

Machine Learning Homework 3

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- 1 Introduction
- 2 Subject
- 3 Conclusion

Problem Grading

The problems are graded as following arrangement:

Problem 3.1 (1)-(6)	Te-Kang Jan
(7)	
Problem 3.2	Chun-Wei Liu
Problem 3.3	
Problem 3.4	Ken-Yi Lin
Problem 3.5	Hsuan-Tien Lin

Problem 3.1 (1)-(6)

- some people lose their points because they didn't write the calculate process.
- even the problem is really easy, make sure you wrote the reason for the answer.

Problem 3.1 (7)

Prove the following hypothesis set for $x \in \mathfrak{R}$ is of an infinite VC dimension:

$$H = \{h_\alpha : h_\alpha(x) = (-1)^{\lfloor \alpha x \rfloor}\}$$

,where $\alpha \in \mathfrak{R}$.

- there must be 2^N 's dichotomies, if we chose a proper data set with N points.
- statement above is true for any N .

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Possible approaches

- show us the α and x .
- there are 2^N dichotomies for a data set with N points.

Problem 3.1 (7)

show me the α and x

$$x_i = 10^{1-i}$$

$$\alpha = \sum (1/2) * (1 - y_i) * 10^{i-1}$$

e.g $N = 4$, *dichotomy* = $\{+, -, +, -\}$

$$\alpha = 0 + 10 + 0 + 1000 = 1010$$

$$h_\alpha(1) = 1$$

$$h_\alpha(10) = -1$$

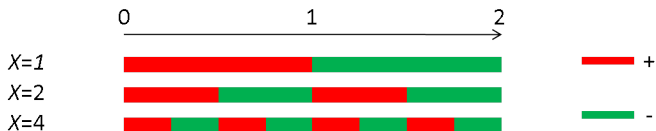
$$h_\alpha(100) = 1$$

$$h_\alpha(1000) = -1$$

Problem 3.1 (7)

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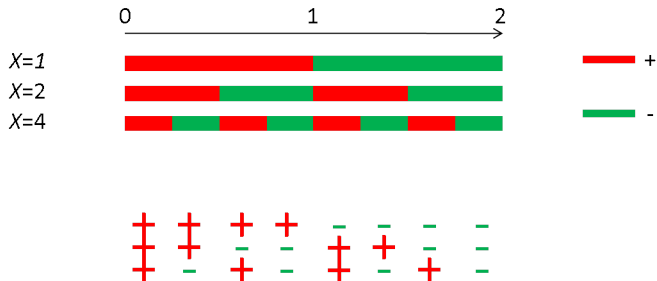
e.g $N = 3$, there are 8 dichotomies could be generated



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Feel free to contact with TAs if you have any question about the homework.