

# 3D photography

Digital Visual Effects, Spring 2005

Yung-Yu Chuang

2005/5/18

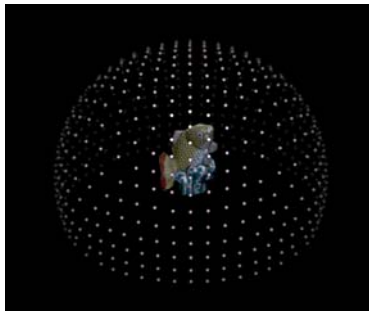
*with slides by Szymon Rusinkiewicz, Richard Szeliski, Steve Seitz and Brian Curless*

## Announcements

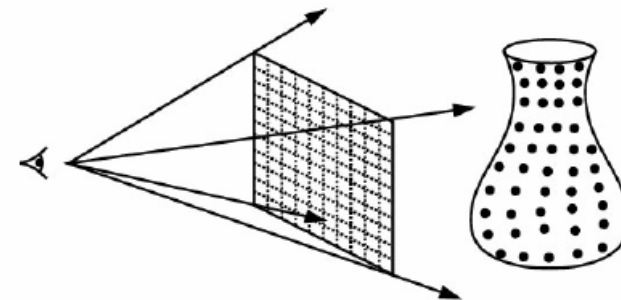
- [Project #2 winning artifacts](#)
- Project #3 is due next Tuesday
- CGCG talk on 5/23, 2:20pm, CSIE 107

## 3D photography

- Acquisition of **geometry** and material



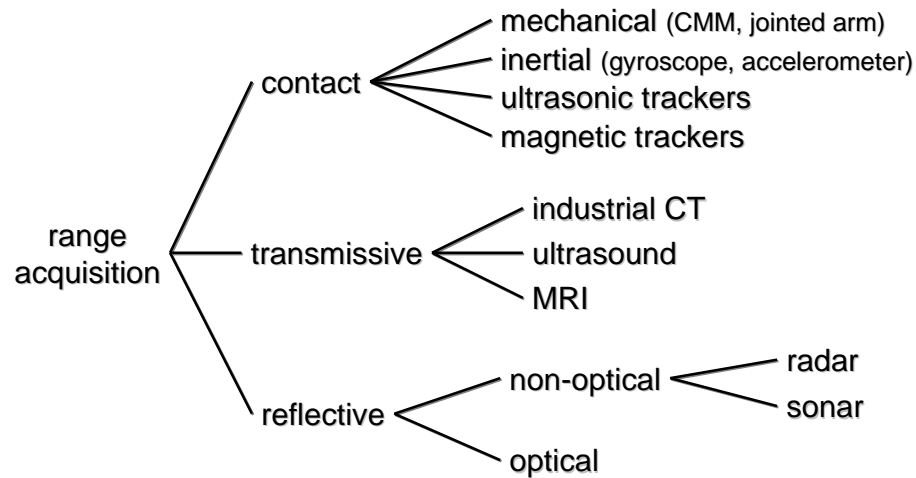
## Range acquisition



**Range image**

## Range acquisition taxonomy

DigiVFX



## Touch Probes

DigiVFX

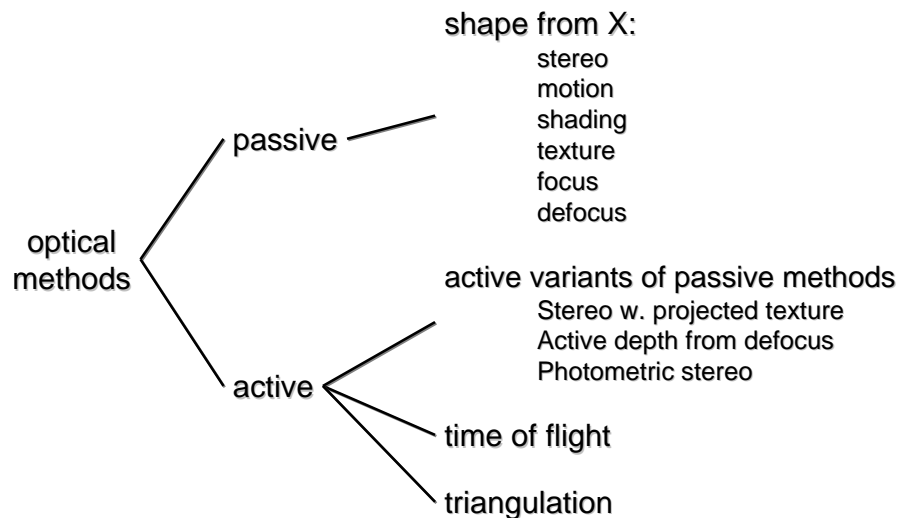
- Jointed arms with angular encoders
- Return position, orientation of tip



Faro Arm – Faro Technologies, Inc.

## Range acquisition taxonomy

DigiVFX



## Outline

DigiVFX

- Passive approaches
  - Stereo
  - Multiview approach
- Active approaches
  - Triangulation
  - Shadow scanning
- Active variants of passive approaches
  - Photometric stereo
  - Example-based photometric stereo
  - Helmholtz stereo

## Passive approaches

Stereo



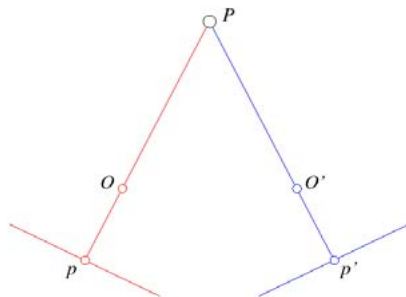
Public Library, Stereoscopic Looking Room, Chicago, by Phillips, 1923



Stereo

DigiVFX

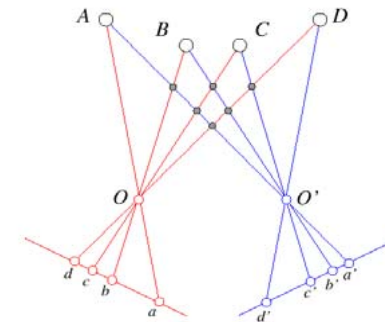
- One distinguishable point being observed
  - The preimage can be found at the intersection of the rays from the focal points to the image points



Stereo

DigiVFX

- Many points being observed
  - Need some method to establish correspondences

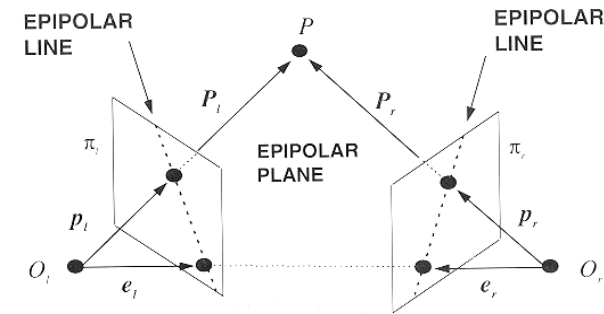


## Components of stereo vision systems

- Camera calibration: previous lecture
- Image rectification: simplifies the search for correspondences
- Correspondence: which item in the left image corresponds to which item in the right image
- Reconstruction: recovers 3-D information from the 2-D correspondences

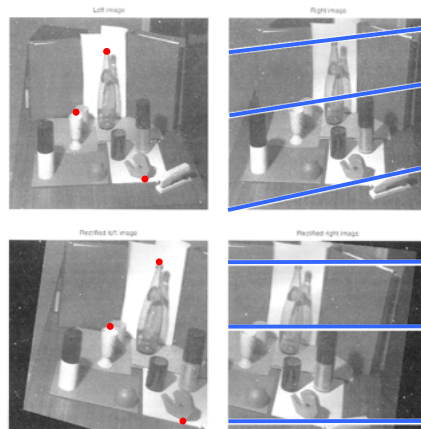
## Epipolar geometry

- Epipolar constraint: corresponding points must lie on conjugate epipolar lines
  - Search for correspondences becomes a 1-D problem



## Image rectification

- Warp images such that conjugate epipolar lines become collinear and parallel to  $u$  axis

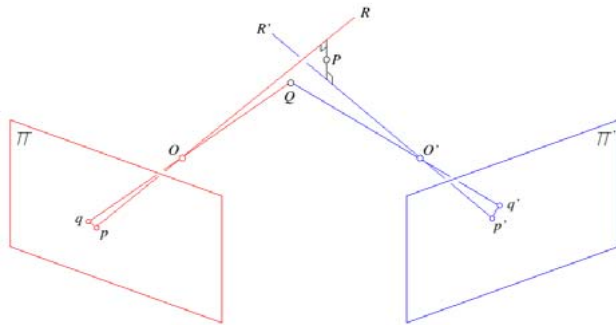


## Disparity

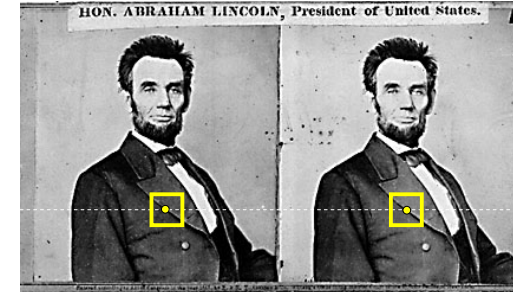
- With rectified images, disparity is just (horizontal) displacement of corresponding features in the two images
  - Disparity = 0 for distant points
  - Larger disparity for closer points
  - Depth of point proportional to  $1/\text{disparity}$

