	2	4	-	8	2	4	20
<i>L</i>	6	16	40	-	4	12	78
<i>I</i>	38	40	46	44	-	38	206
<i>A</i>	16	36	44	36	10	-	142

## Summary

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### *Overall Similarity: Color*

<i>I</i>	<i>P</i>	<i>H</i>	<i>A</i>	<i>L</i>	<i>B</i>
<u>3712</u>	<u>3402</u>	<u>2994</u>	<u>2852</u>	<u>1902</u>	<u>1696</u>

### *Bright Detail*

<i>I</i>	<i>A</i>	<i>P</i>	<i>H</i>	<i>B</i>	<i>L</i>
<u>823</u>	<u>688</u>	<u>569</u>	<u>549</u>	<u>474</u>	<u>347</u>

### *Dark Detail*

<i>P</i>	<i>A</i>	<i>I</i>	<i>L</i>	<i>H</i>	<i>B</i>
<u>815</u>	<u>793</u>	<u>583</u>	<u>491</u>	<u>485</u>	<u>283</u>

## Not settled yet!

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- Some other experiment said bilateral are better than others.
- For your reference, photographic reproduction performs well in both reports.
- There are parameters to tune and the space could be huge.

## References

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- Raanan Fattal, Dani Lischinski, Michael Werman, [Gradient Domain High Dynamic Range Compression](#), SIGGRAPH 2002.
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