

# Image warping/morphing

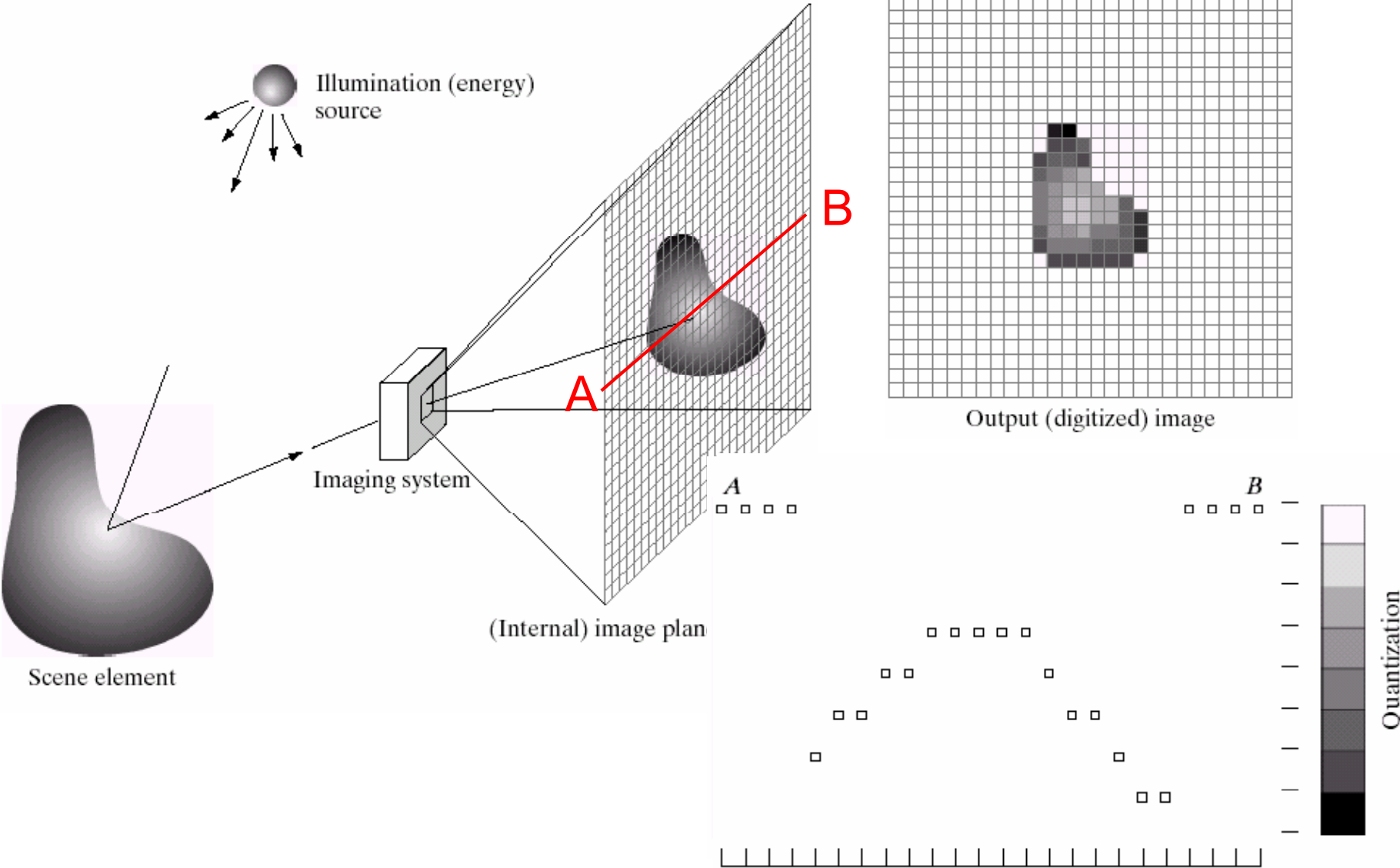
Digital Visual Effects

*Yung-Yu Chuang*

*with slides by Richard Szeliski, Steve Seitz, Tom Funkhouser and Alexei Efros*

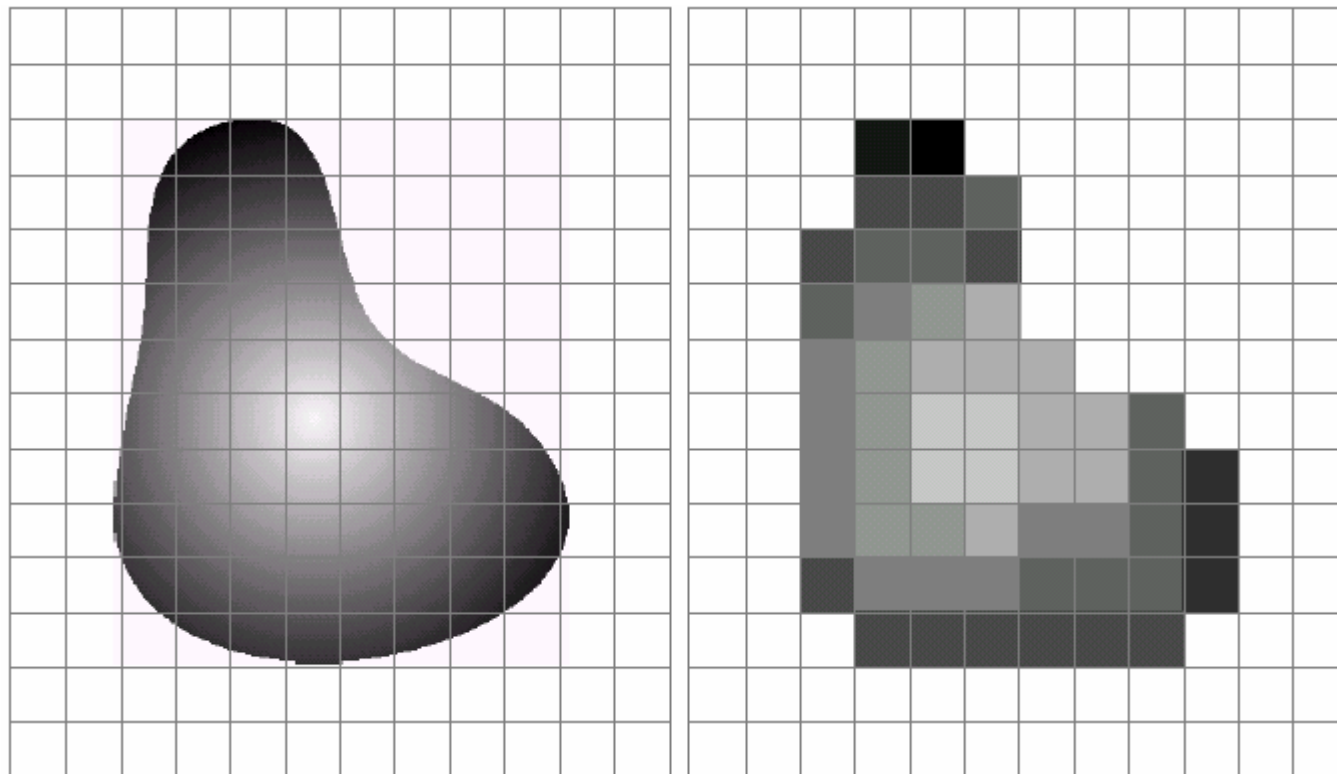
# Image warping

# Image formation



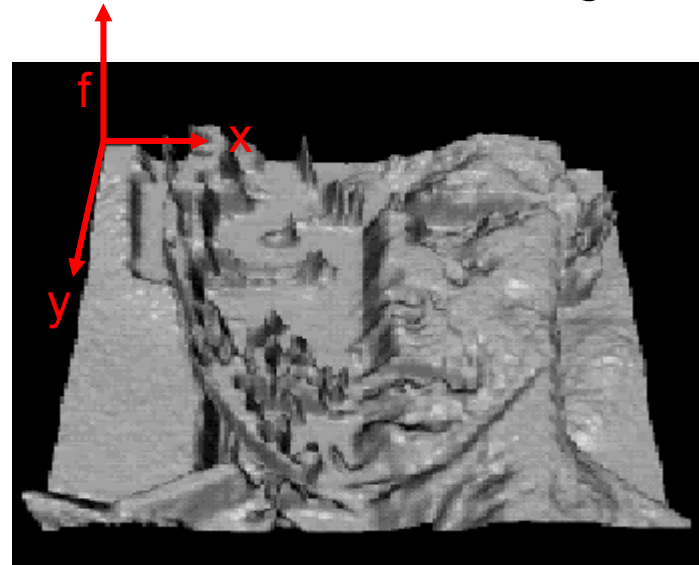
# Sampling and quantization

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# What is an image

- We can think of an image as a function,  $f: \mathbb{R}^2 \rightarrow \mathbb{R}$ :
  - $f(x, y)$  gives the intensity at position  $(x, y)$
  - defined over a rectangle, with a finite range:
    - $f: [a, b] \times [c, d] \rightarrow [0, 1]$



- A color image

$$f(x, y) = \begin{bmatrix} r(x, y) \\ g(x, y) \\ b(x, y) \end{bmatrix}$$

# A digital image

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- We usually operate on **digital (discrete)** images:
  - Sample the 2D space on a regular grid
  - Quantize each sample (round to nearest integer)
- If our samples are  $D$  apart, we can write this as:

$$f[i, j] = \text{Quantize}\{ f(i D, j D) \}$$

- The image can now be represented as a matrix of integer values

$j \longrightarrow$

$i \downarrow$	62	79	23	119	120	105	4	0
	10	10	9	62	12	78	34	0
	10	58	197	46	46	0	0	48
	176	135	5	188	191	68	0	49
	2	1	1	29	26	37	0	77
	0	89	144	147	187	102	62	208
	255	252	0	166	123	62	0	31
	166	63	127	17	1	0	99	30

# Image warping

image filtering: change *range* of image

$$g(x) = h(f(x))$$

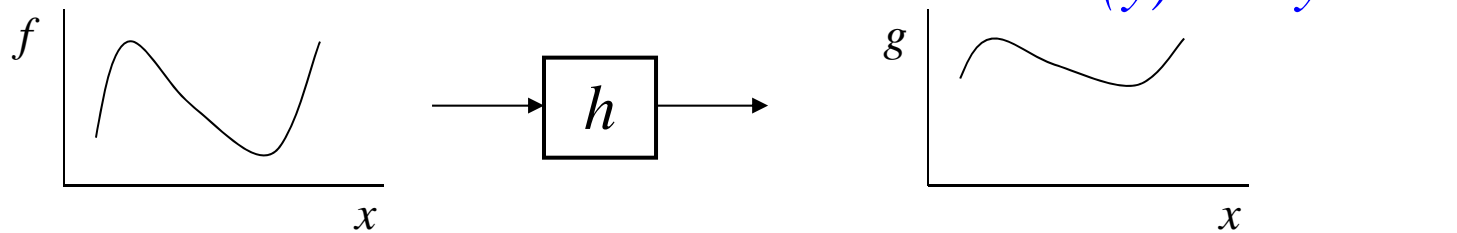
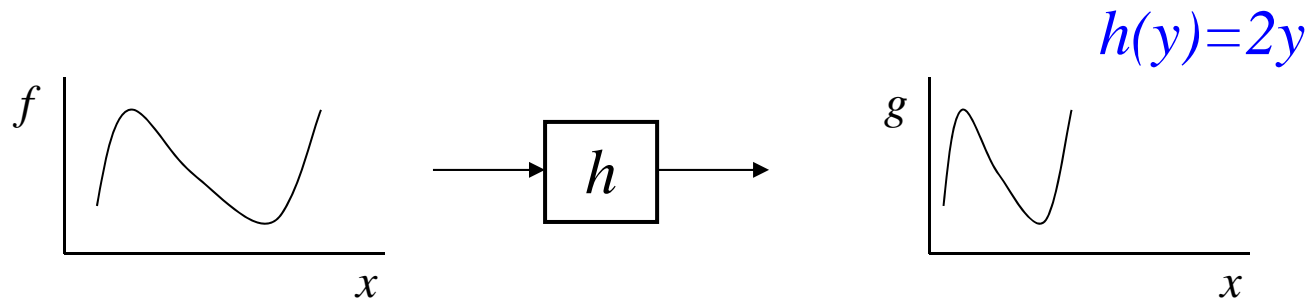


image warping: change *domain* of image

$$g(x) = f(h(x))$$



# Image warping

image filtering: change *range* of image

$$g(x) = h(f(x))$$

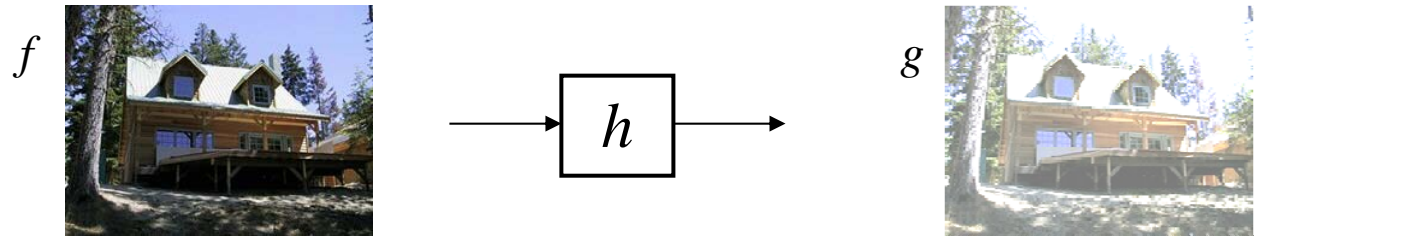
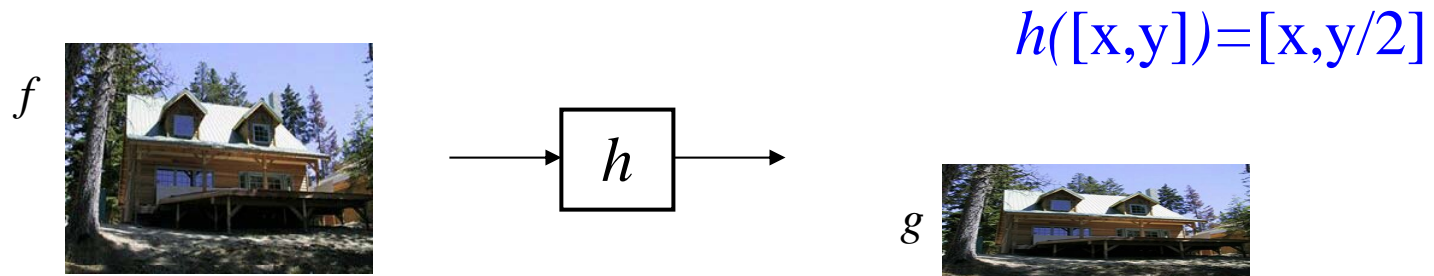


image warping: change *domain* of image

$$g(x) = f(h(x))$$





# Parametric (global) warping

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Examples of parametric warps:



translation



rotation



aspect



affine



perspective

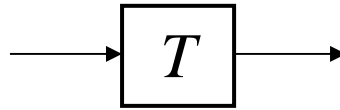


cylindrical

# Parametric (global) warping



$$\mathbf{p} = (x, y)$$

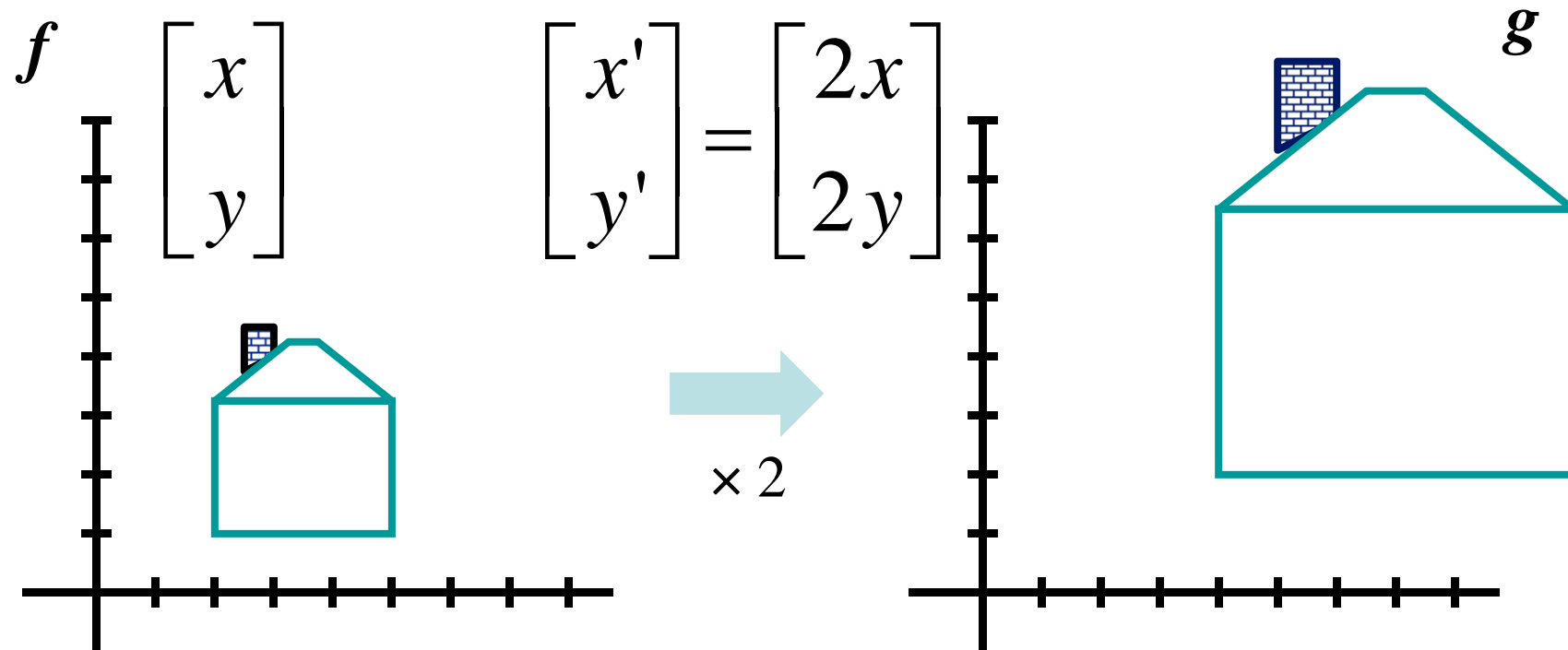


$$\mathbf{p}' = (x', y')$$

- Transformation  $T$  is a coordinate-changing machine:  $\mathbf{p}' = T(\mathbf{p})$
- What does it mean that  $T$  is global?
  - Is the same for any point  $\mathbf{p}$
  - can be described by just a few numbers (parameters)
- Represent  $T$  as a matrix:  $\mathbf{p}' = \mathbf{M}^* \mathbf{p}$  
$$\begin{bmatrix} x' \\ y' \end{bmatrix} = \mathbf{M} \begin{bmatrix} x \\ y \end{bmatrix}$$

# Scaling

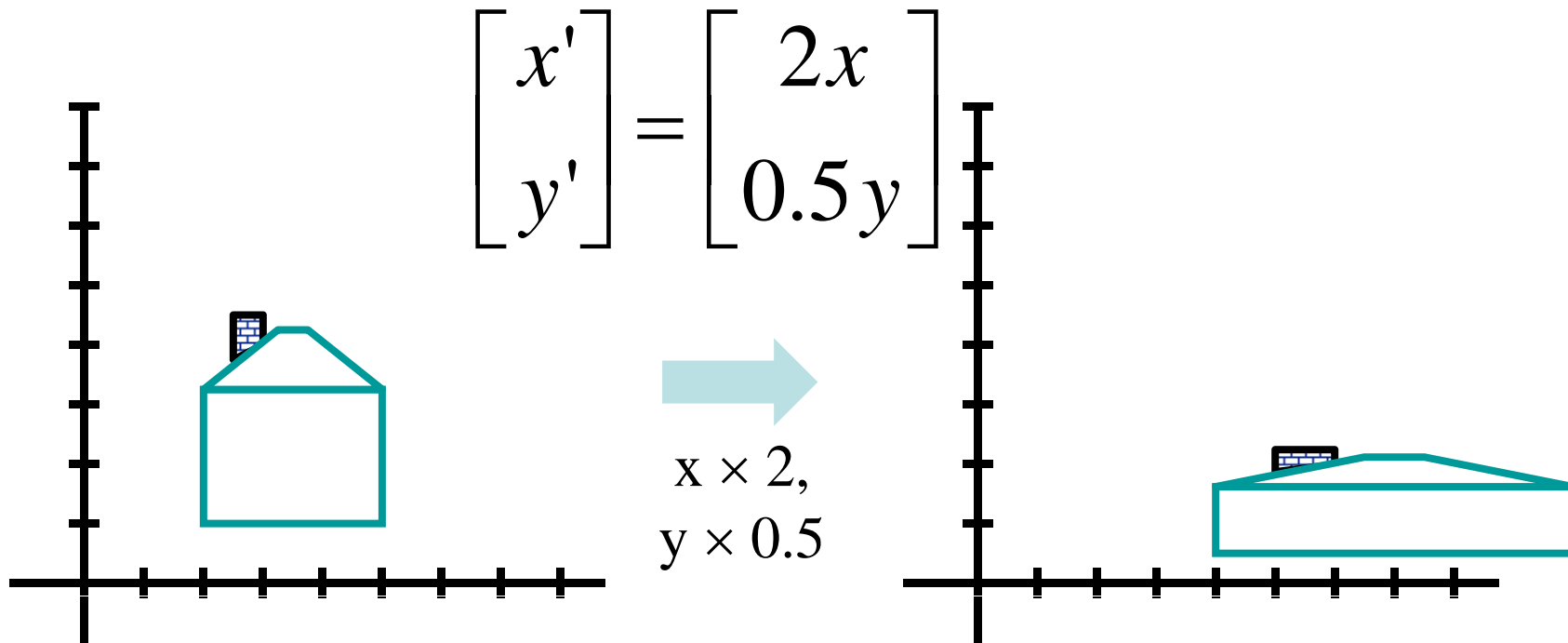
- *Scaling* a coordinate means multiplying each of its components by a scalar
- *Uniform scaling* means this scalar is the same for all components:



# Scaling

- *Non-uniform scaling*: different scalars per component:

$$f\left(\begin{bmatrix} x \\ y \end{bmatrix}\right) = g\left(\begin{bmatrix} x' \\ y' \end{bmatrix}\right)$$



# Scaling

---

- Scaling operation:  $x' = ax$

$$y' = by$$

- Or, in matrix form:

$$\begin{bmatrix} x' \\ y' \end{bmatrix} = \underbrace{\begin{bmatrix} a & 0 \\ 0 & b \end{bmatrix}}_{\text{scaling matrix } S} \begin{bmatrix} x \\ y \end{bmatrix}$$

What's inverse of S?