## Reconstruction

- Geometric
  - Construct the line segment perpendicular to  $R$  and  $R'$  that intersects both rays and take its mid-point



## Basic stereo algorithm



- For each epipolar line
  - For each pixel in the left image
    - compare with every pixel on same epipolar line in right image
    - pick pixel with minimum match cost

Improvement: match **windows**

## Basic stereo algorithm

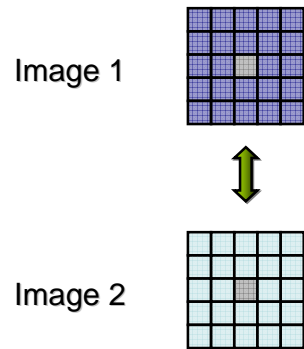
- For each pixel
  - For each disparity
    - For each pixel in window
      - Compute difference
  - Find disparity with minimum SSD

## Reverse order of loops

- For each disparity
  - For each pixel
    - For each pixel in window
      - Compute difference
- Find disparity with minimum SSD at each pixel

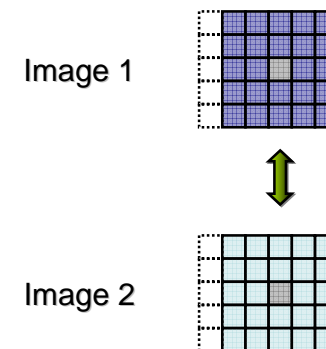
## Incremental computation

- Given SSD of a window, at some disparity



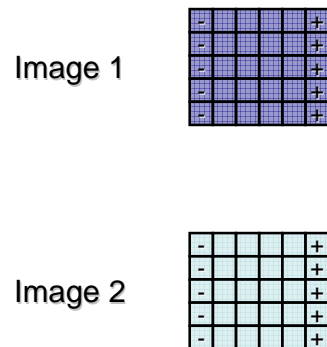
## Incremental computation

- Want: SSD at next location



## Incremental computation

- Subtract contributions from leftmost column, add contributions from rightmost column

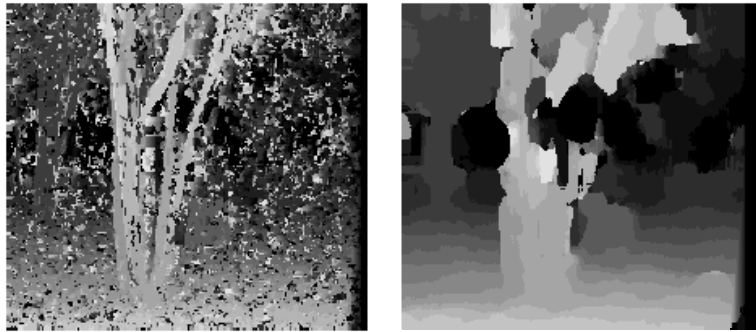


## Selecting window size

- Small window: more detail, but more noise
- Large window: more robustness, less detail
- Example:



## Selecting window size



3 pixel window

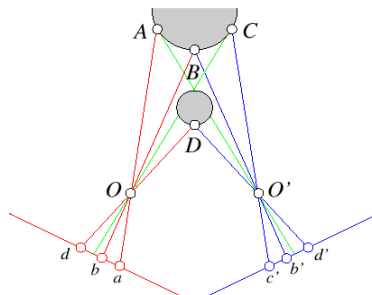
20 pixel window

## Non-square windows

- Compromise: have a large window, but higher weight near the center
- Example: Gaussian
- For each disparity
  - For each pixel
    - Compute weighted SSD

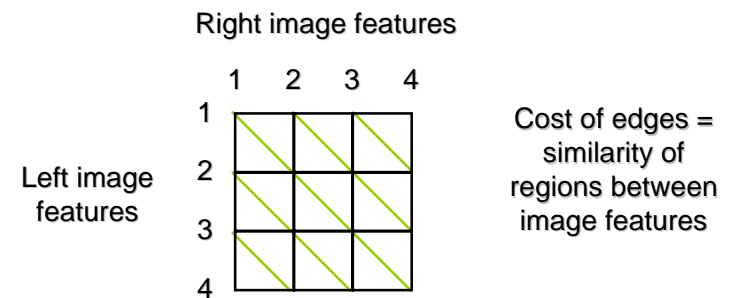
## Ordering constraint

- Order of matching features usually the same in both images
- But not always: occlusion



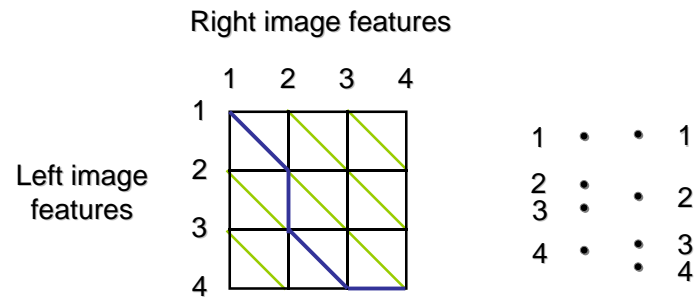
## Dynamic programming

- Treat feature correspondence as graph problem



## Dynamic programming

- Find min-cost path through graph



## Energy minimization

- Another approach to improve quality of correspondences
- Assumption: disparities vary (mostly) smoothly
- Minimize energy function:
 
$$E_{\text{data}} + \lambda E_{\text{smoothness}}$$
- $E_{\text{data}}$ : how well does disparity match data
- $E_{\text{smoothness}}$ : how well does disparity match that of neighbors – regularization

## Energy minimization

- If data and energy terms are nice (continuous, smooth, etc.) can try to minimize via gradient descent, etc.
- In practice, disparities only piecewise smooth
- Design smoothness function that doesn't penalize large jumps too much
  - Example:  $V(\alpha, \beta) = \min(|\alpha - \beta|, K)$

## Stereo as energy minimization

- Matching Cost Formulated as Energy
  - “data” term penalizing bad matches

$$D(x, y, d) = |\mathbf{I}(x, y) - \mathbf{J}(x + d, y)|$$

- “neighborhood term” encouraging spatial smoothness

$$V(d_1, d_2) = \text{cost of adjacent pixels with labels } d_1 \text{ and } d_2$$

$$= |d_1 - d_2| \quad (\text{or something similar})$$

$$E = \sum_{(x,y)} D(x, y, d_{x,y}) + \sum_{\text{neighbors } (x_1,y_1),(x_2,y_2)} V(d_{x_1,y_1}, d_{x_2,y_2})$$



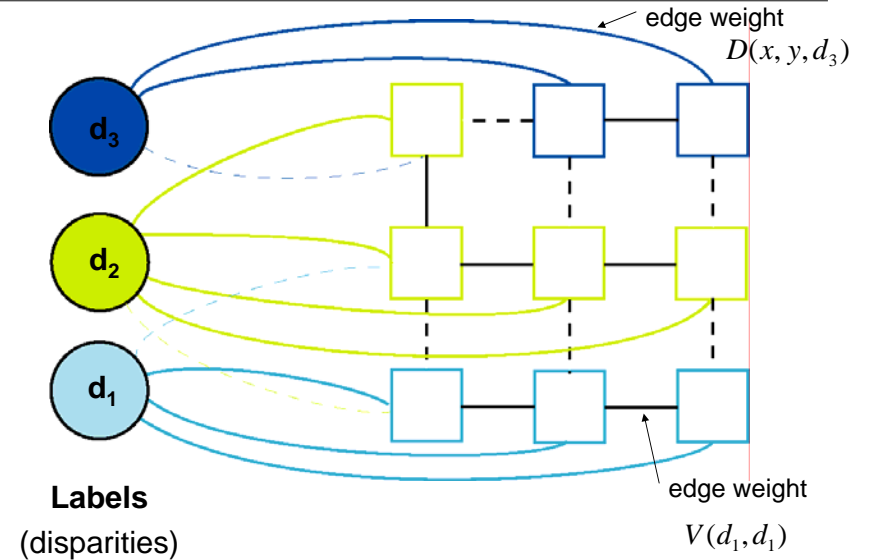
## Energy minimization

DigiVFX

- Hard to find global minima of non-smooth functions
  - Many local minima
  - Provably NP-hard
- Practical algorithms look for approximate minima (e.g., simulated annealing)

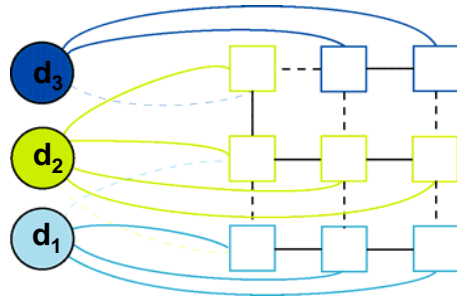
## Energy minimization via graph cuts

DigiVFX



## Energy minimization via graph cuts

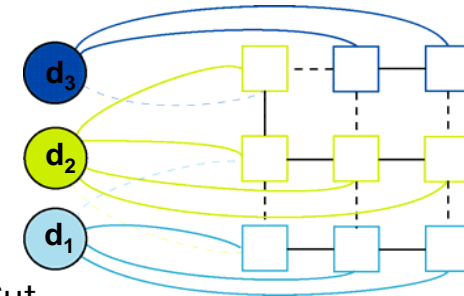
DigiVFX



- Graph Cost
  - Matching cost between images
  - Neighborhood matching term
  - Goal: figure out which labels are connected to which pixels

