Image stitching

Digital Visual Effects, Spring 2005 *Yung-Yu Chuang* 2005/3/30

with slides by Richard Szeliski, Steve Seitz, Matthew Brown and Vaclav Hlavac



- Project #1 was due yesterday.
- Project #2 handout will be available on the web later tomorrow.
- I will set up a webpage for artifact voting soon.



Outline

- Image stitching
- Motion models
- Direct methods
- Feature-based methods
- Applications
- Project #2









Applications of image stitching

- Video stabilization
- Video summarization
- Video compression
- Video matting
- Panorama creation



Video summarization





Video compression









input video





remove foreground





estimate background





background estimation





alpha matte



Panorama creation





- Are you getting the whole picture?
 - Compact Camera FOV = 50 x 35°





- Are you getting the whole picture?
 - Compact Camera FOV = 50 x 35°
 - Human FOV = $200 \times 135^{\circ}$





- Are you getting the whole picture?
 - Compact Camera FOV = 50 x 35°
 - Human FOV = $200 \times 135^{\circ}$
 - Panoramic Mosaic = 360 x 180°



Panorama examples



- Panorama mode in consumer cameras
- Mars:

http://www.panoramas.dk/fullscreen3/f2_mars97.html

• Earth:

http://earthobservatory.nasa.gov/Newsroom/BlueMarble/

Digi<mark>VFX</mark>

2D motion models

- translation: x' = x + t x = (x, y)
- rotation: x' = R x + t
- similarity: x' = s R x + t
- affine: x' = A x + t
- perspective: $\underline{x}' \cong H \underline{x}$ $\underline{x} = (x, y, 1)$ (\underline{x} is a *homogeneous* coordinate)
- These all form a nested group (closed under composition w/ inv.)





Name	Matrix	# D.O.F.	Preserves:	Icon
translation	$igg[egin{array}{c c c c c c c c c c c c c c c c c c c $	2	orientation $+ \cdots$	
rigid (Euclidean)	$\left[egin{array}{c c c c c c c c c c c c c c c c c c c $	3	lengths $+\cdots$	\Diamond
similarity	$\left[\left[\left. s oldsymbol{R} \right oldsymbol{t} ight]_{2 imes 3} ight.$	4	angles $+ \cdots$	\bigcirc
affine	$\left[egin{array}{c} oldsymbol{A} \end{array} ight]_{2 imes 3}$	6	parallelism $+\cdots$	
projective	$\left[egin{array}{c} ilde{H} \end{array} ight]_{3 imes 3}$	8	straight lines	

A pencil of rays contains all views





Can generate any synthetic camera view as long as it has **the same center of projection**!



Mosaic as Image Reprojection



- The images are reprojected onto a common plane
- The mosaic is formed on this plane
- Mosaic is a *synthetic wide-angle camera*

Changing camera center







Planar scene (or far away)



- PP3 is a projection plane of both centers of projection, so we are OK!
- This is how big areal photographs are made



3D motion models





3D motion models

- Rotational
- Cylindrical



- Select a motion model and estimate parameters
- Direct methods use pixel-to-pixel matching
- We have covered this last time actually.
- We will show a case study on constructing cylindrical panorama using a direct method.

A case study: cylindrical panorama



- 1. Take pictures on a tripod (or handheld)
- 2. Warp to cylindrical coordinate
- 3. Compute pairwise alignments using the hierarchical Lucas-Kanade algorithm
- 4. Fix up the end-to-end alignment
- 5. Blending
- 6. Crop the result and import into a viewer



Taking pictures





Kaidan panoramic tripod head



Translation model



A case study: cylindrical panorama



• What if you want a 360° field of view?





Cylindrical projection





Cylindrical reprojection



Image 384x300

f = 180 (pixels)

f = 280

f = 380



We will discuss more accurate methods next time



Distortion



- Radial distortion of the image
 - Caused by imperfect lenses
 - Deviations are most noticeable for rays that pass through the edge of the lens

Radial correction



 Correct for "bending" in wide field of view lenses





 $\hat{r}^2 = \hat{x}^2 + \hat{y}^2$ $\hat{x}' = \hat{x}/(1+\kappa_1\hat{r}^2+\kappa_2\hat{r}^4)$ $\hat{y}' = \hat{y}/(1+\kappa_1\hat{r}^2+\kappa_2\hat{r}^4)$ $x = f\hat{x}'/\hat{z} + x_c$ $y = f\hat{y}'/\hat{z} + y_c$



Input images




Cylindrical warping





Alignment

• a rotation of the camera is a translation of the cylinder!