## 2-D Rotation

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- This is easy to capture in matrix form:

$$\begin{bmatrix} x' \\ y' \end{bmatrix} = \underbrace{\begin{bmatrix} \cos(\theta) & -\sin(\theta) \\ \sin(\theta) & \cos(\theta) \end{bmatrix}}_{\mathbf{R}} \begin{bmatrix} x \\ y \end{bmatrix}$$

- Even though  $\sin(\theta)$  and  $\cos(\theta)$  are nonlinear to  $\theta$ ,
  - $x'$  is a linear combination of  $x$  and  $y$
  - $y'$  is a linear combination of  $x$  and  $y$
- What is the inverse transformation?
  - Rotation by  $-\theta$
  - For rotation matrices,  $\det(\mathbf{R}) = 1$  so  $\mathbf{R}^{-1} = \mathbf{R}^T$

# 2x2 Matrices

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- What types of transformations can be represented with a 2x2 matrix?

## 2D Identity?

$$\begin{aligned}x' &= x \\ y' &= y\end{aligned} \quad \begin{bmatrix} x' \\ y' \end{bmatrix} = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix}$$

## 2D Scale around (0,0)?

$$\begin{aligned}\mathbf{x}' &= s_x * \mathbf{x} \\ \mathbf{y}' &= s_y * \mathbf{y}\end{aligned} \quad \begin{bmatrix} \mathbf{x}' \\ \mathbf{y}' \end{bmatrix} = \begin{bmatrix} s_x & 0 \\ 0 & s_y \end{bmatrix} \begin{bmatrix} \mathbf{x} \\ \mathbf{y} \end{bmatrix}$$

# 2x2 Matrices

---

- What types of transformations can be represented with a 2x2 matrix?

## 2D Rotate around (0,0)?

$$x' = \cos \theta * x - \sin \theta * y$$

$$y' = \sin \theta * x + \cos \theta * y$$

$$\begin{bmatrix} x' \\ y' \end{bmatrix} = \begin{bmatrix} \cos \theta & -\sin \theta \\ \sin \theta & \cos \theta \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix}$$

## 2D Shear?

$$x' = x + sh_x * y$$

$$y' = sh_y * x + y$$

$$\begin{bmatrix} x' \\ y' \end{bmatrix} = \begin{bmatrix} 1 & sh_x \\ sh_y & 1 \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix}$$



# 2x2 Matrices

---

- What types of transformations can be represented with a 2x2 matrix?

2D Mirror about Y axis?

$$\begin{aligned}x' &= -x \\ y' &= y\end{aligned}\quad \begin{bmatrix} x' \\ y' \end{bmatrix} = \begin{bmatrix} -1 & 0 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix}$$

2D Mirror over (0,0)?

$$\begin{aligned}x' &= -x \\ y' &= -y\end{aligned}\quad \begin{bmatrix} x' \\ y' \end{bmatrix} = \begin{bmatrix} -1 & 0 \\ 0 & -1 \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix}$$

# All 2D Linear Transformations

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- Linear transformations are combinations of ...
  - Scale,
  - Rotation,
  - Shear, and
  - Mirror
- Properties of linear transformations:
  - Origin maps to origin
  - Lines map to lines
  - Parallel lines remain parallel
  - Ratios are preserved
  - Closed under composition

$$\begin{bmatrix} x' \\ y' \end{bmatrix} = \begin{bmatrix} a & b \\ c & d \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix}$$

# 2x2 Matrices

---

- What types of transformations can **not** be represented with a 2x2 matrix?

2D Translation?

$$x' = x + t_x \quad \text{NO!}$$

$$y' = y + t_y$$

Only linear 2D transformations  
can be represented with a 2x2 matrix

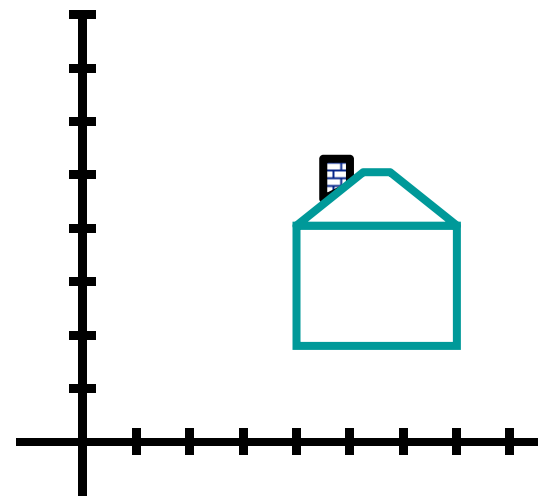
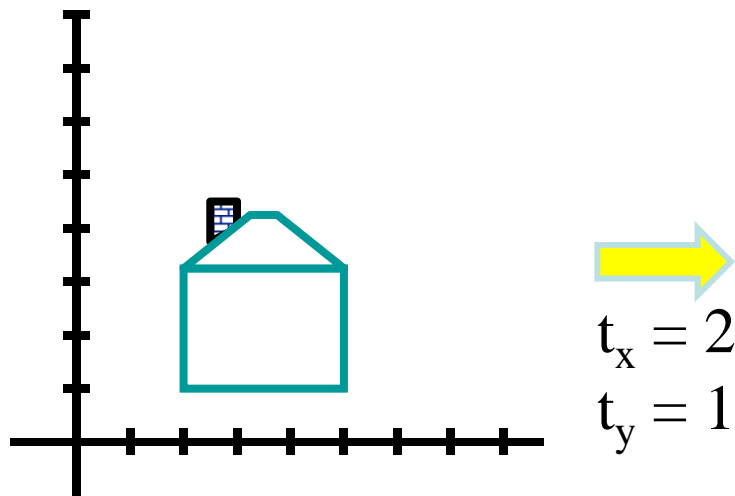
# Translation

- Example of translation

Homogeneous Coordinates



$$\begin{bmatrix} x' \\ y' \\ 1 \end{bmatrix} = \begin{bmatrix} 1 & 0 & t_x \\ 0 & 1 & t_y \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ 1 \end{bmatrix} = \begin{bmatrix} x + t_x \\ y + t_y \\ 1 \end{bmatrix}$$



# Affine Transformations

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- Affine transformations are combinations of ...
  - Linear transformations, and
  - Translations
- Properties of affine transformations:
  - Origin does not necessarily map to origin
  - Lines map to lines
  - Parallel lines remain parallel
  - Ratios are preserved
  - Closed under composition
  - Models change of basis

$$\begin{bmatrix} x' \\ y' \\ w \end{bmatrix} = \begin{bmatrix} a & b & c \\ d & e & f \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ w \end{bmatrix}$$

# Projective Transformations

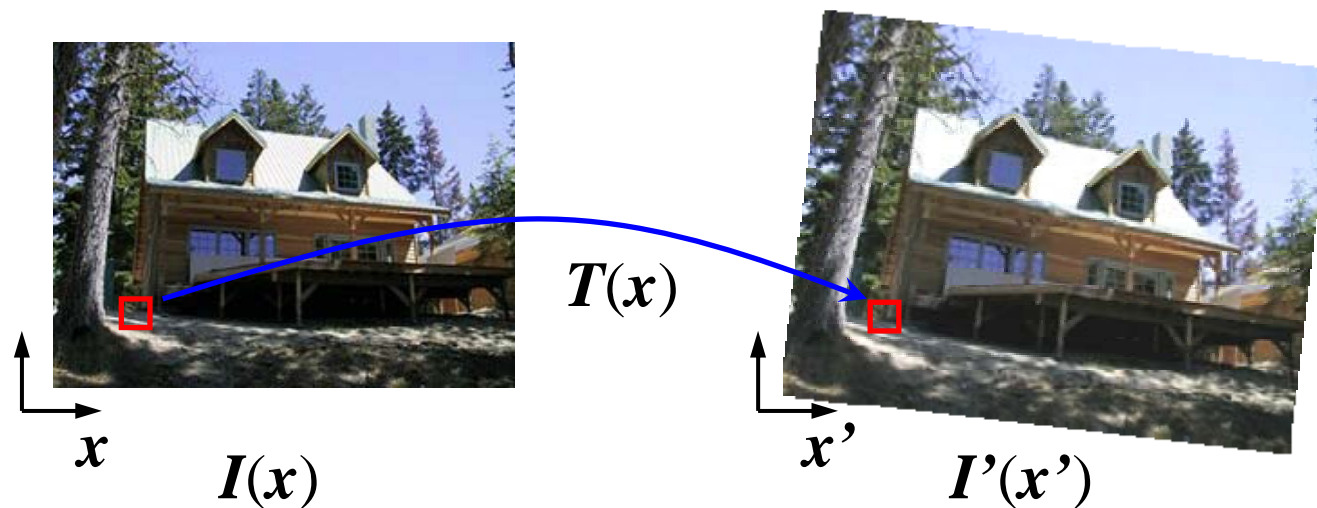
---

- Projective transformations ...
  - Affine transformations, and
  - Projective warps
- Properties of projective transformations:
  - Origin does not necessarily map to origin
  - Lines map to lines
  - Parallel lines do not necessarily remain parallel
  - Ratios are not preserved
  - Closed under composition
  - Models change of basis

$$\begin{bmatrix} x' \\ y' \\ w' \end{bmatrix} = \begin{bmatrix} a & b & c \\ d & e & f \\ g & h & i \end{bmatrix} \begin{bmatrix} x \\ y \\ w \end{bmatrix}$$

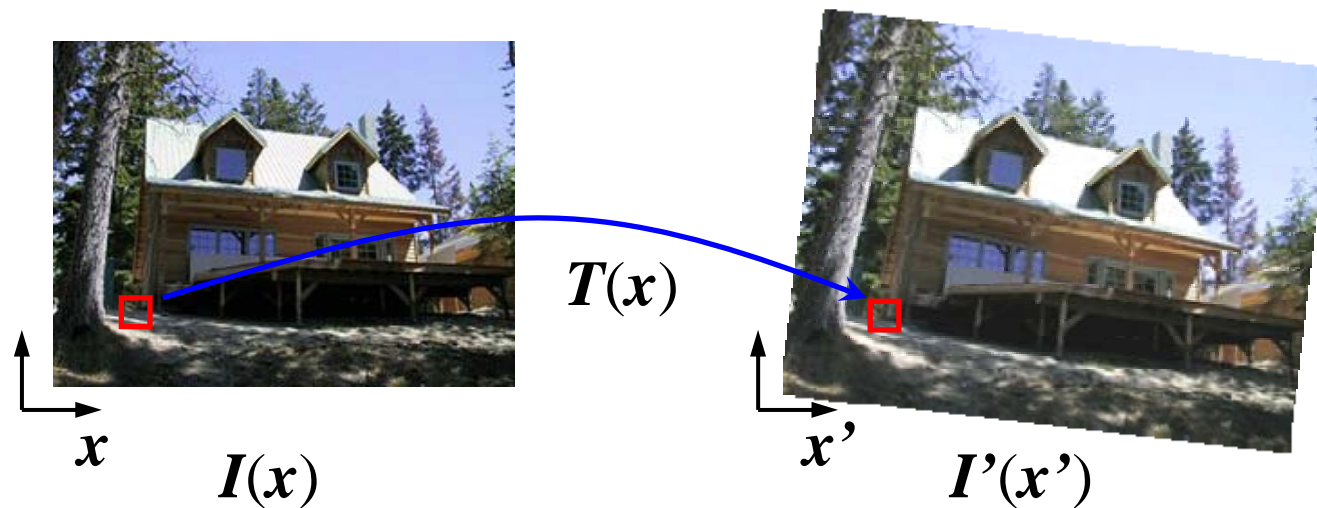
# Image warping

- Given a coordinate transform  $x' = T(x)$  and a source image  $I(x)$ , how do we compute a transformed image  $I'(x') = I(T(x))$ ?



# Forward warping

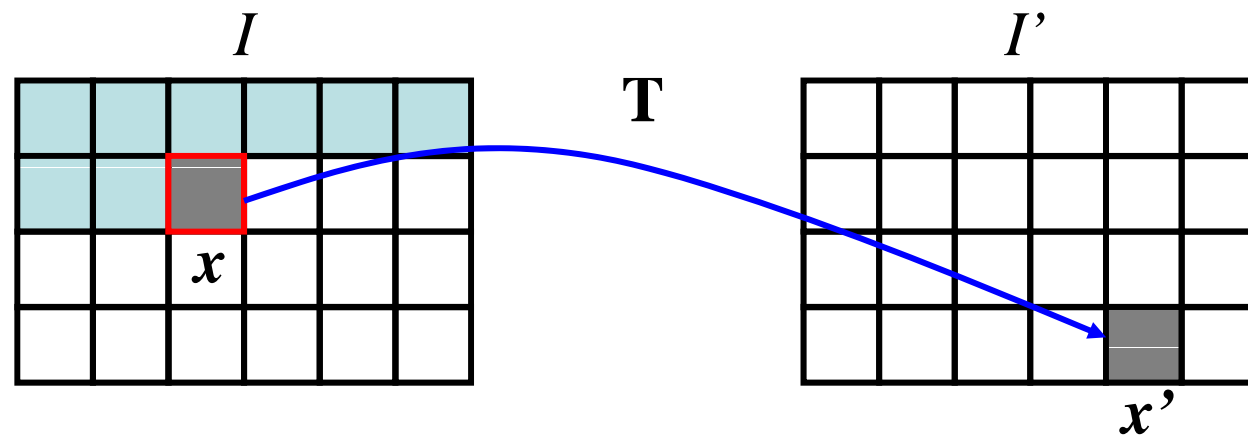
- Send each pixel  $I(x)$  to its corresponding location  $x' = T(x)$  in  $I'(x')$





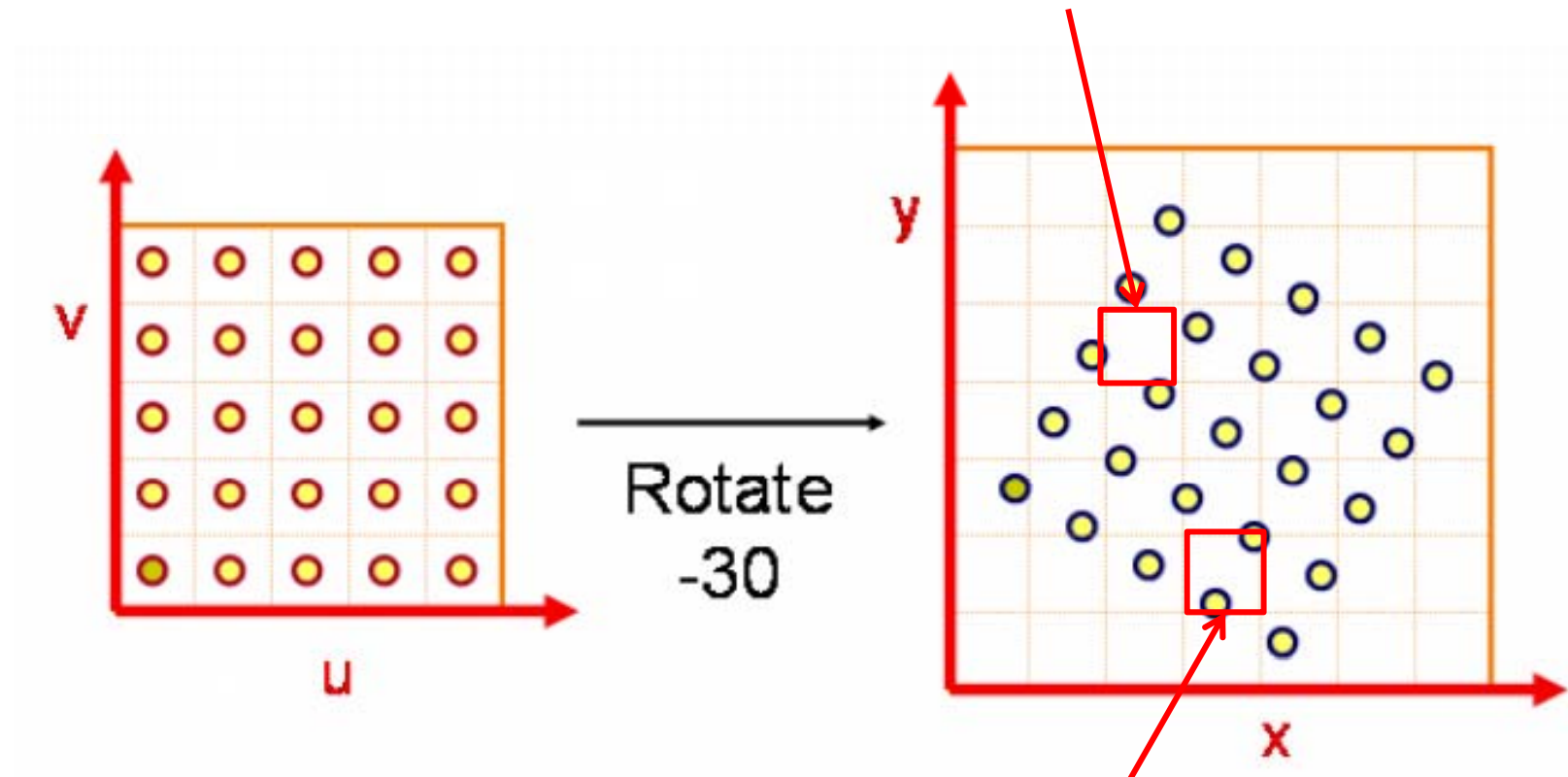
# Forward warping

```
fwarp(I, I', T)
{
  for (y=0; y<I.height; y++)
    for (x=0; x<I.width; x++) {
      (x',y')=T(x,y);
      I'(x',y')=I(x,y);
    }
}
```