## Energy minimization via graph cuts

DigiVFX

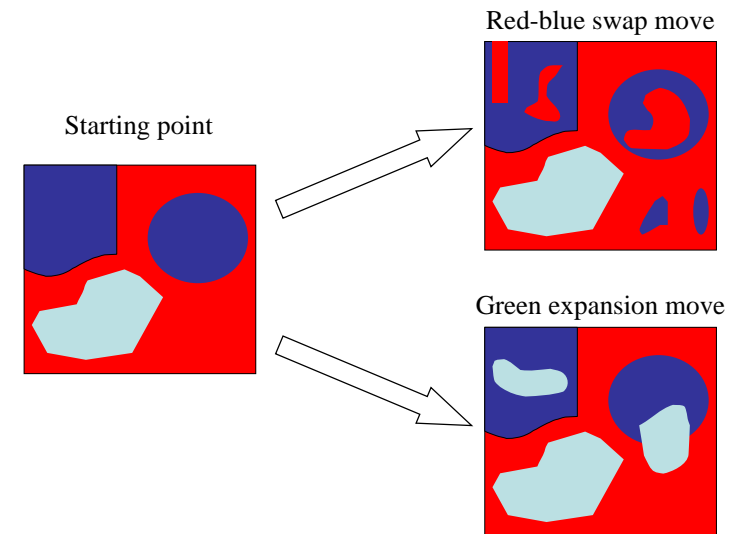


- Graph Cut
  - Delete enough edges so that
    - each pixel is (transitively) connected to exactly one label node
  - Cost of a cut: sum of deleted edge weights
  - Finding min cost cut equivalent to finding global minimum of energy function

## Computing a multiway cut

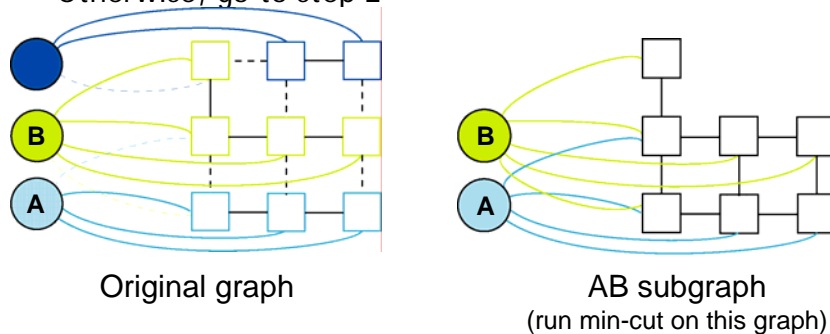
- With 2 labels: classical min-cut problem
  - Solvable by standard flow algorithms
    - polynomial time in theory, nearly linear in practice
  - More than 2 terminals: NP-hard  
[Dahlhaus *et al.*, STOC '92]
- Efficient approximation algorithms exist
  - Within a factor of 2 of optimal
  - Computes local minimum in a strong sense
    - even very large moves will not improve the energy
  - Yuri Boykov, Olga Veksler and Ramin Zabih, [Fast Approximate Energy Minimization via Graph Cuts](#), International Conference on Computer Vision, September 1999.

## Move examples



## The swap move algorithm

1. Start with an arbitrary labeling
2. Cycle through every label pair  $(A, B)$  in some order
  - 2.1 Find the lowest  $E$  labeling within a single  $AB$ -swap
  - 2.2 Go there if it's lower  $E$  than the current labeling
3. If  $E$  did not decrease in the cycle, we're done  
Otherwise, go to step 2



## The expansion move algorithm

1. Start with an arbitrary labeling
2. Cycle through every label  $A$  in some order
  - 2.1 Find the lowest  $E$  labeling within a single  $A$ -expansion
  - 2.2 Go there if it's lower  $E$  than the current labeling
3. If  $E$  did not decrease in the cycle, we're done  
Otherwise, go to step 2

## Stereo results

DigiVFX

– Data from University of Tsukuba



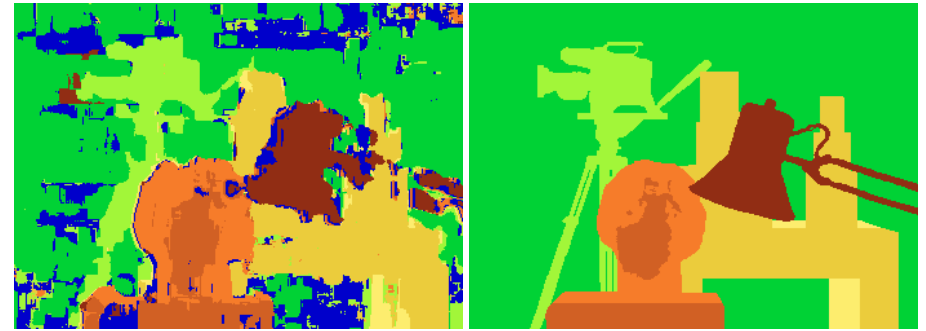
scene



ground truth

## Results with window correlation

DigiVFX



normalized correlation  
(best window size)

ground truth

## Results with graph cuts

DigiVFX



graph cuts  
(Potts model  $E$ ,  
expansion move algorithm)

ground truth

## Volumetric multiview approaches

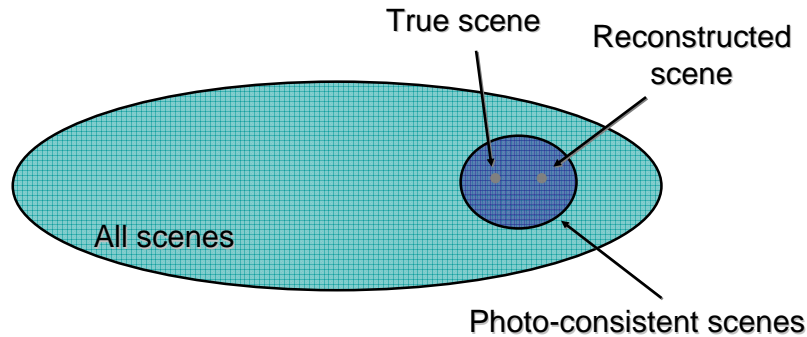
DigiVFX

- Goal: find a model consistent with images
- “Model-centric” (vs. image-centric)
- Typically use discretized volume (voxel grid)
- For each voxel, compute occupied / free (for some algorithms, also color, etc.)

## Photo consistency

DigiVFX

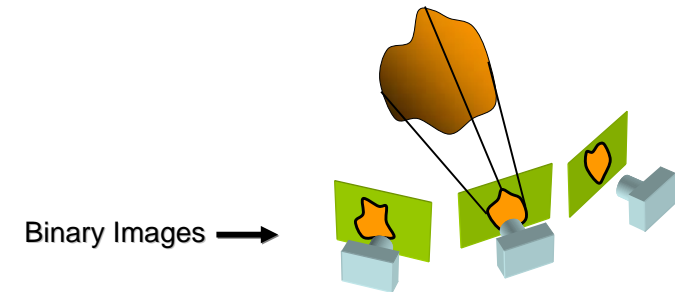
- Result: not necessarily correct scene
- Many scenes produce the same images



## Silhouette carving

DigiVFX

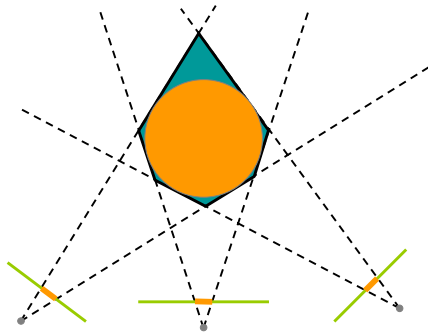
- Find silhouettes in all images
- Exact version:
  - Back-project all silhouettes, find intersection



## Silhouette carving

DigiVFX

- Find silhouettes in all images
- Exact version:
  - Back-project all silhouettes, find intersection



## Silhouette carving

DigiVFX

- Limit of silhouette carving is *visual hull* or *line hull*
- Complement of lines that don't intersect object
  - Can't recover "pits" in object
- In general not the same as object
  - Can't recover "pits" in object
- Not the same as convex hull

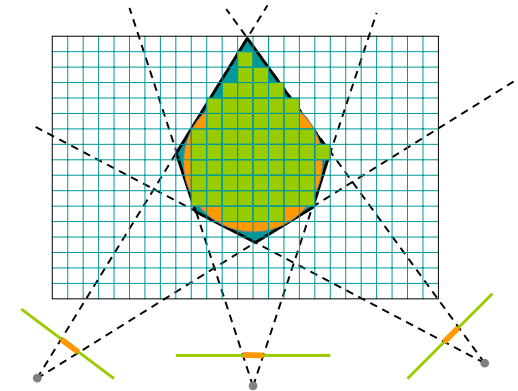
## Silhouette carving

DigiVFX

- Discrete version:
  - Loop over all voxels in some volume
  - If projection into images lies inside all silhouettes, mark as occupied
  - Else mark as free

