

# Theory of Computation

## Homework 5

Due: 2012/12/25

**Problem 1** (Chernoff Bound) Suppose  $x_1, x_2, \dots, x_n$  are independent random variables taking values 1 and 0 with probabilities  $p$  and  $1 - p$ , respectively. Let  $X = \sum_{i=1}^n X_i$ . Then for  $0 \leq \theta \leq 1$ ,  $\Pr[X \leq (1 - \theta)pn] \leq e^{-\frac{\theta^2 pn}{2}}$ .

**Problem 2** Recall that  $\text{EXP} = \text{TIME}(2^{n^k})$ . Show that  $\text{BPP} \subseteq \text{EXP}$ .