# Forward warping

Some destination may  
not be covered

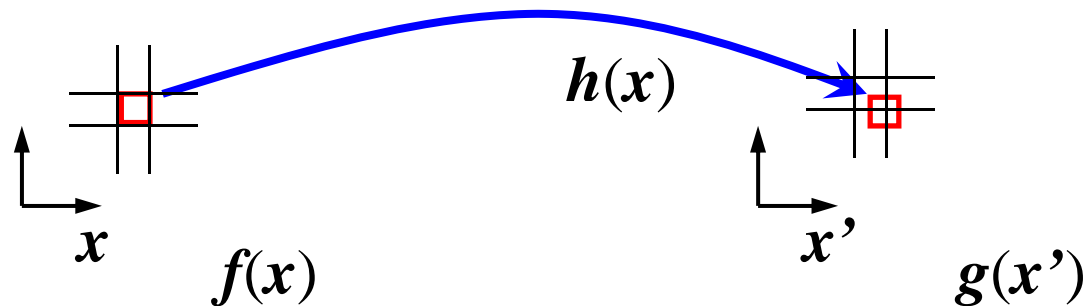


Many source pixels could map  
to the same destination

# Forward warping

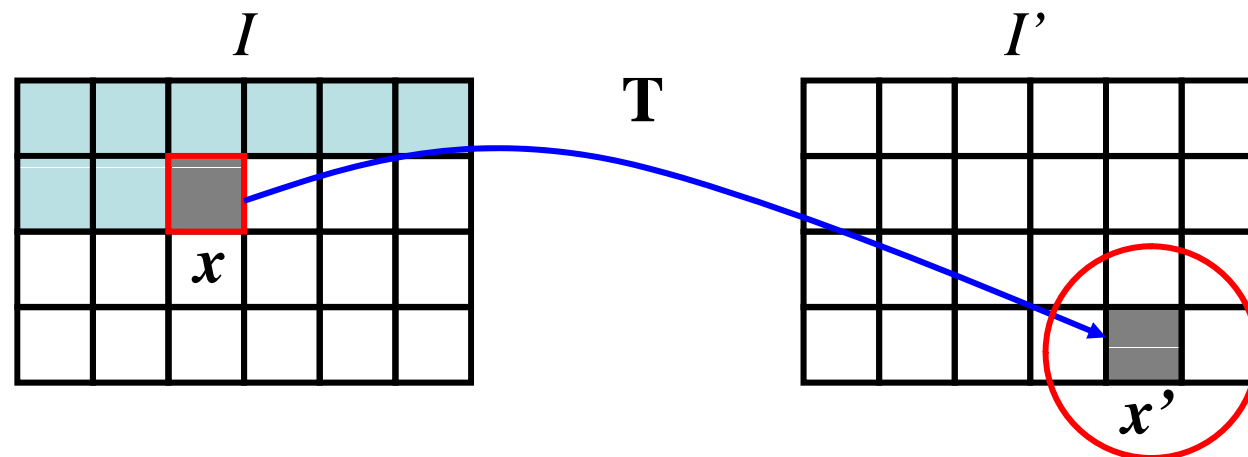
---

- Send each pixel  $I(x)$  to its corresponding location  $x' = T(x)$  in  $I'(x')$
- What if pixel lands “between” two pixels?
- Will be there holes?
- Answer: add “contribution” to several pixels, normalize later (*splatting*)



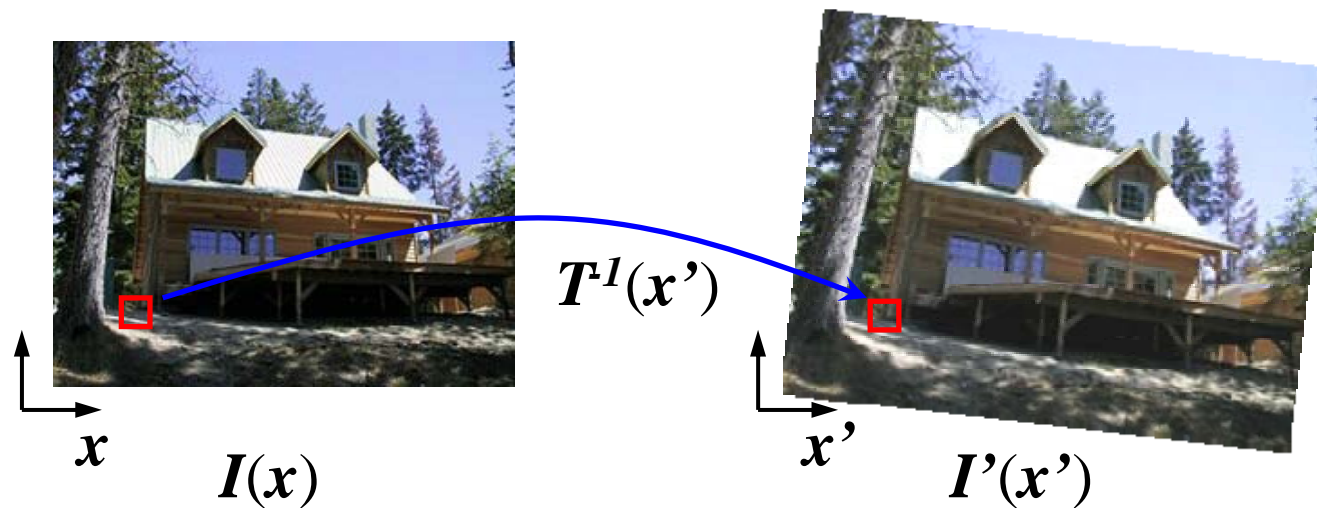
# Forward warping

```
fwarp(I, I', T)
{
  for (y=0; y<I.height; y++)
    for (x=0; x<I.width; x++) {
      (x',y')=T(x,y);
      splatting(I',x',y',I(x,y),kernel);
    }
}
```



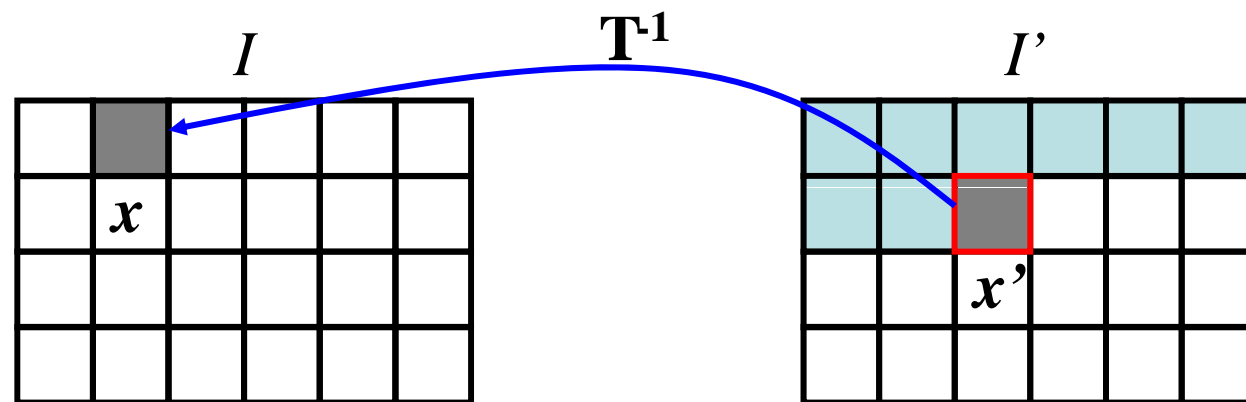
# Inverse warping

- Get each pixel  $I'(x')$  from its corresponding location  $x = T^{-1}(x')$  in  $I(x)$



# Inverse warping

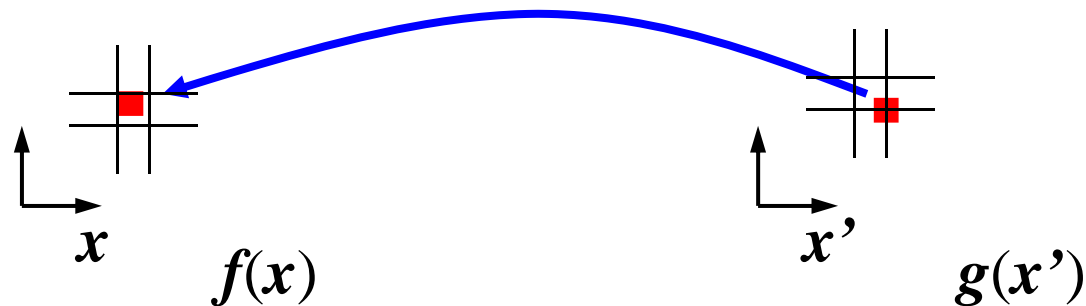
```
iwarp(I, I', T)
{
  for (y=0; y<I'.height; y++)
    for (x=0; x<I'.width; x++) {
      (x,y)=T-1(x',y');
      I'(x',y')=I(x,y);
    }
}
```



# Inverse warping

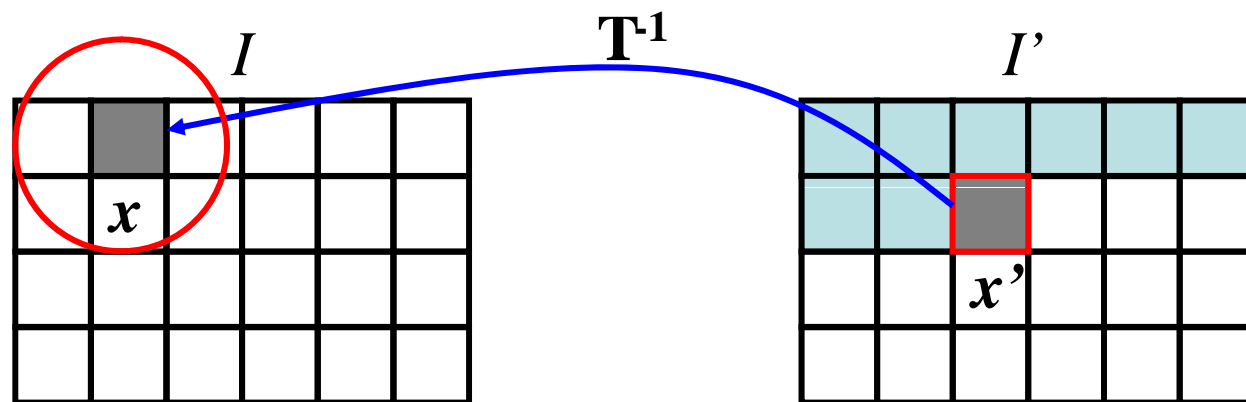
---

- Get each pixel  $I'(x')$  from its corresponding location  $x = T^{-1}(x')$  in  $I(x)$
- What if pixel comes from “between” two pixels?
- Answer: *resample* color value from *interpolated (prefiltered)* source image



# Inverse warping

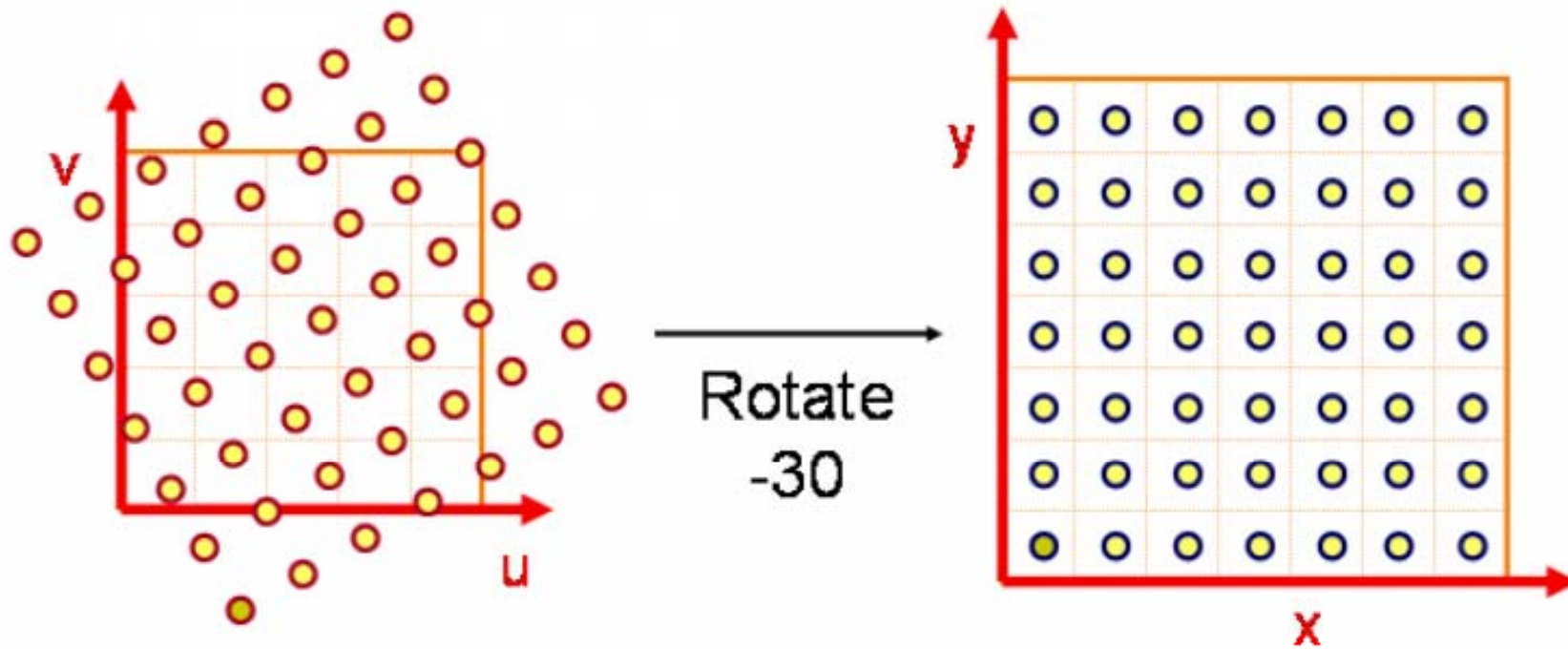
```
iwarp(I, I', T)
{
  for (y=0; y<I'.height; y++)
    for (x=0; x<I'.width; x++) {
      (x,y)=T-1(x',y');
      I'(x',y')=Reconstruct(I,x,y,kernel);
    }
}
```





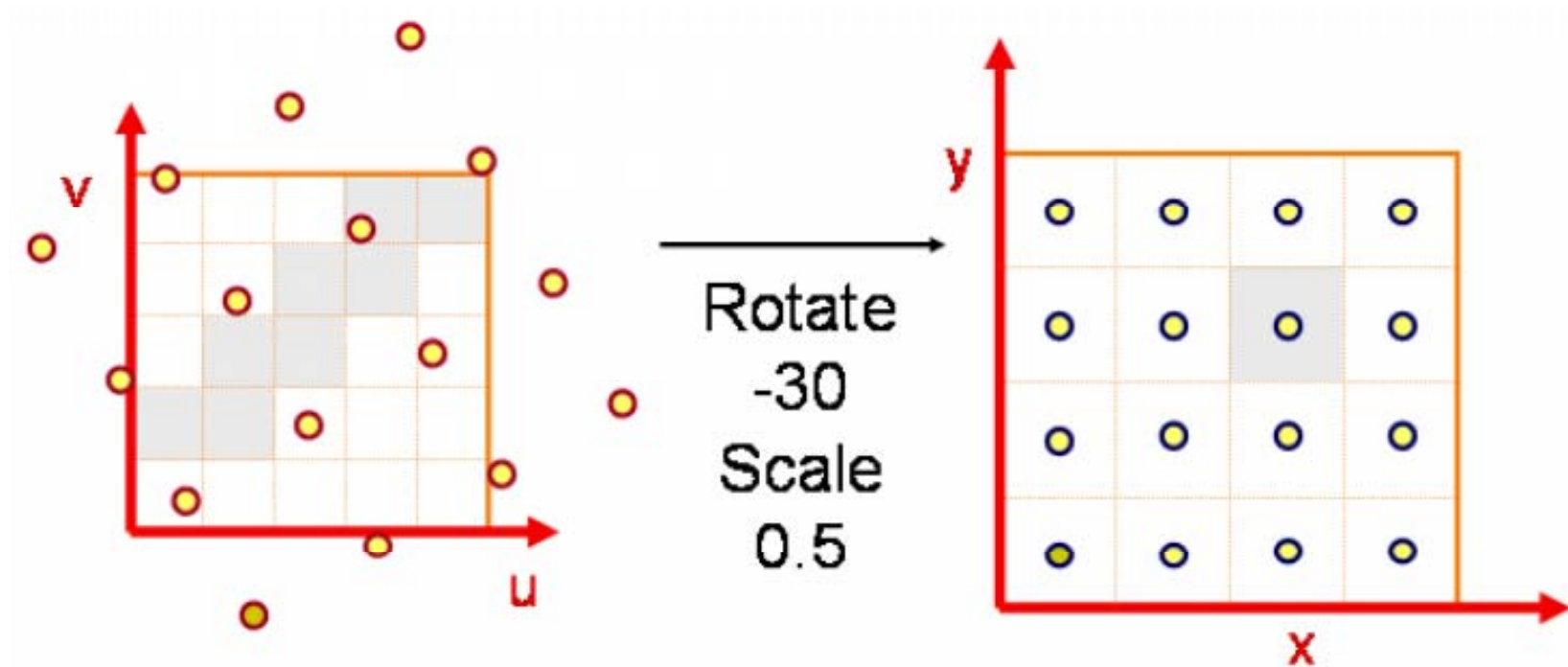
# Inverse warping

- No hole, but must resample
- What value should you take for non-integer coordinate? Closest one?



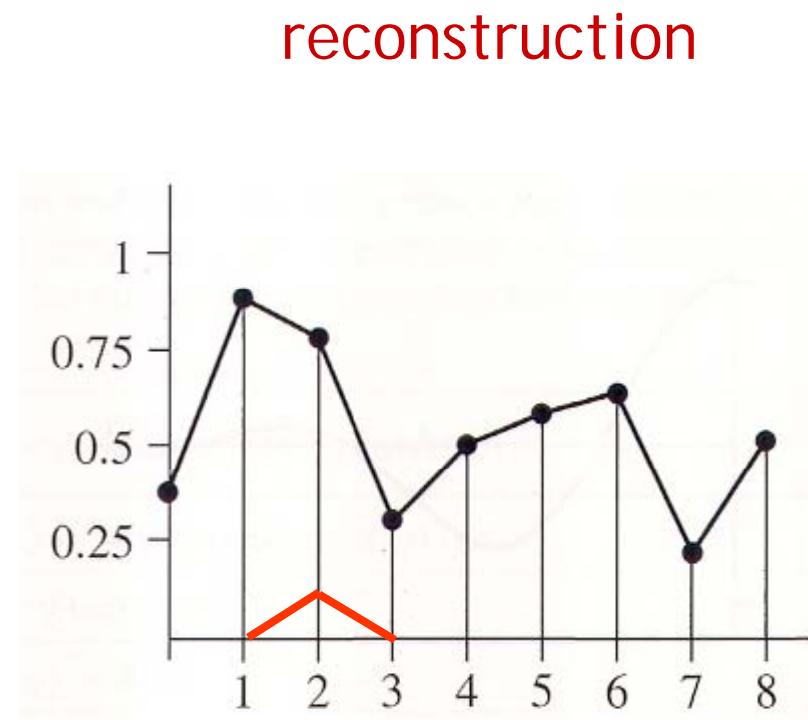
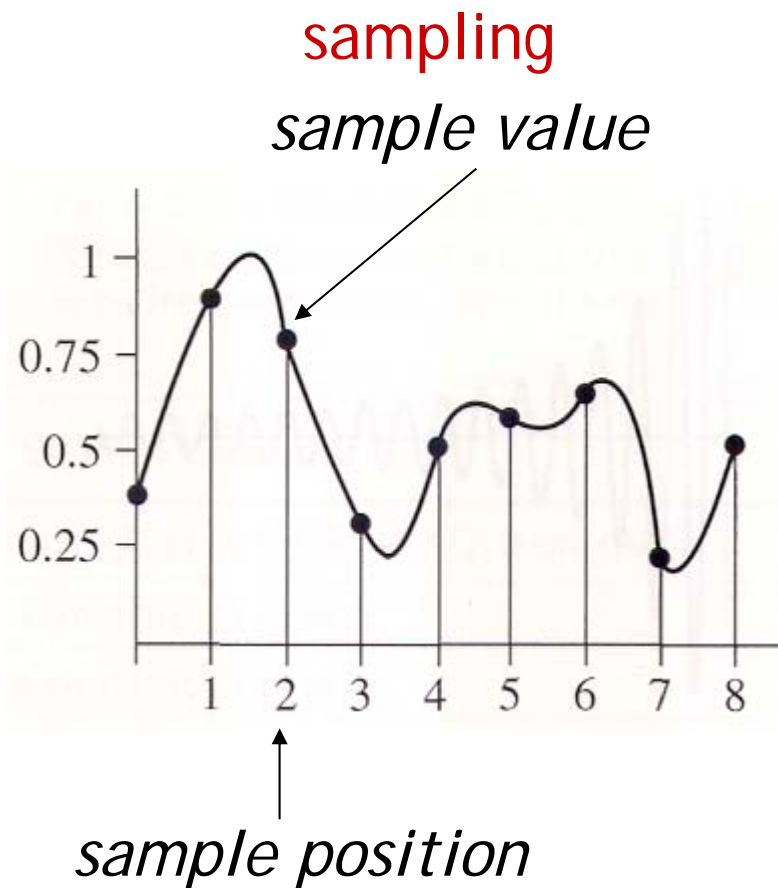
# Inverse warping

- It could cause aliasing



# Reconstruction

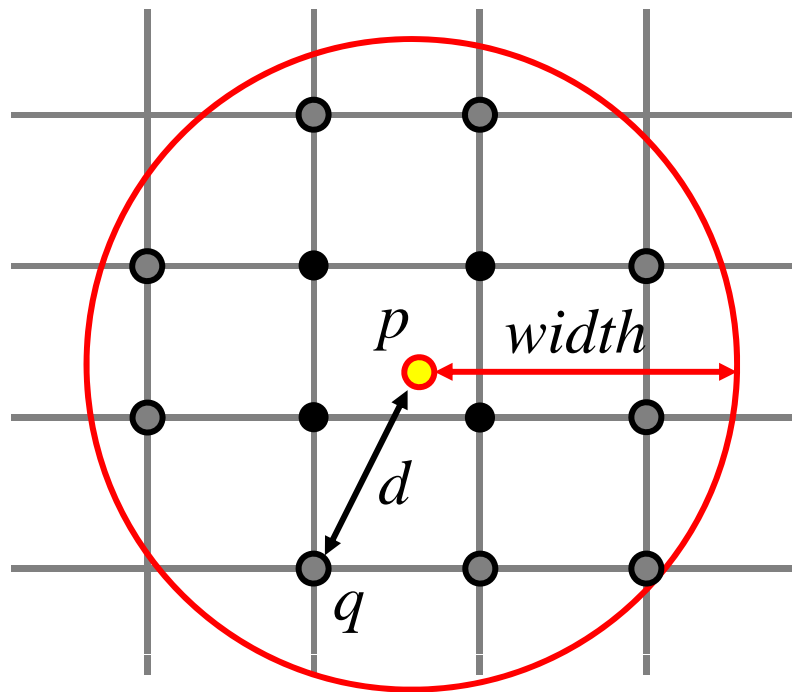
- Reconstruction generates an approximation to the original function. Error is called aliasing.