$$\begin{bmatrix} \sum_{x,y} I_x^2 & \sum_{x,y} I_x I_y \\ \sum_{x,y} I_x I_y & \sum_{x,y} I_y^2 \end{bmatrix} \begin{bmatrix} u \\ v \end{bmatrix} = \begin{bmatrix} \sum_{x,y} I_x (J(x,y) - I(x,y)) \\ \sum_{x,y} I_y (J(x,y) - I(x,y)) \end{bmatrix}$$



LucasKanadeStep

void LucasKanadeStep(CByteImage& img1, CByteImage& img2, float t[2]) {
 // Transform the image
 Translation(img2, img2t, t);

// Compute the gradients and summed error by comparing img1 and img2t double A[2][2], b[2];

```
for (int y = 1; y < height-1; y++) { // ignore borders
```

```
for (int x = 1; x < width-1; x++) {
```

```
// If both have full alphas, then compute and accumulate the error
double e = img2t.Pixel(x, y, k) - img1.Pixel (x, y, k);
```

// Accumulate the matrix entries

```
double gx = 0.5^*(img2t.Pixel(x+1, y, k) - img2t.Pixel(x-1, y, k));
```

```
double gy = 0.5^{(img2t.Pixel(x, y+1, k) - img2t.Pixel(x, y-1, k)));
```

```
A[0][0] += gx^*gx; A[0][1] += gx^*gy;
A[1][0] += gx^*gy; A[1][1] += gy^*gy;
```

```
b[0] += e*gx; b[1] += e*gy;
```

LucasKanadeStep (cont.)

}



// Solve for the update At=b and update the vector

```
double det = 1.0 / (A[0][0]*A[1][1] - A[1][0]*A[1][0]);
```

```
t[0] += (A[1][1]*b[0] - A[1][0]*b[1]) * det;
t[1] += (A[0][0]*b[1] - A[1][0]*b[0]) * det;
```

PyramidLucasKanade



void PyramidalLucasKanade(CByteImage& img1, CByteImage& img2, float t[2], int nLevels, int nLucasKanadeSteps)

```
CBytePyramid p1(img1); // Form the two pyramids CBytePyramid p2(img2);
```

```
// Process in a coarse-to-fine hierarchy
for (int I = nLevels-1; I >= 0; I--)
{
    t[0] /= (1 << I); // scale the t vector
    t[1] /= (1 << I);
    CByteImage& i1 = p1[I];
    CByteImage& i2 = p2[I];
    for (int k = 0; k < nLucasKanadeSteps; k++)
        LucasKanadeStep(i1, i2, t);
    t[0] *= (1 << I); // restore the full scaling</pre>
```

```
t[1] *= (1 << I);
```

}

{



Gaussian pyramid





• Why blending: parallax, lens distortion, scene motion, exposure difference



Blending





Blending





Blending



Assembling the panorama





• Stitch pairs together, blend, then crop





- Error accumulation
 - small errors accumulate over time



Problem: Drift



- add another copy of first image at the end
- there are a bunch of ways to solve this problem
 - add displacement of (y₁ y_n)/(n -1) to each image after the first
 - compute a global warp: y' = y + ax
 - run a big optimization problem, incorporating this constraint
 - best solution, but more complicated
 - known as "bundle adjustment"









Viewer: panorama



example: http://www.cs.washington.edu/education/courses/cse590ss/01wi/projects/project1/students/dougz/index.html

Viewer: texture mapped model





example: http://www.panoramas.dk/



- Only use feature points to estimate parameters
- We will study the "Recognising panorama" paper published in ICCV 2003



- RANSAC = Random Sample Consensus
- an algorithm for robust fitting of models in the presence of many data outliers
- Compare to robust statistics
- Given N data points x_i, assume that mjority of them are generated from a model with parameters Θ, try to recover Θ.



RANSAC algorithm



Depends on the problem.



p: probability of real inliers

P: probability of success after k trials

$$P = 1 - (1 - p^{n})^{k}$$

n samples are all inliers
a failure
failure after k trials

$$k = \frac{\log(1 - P)}{\log(1 - p^{n})}$$
 for $P = 0.99$

$$\frac{n p k}{3 0.5 35}$$

$$\frac{1}{6 0.6 97}$$

$$\frac{1}{6 0.5 293}$$



Example: line fitting









Model fitting





Measure distances





Count inliers





Another trial











- 1D Rotations (θ)
 - Ordering \Rightarrow matching images





- 1D Rotations (θ)
 - Ordering \Rightarrow matching images





- 1D Rotations (θ)
 - Ordering \Rightarrow matching images





- 1D Rotations (θ)
 - Ordering \Rightarrow matching images



- 2D Rotations (q, f)
 - Ordering Amatching images



- 1D Rotations (θ)
 - Ordering \Rightarrow matching images



- 2D Rotations (q, f)
 - Ordering \neq matching images





- 1D Rotations (θ)
 - Ordering \Rightarrow matching images



- 2D Rotations (q, f)
 - Ordering \neq matching images











Overview

- SIFT Feature Matching
- Image Matching
- Bundle Adjustment
- Multi-band Blending



