

sorting
selection sort

for $i = 0$ to $len-1$

(a) find the minimum index in $a[i], a[i+1], \dots, a[len-1]$

(b) swap $a[\text{min_index}]$ with $a[i]$

swap: $O(n)$

comparison: $O(n^2)$, or $\Theta(n^2)$

space: $O(1)$ ---in-place sorting

time: $O(n^2)$

tournament sort

build a min-winner tree with a

for $i = 0$ to $len-1$

(a) find the minimum index in $a[i], a[i+1], \dots, a[len-1]$
with the min-winner tree

(b) swap $a[\text{min_index}]$ with $a[i]$

(c) update leaf min_index and leaf i in the winner tree

time: $O(n \log n)$

space: $O(n)$

bubble sort

```
for(i=0;i<len;i++){
  changed = 0;
  for(j=1;j<len-i;j++){
    if (arr[j] < arr[j-1]){
      changed = 1;
      swap(arr+j, arr+j-1);
    }
  }
  if (changed == 0)
    break;
}
```

time: $O(n^2)$ in comparison, $O(n^2)$ in swap

space: $O(1)$ ---in-place

can early stop ($changed == 0$) when a ordered

insertion sort

for $i = 0$ to $len-1$

(a) pick card $a[i]$

(b) insert $a[i]$ into $a[0], a[1], \dots, a[i-1]$

time: $O(n^2)$

space: $O(1)$

can be fast when a almost ordered

usually,

insertion better than bubble;

selection better than bubble;

insertion faster than selection in practice

winner tree

```
      1
     / \
    1   2
   / \ / \
  5  1 4  2
 / \ / \ / \
5 7 1 3 4 6 8 2
```

merge tree

```
(1, 2, 3, 4, 5, 6, 7, 8): O(n) time
(1, 3, 5, 7) (2, 4, 6, 8): O(n) time
(5, 7) (1, 3) (4, 6) (2, 8): O(n) time
5 7 1 3 4 6 8 2
```

merge sort

(a) build a merge tree from a

(b) output the root

space: $O(n \log n)$,

can go down to $O(n)$

[hard to go down to $O(1)$]

time: $O(n \log n)$

heapsort

modify a to a max-heap

for $i = 0$ to $\text{len}-1$

(a) $\text{max_index} = 0$ because of max-heap

(b) swap $a[\text{max_index}]$ with $a[\text{len}-i-1]$

(c) heapify $a[\text{max_index}]$ (maintain)

space: $O(1)$

time: $O(n \log n)$ for modify, $O(n \log n)$ for maintain