# Reconstruction

- Computed weighted sum of pixel neighborhood; output is weighted average of input, where weights are normalized values of filter kernel  $k$

$$p = \frac{\sum_i k(q_i)q_i}{\sum_i k(q_i)}$$

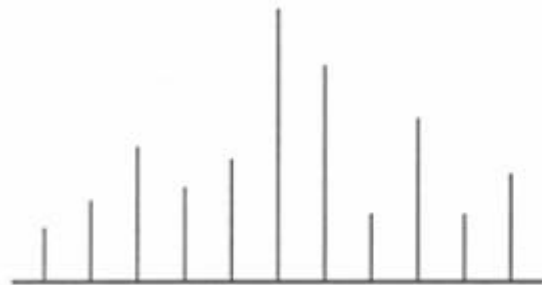


```

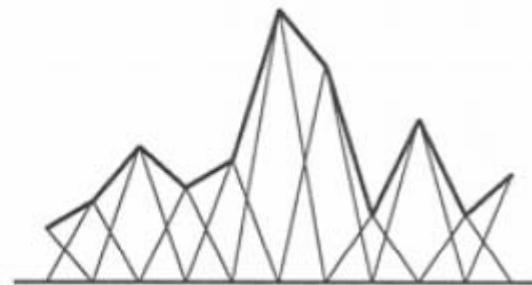
color=0;
weights=0;
for all q's dist < width
  d = dist(p, q);
  w = kernel(d);
  color += w*q.color;
  weights += w;
p.Color = color/weights;

```

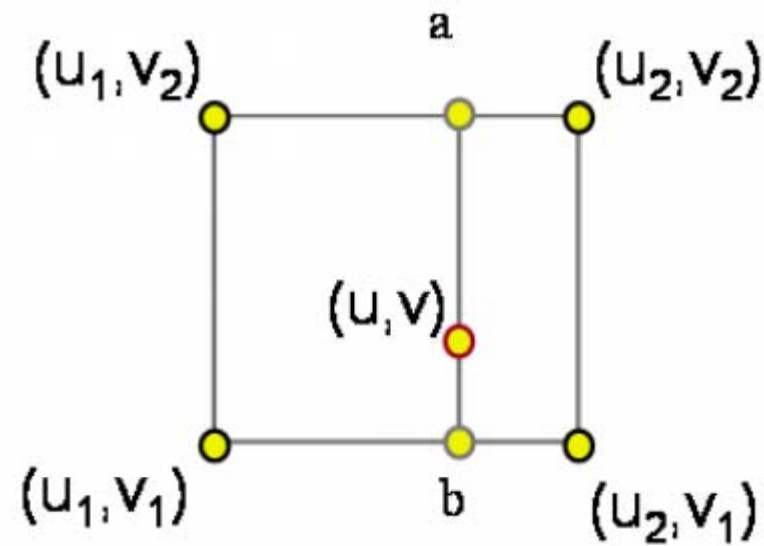
# Triangle filter



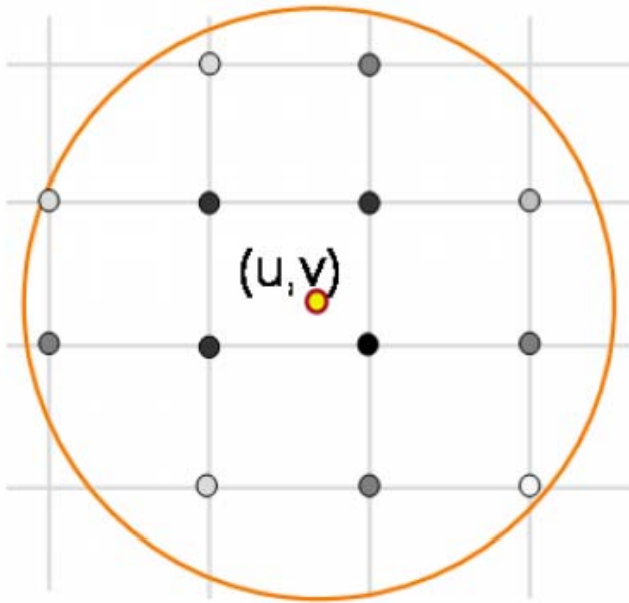
Input



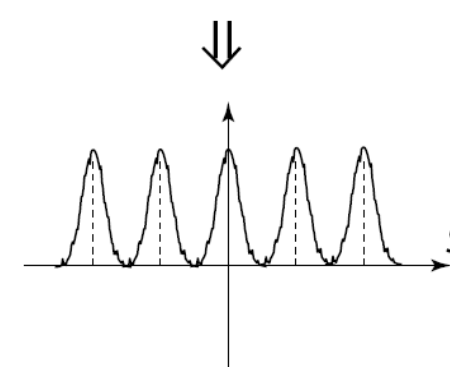
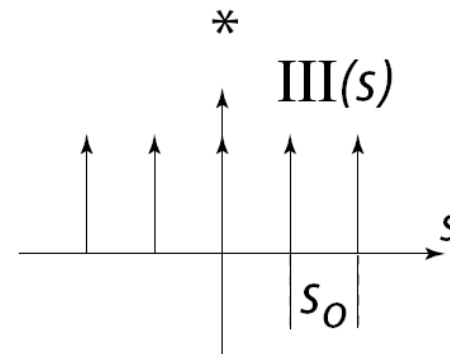
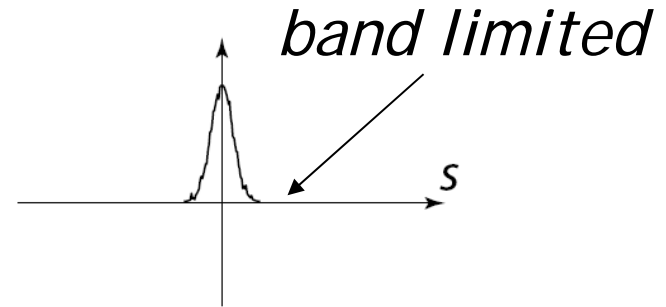
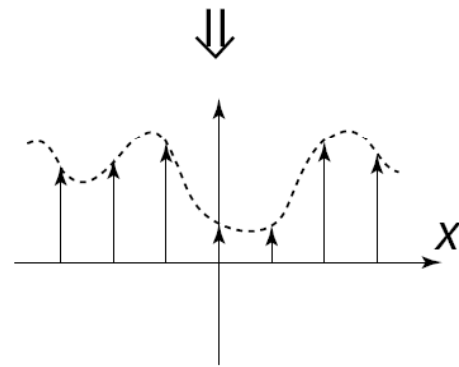
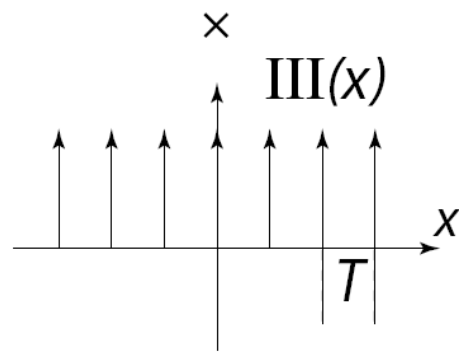
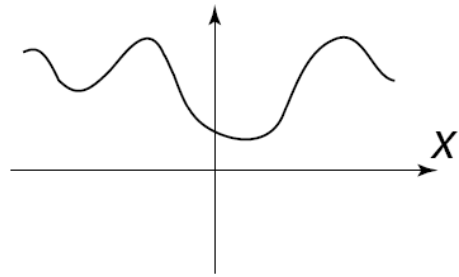
Output



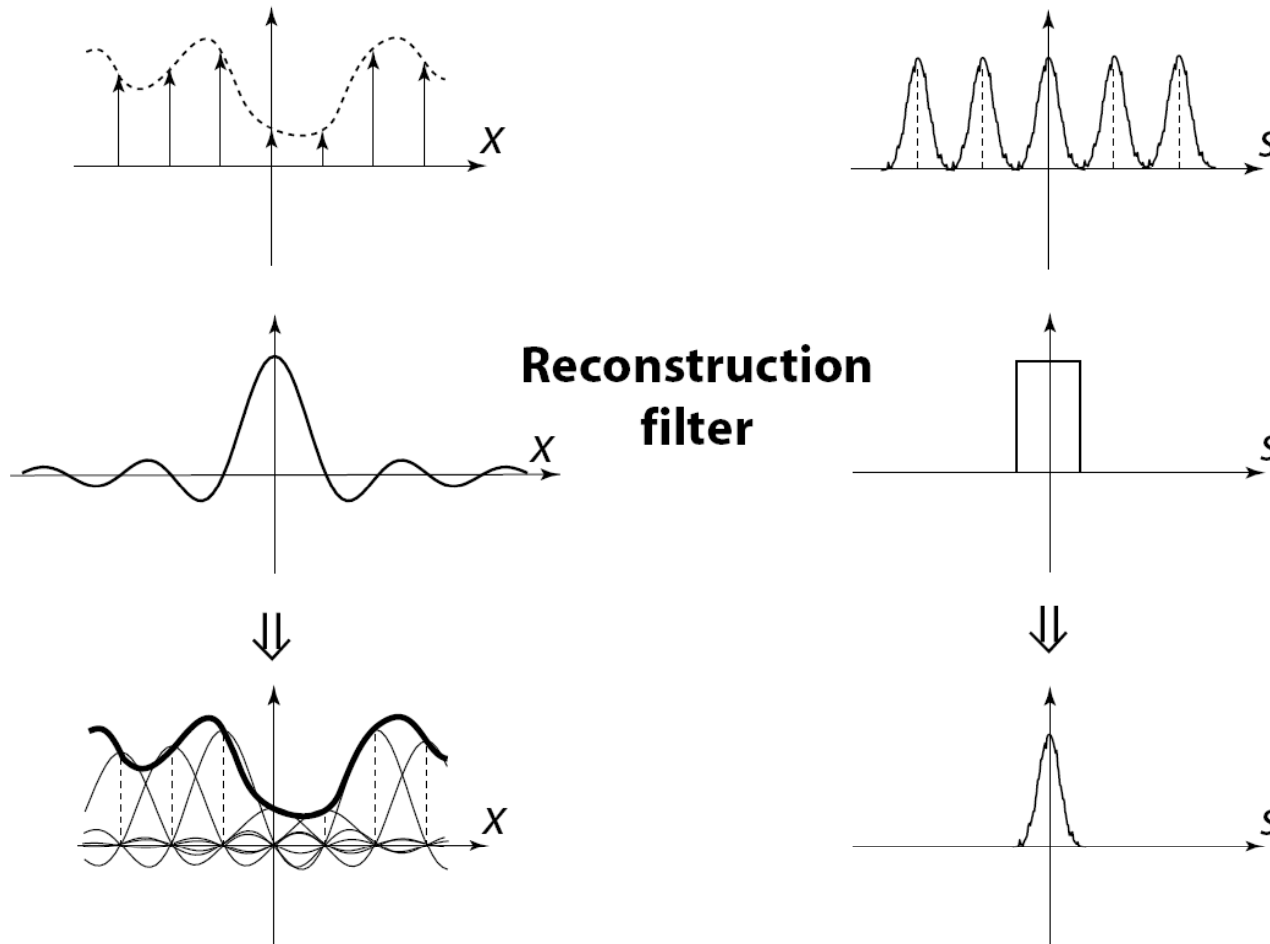
# Gaussian filter



# Sampling



# Reconstruction



*The reconstructed function is obtained by interpolating among the samples in some manner*



# Reconstruction (interpolation)

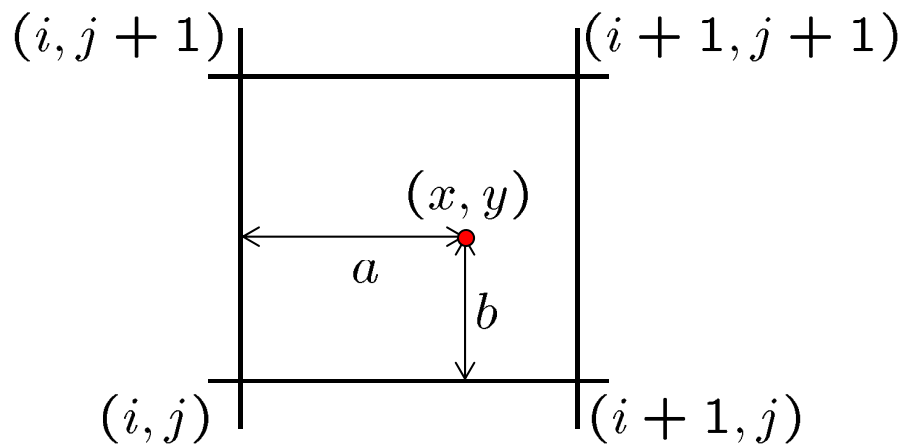
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- Possible reconstruction filters (kernels):
  - nearest neighbor
  - bilinear
  - bicubic
  - sinc (optimal reconstruction)



# Bilinear interpolation (triangle filter)

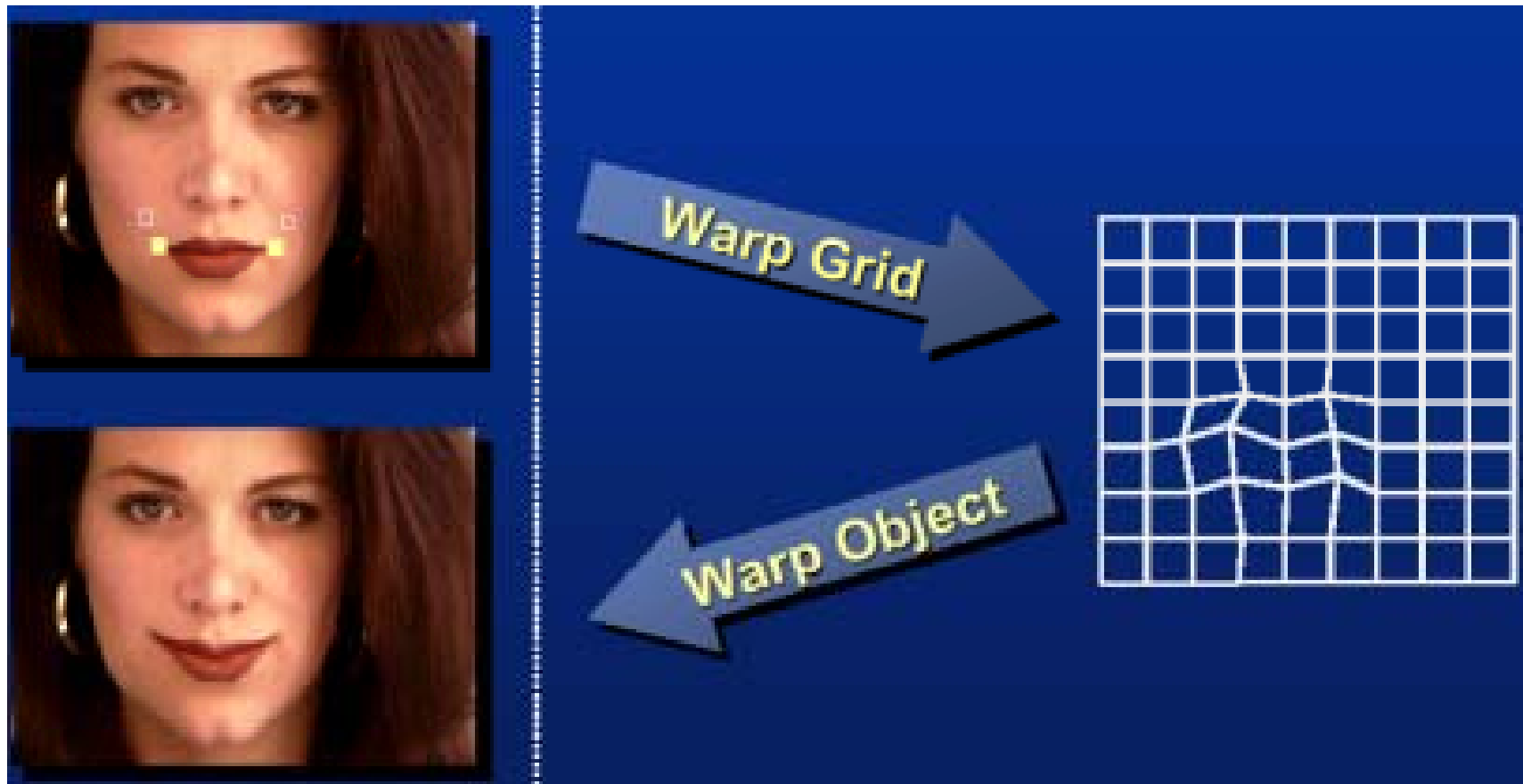
- A simple method for resampling images



$$\begin{aligned} f(x, y) = & (1 - a)(1 - b) f[i, j] \\ & + a(1 - b) f[i + 1, j] \\ & + ab f[i + 1, j + 1] \\ & + (1 - a)b f[i, j + 1] \end{aligned}$$

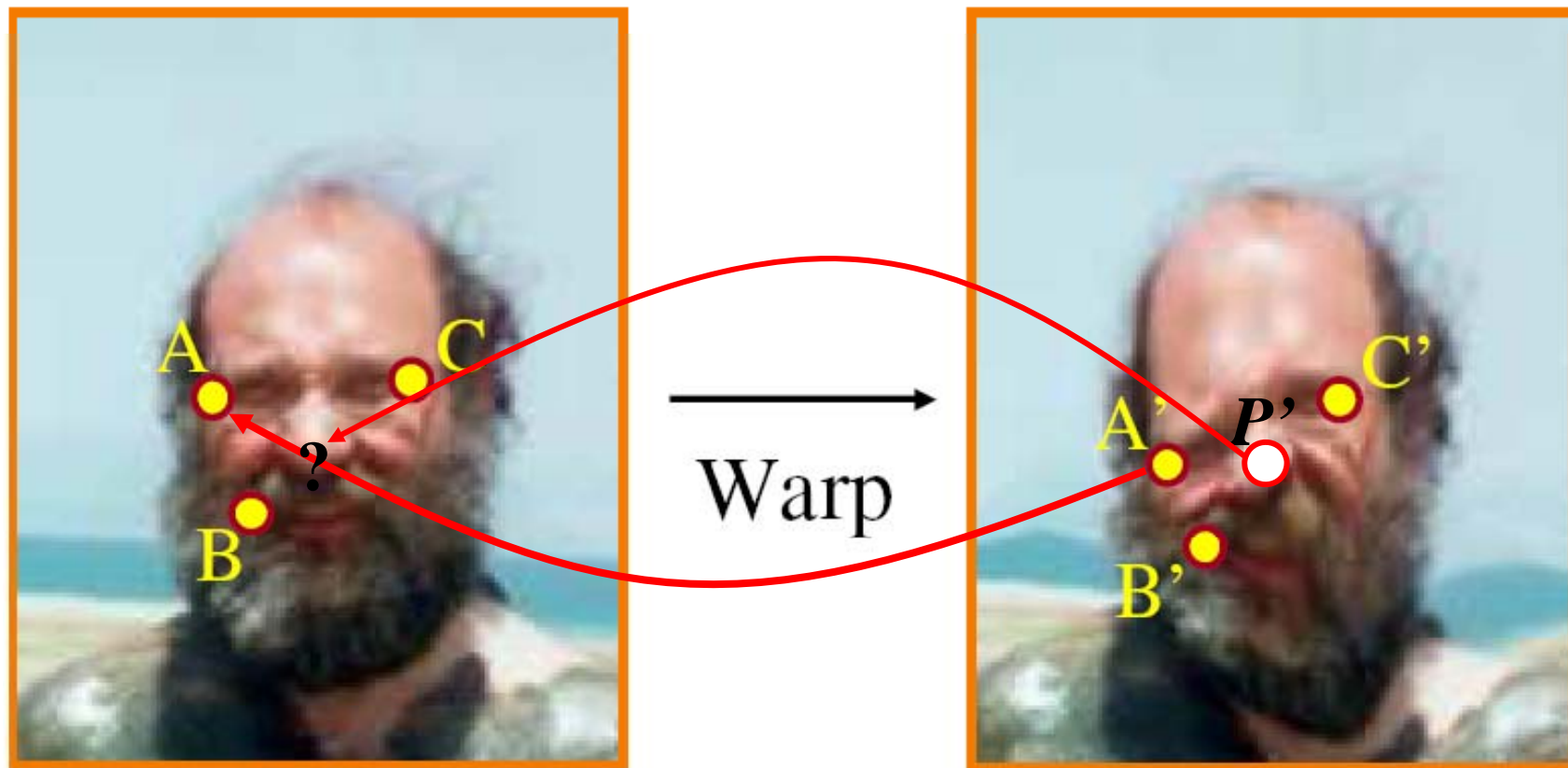
# Non-parametric image warping

- Specify a more detailed warp function
- Splines, meshes, optical flow (per-pixel motion)



