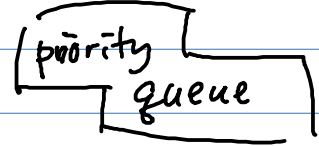


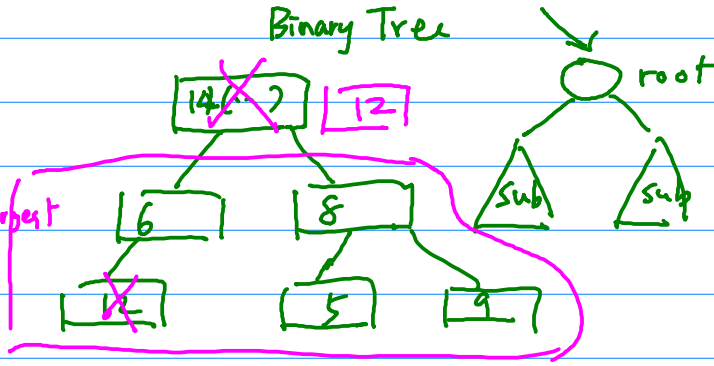
* task: find the node w/ largest

node (key to mean priority
 data to mean todo



FAST

*

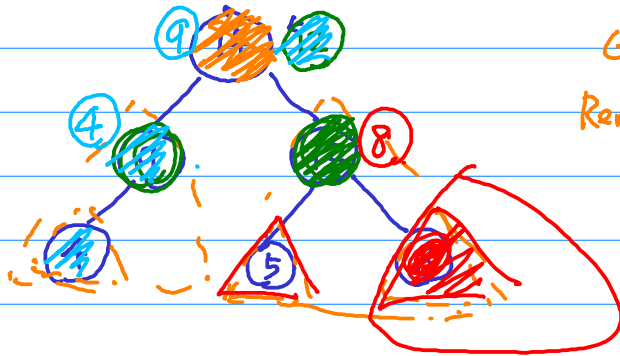


*

binary max-tree

- ① root key \geq other node's key) ✓
- ② every sub-tree is bin-maxtree ←

14 12



Get Largest ? root

Remove Largest ?

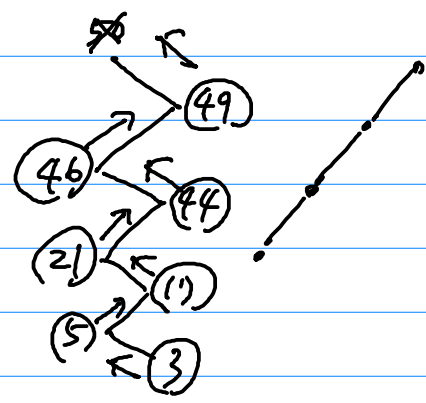
replace w/
 larger of sub-root
 recursively

* Worst time complexity :

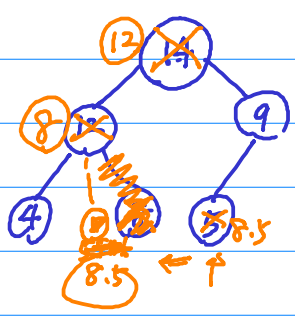
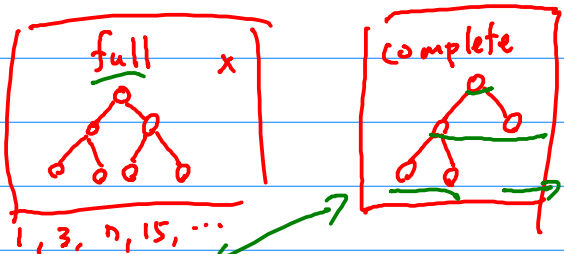
$O(h)$

smaller than $O(n)$

$O(n)$



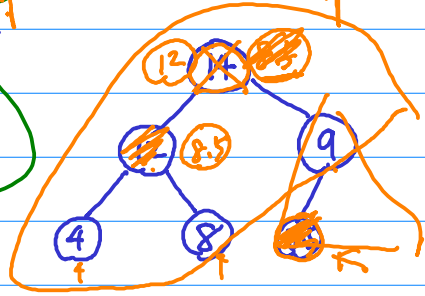
$h = O(\log n)$



Remove Largest

* complete binary max-tree

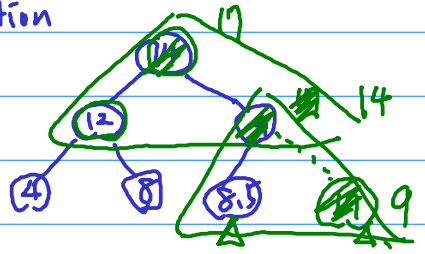
max-heap



Remove Largest

- ① last \rightarrow root (complete)
- ② sink down ? $O(h)$
(max) $O(\log n)$

* insertion



- ① insert at last
- ② flat up $O(h)$

complete

* Complete bin. tree \leftrightarrow heap

array \leftrightarrow partially ordered array \leftrightarrow ordered array



sel. sort on

(unordered) array

$O(n) \cdot O(n) = O(n^2)$

heap sort

$O(n \log n)$ (insertion $O(h)$)

$O(n \cdot (O(1) + O(\log n))) = O(n \log n)$



PQ		↙ insert	↘ remove Largest
	heap	$O(\log n)$	$O(\log n)$
	max-tree	$O(h)$	$O(h)$
	unordered linked-list	$O(1)$	$O(n)$
	ordered linked-list	$O(n)$	$O(1)$

max-heap

min-heap