## Silhouette carving

DigiVFX



## Voxel coloring

DigiVFX

- Seitz and Dyer, 1997
- In addition to free / occupied, store color at each voxel
- Explicitly accounts for occlusion

## Voxel coloring

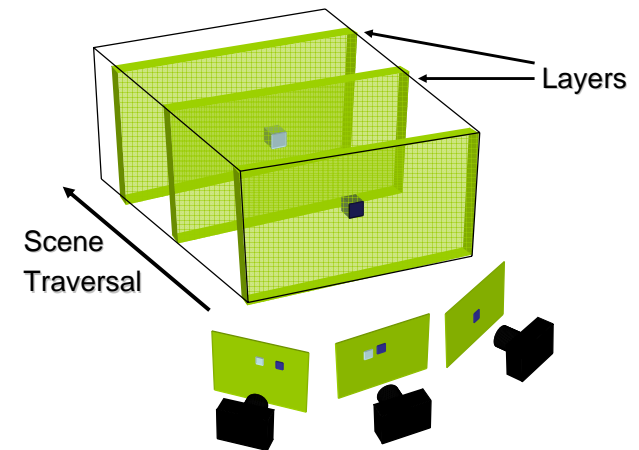
DigiVFX

- Basic idea: sweep through a voxel grid
  - Project each voxel into each image in which it is visible
  - If colors in images agree, mark voxel with color
  - Else, mark voxel as empty
- Agreement of colors based on comparing standard deviation of colors to threshold

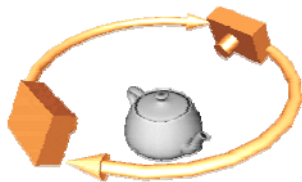
## Voxel coloring and occlusion

- Problem: which voxels are visible?
- Solution: constrain camera views
  - When a voxel is considered, necessary occlusion information must be available
  - Sweep occluders before occludees
  - Constrain camera positions to allow this sweep

## Voxel coloring sweep order



## Voxel coloring camera positions



Inward-looking  
Cameras above scene



Outward-looking  
Cameras inside scene

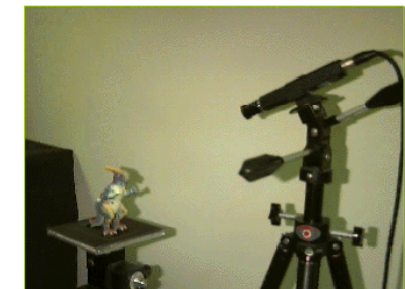
## Image acquisition



Selected Dinosaur Images



Selected Flower Images



- Calibrated Turntable
- 360° rotation (21 images)

## Voxel coloring results

DigiVFX



Dinosaur Reconstruction

72 K voxels colored  
7.6 M voxels tested  
7 min. to compute  
on a 250MHz SGI

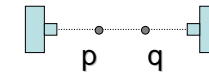


Flower Reconstruction

70 K voxels colored  
7.6 M voxels tested  
7 min. to compute  
on a 250MHz SGI

## Limitations of voxel coloring

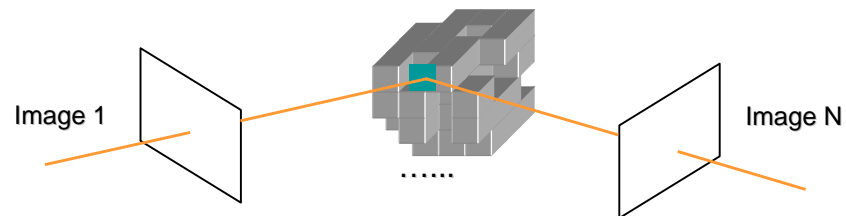
DigiVFX



- A view-independent depth order may not exist
- Need more powerful general-case algorithms
  - Unconstrained camera positions
  - Unconstrained scene geometry/topology

## Space carving

DigiVFX



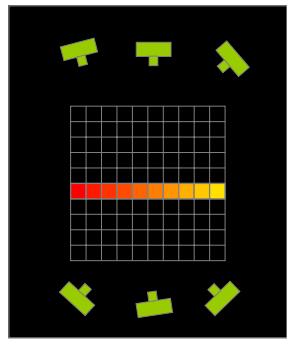
Initialize to a volume  $V$  containing the true scene  
Choose a voxel on the current surface  
Project to visible input images  
Carve if not photo-consistent  
Repeat until convergence

## Multi-pass plane sweep

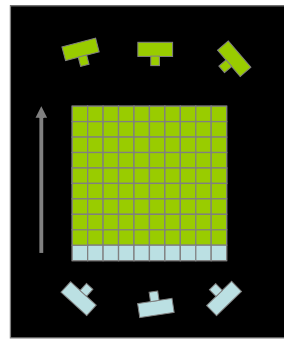
DigiVFX

- Faster alternative:
  - Sweep plane in each of 6 principal directions
  - Consider cameras on only one side of plane
  - Repeat until convergence

# Multi-pass plane sweep

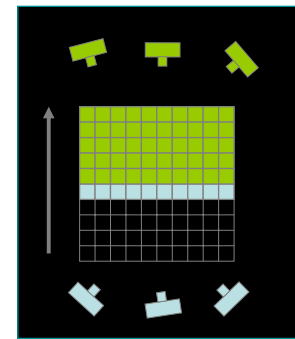
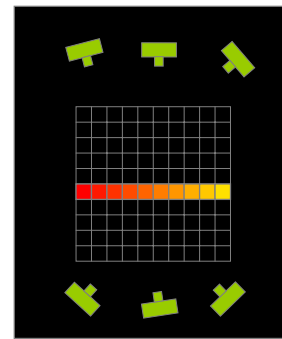


True Scene

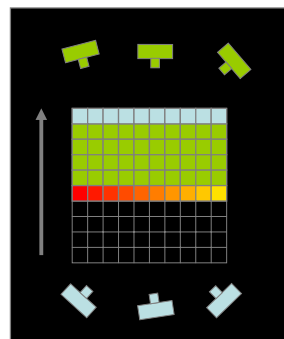
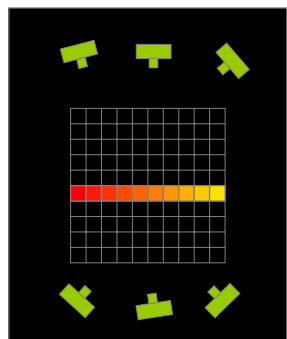


Reconstruction

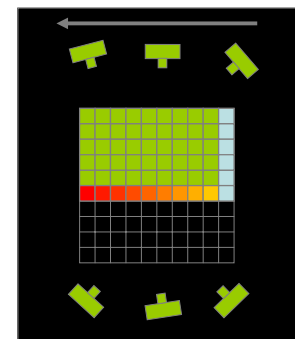
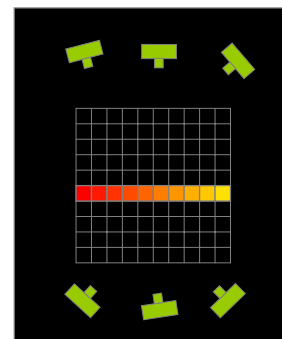
# Multi-pass plane sweep



# Multi-pass plane sweep



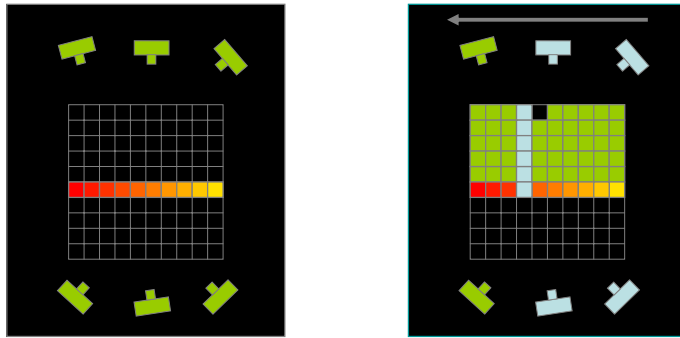
# Multi-pass plane sweep





## Multi-pass plane sweep

DigiVFX



## Space carving results: African violet

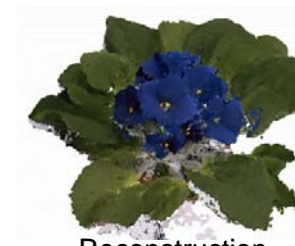
DigiVFX



Input image (1 of 45)



Reconstruction



Reconstruction



Reconstruction

## Space carving results: hand

DigiVFX



Input image  
(1 of 100)



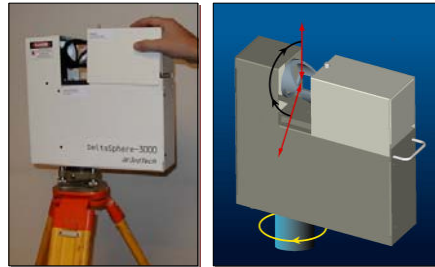
Reconstruction

Active approaches

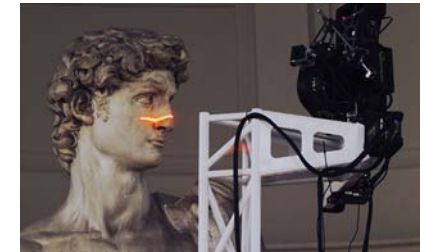
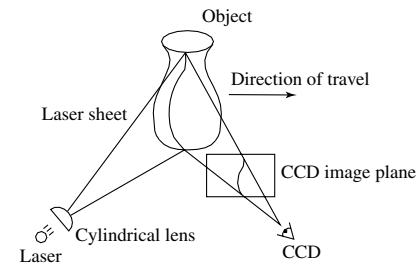
## Time of flight