# Non-parametric image warping

- Mappings implied by correspondences
- Inverse warping

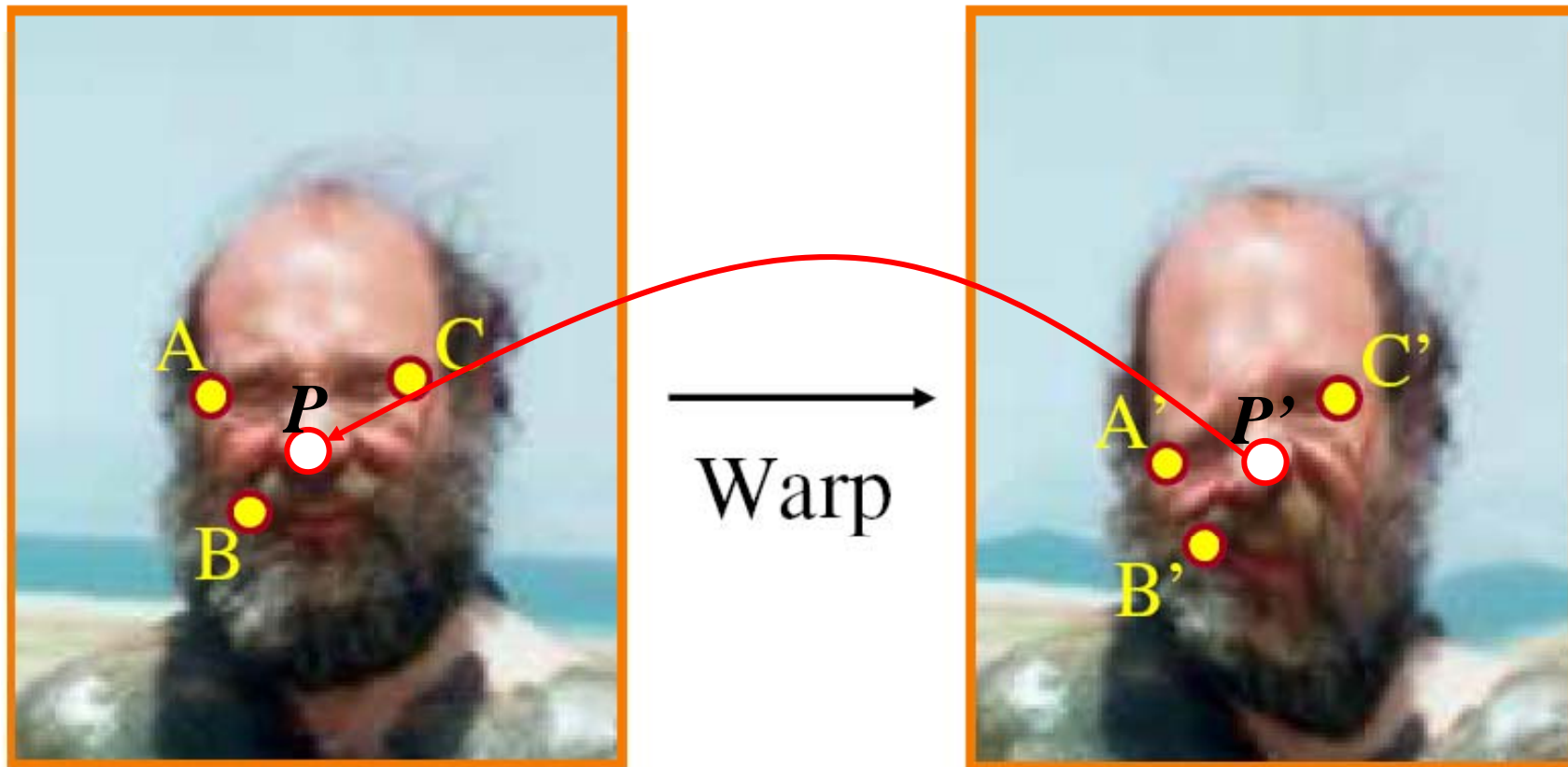


# Non-parametric image warping

$$P = w_A A + w_B B + w_C C$$

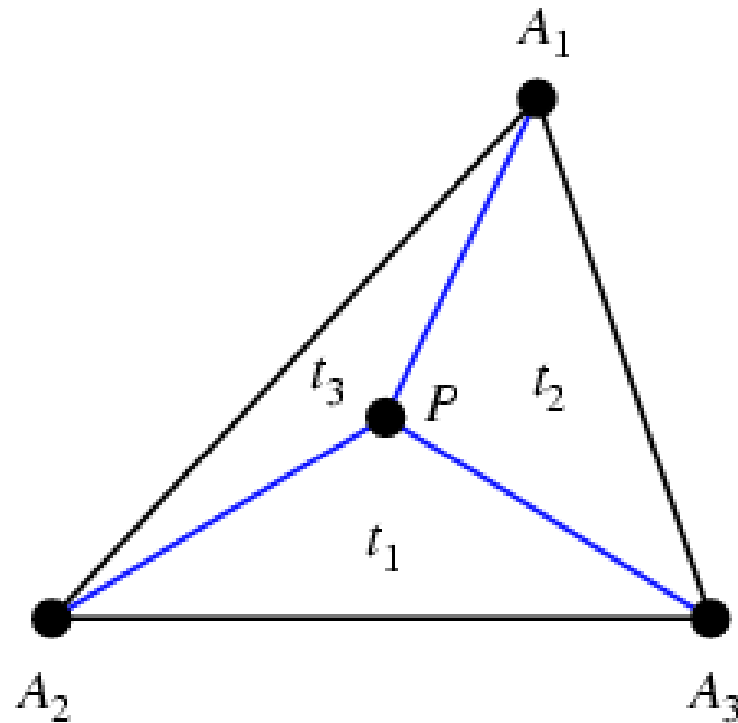
$$P' = w_A A' + w_B B' + w_C C'$$

*Barycentric coordinate*



# Barycentric coordinates

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$$P = t_1 A_1 + t_2 A_2 + t_3 A_3$$

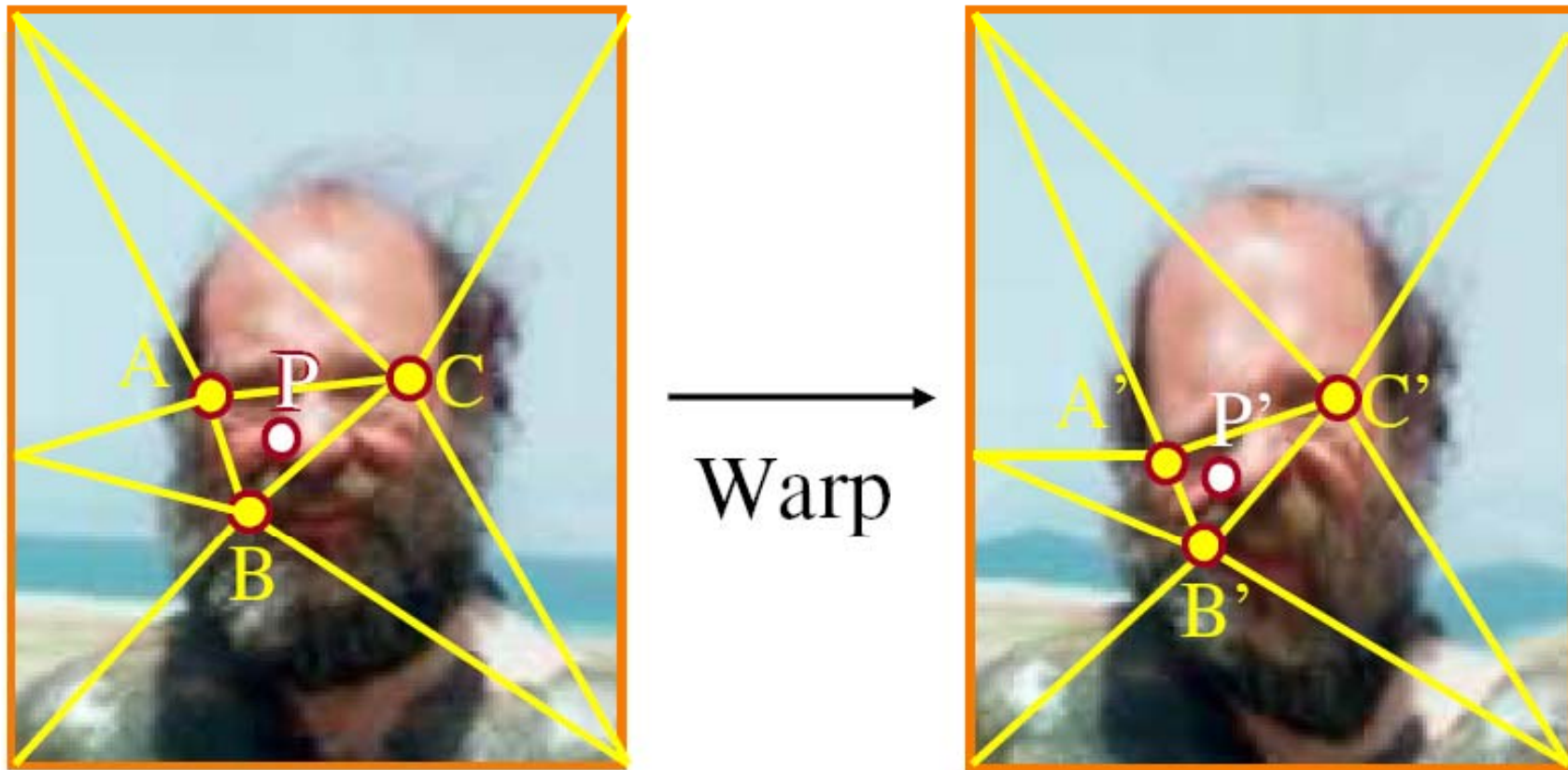
$$t_1 + t_2 + t_3 = 1$$

# Non-parametric image warping

$$P = w_A A + w_B B + w_C C$$

$$P' = w_A A' + w_B B' + w_C C'$$

*Barycentric coordinate*



# Non-parametric image warping

Gaussian  $\rho(r) = e^{-\beta r^2}$   
 thin plate spline  $\rho(r) = r^2 \log(r)$

$$\Delta P = \frac{1}{K} \sum_i k_{X_i}(P') \Delta X_i$$

*radial basis function*



Warp





# Image warping

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- Warping is a useful operation for mosaics, video matching, view interpolation and so on.

**An application of image warping:  
face beautification**

# Data-driven facial beautification

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# Facial beautification

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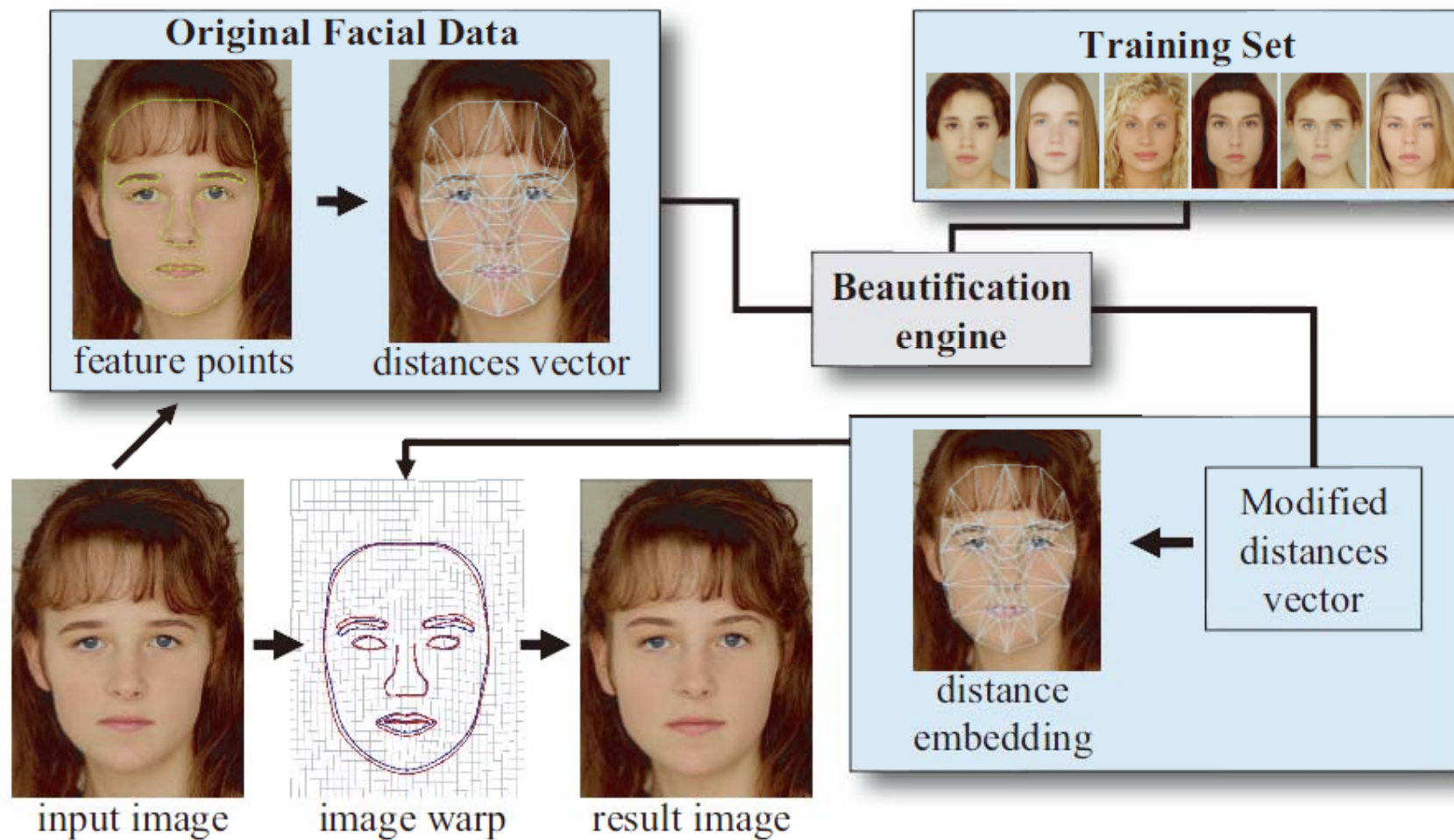


# Facial beautification

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# Facial beautification

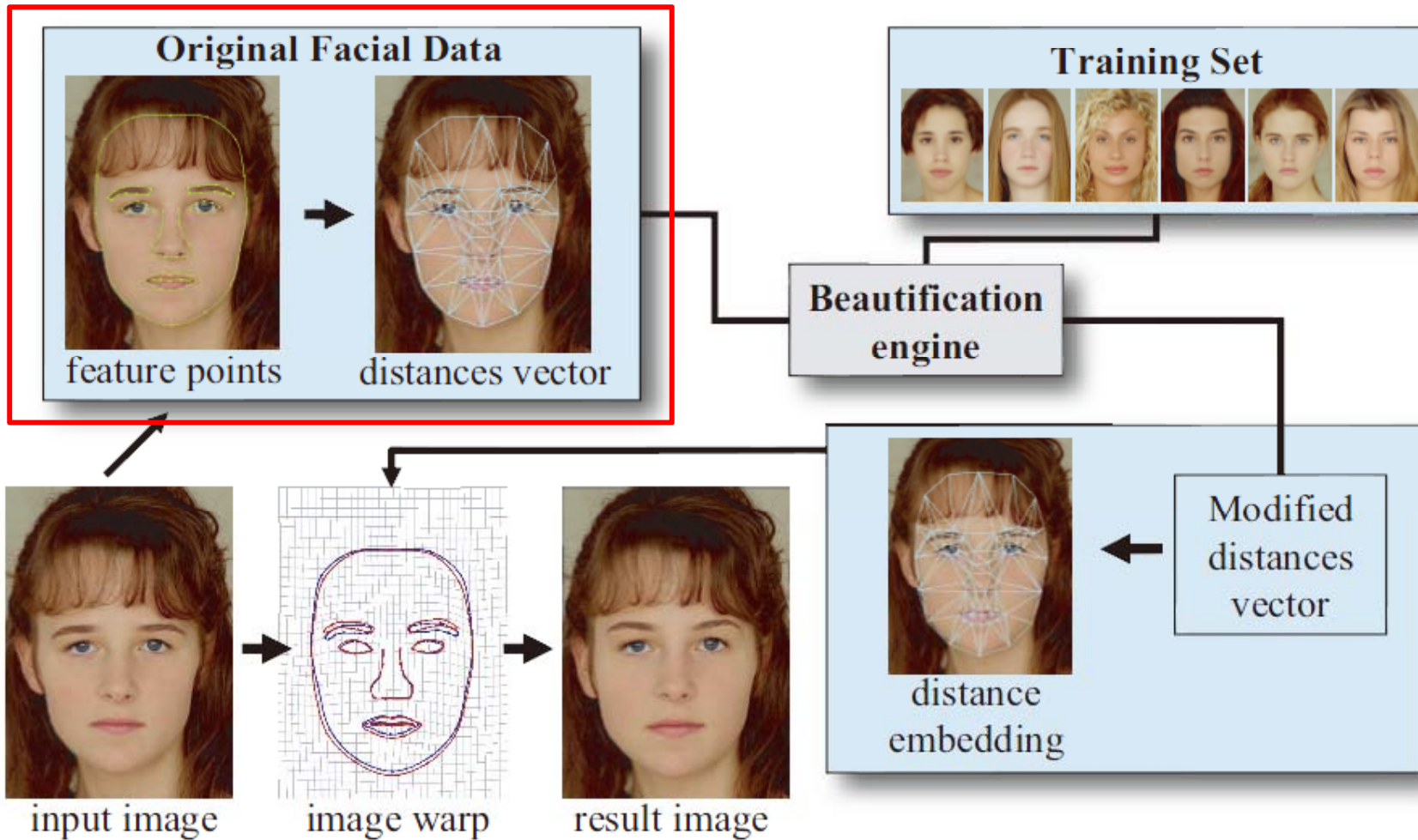


# Training set

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- Face images
  - 92 young Caucasian female
  - 33 young Caucasian male

