

* priority queue w/ $O(1)$ insert and $O(1)$ getMin?
hard for each individual operation, (and $O(\log n)$ extractMin)
but possible "amortized"

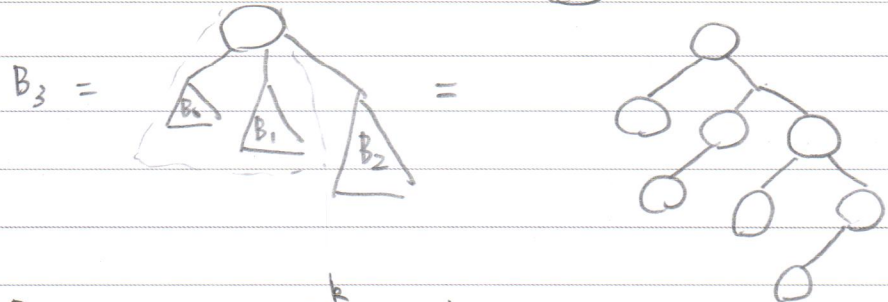
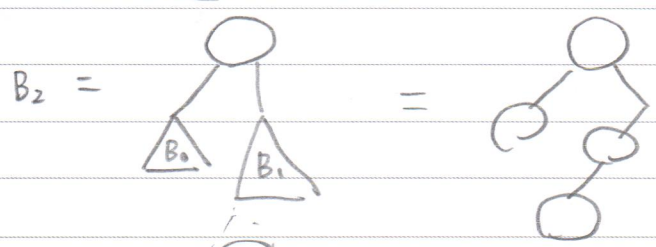
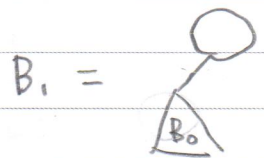
* Binomial } cheap insert usually
 } expensive insert some time

* observation :

insert to (merge w/) small tree : cheap
 large : expensive

idea: instead of using one tree (heap or leftist)
use many trees, from small to large
try merge w/ small trees first

* binomial tree



B_k contains 2^k nodes

* binomial forest

{ at most one B_k per each k }
 \Rightarrow can represent any n elements in node

$n=10$: { B_3, B_1 }

$n=11$: { B_3, B_1, B_0 }

binary number representation

* ^(min-) binomial heap

binomial forest w/ min-trees

insert \circ to { B_0 } \Rightarrow merge $B_0, B_0 \Rightarrow B_1$

insert \circ to { B_1 } \Rightarrow { B_0, B_1 }

insert \circ to { B_0, B_1 } \Rightarrow merge $B_0, B_0 \Rightarrow$ merge $B_1, B_1 \Rightarrow B_2$

insert \circ to { B_2 } \Rightarrow { B_0, B_2 }

- every one insertions : add B_0
- two : merge B_0, B_0
- four : merge B_1, B_1
- eight : merge B_2, B_2

after n insertions

$\frac{n}{2^k} + \frac{n}{2^{k-1}} + \dots + n = O(n)$ operations \Rightarrow amortized $O(1)$

(like incrementing binary numbers)

* get Min : search for { B_0, B_1, \dots, B_k } for min
 at most $O(\log n)$ trees for n nodes
 $\Rightarrow O(\log n)$

can be improved by keeping a pmin pointer to min-min-tree

* merge : $O(\log n)$, like adding to binary numbers

* del Min : remove and merge sub-trees w/ existing trees