- Basic idea: send out pulse of light (usually laser), time how long it takes to return

$$r = \frac{1}{2} c \Delta t$$



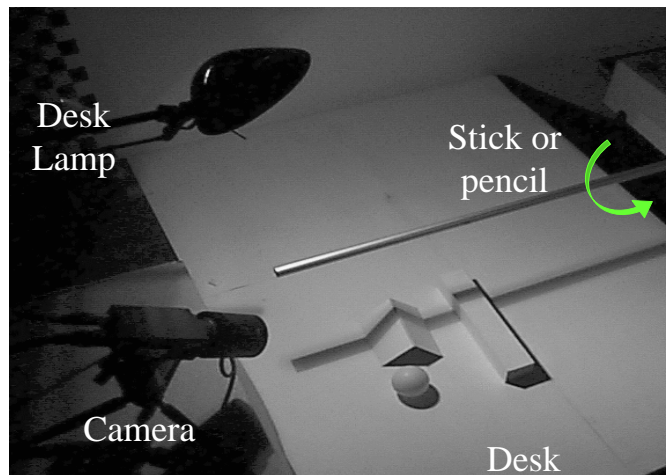
## Laser scanning (triangulation)



Digital Michelangelo Project  
<http://graphics.stanford.edu/projects/mich/>

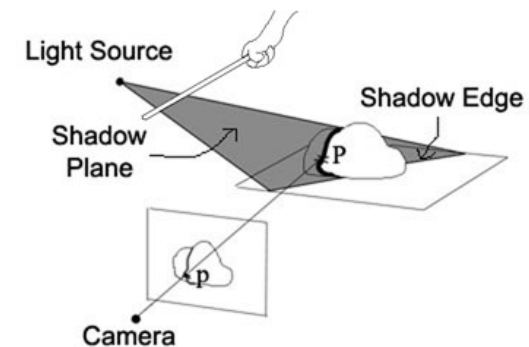
- Optical triangulation
  - Project a single stripe of laser light
  - Scan it across the surface of the object
  - This is a very precise version of structured light scanning
- Other patterns are possible

## Shadow scanning



<http://www.vision.caltech.edu/bouquetj/ICCV98/>

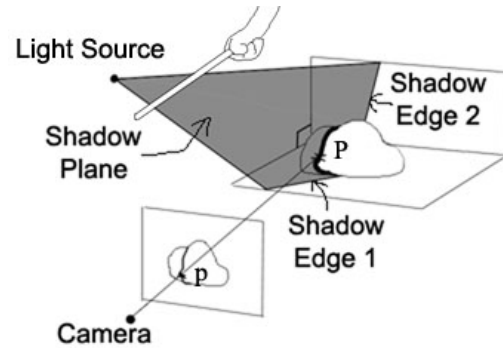
## Basic idea



- Calibration issues:
  - where's the camera wrt. ground plane?
  - where's the shadow plane?
    - depends on light source position, shadow edge

## Two Plane Version

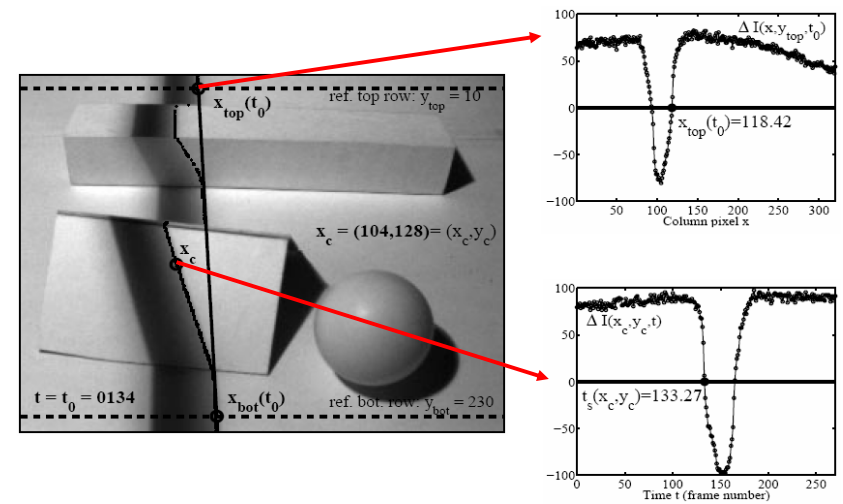
DigiVFX



- Advantages
  - don't need to pre-calibrate the light source
  - shadow plane determined from two shadow edges