# Feature extraction

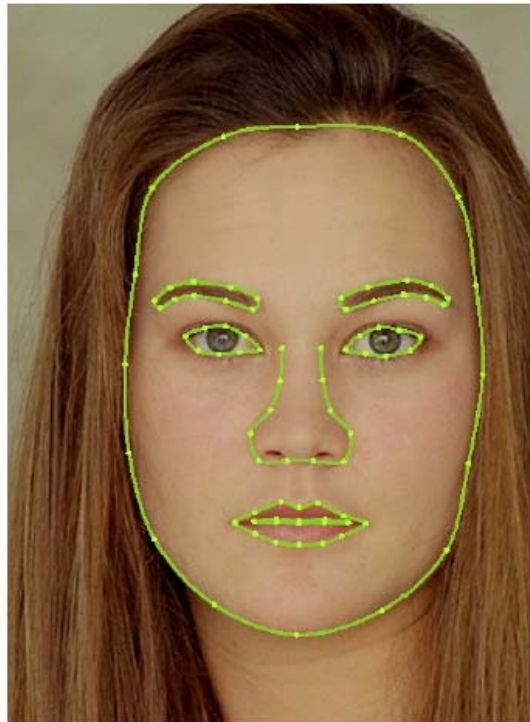




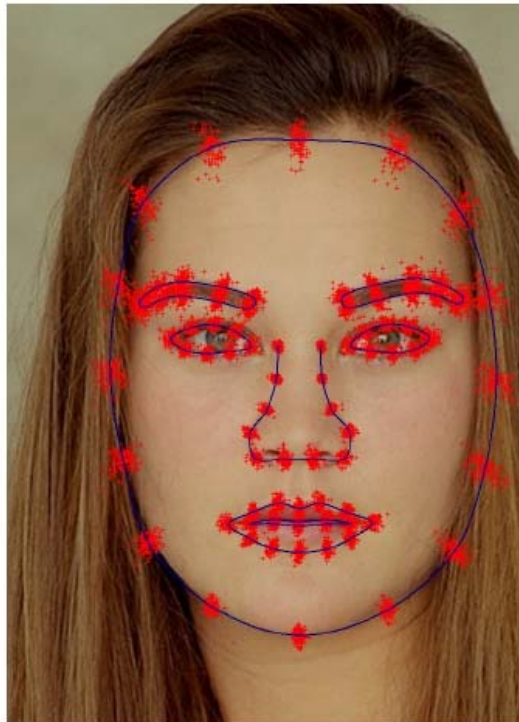
# Feature extraction

---

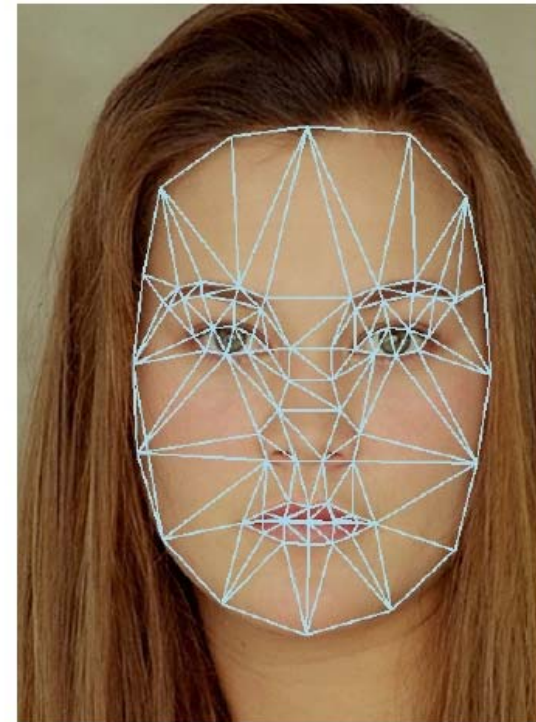
- Extract 84 feature points by BTSM
- Delaunay triangulation -> 234D distance vector (normalized by the square root of face area)



BTSM

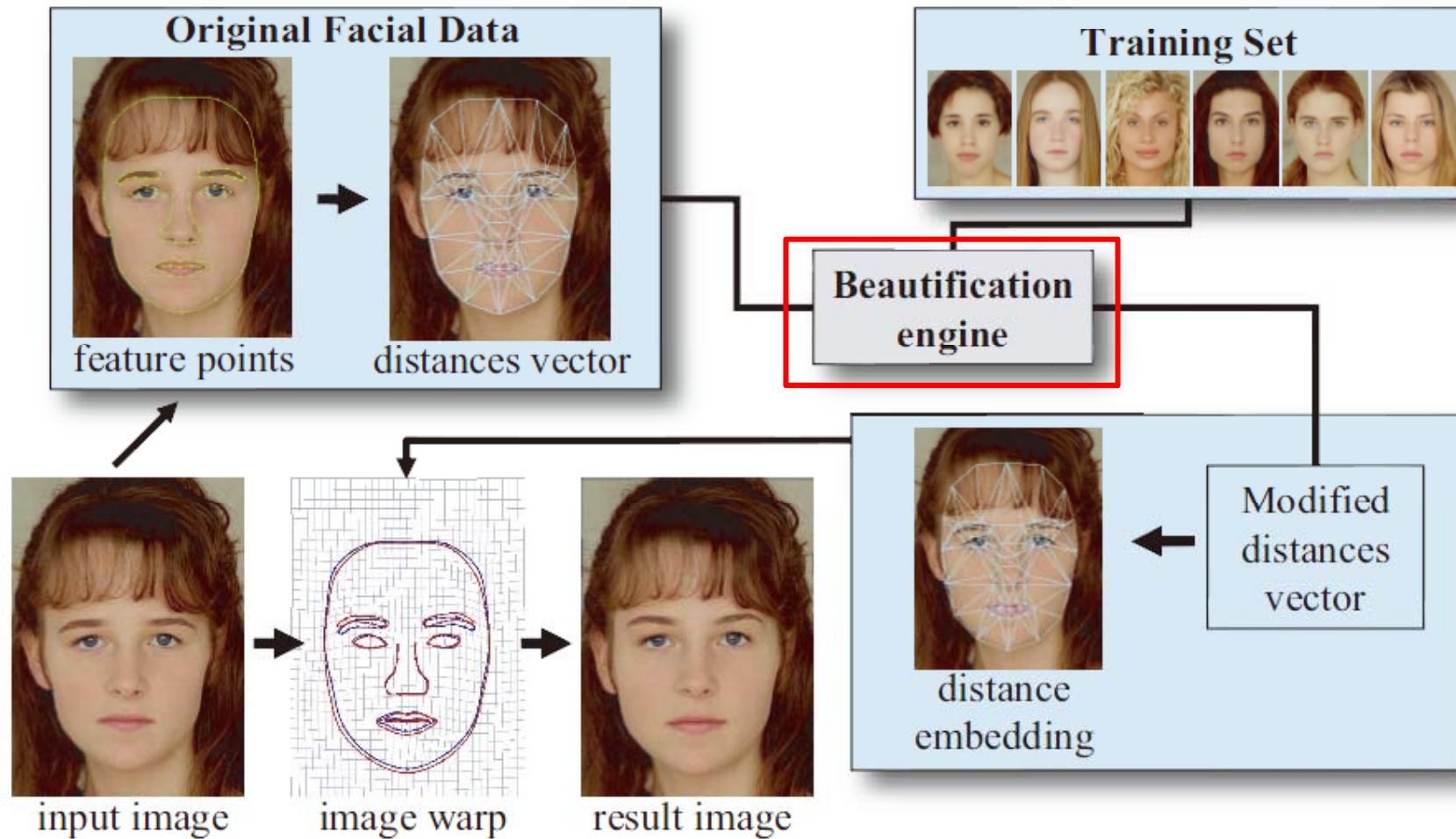


scatter plot for  
all training faces



234D vector

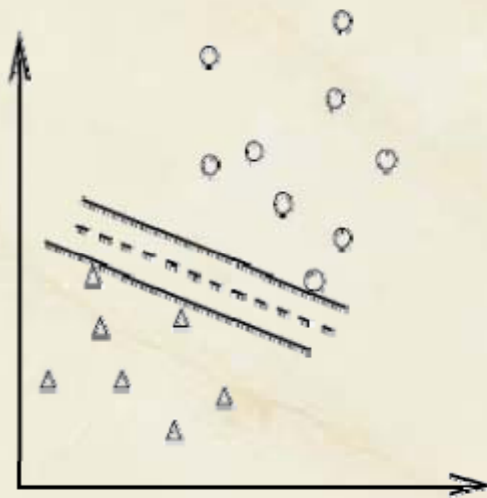
# Beautification engine



# Support vector regression (SVR)

- Similar concept to SVM, but for regression
- RBF kernels
- $f_b(v)$

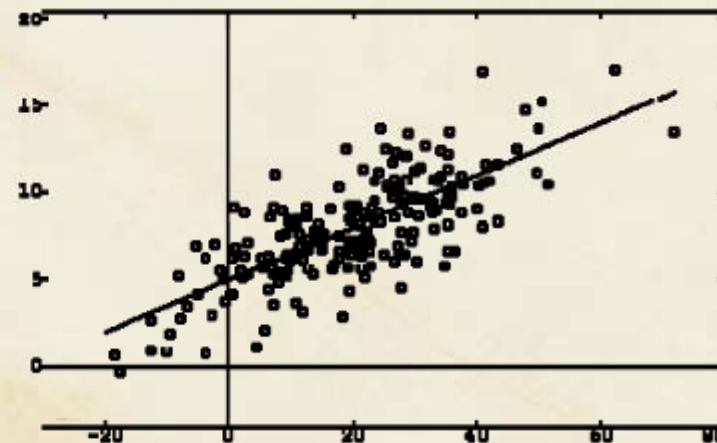
$$\text{SVM } f(x) = \text{sign}(\mathbf{w}^T \mathbf{x} + b)$$



$$\text{minimize } \frac{1}{2} \|\mathbf{w}\|^2$$

$$\text{subject to } y_i(\mathbf{w}^T \cdot \mathbf{x}_i + b) \geq 1$$

$$\text{SVR } f(x) = \mathbf{w}^T \mathbf{x} + b$$



$$\text{minimize } \frac{1}{2} \|\mathbf{w}\|^2$$

$$\text{subject to } \|y_i - (\mathbf{w}^T \cdot \mathbf{x}_i + b)\| \leq \varepsilon$$

# Beautification process

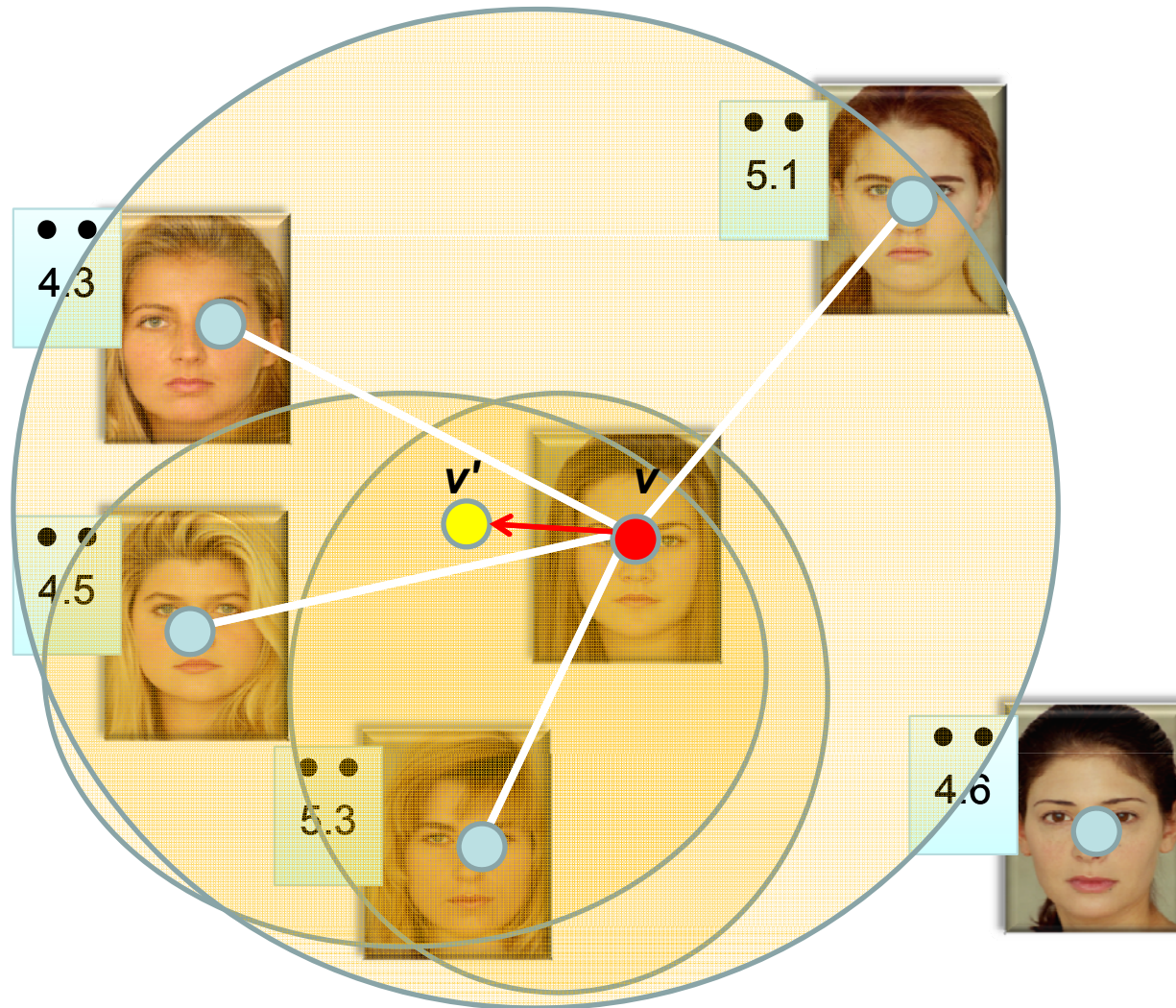
---

- Given the normalized distance vector  $v$ , generate a nearby vector  $v'$  so that

$$f_b(v') > f_b(v)$$

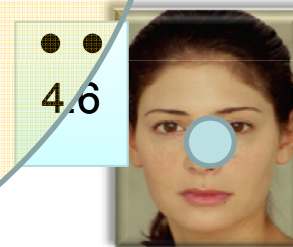
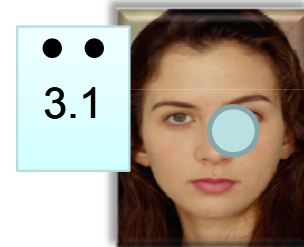
- Two options
  - KNN-based
  - SVR-based

# KNN-based beautification



$$w_i = \frac{b_i}{\|\mathbf{v} - \mathbf{v}_i\|}$$

$$\mathbf{v}' = \frac{\sum_{i=1}^K w_i \mathbf{v}_i}{\sum_{i=1}^K w_i}$$



# SVR-based beautification

---

- Directly use  $f_b$  to seek  $v'$

$$\mathbf{v}' = \underset{\mathbf{u}}{\operatorname{argmin}} E(\mathbf{u}), \text{ where } E(\mathbf{u}) = -f_b(\mathbf{u})$$

- Use standard no-derivative direction set method for minimization
- Features were reduced to 35D by PCA

# SVR-based beautification

- Problems: it sometimes yields distance vectors corresponding to invalid human face
- Solution: add log-likelihood term (LP)

$$E(\mathbf{u}) = (\alpha - 1)f_b(\mathbf{u}) - \alpha LP(\mathbf{u})$$

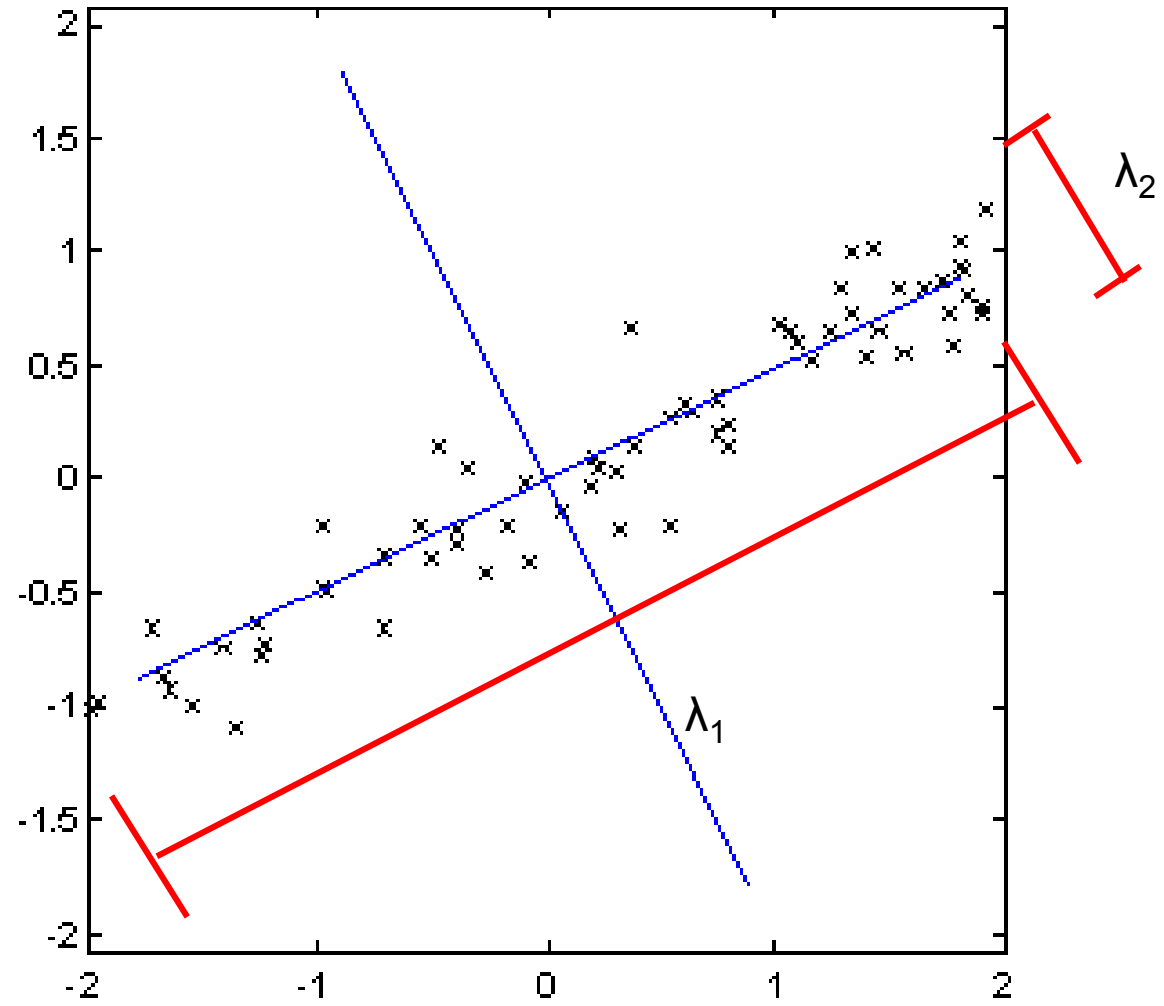
- LP is approximated by modeling face space as a multivariate Gaussian distribution

$$P(\hat{\mathbf{u}}) = \frac{1}{(2\pi)^{N/2} \sqrt{\prod_i \lambda_i}} \prod_i \exp\left(\frac{-\beta_i^2}{2\lambda_i}\right)$$

$\hat{\mathbf{u}}$ 's projection in PCA space
  $\hat{\mathbf{u}}$ 's i-th component
i-th eigenvalue

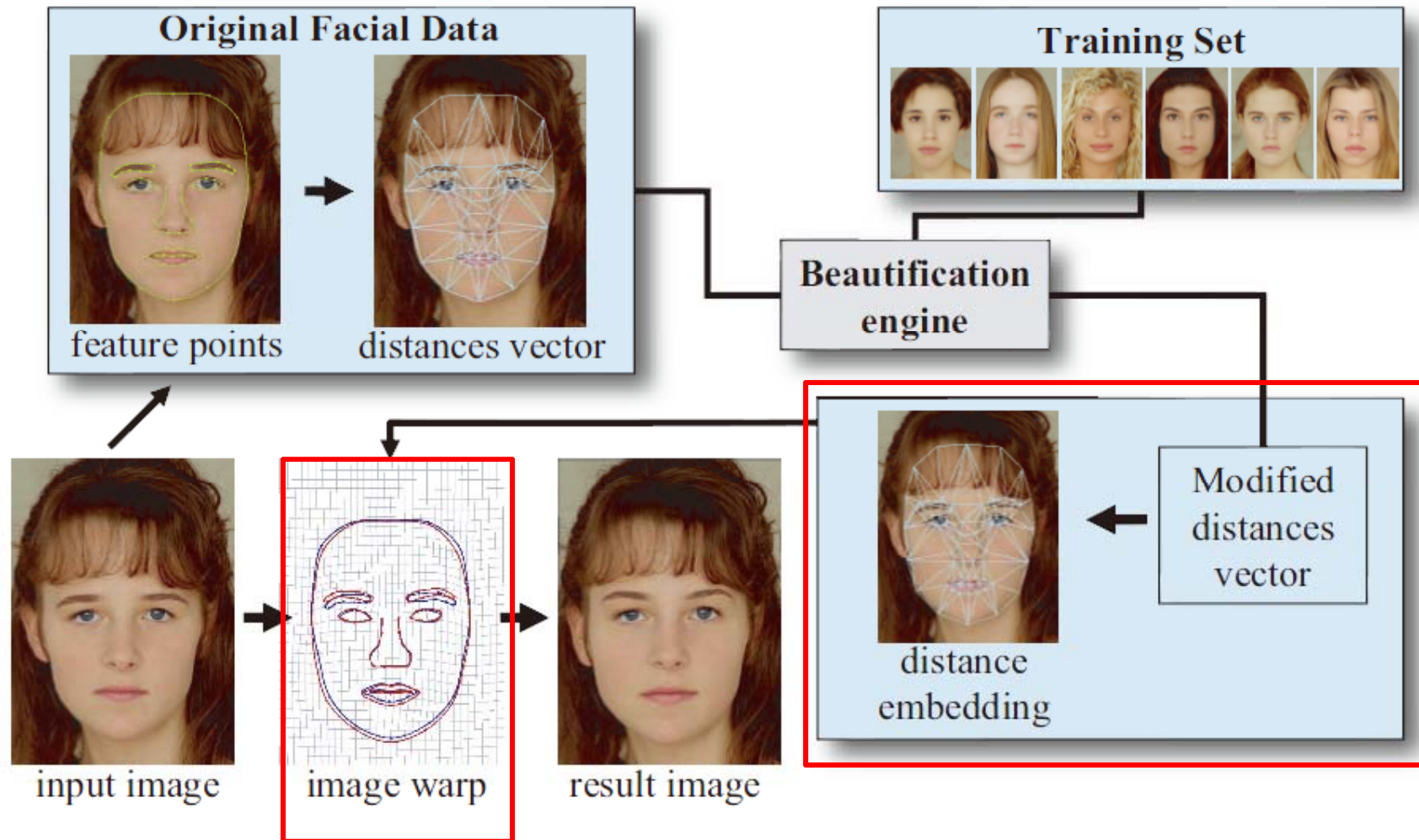
$$LP(\hat{\mathbf{u}}) = \sum \frac{-\beta_i^2}{2\lambda_i} + \text{const}$$