- Find k-NN for each feature
 - $k \approx$ number of overlapping images (we use k = 4)
- Use k-d tree
 - k-d tree recursively bi-partitions data at mean in the dimension of maximum variance
 - Approximate nearest neighbours found in O(nlogn)


Overview

- SIFT Feature Matching
- Image Matching
 - For each image, use RANSAC to select inlier features from 6 images with most feature matches
- Bundle Adjustment
- Multi-band Blending

RANSAC for Homography





RANSAC for Homography





RANSAC for Homography





Probabilistic model for verification

- Compare probability that this set of RANSAC inliers/outliers was generated by a correct/false image match
- Choosing values for $p_1,\ p_0$ and p_{min}

 $n_i > 5.9 + 0.22n_f$





































Overview

- SIFT Feature Matching
- Image Matching
- Bundle Adjustment
- Multi-band Blending

Homography for Rotation



Parameterise each camera by rotation and focal length

$$\mathbf{R}_{i} = e^{[\boldsymbol{\theta}_{i}]_{\times}}, \quad [\boldsymbol{\theta}_{i}]_{\times} = \begin{bmatrix} 0 & -\theta_{i3} & \theta_{i2} \\ \theta_{i3} & 0 & -\theta_{i1} \\ -\theta_{i2} & \theta_{i1} & 0 \end{bmatrix}$$
$$\mathbf{K}_{i} = \begin{bmatrix} f_{i} & 0 & 0 \\ 0 & f_{i} & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

• This gives pairwise homographies

$$\tilde{\mathbf{u}}_i = \mathbf{H}_{ij} \tilde{\mathbf{u}}_j$$
, $\mathbf{H}_{ij} = \mathbf{K}_i \mathbf{R}_i \mathbf{R}_j^T \mathbf{K}_j^{-1}$



Error function

• Sum of squared projection errors

$$e = \sum_{i=1}^{n} \sum_{j \in \mathcal{I}(i)} \sum_{k \in \mathcal{F}(i,j)} f(\mathbf{r}_{ij}^k)^2$$

- n = #images
- I(i) = set of image matches to image i
- F(i, j) = set of feature matches between images i, j
- r_{ij}^k = residual of kth feature match between images i,j

• Robust
$$\operatorname{err}_{f(\mathbf{x})} = \begin{cases} |\mathbf{x}|, & \text{if } |\mathbf{x}| < x_{max} \\ x_{max}, & \text{if } |\mathbf{x}| \ge x_{max} \end{cases}$$



Overview

- SIFT Feature Matching
- Image Matching
- Bundle Adjustment
- Multi-band Blending

Multi-band Blending



- Burt & Adelson 1983
 - Blend frequency bands over range $\propto \lambda$





2-band Blending



Low frequency ($\lambda > 2$ pixels)



High frequency (λ < 2 pixels)







Results







- Direct methods use all information and can be very accurate, but they depend on the fragile "brightness constancy" assumption
- Iterative approaches require initialization
- Not robust to illumination change and noise images
- In early days, direct method is better.
- Feature based methods are now more robust and potentially faster
- Even better, it can recognize panorama without initialization



Applications of panorama in VFX

- Background plates
- Image-based lighting

Spiderman 2 (background plate)











http://www.cgnetworks.com/story_custom.php?story_id=2195&page=4



Project #2 Image stitching

- Assigned: 3/30
- Due: 11:59pm 4/19
- Work in pairs

Reference software



• Autostitch

http://www.cs.ubc.ca/~mbrown/autostitch/autostitch.html

• Many others are available online.





- Full SIFT implementation
- Recognizing panorama
- Bundle adjustment
- Handle dynamic objects
- Better blending techniques



- Take your own pictures and generate a stitched image, be creative.
- <u>http://www.cs.washington.edu/education/courses/cse590ss/01wi/projec</u> <u>ts/project1/students/allen/index.html</u>

Tips for taking pictures

- Common focal point
- Rotate your camera to increase vertical FOV
- Tripod
- Fixed exposure?



- You have to turn in your complete source, the executable, a html report and an artifact.
- Report page contains:

description of the project, what do you learn, algorithm, implementation details, results, bells and whistles...

• Artifacts must be made using your own program. artifacts voting on forum.

Reference



- Richard Szeliski, <u>Image Alignment and Stitching</u>, unpublished draft, 2005.
- R. Szeliski and H.-Y. Shum. <u>Creating full view panoramic image</u> mosaics and texture-mapped models, SIGGRAPH 1997, pp251-258.
- M. Brown, D. G. Lowe, <u>Recognising Panoramas</u>, ICCV 2003.