## Estimating shadow lines

DigiVFX



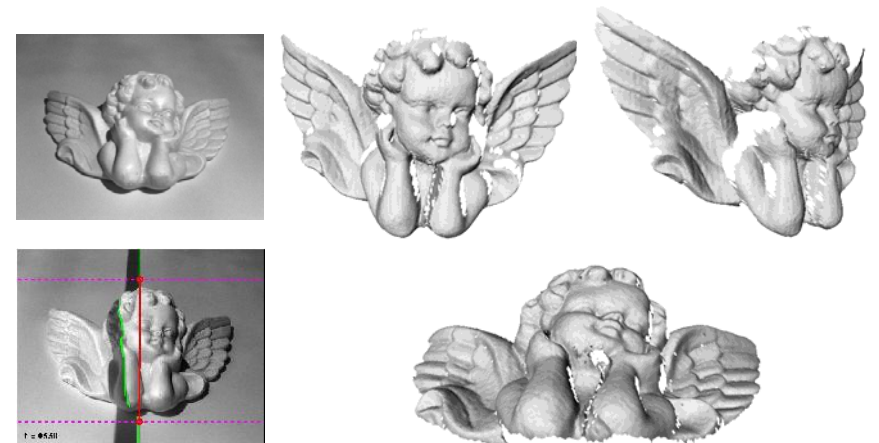
## Shadow scanning in action

DigiVFX



## Results

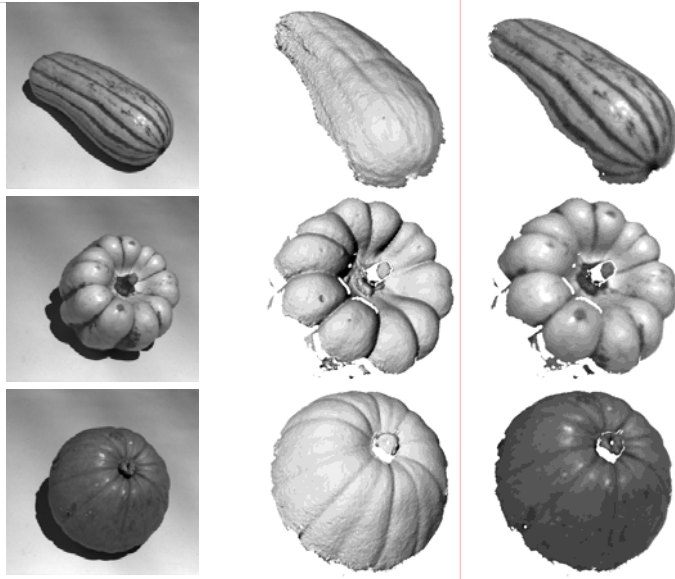
DigiVFX



accuracy: 0.1mm over 10cm  $\rightarrow$  ~ 0.1% error

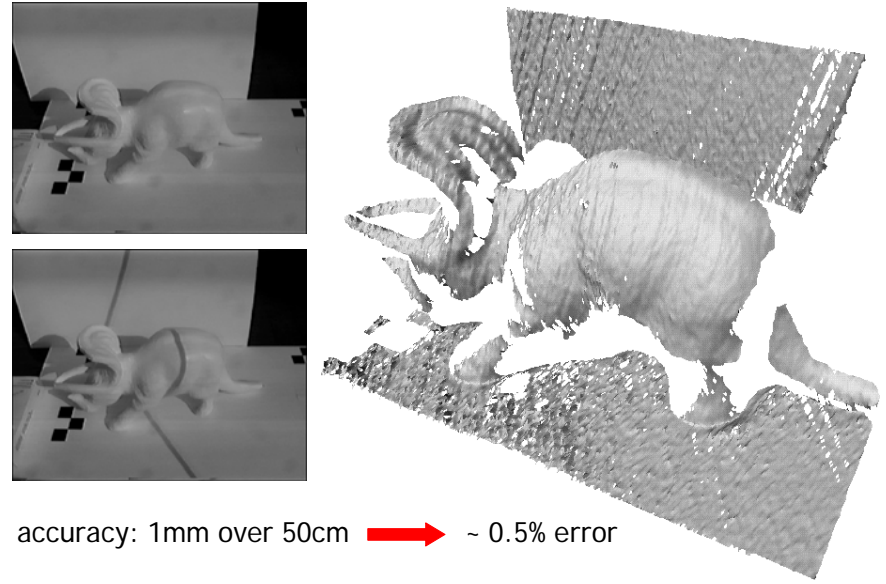
## Textured objects

DigiVFX



## Scanning with the sun

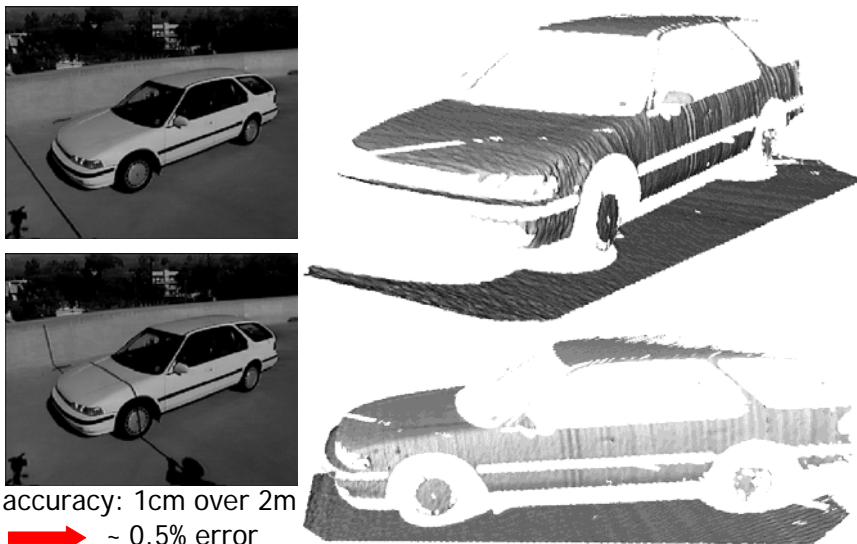
DigiVFX



accuracy: 1mm over 50cm → ~ 0.5% error

## Scanning with the sun

DigiVFX

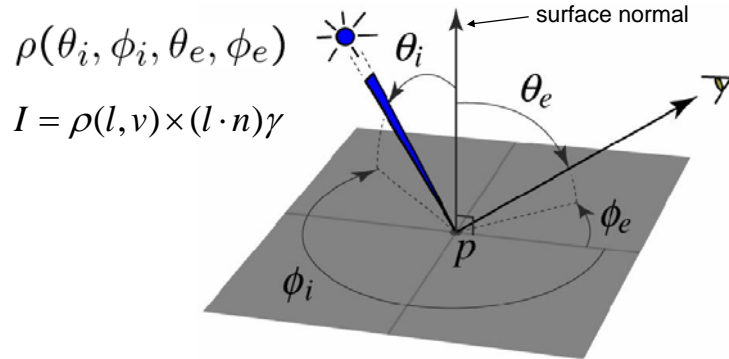


accuracy: 1cm over 2m → ~ 0.5% error

Active variants of  
passive approaches

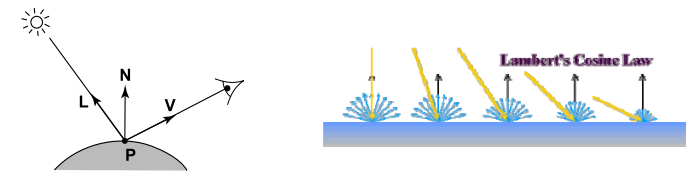
## The BRDF

- The Bidirectional Reflection Distribution Function
  - Given an incoming ray  $(\theta_i, \phi_i)$  and outgoing ray  $(\theta_e, \phi_e)$  what proportion of the incoming light is reflected along outgoing ray?



$$I = \rho(l, v) \times (l \cdot n) \gamma$$

## Diffuse reflection (Lambertian)

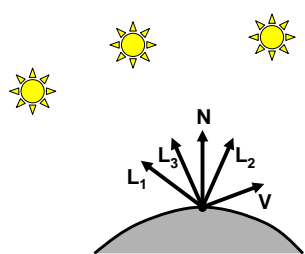


$$\rho(l, v) = k_d \leftarrow \text{albedo}$$

$$I = k_d N \cdot L$$

Assuming that light strength is 1.

## Photometric stereo



$$\begin{aligned} I_1 &= k_d N \cdot L_1 \\ I_2 &= k_d N \cdot L_2 \\ I_3 &= k_d N \cdot L_3 \end{aligned}$$

- Can write this as a matrix equation:

$$\begin{bmatrix} I_1 \\ I_2 \\ I_3 \end{bmatrix} = k_d \begin{bmatrix} L_1^T \\ L_2^T \\ L_3^T \end{bmatrix} N$$

## Solving the equations

$$\underbrace{\begin{bmatrix} I_1 \\ I_2 \\ I_3 \end{bmatrix}}_{\mathbf{I} \quad 3 \times 1} = \underbrace{\begin{bmatrix} L_1^T \\ L_2^T \\ L_3^T \end{bmatrix}}_{\mathbf{L} \quad 3 \times 3} \underbrace{k_d N}_{\mathbf{G} \quad 3 \times 1}$$

$$\mathbf{G} = \mathbf{L}^{-1} \mathbf{I}$$

$$k_d = \|\mathbf{G}\|$$

$$\mathbf{N} = \frac{1}{k_d} \mathbf{G}$$

## More than three lights

- Get better results by using more lights

$$\begin{bmatrix} I_1 \\ \vdots \\ I_n \end{bmatrix} = \begin{bmatrix} \mathbf{L}_1 \\ \vdots \\ \mathbf{L}_n \end{bmatrix} k_d \mathbf{N}$$

- Least squares solution:

$$\begin{aligned} \mathbf{I} &= \mathbf{L}\mathbf{G} \\ \mathbf{L}^T \mathbf{I} &= \mathbf{L}^T \mathbf{L} \mathbf{G} \\ \mathbf{G} &= (\mathbf{L}^T \mathbf{L})^{-1} (\mathbf{L}^T \mathbf{I}) \end{aligned}$$

- Solve for  $\mathbf{N}$ ,  $k_d$  as before

## Trick for handling shadows

- Weight each equation by the pixel brightness:

$$I_i(I_i) = I_i[k_d \mathbf{N} \cdot \mathbf{L}_i]$$

- Gives weighted least-squares matrix equation:

$$\begin{bmatrix} I_1^2 \\ \vdots \\ I_n^2 \end{bmatrix} = \begin{bmatrix} I_1 \mathbf{L}_1^T \\ \vdots \\ I_n \mathbf{L}_n^T \end{bmatrix} k_d \mathbf{N}$$

- Solve for  $\mathbf{N}$ ,  $k_d$  as before

## Photometric Stereo Setup



## Procedure

- Calibrate camera
- Calibrate light directions/intensities
- Photographing objects (HDR recommended)
- Estimate normals
- Estimate depth

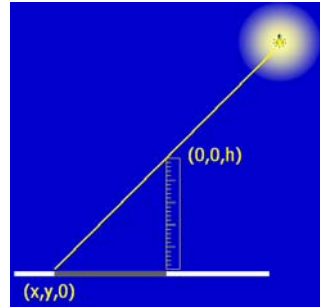
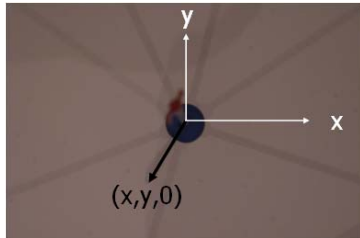
## Estimating light directions

- Trick: place a chrome sphere in the scene



– the location of the highlight tells you where the light source is

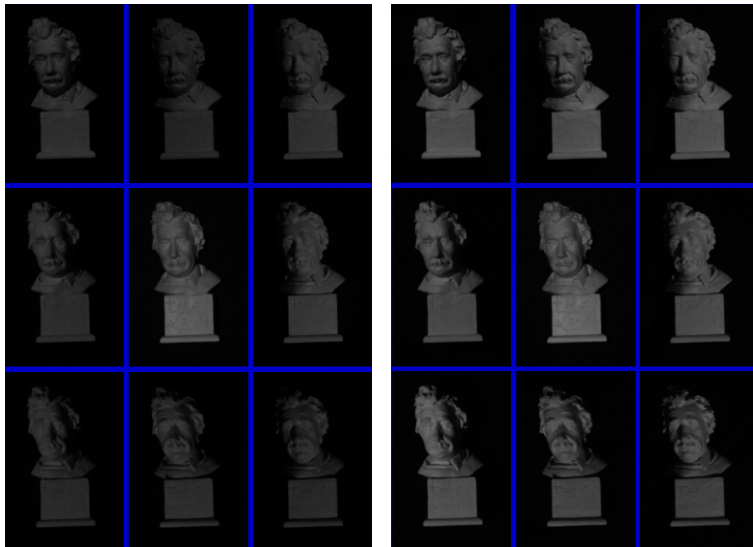
- Use a ruler



## Photographing objects



## Normalize light intensities



## Estimate normals



## Depth from normals

DigiVFX

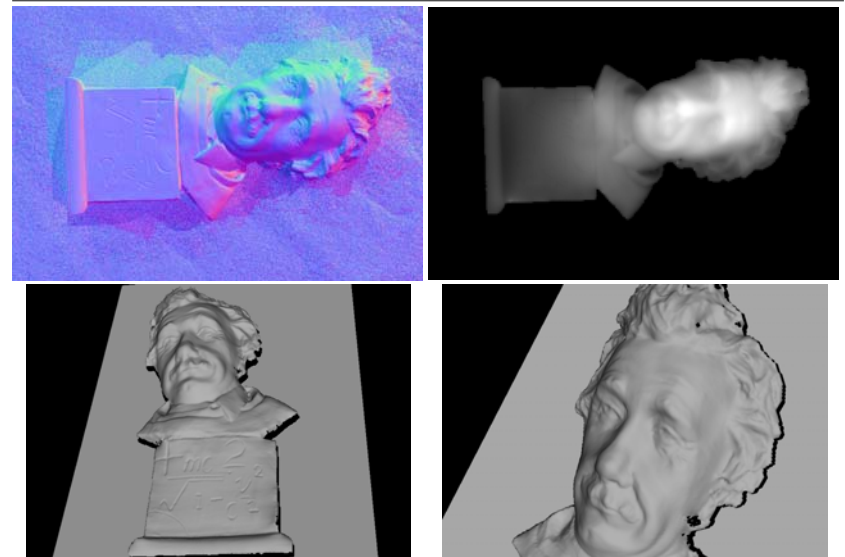
$$(n_x, n_y, n_z) = \left( \frac{\partial z}{\partial x}, \frac{\partial z}{\partial y}, -1 \right) = (p, q, -1)$$