# PCA





# Embedding and warping



# Distance embedding

---

- Convert modified distance vector  $v'$  to a new face landmark

$$E(q_1, \dots, q_N) = \sum_{e_{ij}} \alpha_{ij} \left( \|q_i - q_j\|^2 - d_{ij}^2 \right)^2$$

- 1 if  $i$  and  $j$  belong to different facial features
- 10 otherwise

- A graph drawing problem referred to as a stress minimization problem, solved by LM algorithm for non-linear minimization

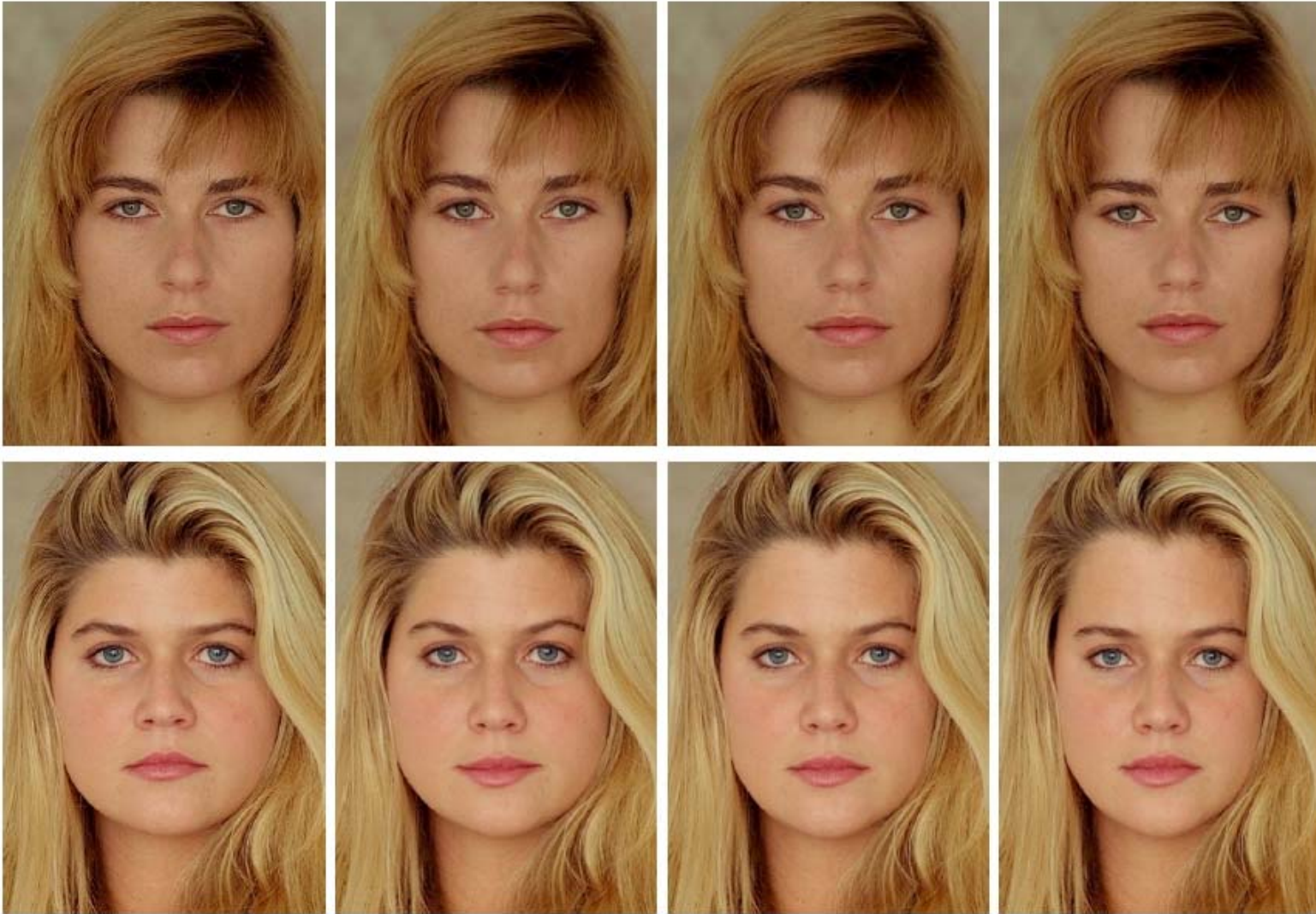
# Distance embedding

---

- Post processing to enforce similarity transform for features on eyes by minimizing

$$\sum \|Sp_i - q_i\|^2$$

$$S = \begin{pmatrix} a & b & t_x \\ -b & a & t_y \\ 0 & 0 & 1 \end{pmatrix}$$



Original

K=3

K=5

SVR

# Results (in training set)



# User study

---

Original portrait	3.37 (0.49)
Warped to mean	3.75 (0.49)
KNN-beautified (best)	4.14 (0.51)
SVR-beautified	4.51 (0.49)

# Results (not in training set)

---



# By parts



(a)



(b)

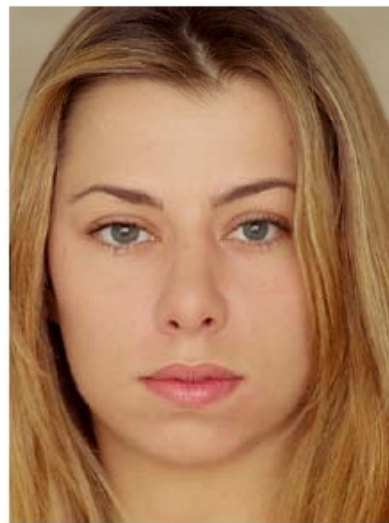


(c)

eyes



(d)



(e) full



(f)

mouth



# Different degrees

---



50%



100%

# Facial collage

---



# Image morphing

# Image morphing

---

- The goal is to synthesize a fluid transformation from one image to another.
- Cross dissolving is a common transition between cuts, but it is not good for morphing because of the ghosting effects.



image #1



dissolving



image #2

# Artifacts of cross-dissolving

---

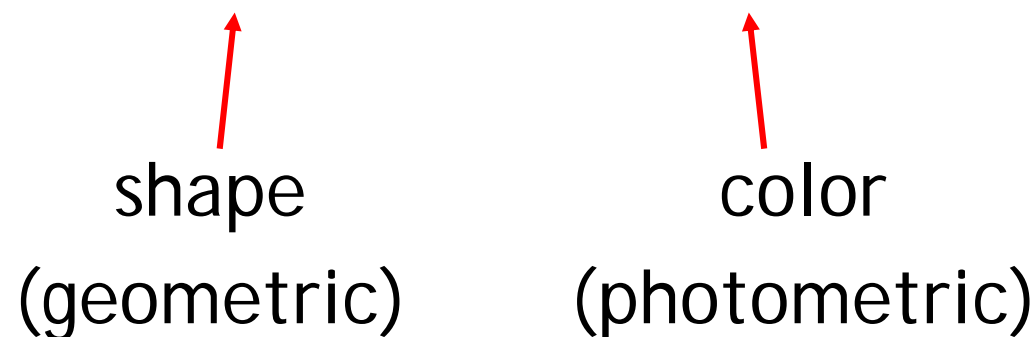


<http://www.salavon.com/>

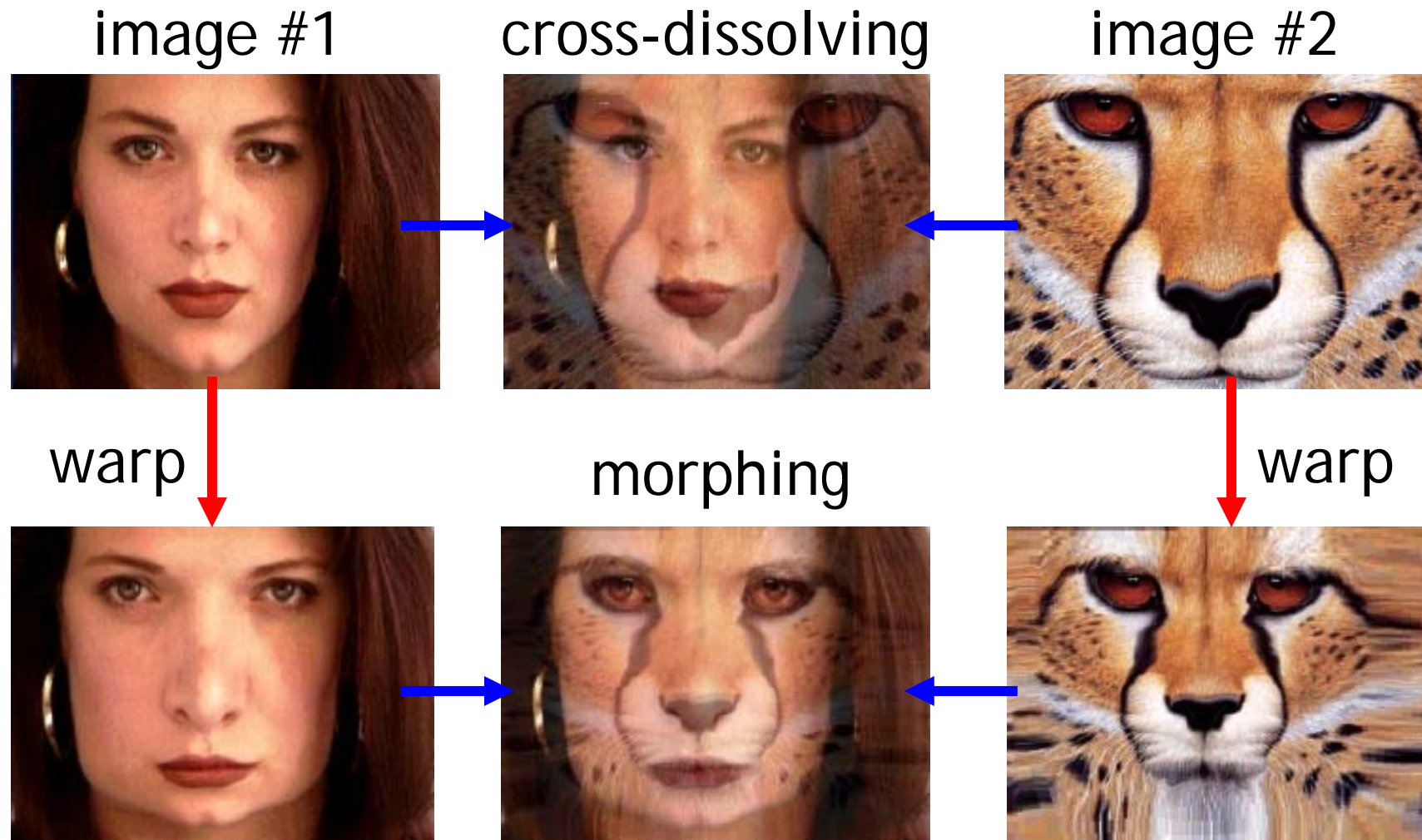
# Image morphing

---

- Why ghosting?
- Morphing = warping + cross-dissolving



# Image morphing



# Morphing sequence

---





# Face averaging by morphing

---



average faces

# Image morphing

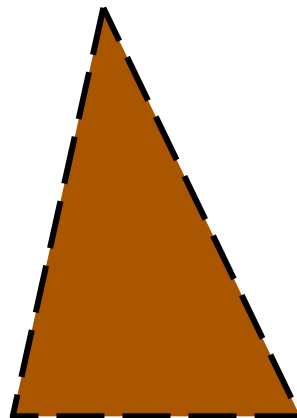
---

create a morphing sequence: for each time  $t$

1. Create an intermediate warping field (by interpolation)
2. Warp both images towards it
3. Cross-dissolve the colors in the newly warped images



$t=0$



$t=0.33$



$t=1$

# An ideal example (in 2004)

---



t=0



morphing



t=1

# An ideal example

---



t=0



middle face (t=0.5)

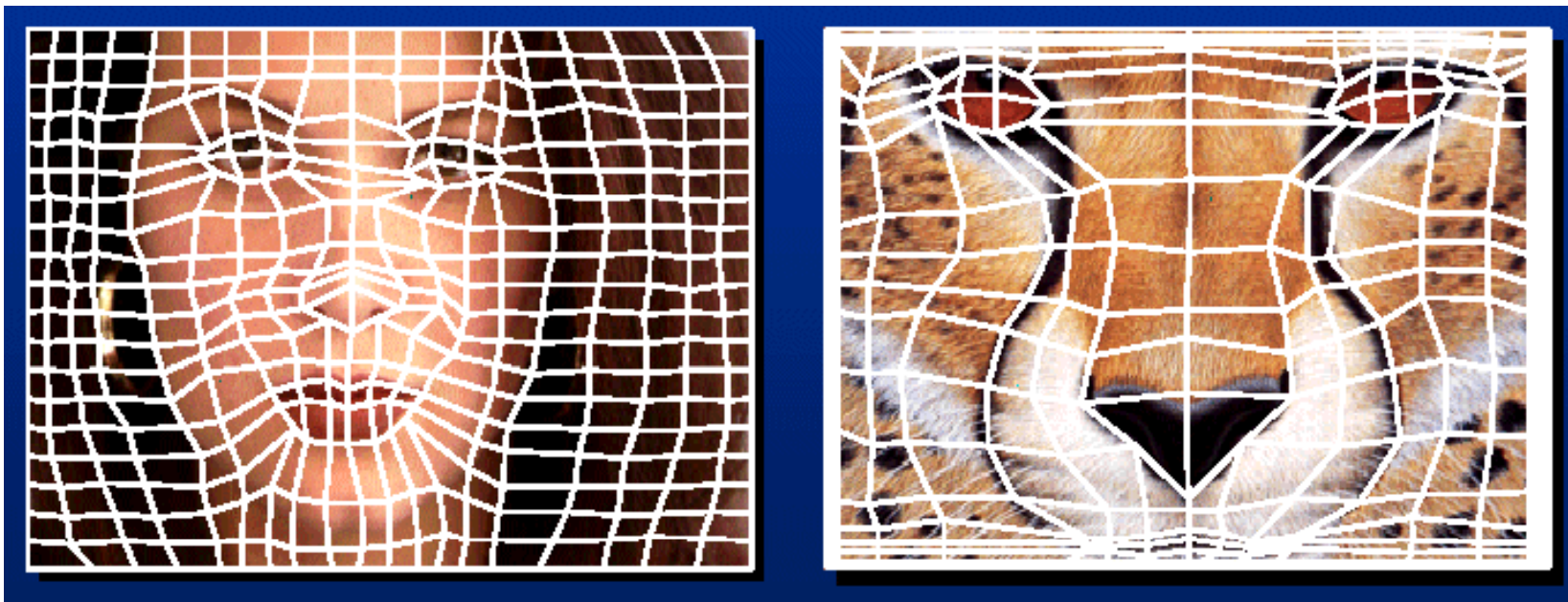


t=1

# Warp specification (mesh warping)

---

- How can we specify the warp?
  1. Specify corresponding *spline control points* *interpolate* to a complete warping function

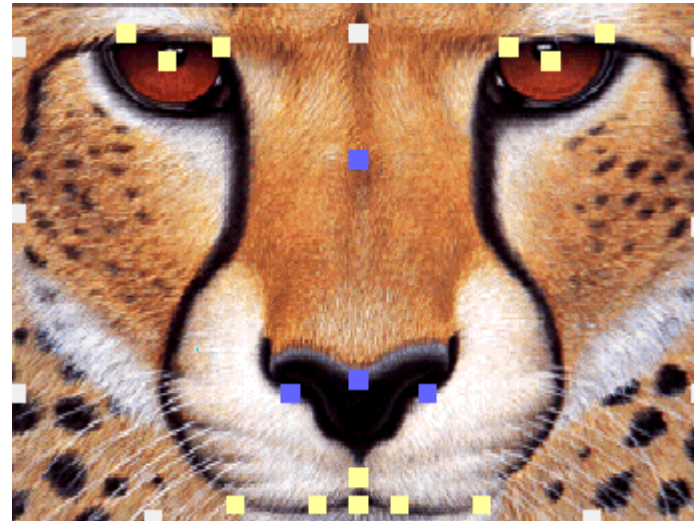
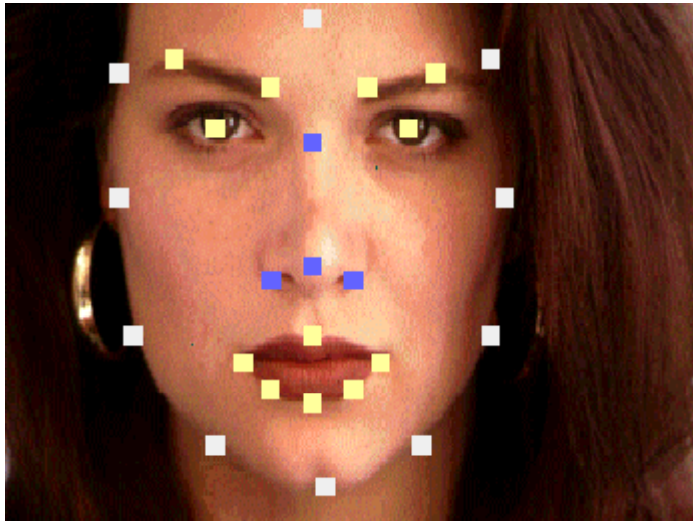


easy to implement, but less expressive

# Warp specification

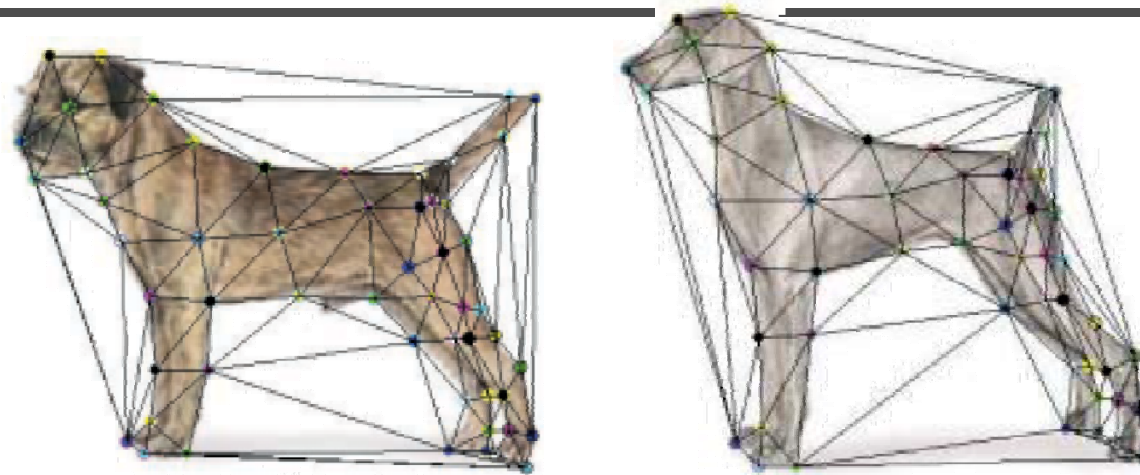
---

- How can we specify the warp
  1. Specify the source image
  2. Specify corresponding *points*
    - *interpolate* to a complete warping function



# Solution: convert to mesh warping

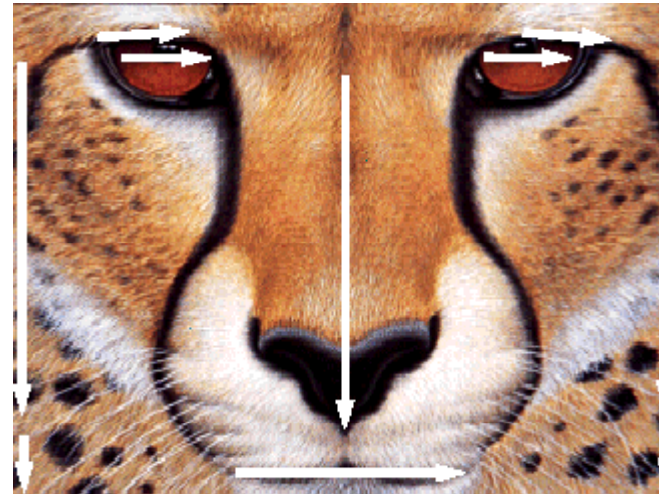
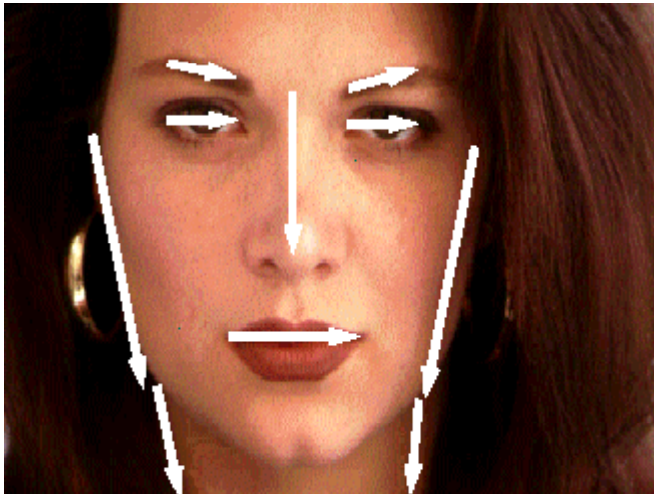
---



1. Define a triangular mesh over the points
  - Same mesh in both images!
  - Now we have triangle-to-triangle correspondences
2. Warp each triangle separately from source to destination
  - How do we warp a triangle?
  - 3 points = affine warp!
  - Just like texture mapping

# Warp specification (field warping)

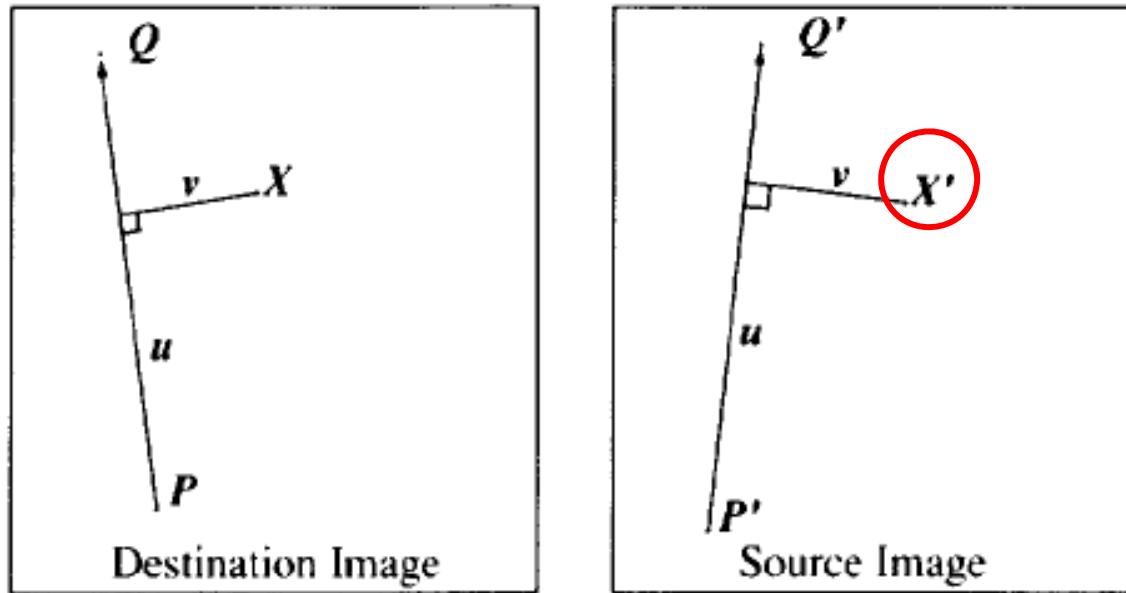
- How can we specify the warp?
  3. Specify corresponding *vectors*
    - *interpolate* to a complete warping function
    - The Beier & Neely Algorithm





# Beier&Neely (SIGGRAPH 1992)

- Single line-pair PQ to P'Q':



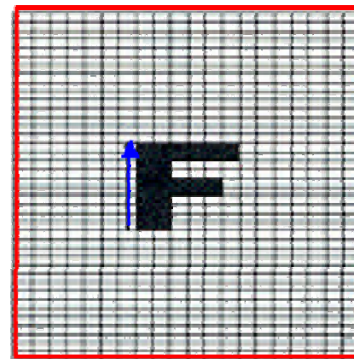
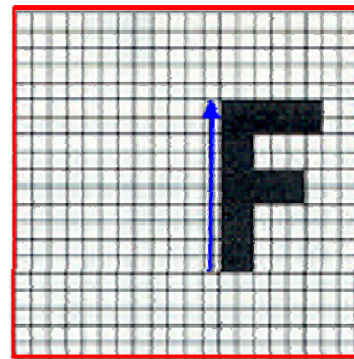
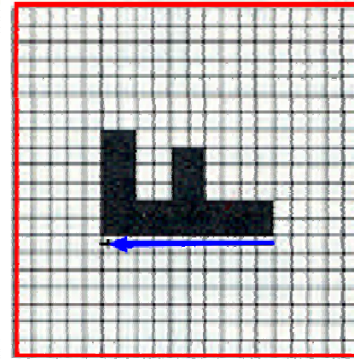
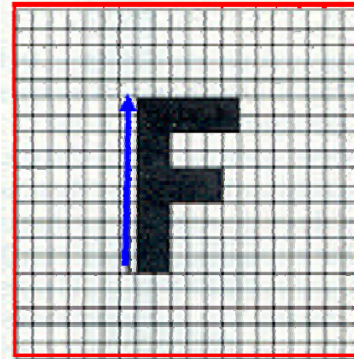
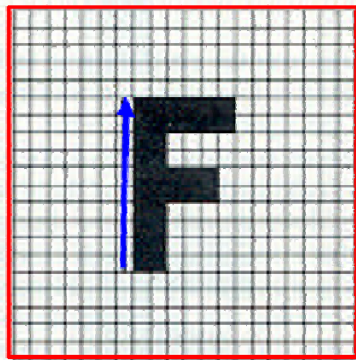
$$u = \frac{(X - P) \cdot (Q - P)}{\|Q - P\|^2} \quad (1)$$

$$v = \frac{(X - P) \cdot \text{Perpendicular}(Q - P)}{\|Q - P\|} \quad (2)$$

$$X' = P' + u \cdot (Q' - P') + \frac{v \cdot \text{Perpendicular}(Q' - P')}{\|Q' - P'\|} \quad (3)$$

# Algorithm (single line-pair)

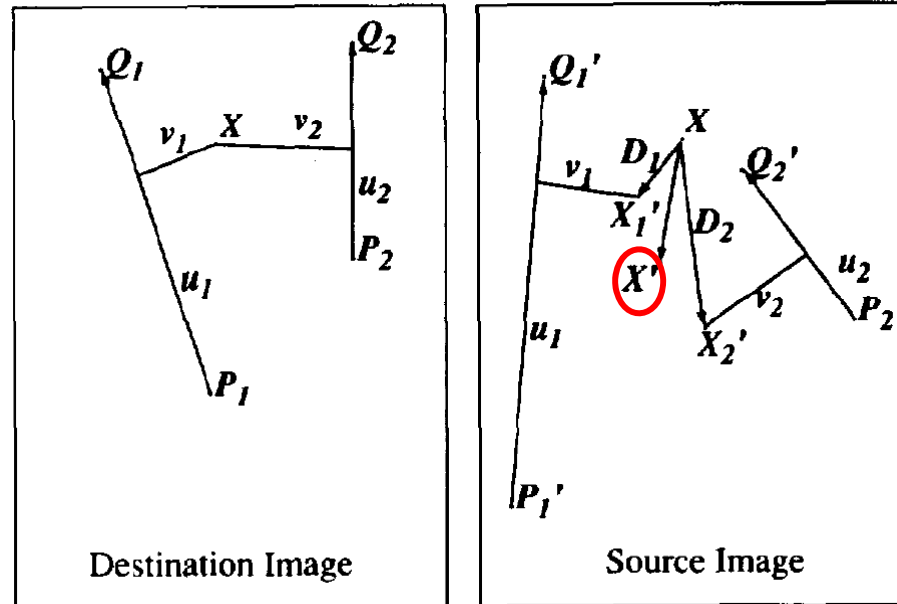
- For each  $X$  in the destination image:
  1. Find the corresponding  $u, v$
  2. Find  $X'$  in the source image for that  $u, v$
  3.  $\text{destinationImage}(X) = \text{sourceImage}(X')$
- Examples:



Affine transformation

# Multiple Lines

$$D_i = X_i' - X_i$$



$$weight[i] = \left( \frac{length[i]^p}{a + dist[i]} \right)^b$$

*length* = length of the line segment,

*dist* = distance to line segment

The influence of *a*, *p*, *b*. The same as the average of  $X_i'$

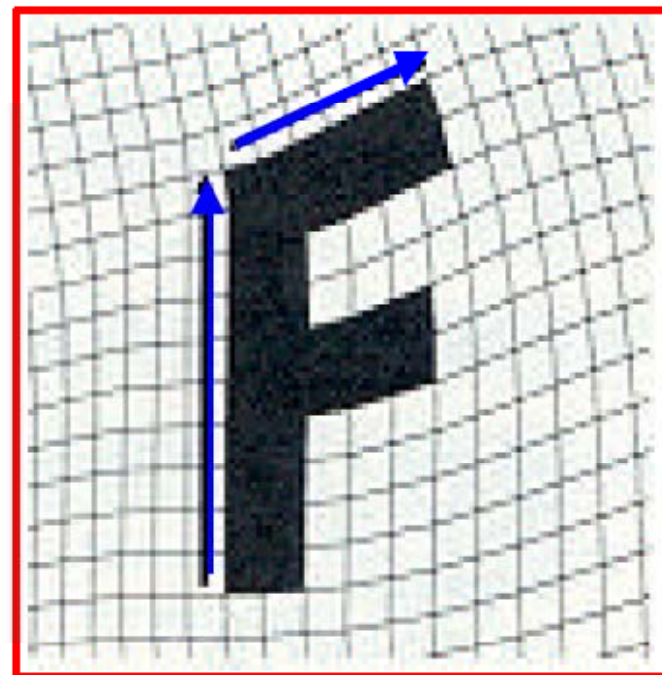
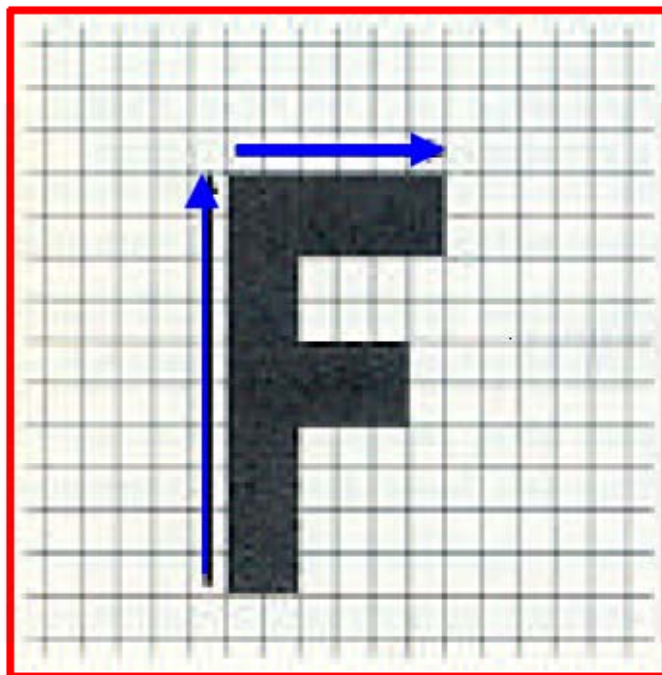
# Full Algorithm

---

```
WarpImage(SourceImage, L'[...], L[...])
begin
    foreach destination pixel X do
        XSum = (0,0)
        WeightSum = 0
        foreach line L[i] in destination do
            X'[i] = X transformed by (L[i],L'[i])
            weight[i] = weight assigned to X'[i]
            XSum = Xsum + X'[i] * weight[i]
            WeightSum += weight[i]
        end
        X' = XSum/WeightSum
        DestinationImage(X) = SourceImage(X')
    end
return Destination
end
```

# Resulting warp

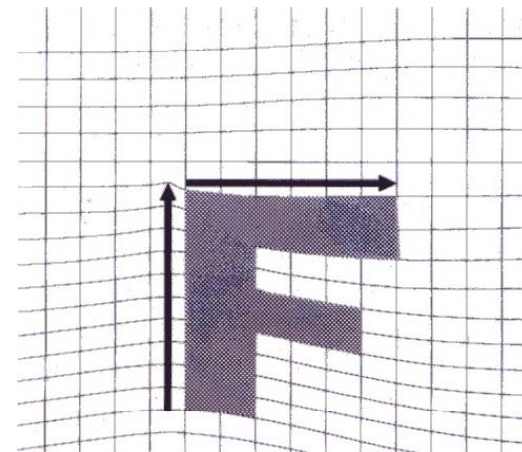
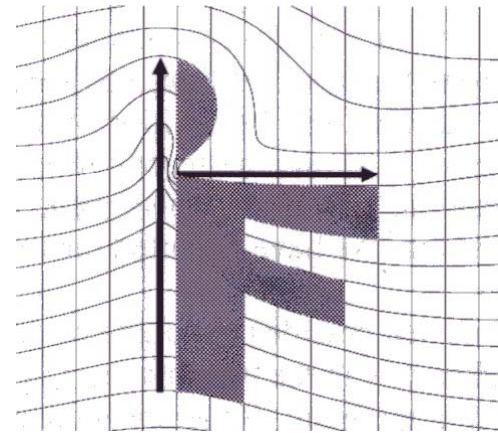
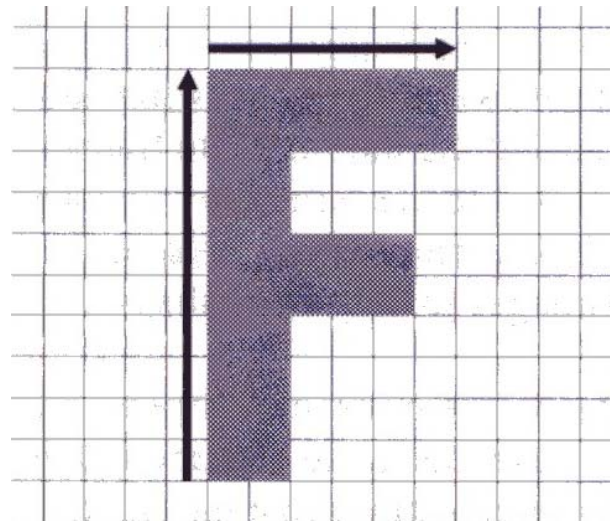
---



# Comparison to mesh morphing

---

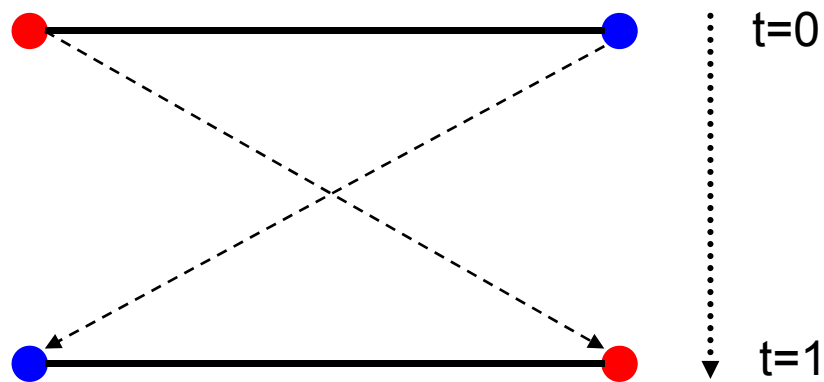
- Pros: more expressive
- Cons: speed and control



# Warp interpolation

---

- How do we create an intermediate warp at time  $t$ ?
  - linear interpolation for line end-points
  - But, a line rotating 180 degrees will become 0 length in the middle
  - One solution is to interpolate line mid-point and orientation angle



# Animation

---

GenerateAnimation(Image<sub>0</sub>, L<sub>0</sub>[...], Image<sub>1</sub>, L<sub>1</sub>[...])

**begin**

**foreach** intermediate frame time  $t$  **do**

**for**  $i=1$  to number of line-pairs **do**

$L[i] =$  line  $t$ -th of the way from  $L_0[i]$  to  $L_1[i]$ .

**end**

        Warp<sub>0</sub> = WarpImage( Image<sub>0</sub>, L<sub>0</sub>[...], L[...])

        Warp<sub>1</sub> = WarpImage( Image<sub>1</sub>, L<sub>1</sub>[...], L[...])

**foreach** pixel  $p$  in FinalImage **do**

            FinalImage( $p$ ) =  $(1-t)$  Warp<sub>0</sub>( $p$ ) +  $t$  Warp<sub>1</sub>( $p$ )

**end**

**end**

**end**



# Animated sequences

---

- Specify keyframes and interpolate the lines for the inbetween frames
- Require a lot of tweaking

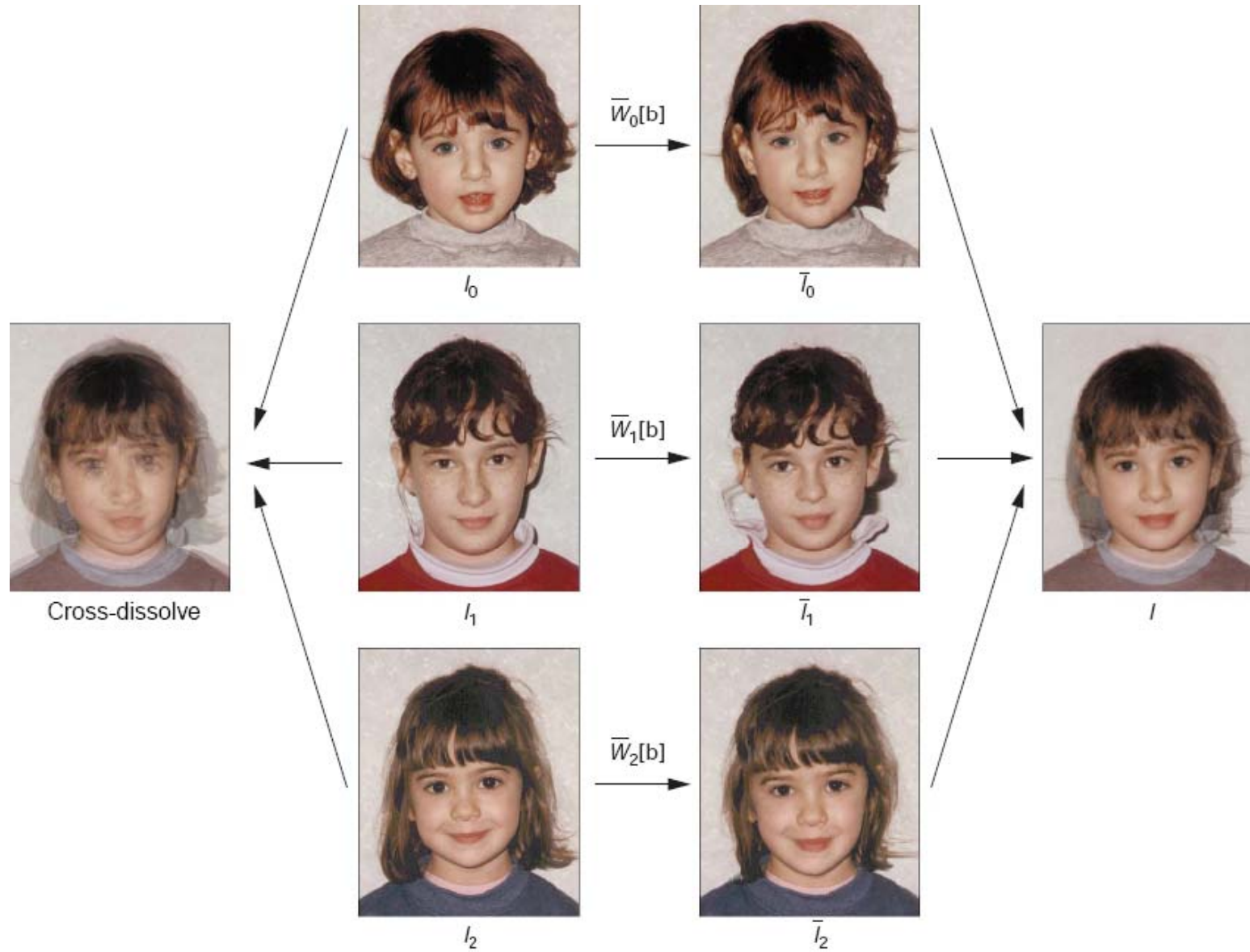
# Results

---



*Michael Jackson's MTV "Black or White"*

# Multi-source morphing



# Multi-source morphing



(a)



(b)



(c)



(d)



(e)



(f)



(g)



(h)

# Woman in arts

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# References

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