$$\begin{aligned} E &= E_{data} + E_{smooth} + E_{cons} \\ &= \sum_{i,j} w_{data} * \left[ \left( \frac{\partial z(i,j)}{\partial x} - p_{ij} \right)^2 + \left( \frac{\partial z(i,j)}{\partial y} - q_{ij} \right)^2 \right] \\ &+ \sum_{i,j} w_{smooth} * \left[ \left( \frac{\partial^2 z(i,j)}{\partial x^2} \right)^2 + 2 \left( \frac{\partial^2 z(i,j)}{\partial x \partial y} \right)^2 + \left( \frac{\partial^2 z(i,j)}{\partial y^2} \right)^2 \right] \\ &+ \sum_{(i,j) \in Cons} w_{cons} * (z(i,j) - c_{ij})^2 \end{aligned}$$

$$E = \frac{1}{2} z^T A z - b^T z + c \quad \equiv \quad A z = b$$

## Results

DigiVFX



## Limitations

DigiVFX

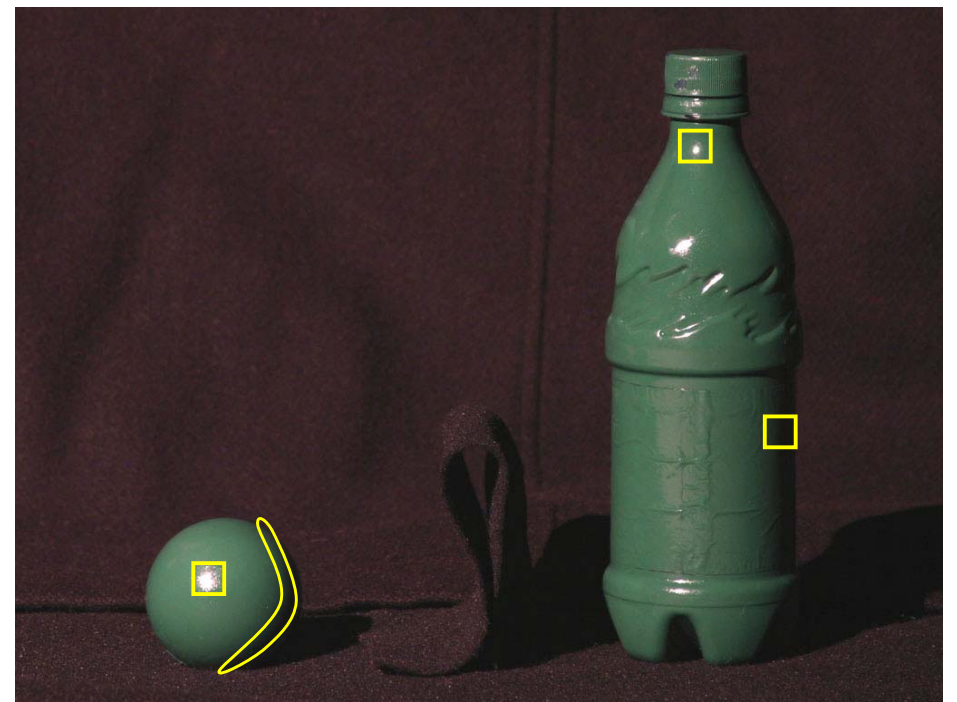
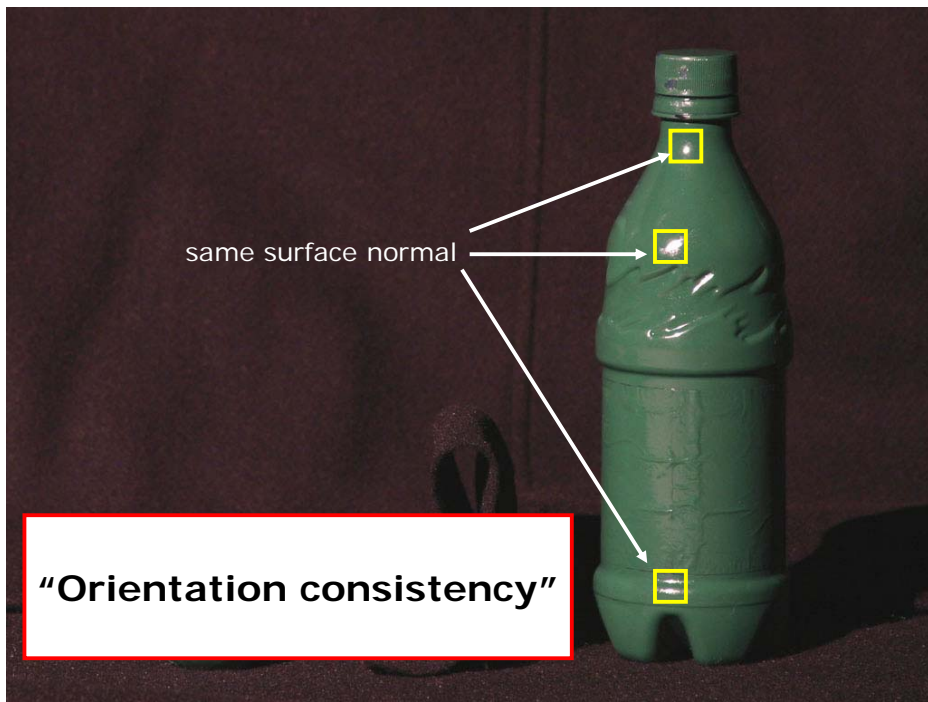
- Big problems
  - doesn't work for shiny things, semi-translucent things
  - shadows, inter-reflections
- Smaller problems
  - calibration requirements
    - measure light source directions, intensities
    - camera response function

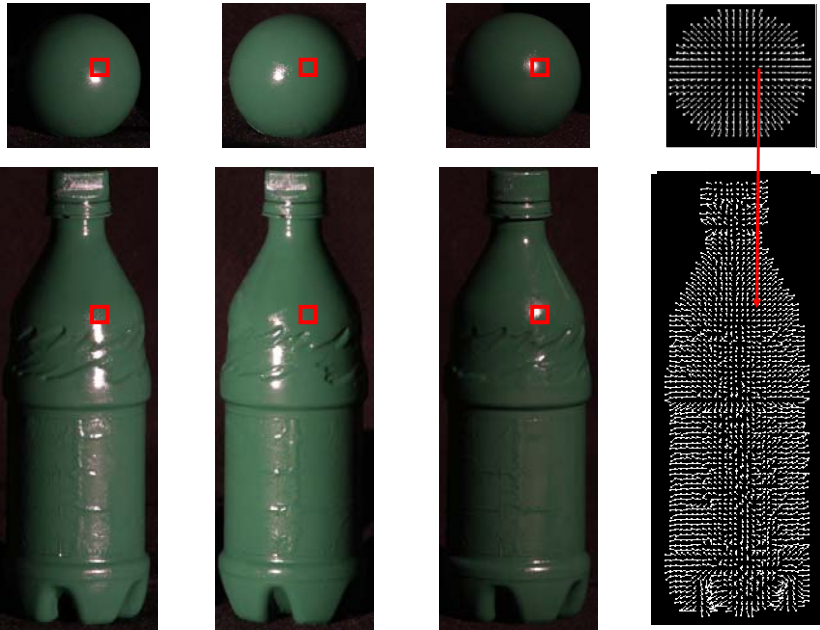
## Example-based photometric stereo

DigiVFX

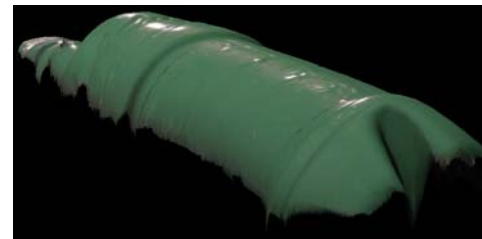
- Estimate 3D shape by varying illumination, fixed camera
- Operating conditions
  - any opaque material
  - distant camera, lighting
  - reference object available
  - no shadows, interreflections, transparency







Virtual views



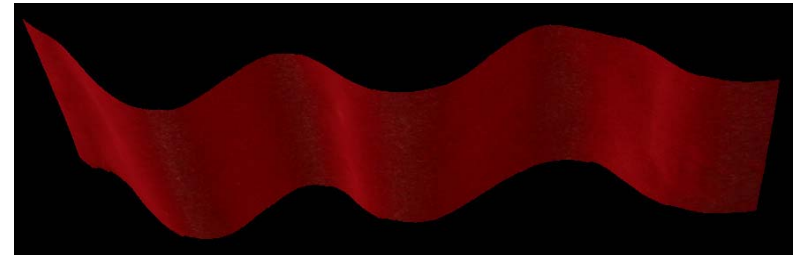
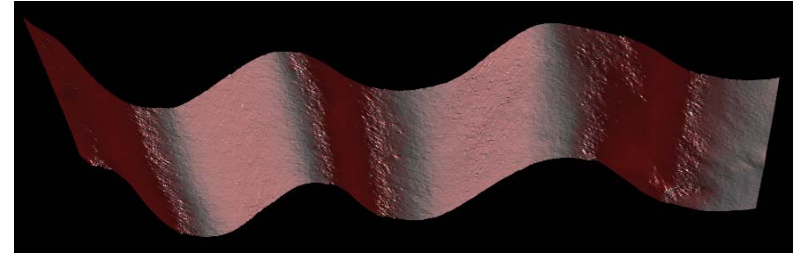
## Velvet

DigiVFX



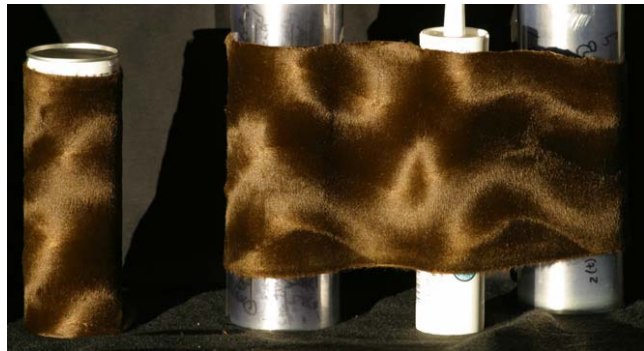
## Virtual Views

DigiVFX



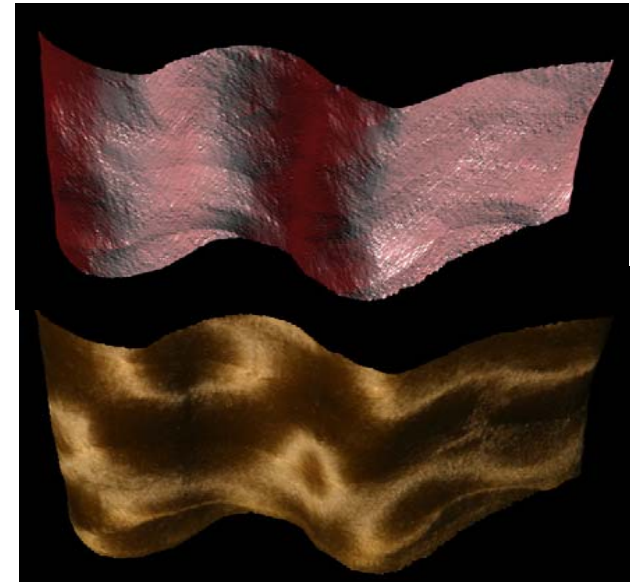
## Brushed Fur

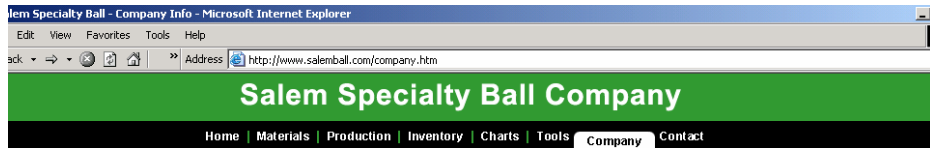
DigiVFX



## Virtual Views

DigiVFX





Quality Control Phone & Fax Addresses E-mail Directory Methods of Payment

Salem Specialty Ball supplies industrial grade balls that are used in bearings, pumps, valves and other commercial applications. We can supply balls in just about any size that is machineable. We have produced precision balls from .002" all the way up to 12.0" and beyond. We can also produce these balls in any material. **Almost without exception, if the material exists, we can make it into a ball.** Not only do we specialize in hard to find materials, we also carry standard materials such as Chrome steel and the stainless steels. We stock an extensive inventory of ready to ship balls. Most orders are shipped the same day. And if it isn't in stock, we can make it for you in matter of days. In addition, you will find that our prices are very competitive.



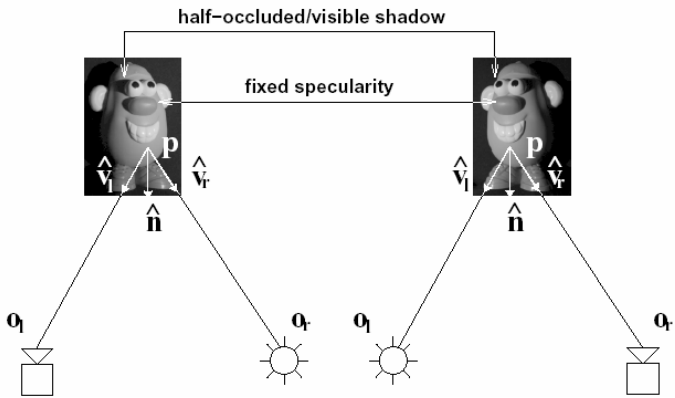
Located in the beautiful northwest corner of Connecticut, Canton has been our company's home for the last three years and we have been in complete operation for over ten years. Proud of our reputation, Salem Specialty Ball Company has over fifty years of combined experience allowing us to provide top-notch quality technical support and expert engineering consultation.



# Helmholtz Stereo

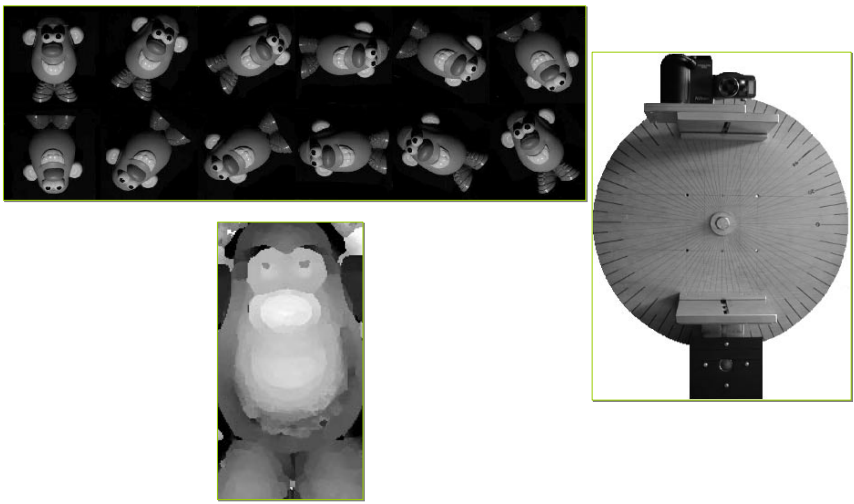
- Based on Helmholtz reciprocity: surface reflectance is the same under interchange of light, viewer
- So, take pairs of observations w. viewer, light interchanged
- Ratio of the observations in a pair is independent of surface material

# Helmholtz Stereo

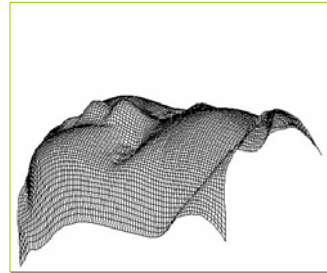
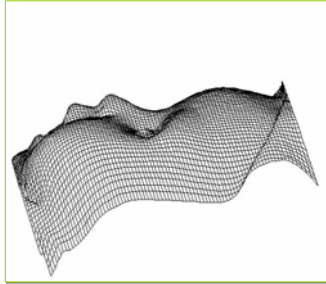


$$\left( i_l \frac{\hat{v}_l}{|\mathbf{o}_l - \mathbf{p}|^2} - i_r \frac{\hat{v}_r}{|\mathbf{o}_r - \mathbf{p}|^2} \right) \cdot \hat{\mathbf{n}} = \mathbf{w}(d) \cdot \hat{\mathbf{n}} = 0 \quad \mathbf{W}(d^*) \text{ will be rank 2}$$

# Helmholtz Stereo



## Helmholtz Stereo



## Reference

- D. Scharstein and R. Szeliski. [A Taxonomy and Evaluation of Dense Two-Frame Stereo Correspondence Algorithms](#), IJCV 2002.
- S. Seitz and C. Dyer. [Photorealistic Scene Reconstruction by Voxel Coloring](#), CVPR 1997.
- J.-Y. Bouguet and P. Perona. [3D Photography on Your Desk](#), ICCV 1998.
- T. Zickler, P. Belhumeur and D. Kriegman. [Helmholtz Stereopsis: Exploiting Reciprocity for Surface Reconstruction](#), ECCV 2002.
- A. Hertzman and S. Seitz. [Shape and Materials by Example: A Photometric Stereo Approach](#), CVPR 2003.